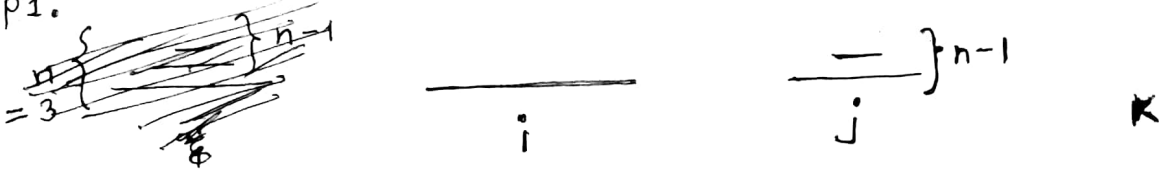


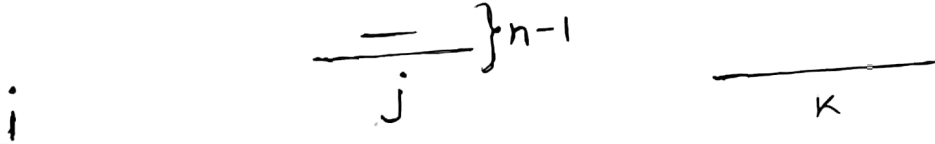
Tower of Hanoi:



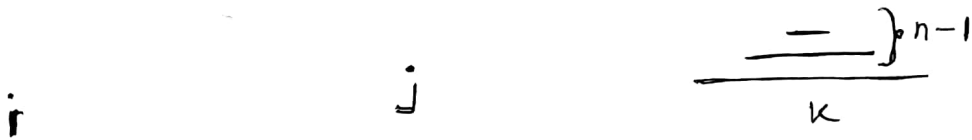
step 1:



step 2:



step 3:



When $n > 1$

$n-1, i \rightarrow j$
 $1, i \rightarrow k$
 $n-1, j \rightarrow k$

When $n = 1$

$i \rightarrow k$

```
void Hanoi(int n, int i, int j, int k) {
    if (n == 1)
        printf("%d → %d", i, k);
    else {
        Hanoi(n-1, i, j, k);
        printf("%d → %d", i, k);
        Hanoi(n-1, j, k, i);
    }
}
```

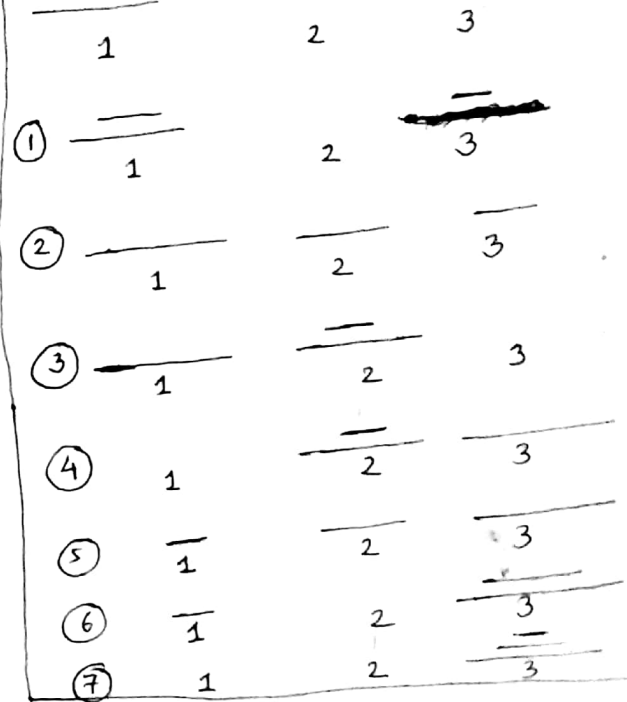
Find output sequence for Tower of Hanoi algorithm when $n=3$.

