

Recursion and External Packages

Lecture 7 in 1DV507 - Programming and Data Structures

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Agenda

- ▶ Recursive Methods
 - ▶ Definition and example
 - ▶ Solving problems using recursion
- ▶ Using External Packages
 - ▶ A concrete example: MP3 Player
 - ▶ A quick look at Exercise 4, Assignment 1
- ▶ Reading Instructions

Liang: Chapter 18 (skip 18.8)

Recursion

- ▶ What is recursion?
 - ▶ A way to think when solving problems.
 - ▶ An implementation where a method calls itself.
- ▶ Why is it important?
 - ▶ The recursive solution is sometimes much easier than the iterative.
 - ▶ Examples: Binary search trees, Hanoi Tower, Fibonacci numbers
- ▶ Is it always good?
 - ▶ No, in many cases an iterative solution is just as good.
 - ▶ In certain cases (e.g. Fibonacci) recursion is simple but very costly.
 - ▶ We will today see many examples that can just as easily be handled using iteration.
- ▶ Is it possible to solve more problems using recursion than without?
 - ▶ Speaking purely computationally, no. On the other hand, many problems are much simpler using recursion.

Arithmetic Sum (Recursion intro.)

$$S(n) = \sum_{i=1}^n i = 1 + 2 + 3 + \cdots + (n-2) + (n-1) + n$$

- Can be computed iteratively:

ARITHMSUMIT(N)

1. *sum* = 0
2. *count* = 0
3. Repeat N times:
 - 3.1 *count* = *count* + 1
 - 3.2 *sum* = *sum* + *count*
4. The answer is now in SUM

Computing Sum using smaller sums

$$S(n) = \sum_{i=1}^n i = \underbrace{1 + 2 + 3 + \dots + (n-2) + (n-1)}_{S(n-1)} + n$$

- ▶ The problem can be expressed using a smaller problem:

$$S(n) = S(n-1) + n$$

- ▶ **Ex:** $S(5) = S(4) + 5$

- ▶ And moving on ...

- ▶ $S(4) = S(3) + 4$

- ▶ $S(3) = S(2) + 3$

- ▶ $S(2) = S(1) + 2$

- ▶ $S(1) = S(0) + 1$

- ▶ $S(0) = S(-1) + 0$???

We must find a base case \Rightarrow a case where it all stops!

Arithmetic Sum: Introducing a Base Case

- ▶ We need a *base case* to terminate the computation.
- ▶ We choose to set the base case to $S(1) = 1$ ($S(0) = 0$ would also work).
- ▶ The base case is expressed as a fact, not referring to any smaller problems.
- ▶ We now have a *recursive definition*:

$$S(n) = \begin{cases} 1 & n = 1 & (\text{base case}) \\ S(n-1) + n & n \geq 2 & (\text{recursive step}) \end{cases}$$

- ▶ $S(4) = S(3) + 4 = S(2) + 3 + 4 = S(1) + 2 + 3 + 4 = 1 + 2 + 3 + 4$

Arithmetic Sum: A Recursive Solution

- From the recursive definition a recursive algorithm to compute $S(n)$ can be constructed:

ARITHMSUMREC(N)

1. If $N = 1$
 - 1.1 return 1
2. Else
 - 2.1 return ARITHMSUMREC($N-1$) + N

Example: Executing ArithmSumRec(5)

ARITHMSUMREC(N)

1. If $N = 1$
 - 1.1 return 1
2. Else
 - 2.1 return ARITHMSUMREC(N-1) + N

Executing ArithmSumRec(5) \Rightarrow 5 calls to ArithmSumRec(...)

ArithmSumRec(5)

ArithmSumRec(4)

ArithmSumRec(3)

ArithmSumRec(2)

ArithmSumRec(1)

return 1

// base case

return 1 + 2

(= 3)

return 3 + 3

(= 6)

return 6 + 4

(= 10)

return 10 + 5

(= 15)

Recursion

- ▶ Compute a solution to a problem using a smaller (but similar) problem is called *recursion*.
- ▶ In general, recursion \Rightarrow a method calls itself.
- ▶ In order not to be trapped in an infinite loop, a base case (at least one) must be part of the definition.
- ▶ Everything that can be done recursively, can also be done iteratively but not always as easy.
- ▶ Recursive definitions and algorithms are common in mathematics and computer science.

Factorial: A Recursive Definition

- ▶ The factorial, for example $5!$, is computed as:

$$5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$$

- ▶ The factorial ($N!$) for a positive integer N can be defined as:

$$N! = \begin{cases} 1 & \text{when } N = 1 \\ N \cdot (N - 1)! & \text{when } N > 1 \end{cases}$$

Note

- ▶ We use $(N-1)$ factorial to define N -factorial.
 \Rightarrow *recursion*.
- ▶ Repeated usage of the definition for $N!$ gives the answer

$$5! = 5 \cdot 4! = 5 \cdot 4 \cdot 3! = 5 \cdot 4 \cdot 3 \cdot 2! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

Palindrome: A Recursive Definition

- ▶ A string is a *simple palindrome* if it has the same text in reverse.
- ▶ Examples: x, anna, madam, abcdefedcba, yyyyyyyy
- ▶ A palindrome can be defined as:
 1. An empty string is a palindrome
 2. A string with the length 1 is a palindrome.
 3. A string is a palindrome if the first and last characters are equal, and all characters in between is a palindrome.
- ▶ 1 and 2 are our base cases
- ▶ 3 is our recursive step

Java: Recursive Method (1)

- A recursive method to compute n-factorial.

```
public int factorial (int n) {  
    if (n == 1)  
        return 1;  
    else  
        return n* factorial (n-1);  
}
```

Note

- Recursive methods calls themselves in one or several steps.
- Indirect recursion \Rightarrow call oneself after several steps.

```
public void a(int n) {  
    ...  
    ...  
    b(7);  
    ...  
}
```

```
public void b(int n) {  
    ...  
    ...  
    a(23);    // recursion!  
    ...  
}
```

Java: Recursive Method (2)

- ▶ A recursive method for checking a palindrome.

```
public boolean isPalindrome(char[] str, int p, int q) {  
    if (q <= p)                // Base case  
        return true;  
    else if (str[p] != str[q])  
        return false;  
    else  
        return isPalindrome(str, p+1, q-1);  
}
```

- ▶ Usage:

```
char[] word = "madam".toCharArray();    // Example  
boolean b = isPalindrome(word,0,4);      // true
```

```
char[] word = ...                       // In general  
b = isPalindrome(word,0,word.length-1); // true or false
```

Recursive Helper Methods

```
public static void main(String[] args) {  
    String word = "madam";  
    char[] chars = word.toCharArray();  
    boolean b = isPalindrome(chars, 0, chars.length-1);  
  
    // Using a helper method  
    b = isPalindrome(word);  
}  
  
public static boolean isPalindrome(String word) { // Helps to get started  
    return isPalindrome( word.toCharArray() , 0, chars.length-1);  
}  
  
public static boolean isPalindrome(char[] str , int p, int q) {  
    if (q <= p) // Base case  
        return true;  
    else if (str[p] != str[q])  
        return false;  
    else  
        return isPalindrome( str , p+1,q-1);  
}
```

Recursive Methods (In General)

- ▶ A recursive method consists of:
 - ▶ One or more *base cases* where “simple” results are given explicitly.
 - ▶ One or more recursive rules (or steps) where “larger” results are expressed using “smaller” results.
- ▶ **Note**
 - ▶ We use *recursive rules* until a problem has been reduced to size where a base case can be used.
 - ▶ No base case \Rightarrow infinite recursion \Rightarrow program will crash.

