

$$w = x^4 y^3 z^2 + x^3 y^2 + x^2 z + y + 3 \text{ at } (2, 1, 1)$$

$$\frac{dw}{dt} = \frac{\partial w}{\partial x} \frac{dx}{dt} + \frac{\partial w}{\partial y} \frac{dy}{dt} + \frac{\partial w}{\partial z} \frac{dz}{dt}$$

$$w_x = 4x^3 y^3 z^2 + 3x^2 y^2 + 2xz$$

$$w_y = x^4 3y^2 z^2 + x^3 2y + 1$$

$$w_z = x^4 y^3 2z + x^2$$

$$w_x(2, 1, 1) = 32 + 12 + 4 = 48$$

$$w_y(2, 1, 1) = 48 + 16 + 1 = 65$$

$$w_z(2, 1, 1) = 32 + 4 = 36$$

$$dw = 48dx + 65dy + 36dz$$