

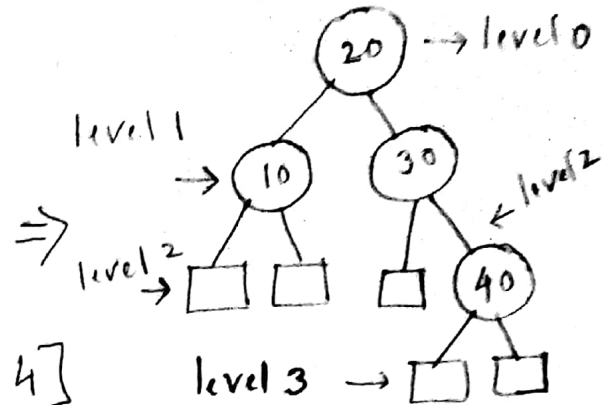
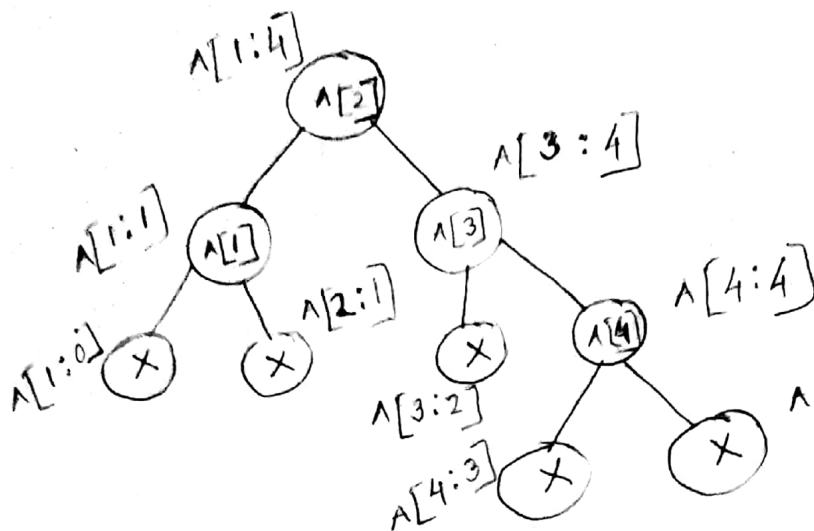
# Binary Search Tree

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Draw a binary search Tree for  $A[1:4]$

Ans:

A	10	20	30	40
	1	2	3	4



Binary Search Tree

$$I(T) = \text{Internal Path length} \\ = 0 + 1 + 1 + 2 = 4$$

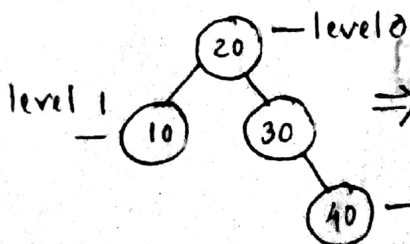
$$E(T) = \text{External Path length} \\ = 2 + 2 + 2 + 3 + 3 = 12$$

$$E(T) - I(T) = 2n \\ \Rightarrow 12 - 4 = 2 * 4$$

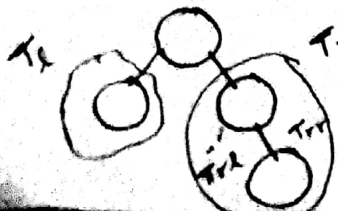
Height of a binary Tree

$$I(n) = \bigcirc = \text{internal node} \\ E(n) = \square = \text{External node} \\ E(n) = I(n) + 1 \\ \Rightarrow 5 = 4 + 1$$

$$\text{Tree} = \text{NULL} \quad \text{height} = -1 \\ \bigcirc \text{ single node, height} = 0 \\ \text{otherwise, height}(\text{Tree}) \\ = \max(\text{height}(T_L), \text{height}(T_R)) + 1$$