- ▶ **Crash in practice**

```
public static void main(String[] args) {  
    m(0);  
}
```

```
public static int m(int n) {  
    return m(n+1);    // no base case ==> infinite recursion  
}
```

The program runs for a second and raises a `StackOverflowError`
Stack: Part of JVM memory keeping track of ongoing calls.

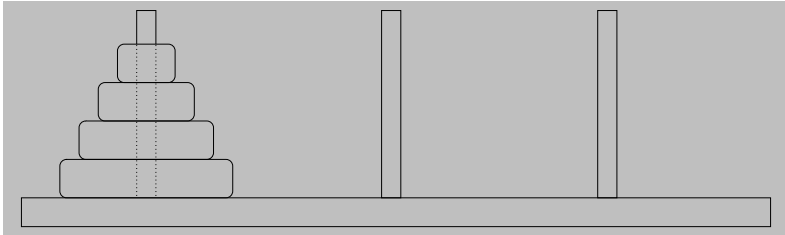
Examples and Exercises

- ▶ In the *Fibonacci* sequence the first two numbers are 0 and 1 and the others are the sum of the two previous numbers.

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, ...

- ▶ **Exercise:** Write a recursive method `int fib(int n)` that computes the n :th number in the Fibonacci sequence. For example `fib(0) = 0`, `fib(1) = 1`, and `fib(6) = 8`.
- ▶ **Exercise:** Write a recursive method `int mult(int a, int b)` that computes the multiplication $a \cdot b$ with the use of addition. Assume that both a and b are positive.
- ▶ **Exercise:** Write a recursive method `print(int[] a, int n)` printing the content of `a`:
 - ▶ a) starting from position 0 and onwards
 - ▶ b) in reverse order

Towers of Hanoi (Problem)



- ▶ **Problem:** Move the discs from one pole to the other.
- ▶ Rules:
 - ▶ Only one disc can be moved at a time.
 - ▶ A larger disc can not be placed on a smaller disc.
 - ▶ All discs must be on a pole, except for the one that is moved.
- ▶ See Section 18.7 in Liang for more details.

Tower of Hanoi

► Algorithm:

1. Move N-1 discs from start to help pole.
2. Move the lowest disc from start to end pole.
3. Move N-1 discs from help to end pole.

► Usage: moveTower(6,1,2,3)

6 is the number of discs, 1 is start pole, 2 is end pole, and 3 is temp pole

► Solution:

```
void moveTower(int NumDisks, int start, int end, int temp) {  
    if (numDisks == 1)  
        System.out.println("Move disc from "+start+" to "+end);  
    else {  
        moveTower(numDisks-1,start,temp,end);  
        System.out.println("Move disc from "+start+" to "+end);  
        moveTower(numDisks-1,temp,end,start);  
    }  
}
```

► See Section 18.7 in Liang for more details.

DirectoryMain.java

- Problem: List all subdirectories.

```
public static void main(String[] args) {  
    File startDir = new File("C:\\undervisning\\DA1021");  
    visitSub (startDir );           // Start recursive visit of subdirectories  
}
```

Printing :

```
1  DA1021  
2    kursutv  
3    labbar  
4    lectures  
5      array_list  
6      figures  
7    graphics1  
8      figures  
9    graphics2  
10     figures  
11    graphics3  
12     figures  
13    intro  
14     figures
```

Visit Subdirectories – Continued

- Visit and print each subdirectory recursively.

```
private static int depth = 1, count = 0;           // Indentation

private static void visitSub (File file) {
    if ( file . isDirectory () ) {
        printDir ( file );
        depth++;                                // Increase before visiting subdirectories
        File [] subs = file . listFiles ();
        for ( File f : subs)
            visitSub (f);
        depth--;                                // Decrease after visiting subdirectories
    }
}

private static void printDir (File file) { // Indented printing
    StringBuffer buf = new StringBuffer();
    for (int i=0; i<depth; i++)                // Add indentation
        buf.append(" ");
    System.out.println ((++count) + buf.toString() + file . getName());
}
```

The First 100 Fibonacci Numbers

- ▶ A recursive method for computing the N:th number in the Fibonacci sequence.

```
public int fib(int N) {  
    if (N==0)  
        return 0;  
    else if (N==1)  
        return 1;  
    else  
        return fib(N-1) + fib(N-2);  
}
```

Problem: Print the first 100 numbers in the Fibonacci sequence.

