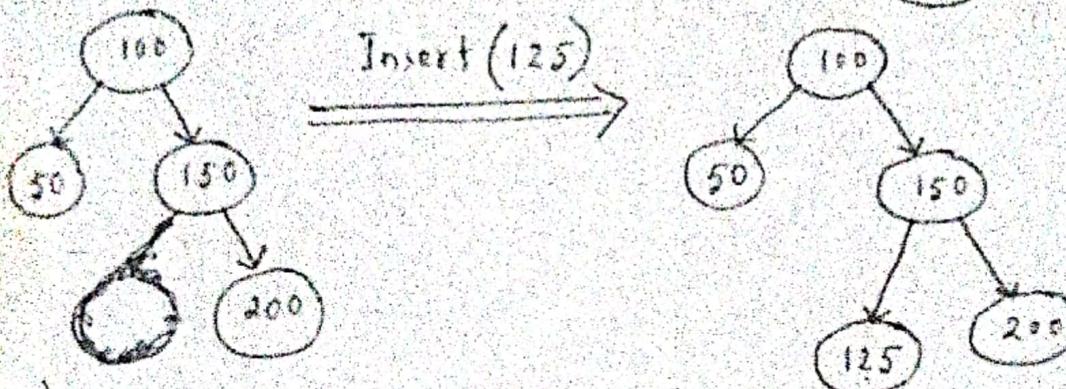
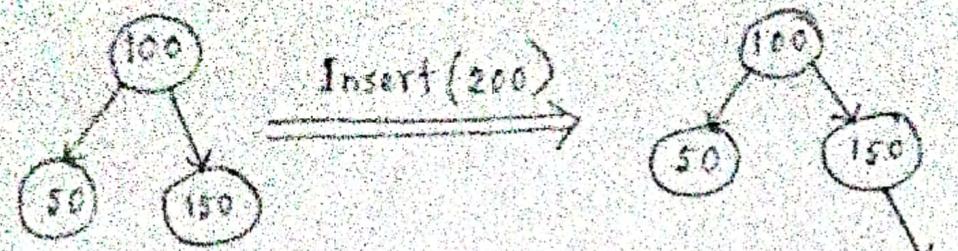


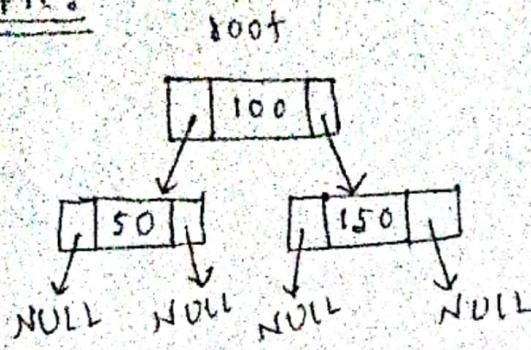
# Inserting a node in a binary search tree

1



Recursive algorithm

```
node *Insert( node *root, node *newnode){  
    if (root == NULL)  
        root = newnode newnode;  
    else if (root->data < newnode->data)  
        root->right = Insert( root->right, newnode);  
    else if (root->data > newnode->data)  
        root->left = Insert( root->left, newnode);  
    return root;  
}
```

Example:

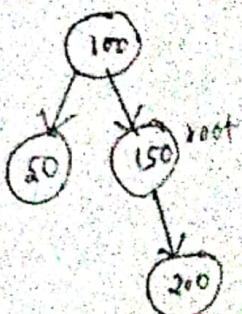
$\text{root} = \text{Insert}(\text{root}, \text{newnode})$

$\text{root} \rightarrow \text{right} = \text{Insert}(\text{root}, \text{newnode})$

$\text{root} \rightarrow \text{right} = \text{Insert}(\text{root}, \text{newnode})$

