

Homework 6 - Problem 4

a) Reducing problem P to problem Q_1 - Finding the longest path for G_1 , s_1 and t_1 :

1. Construct G_1 , s_1 and t_1 :

Given you get G , S and t ,

Duplicate G into G_1 ,

Copy s into s_1 ,

Copy t into t_1 ,

2. Run algorithm A_{Q1} on G_1 , s_1 , and t_1

Now Given L:

If the length of the longest path from s_1 and t_1 is equal to the number of vertices in G , then there is an s-t hamiltonian path in G , otherwise there is no path.

b) Reducing problem P to problem Q_2 - Finding the shortest path for G_2 , s_2 and t_2

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1. Construct G_2 , s_2 and t_2 :

Given you get G , S and t ,

Duplicate G into G_2

Copy s into s_2

Copy t into t_2

2. Run algorithm A_{Q2} on G_2 , s_2 , and t_2

Now Given L:

If the length of the longest path from s_1 and t_1 is equal to the number of vertices in G , then there is an s-t hamiltonian path in G , otherwise there is no path.