

Homework 2 - Problem 1

Algorithm that finds the maximum possible number of lines crossed by a horizontal line through a shape.

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Let Set A be an Set of the shape's Y values
Let Set B be an Set of the indices of each value of A
Set index = 0
findMaxCrossing:
    Let Set C be a copy of A
    Use MERGESORT to sort C and B //B sorted through C, Indexes of B align with C
    Set max, maxCurrent = 0;
    For n in C:
        Let point1 = B at same index as n
        Set rightPoint as the following point adjacent to n
        Set leftPoint as the point before adjacent to n

        If leftPoint has a different value to n then
            If leftpoint is larger than n then maxCurrent = maxCurrent + 1
            Else maxCurrent = maxCurrent - 1;
        If rightPoint has a different value to n then
            If rightpoint is larger than n then maxCurrent = maxCurrent + 1
            Else maxCurrent = maxCurrent - 1;

        If n is not the same as the proceeding n and maxCurrent is larger than max then
            max = maxCurrent
    Return max
```

This program produces the right output because it checks for all the points, and is sorted, meaning it will always check from one end to the other (smallest Y value -> largest Y value).

Time estimate: $O(n \log n)$

Proof (Master Theorem):

Using Case 2: $f(n) = \Theta(n^a (\log a \log b))$, $2T(n/2) + n$

Considering a: 2, and b: 2

This means using Case 2 that $f(n) = \Theta(n^a (\log 2 / \log 2)) = n^1$.