$$* \text{height}(\text{Tree}) = \max(\text{level}_i) = 2$$

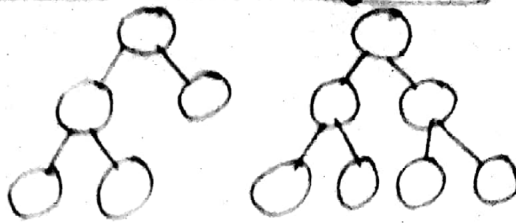


$$\begin{aligned} * \text{height}(T) &= \max(\text{height}(T_L), \text{height}(T_R)) + 1 \\ &= \max(0, \max(\text{height}(T_{LL}), \text{height}(T_{LR})) + 1) + 1 \\ &= \max(0, \max(-1, 0) + 1) + 1 \\ &= \max(0, 0 + 1) + 1 = 1 + 1 = 2 \end{aligned}$$

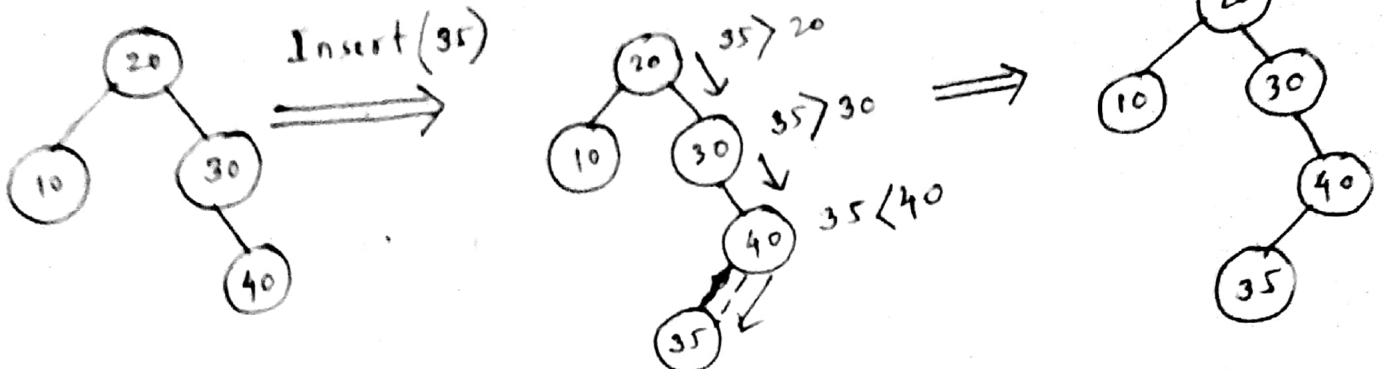
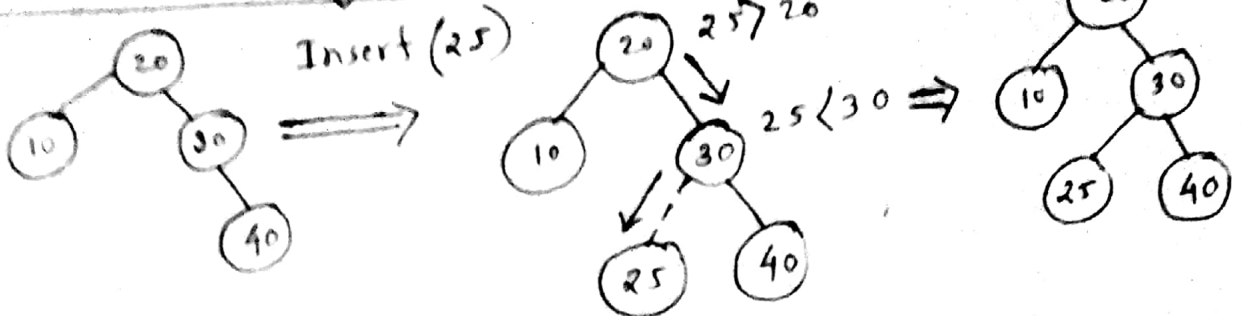
## Balanced Binary Tree:



## Completed Binary Tree:



## Insertion in a Binary Search Tree:



## Deletion from a Binary Search Tree:

