

Task 1:

1. R (A, B, C, D)

$F = \{AB \rightarrow C, D \rightarrow C\}$

- i. $AB \rightarrow C, D \rightarrow C$, then $ABD \rightarrow C$

Minimal Key: ABD

Derivations: A(B,D), B(A,D)

Normal Forms: 1NF

- ii. $A, B, D \rightarrow C$

Checking 2NF: LHS is a proper subset of some minimal key

Checking 3NF: Non-trivial, LHS is not a superkey, RHS contains a non-key attribute

Checking BCNF: Non-trivial, LHS is not a superkey

Therefore, 1NF

2. R (A, B, C, D)

$F = \{AB \rightarrow C, AB \rightarrow D, D \rightarrow C\}$

- i. $AB \rightarrow C, AB \rightarrow D$, then $AB \rightarrow CD$
 $AB \rightarrow CD, D \rightarrow C$, then $AB \rightarrow C$

Minimal Key: AB

Derivations: A(B,C), B(A,C)

Normal Forms: 2NF

- ii. $A, B \rightarrow C$

$A, B \rightarrow C$

$D \rightarrow C$

Checking 2NF: Check if LHS is a proper subset of some minimal key or if RHS are not all key attributes.

Checking FD: $A, B \rightarrow C$

Checking FD: $A, B \rightarrow D$

Checking FD: $D \rightarrow C$

Checking 3NF: Non-trivial, LHS is not a superkey, RHS contains a non-key attribute

Checking BCNF: $D \rightarrow C$ is non-trivial and LHS is not a superkey

Therefore, 2NF

3. R (A, B, C, D)

F = { $A \rightarrow B$, $A \rightarrow C$ }

i. $A \rightarrow B$, $A \rightarrow C$, then $A \rightarrow BC$

Minimal Key: A

Derivations: A(B,D), B(A,D)

Normal Forms: 1NF

ii. $A \rightarrow B$

Checking 2NF: LHS is a proper subset of some minimal key

Checking 3NF: Non-trivial, LHS is not a superkey, RHS contains a non-key attribute

Checking BCNF: Non-trivial, LHS is not a superkey

Therefore, 1NF