

## Homework 6 - Problem 2

The algorithm helps find the quickest path from one starting point to every other location, then loops through to find if there is a negative cycle. If so returns "YES", otherwise returns "NO"

```
negativeCycle:
  Let graph be the graph to check
  Let n be the number of vertices
  Let m be the number of edges
  Let len be a list of size n + 1, to be the length to each location

  for each n:
    for each m: if new len is less than known len:
      Change current len to new len

  for m:
    if new len is still less than known len
      Return "YES" <- Negative Cycle found

  Return "NO"
```

This works because:

The algorithm correctly computes the shortest path from the source to every vertex. Then, the additional loop afterwards checks for negative-weight cycles.

Time Complexity:  $O(m \cdot n)$

The outer loop runs  $N-1$  times, and the inner loop runs  $M$  times for each for loop. In the worst case, the algorithm may need to relax all edges for each vertex in each iteration.