

Extra example ☺

To clarify some of the confusions from yesterday, I thought to present one more example which also helped me personally when I was putting it together.

With a single output like yesterday, the mapping was to \mathbb{R} , that is why we found a single equation for total derivative. The Jacobian is used to find the total derivative when we have a mapping that is $\mathbb{R}^n \rightarrow \mathbb{R}^m$.

For instance, define $f: \mathbb{R}^3 \rightarrow \mathbb{R}^4$ to be given by:

$$f(x, y, z) = (x + 2y + 3z, xyz^3, \ln(x^2y), e^{2xy^2}y^2)$$

1. What is the dimension of this Jacobian?
2. Find the Jacobian Df .
3. Use the Jacobian to write out matrices that give the total derivative of f .
4. Write out the total derivative equation for each function f_i in f .