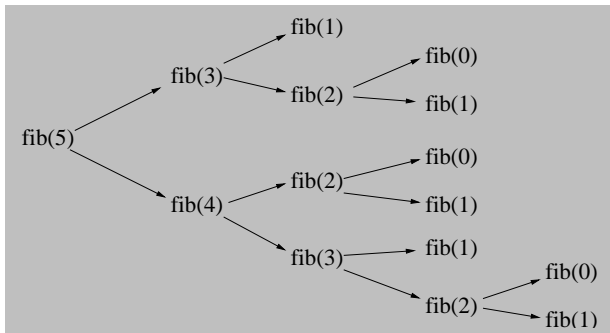
Simple!

```
for (int i=0;i<100;i++)  
    System.out.println ( fib(i) );
```

Result: The program races and then dies.

Exponential Number of Calls

- Computing `fib(5)`



- `fib(5)` takes 15 calls to `fib(N)`.
- `fib(6)` takes 25 calls to `fib(N)`.
- `fib(100)` takes an enormous amount of calls to `fib(N)`.
- All values between 1 and $N \Rightarrow$ the number is proportional to 2^N
 \Rightarrow the computer crashes for $N = 100$.

A better solution

```
public static void main(String[] args) {  
    int N = 90;           // N=100 does not work  
    long fm2 = 0, fm1 = 1, f;  
    for (int i = 3; i < N; i++) {  
        f = fm1 + fm2;  
        System.out.println (i + "\t" + f);  
        fm2 = fm1;  
        fm1 = f;  
    }  
}
```

The last five numbers

```
85  259695496911122585  
86  420196140727489673  
87  679891637638612258  
88  1100087778366101931  
89  1779979416004714189
```

- $N = 100$ does not work, the number is too large for a long.

A working solution for $N = 100$

- With the `BigInteger` library class it is possible to use $N = 100$.

```
public static void fiblterate (int N) {  
    BigInteger fm2 = new BigInteger("0");  
    BigInteger fm1 = new BigInteger("1");  
    BigInteger f = new BigInteger("0");  
    for (int i = 2; i < N; i++) {  
        f = fm1.add(fm2);  
        System.out.println (i + "\t" + f);  
        fm2 = fm1;  
        fm1 = f;  
    }  
}
```

- The library class `BigInteger` is designed to handle very large integer numbers

Assignment 3: Three Recursive Exercises

- Exercise 3: Print the N:th line in Pascal's triangle.

linje 0	→							1														
linje 1	→							1		1												
linje 2	→							1		2				1								
linje 3	→							1		3			3			1						
linje 4	→							1		4			6			4		1				
linje 5	→							1		5			10			10		5		1		
linje 6	→							1		6			15			20		15		6		1

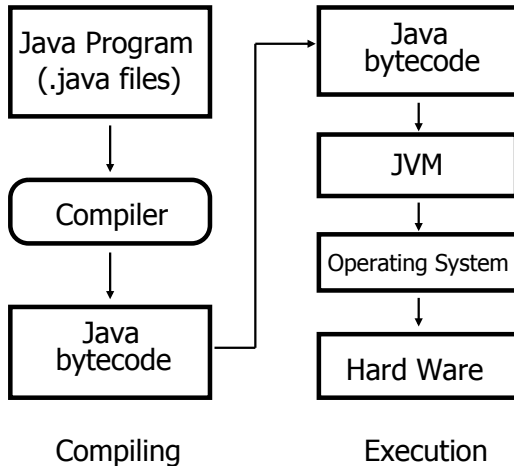
- ▶ The program must have a recursive method
 `int[] pascalLine(int order)`
- ▶ that calculates the n:th line in the triangle.