~~$\text{root} = \text{newnode}$~~

$= \text{newnode}$



## Naive Algorithm

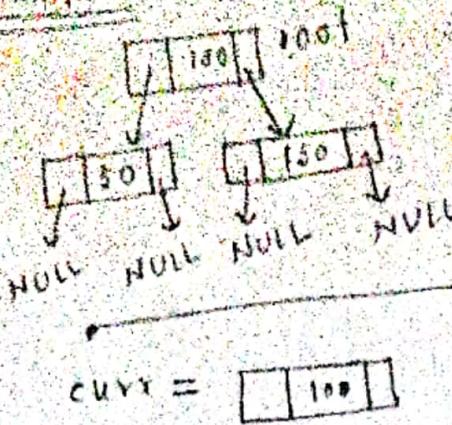
3

```
node *insert(node *root, int key) {
    node *tinsert, *curr, *prev;
    tinsert = (node *)malloc(sizeof(node));
    tinsert->data = key;
    tinsert->left = NULL;
    tinsert->right = NULL;

    curr = root;
    prev = NULL;
    while (curr != NULL) {
        prev = curr;
        if (curr->data > key)
            curr = curr->left;
        if (curr->data < key)
            curr = curr->right;
    }

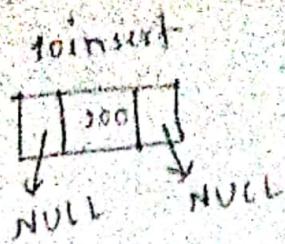
    if (prev == NULL)
        root = tinsert;
    else if (prev->data > key)
        prev->left = tinsert;
    else if (prev->data < key)
        prev->right = tinsert;
    return root;
}
```

Example:



$$key = 200$$

(4)



$$\text{curr} = \boxed{\begin{array}{|c|}\hline 100 \\ \hline\end{array}}$$

$$\text{prev} = \text{NULL}$$

while (true)  $\Rightarrow$   $\text{prev} = \boxed{\begin{array}{|c|}\hline 100 \\ \hline\end{array}}$  if ( $100 > 200$ )  $\text{if } 100 < 200 \text{ True}$   
 $\text{curr} = \boxed{\begin{array}{|c|}\hline 150 \\ \hline\end{array}}$

while (true)  $\Rightarrow$   $\text{prev} = \boxed{\begin{array}{|c|}\hline 150 \\ \hline\end{array}}$  if ( $150 > 200$ )  $\text{if } 150 < 200 \text{ False}$   
 $\text{curr} = \text{NULL}$

while (false)

if (false)

false

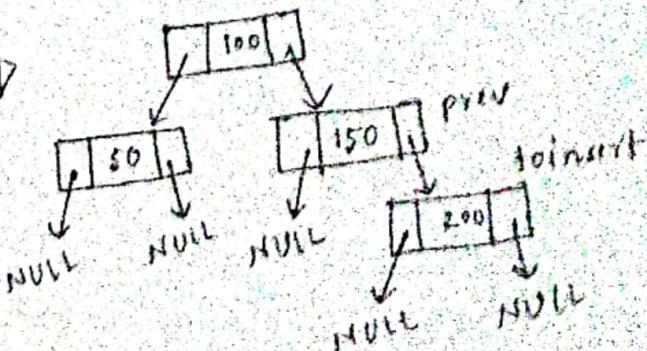
else if ( $150 > 200$ )

true  
else if ( $150 < 200$ )

$150 < 200$

$\text{prev} \rightarrow \text{right} = \text{toinsert} \Rightarrow$

=  $\boxed{\begin{array}{|c|}\hline 200 \\ \hline\end{array}}$   
toinsert



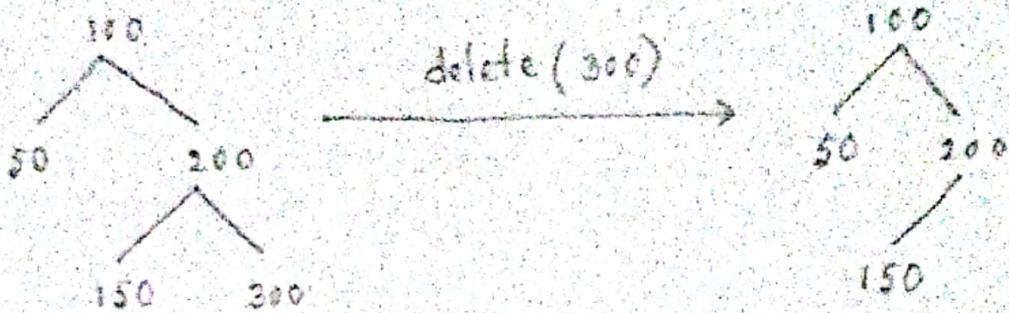
## Deletion from Binary Search Tree

(5)

### 2. Leaf node:

If the node is leaf (both left and right will be NULL), remove the node directly and free its memory.