Tower of Hanoi algorithm

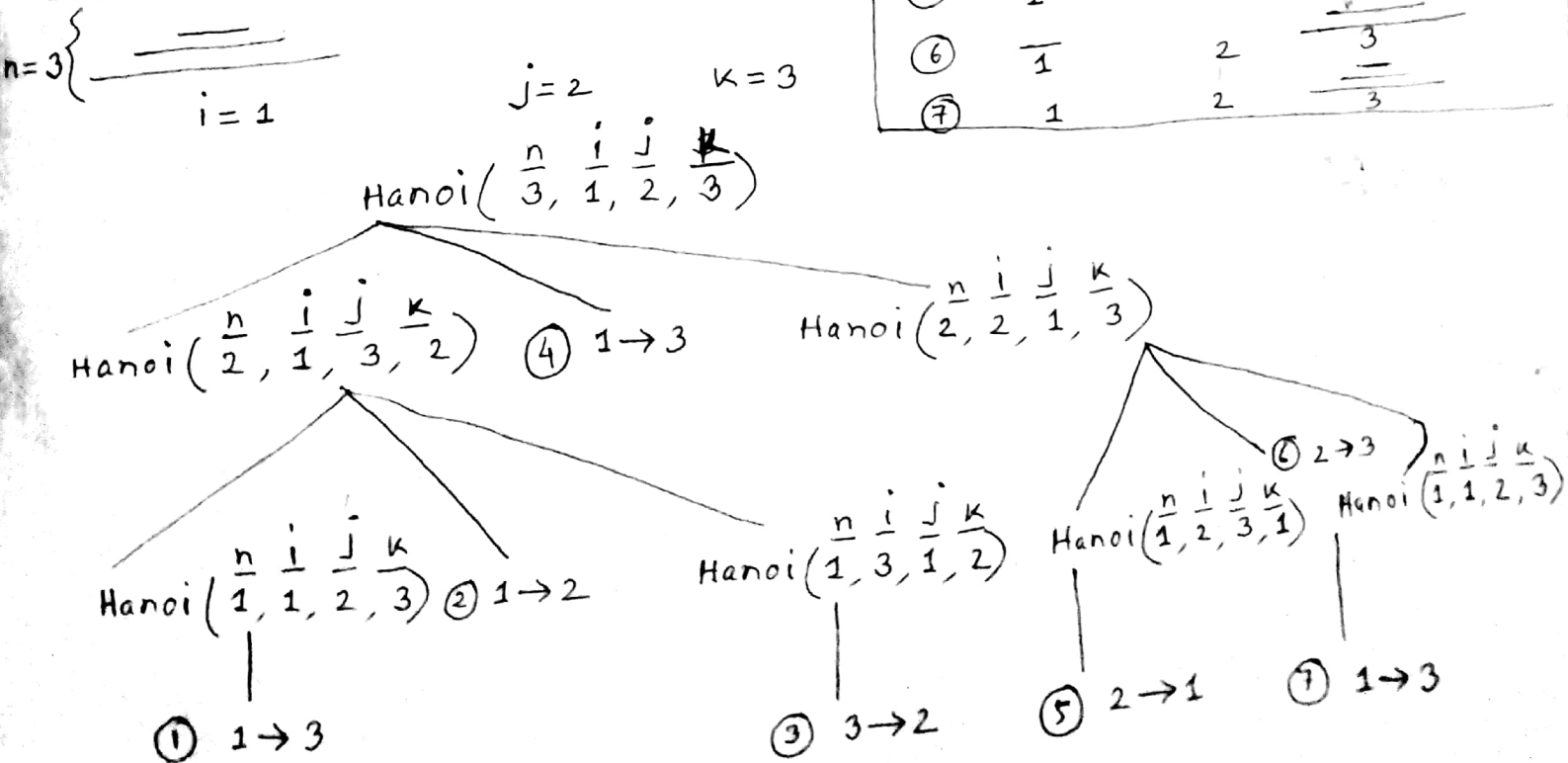
```
void Hanoi(int n, int i, int j, int k)
{
    if (n == 1)
        printf("%d → %d", i, k);
    else {
        Hanoi(n-1, i, k, j);
        printf("%d → %d", i, k);
        Hanoi(n-1, j, i, k);
    }
}
```

output sequence

- | | |
|---------|---------|
| ① 1 → 3 | ⑤ 2 → 1 |
| ② 1 → 2 | ⑥ 2 → 3 |
| ③ 3 → 2 | ⑦ 1 → 3 |
| ④ 1 → 3 | |