Exercises 1-3 are all about recursion. Not much coding. Tricky if you are not used to recursion.

Closing remarks on recursion

- ▶ At first glance recursive solutions to problems can seem difficult.
 - ▶ Mainly because they are different than an iterative solution.
- ▶ See it as yet another tool that is possible to use for some problems.
 - ▶ And as almost the only solution to some problems as we will see when discussing binary search trees.
- ▶ It is also important to remember that a recursive solution very seldom runs faster than an iterative – so make careful analysis before using it.

Java Compilation/Execution



Example Program – ArgsMain

```
package lecture2;  
  
public class ArgsMain {  
    public static void main(String[] args) {  
        System.out.println ("Arguments: "+args.length);  
        for (String s : args)  
            System.out.println ("\t"+s);  
    }  
}
```

Eclipse

- ▶ Open Run ⇒ Open Run Dialog ⇒ Arguments
- ▶ Write the program parameters in Program arguments
(I wrote: A few input-parameters)
- ▶ Press Apply and Close

Output

```
Arguments: 3  
A  
few  
input-parameters
```

Java in a Terminal Window

Compile/execute ArgsMain in package lecture2

- ▶ The fully qualified name of the program is

```
lecture2.ArgsMain
```

- ▶ Open a terminal window and go to (using `cd`) the directory containing lecture2. For example:

```
C:\software\dv507\src
```

- ▶ Compile

```
prompt> javac lecture2\ArgsMain.java
```

⇒ An executable file `ArgsMain.class` is created in the directory `lecture2`

- ▶ Execute

```
prompt> java lecture2.ArgsMain param1 param2 param3
```

⇒ run `ArgsMain` with the parameters `param1`, `param2`, `param3`

Note: This will only work if you have a *complete* java installation!

1. You have downloaded and installed a *Java Development Kit* (jdk)
2. You have configured the environment variables `Path` and `CLASSPATH`

Java Installation (For Windows)

- ▶ *Java Runtime Environment (JRE)* (e.g. jre1.6.0_02)
 - ▶ Everything needed to *execute* Java programs
 - ▶ A *Java Virtual Machine* (JVM) (\Rightarrow the command `java`)
 - \Rightarrow C:\ ... \jre1.6.0_02\bin\java.exe
 - ▶ The Java class library in bytecode format
 - \Rightarrow C:\ ... \jre1.6.0_02\lib\rt.jar
 - ▶ Present in most operating systems.
- ▶ *Java Development Kit (JDK)* (e.g. jdk1.6.0_04)
 - ▶ Everything needed to *develop* Java programs. JRE (as above) plus...
 - ▶ A java compiler (\Rightarrow the command `javac`)
 - \Rightarrow C:\ ... \jdk1.6.0_04\bin\javac.exe
 - ▶ A JavaDoc generator (\Rightarrow the command `javadoc`)
 - \Rightarrow C:\ ... \jdk1.6.0_04\bin\javadoc.exe
- ▶ Java API Documentation
 - \Rightarrow HTML documentation of Java's class library.
- ▶ Java Source Code
 - \Rightarrow Source code (.java filer) to Java's class library.

All are available on Oracle/Java's homepage. Current version: jdk1.13, update 2

Note: We are always referring to Java SE (Standard Edition)

Environment variables Path and CLASSPATH

```
prompt> javac lecture2\ArgsMain.java
'javac' is not recognized as a command, operable program or batch file.
```

- ▶ Problem: Windows cannot find the javac program.
- ▶ Path decides where Windows should look for programs.
- ▶ We need to add C:\ ... \jdk1.6.0_04\bin to the Path variable
- ▶ Open Control Panel ⇒ System ⇒ Advanced ⇒ Environmental variables
- ▶ and add C:\ ... \jdk1.6.0_04\bin for the variable Path

```
prompt>javac lecture2\MP3Main.java
.\lecture2\MP3Track.java:12: package javazoom.jl.player does not exist
.\lecture2\MP3Track.java:20: cannot find symbol: class Player
```