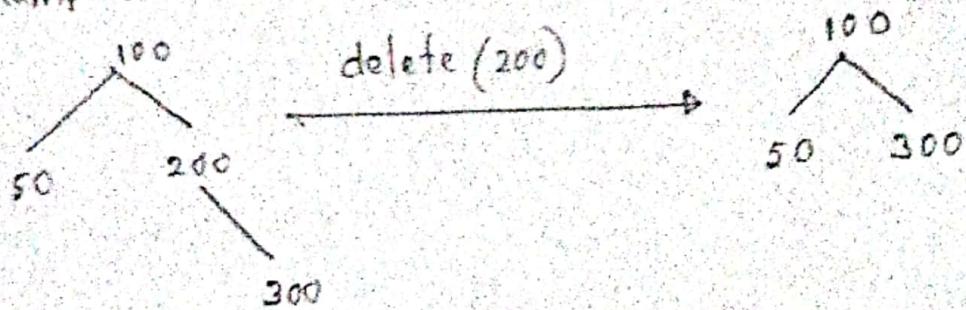
Example:



### 2. Node with Right child:

If the node has only right child (left will be NULL), make the node points to the right node and free the node.

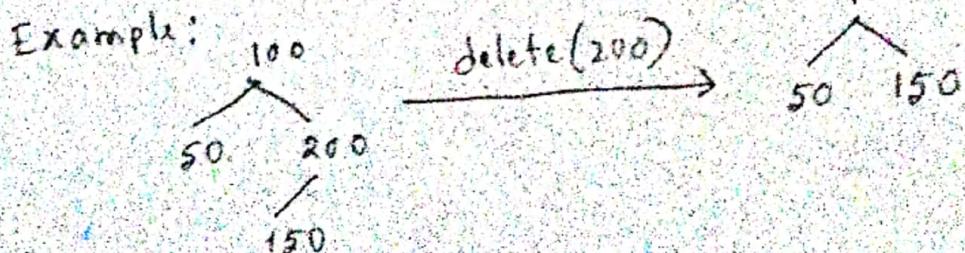
Example:



### 3. Node with Left child

If the node has only left child (right will be NULL), make the node points to the left node and free the node.

Example:

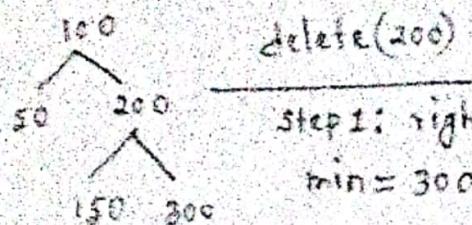


Note has both left and right child

If the node has left and right child

1. Find the smallest node in the right subtree, say min
2. Make  $\text{node} \rightarrow \text{data} = \text{min}$
3. Again delete the min node

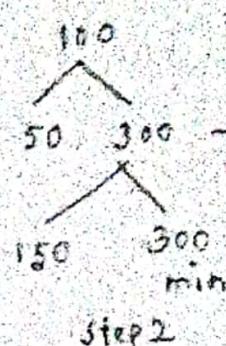
Example:



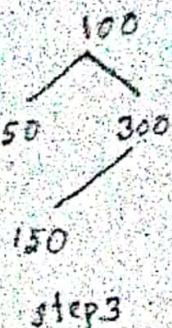
$\text{delete}(200)$

Step 1: right subtree

$\text{min} = 300$



Step 2



Step 3

### Deletion Function

```

node *Delete(node *root, int val) {
    if (root == NULL) return NULL;
    if (root->key < val)
        root->right = Delete(root->right, val);
    else if (root->key > val)
        root->left = Delete(root->left, val);
    else {
        if (root->left == NULL && root->right == NULL) {
            free(root);
            return NULL;
        }
        else if (root->left == NULL) {
            node *temp = root->right; free(root);
            return temp;
        }
        else if (root->right == NULL) {
            node *temp = root->left; free(root);
            return temp;
        }
        else {
            int rightMin = getRightMin(root->right);
            root->key = rightMin;
            root->right = Delete(root->right, rightMin);
        }
    }
    return root;
}
  
```