Recursion Tree for $n=3$



① Convert the following infix expression into postfix using stack
 $a + b - (c * d / e - f) \uparrow c$

Ans:

<u>Infix expression</u>	<u>stack</u>	<u>Postfix expression</u>
$a + b - (c * d / e - f) \uparrow c$		a
$+ b - (c * d / e - f) \uparrow c$		a
$b - (c * d / e - f) \uparrow c$	$+$	ab
$- (c * d / e - f) \uparrow c$	$+$	$ab +$
$(c * d / e - f) \uparrow c$	$-$	$ab +$
$c * d / e - f) \uparrow c$	$- ($	$ab + c$
$* d / e - f) \uparrow c$	$- ($	$ab + c$
$d / e - f) \uparrow c$	$- (*$	$ab + cd$
$/ e - f) \uparrow c$	$- (*$	$ab + cd *$
$e - f) \uparrow c$	$- (/$	$ab + cd * e$
$- f) \uparrow c$	$- (/$	$ab + cd * e /$
$f) \uparrow c$	$- (-$	$ab + cd * e / f$
$) \uparrow c$	$- (-$	$ab + cd * e / f -$
$\uparrow c$	$-$	$ab + cd * e / f -$
c	$- \uparrow$	$ab + cd * e / f -$
	$- \uparrow$	$ab + cd * e / f - c$
	\leftarrow	

~~Priority~~
 $\text{top(stack)} \gg \text{insert}$
 $\Rightarrow + \gg - \text{ (True)}$

$\text{top(stack)} \gg \text{insert}$
 $\Rightarrow * \gg / \text{ (True)}$

$\text{top(stack)} \gg \text{insert}$
 $\Rightarrow / \gg - \text{ True}$

$\text{top(stack)} \gg \text{insert}$
 $\Rightarrow - \gg \uparrow \text{ false}$

$ab + cd * e / f - c \uparrow -$

Postfix

Operator	Priority
$+$	1
$-$	1
$*$	2
$/$	2
\uparrow	3

Evaluate the Postfix expression when $a=1$, $b=2$, $c=1$
 $d=2$, $e=2$, $f=1$

Page-4

<u>Postfix expression</u>	<u>stack</u>	<u>operation</u>
$a b + c d * e / f - c \uparrow -$	\bullet	
$b + c d * e / f - c \uparrow -$	a	
$+ c d * e / f - c \uparrow -$	$a \ b$	
$c d * e / f - c \uparrow -$	3	$a + b = 1 + 2 = 3$
$d * e / f - c \uparrow -$	$3 \ c$	
$* e / f - c \uparrow -$	$3 \ c \ d$	
$e / f - c \uparrow -$	$3 \ 2$	$c * d = 1 * 2 = 2$
$/ f - c \uparrow -$	$3 \ 2 \ e$	
$f - c \uparrow -$	$3 \ 1$	$2 / e = 2 / 2 = 1$
$- c \uparrow -$	$3 \ 1 \ f$	
$c \uparrow -$	$3 \ 0$	$1 - f = 1 - 1 = 0$
$\uparrow -$	$3 \ 0 \ c$	
$-$	3	$0 \uparrow c = 0^1 = 0$
	3	$3 - 0 = 3$

Result = 3

Verification

$$\begin{aligned}
 & a + b - (c * d / e - f) \uparrow c \\
 &= 1 + 2 - (1 * 2 / 2 - 1) \uparrow 1 \\
 &= 3 - (1 - 1) \uparrow 1 \\
 &= 3 - 0 \uparrow 1 \\
 &= 3 - 0^1 \\
 &= 3 - 0 \\
 &= \boxed{3} \Rightarrow \text{Result}
 \end{aligned}$$