- ▶ Problem: Java compiler cannot find the package javazoom and the class Player
- ▶ CLASSPATH decides where (javac/java) should look.
- ▶ Open Environmental variables and add the missing path.
(You might need to create the CLASSPATH variable.)
- ▶ A minimum is: CLASSPATH .;C:\ ... \jre1.6.0_02\lib\rt.jar
That is, the present directory and Java's class library.

```
prompt> set ⇒ current environment variables are shown
```


However, Eclipse takes care of everything!

- ▶ Install Eclipse \Rightarrow Eclipse takes care of everything!
- ▶ Advantage: Easy to get started using Java
- ▶ Disadvantage: You never realise what is going on in the background

If time permits

Try at home to compile and run a Java program using the Terminal Window. It is strongly recommended if you want to learn how Java works.

MP3 in Java programs (External libraries)

Purpose: Learn how to use an external package.

- ▶ Looked around on the Internet for MP3 support in Java programs.
- ▶ Decided to use javazoom.JLayer from
<http://www.javazoom.net/projects.html>
 - ▶ Also possible to use Java Media Framework and ... (many available)
- ▶ Contents:
 - ▶ 10-20 classes (in bytecode) packed in one .jar-file (javazoom.jar)
 - ▶ Supports the development of programs playing MP3 files
 - ▶ Most important: MP3-to-Analogue decoder.
 - ▶ Cons: Playing is not threaded \Rightarrow blocks the program.
- ▶ Installation in Eclipse:
 1. Download javazoom.jar and save it
(as for example C:\software\jars\javazoom.jar)
 2. Update the Eclipse project Build Path to point the External Archieve
C:\software\jars\javazoom.jar
 3. Try to execute my test program MP3Main (next slide).

The .jar file javazoom.jar is a part of the Java Examples for this lecture.

Example Program MP3Main.java

```
try {  
    //String mp3Path = "C:\\software\\java_kurser\\mp3\\"; // My PC  
    String mp3Path = "/Users/jlnmsi/Software/java_kurser/mp3/"; // My Mac  
    String filename = mp3Path+"Kylie Minogue.mp3";  
  
    FileInputStream fis      = new FileInputStream(filename);  
    BufferedInputStream bis = new BufferedInputStream(fis);  
    Player player = new Player(bis);  
    player.play();           // Blocks main thread  
    System.out.println("Done - MP3 track completed!");  
}  
catch (JavaLayerException e){  
    e.printStackTrace();  
}
```

Notice

- ▶ The Player class comes from javazoom
- ▶ The print statement is not printed before track completed
⇒ main thread is blocked!

Assignment 3, Exercise 4: XChart

- ▶ XChart is a chart library \Rightarrow xy-plots, pie and bar charts
- ▶ XChart website: <http://knowm.org/open-source/xchart/>

This is an exercise in downloading, installing and using a number of unknown Java packages on the Internet. Therefore, we don't give too much instructions.

Usage Test your installation using `ScatterPlot.java` (part of lecture examples)

```
public static void main(String[] args) {  
    // Create and Customize Chart  
    XYChart chart = new XYChartBuilder().width(800).height(600).build();  
    chart.getStyler().setDefaultSeriesRenderStyle(XYSeriesRenderStyle.Scatter);  
    chart.getStyler().setChartTitleVisible(false);  
    chart.getStyler().setLegendPosition(LegendPosition.InsideSW);  
    chart.getStyler().setMarkerSize(5);  
  
    // Generate data  
    List<Double> xData = new ArrayList<Double>();  
    List<Double> yData = new ArrayList<Double>();  
    Random random = new Random();  
    int size = 1000;  
    for (int i = 0; i < size; i++) {
```