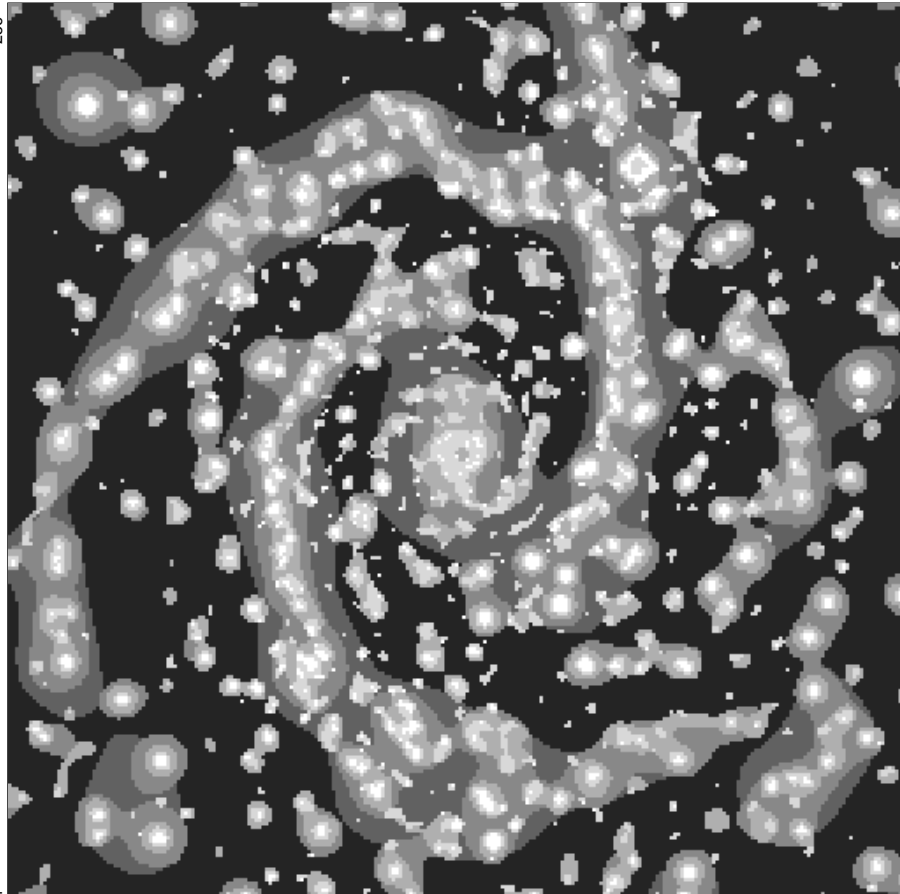


# The Multiresolution Analysis Software

- MR/1 V2.0: Multiresolution Environment
- MR/2 V1.0: Multiscale Entropy

CEA-SACLAY/SEI-SAP





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