Capstone assessment for the undergraduate statistics major

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Assessment Outline

- **Goal: Measure learning outcomes of students upon completion of undergraduate statistics program (e.g. major)**
  - snapshot of student learning outcomes
  - facilitate cohort comparisons for program evaluation
  - comprehensive scope
- Constraints
  - closely aligned to (2014) ASA Curriculum Guidelines[1]
  - ease of use across institutions, instructors, years
- Outcomes
  - two capstone assessment tools (i.e., test & survey)
  - multi-year pilot
  - good psychometric quality

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[1] American Statistical Association Undergraduate Guidelines Workgroup (2014). 2014 Curriculum guidelines for undergraduate programs in statistical science. Alexandria, VA: American Statistical Association. http://www.amstat.org/education/curriculumguidelines.cfm

(2014) ASA Guidelines for Undergraduate Programs in Statistical Sciences

data. Such skills underpin strategies for assessing and ensuring data quality as part of data preparation and are a necessary precursor to many analyses[43].

- Use of one or more professional statistical software environments[44]
- Data management using software in a well-documented and reproducible way[45], data processing in different formats, and methods for addressing missing data
- Basic programming concepts (e.g., breaking a problem into modular pieces, algorithmic thinking[46], structured programming[47], debugging, and efficiency)
- Computationally intensive statistical methods (e.g., iterative methods, optimization, resampling, and simulation/Monte Carlo methods)[48]
- Use of multiple data tools[49], so graduates are not wedded to one and are better able to learn new technologies[50]

Mathematical Foundations

The study of mathematics lays the foundation for statistical theory. Undergraduate statistics majors should have a firm understanding of why and when statistical methods work. They should be able to communicate in the language of mathematics and explain the interplay between mathematical derivations and statistical applications.

- Calculus (e.g., integration and differentiation)[51]
- Linear algebra (e.g., matrix manipulations, linear transformations, projections in Euclidean space, eigenvalues/eigenvectors, and matrix decompositions)
- Probability (e.g., properties of univariate and multivariate random variables, discrete and continuous distributions)[52]
- Emphasis on connections between concepts in these mathematical foundations courses and their applications in statistics[53]

Statistical Practice

Strong communication skills complement technical knowledge and are particularly necessary for statisticians; graduates need technical skills to perform analyses and communication skills to understand clients' needs and then effectively discuss results and conclusions. Important practical skills include the following:

43 See Zhu et al. (2013) "Data acquisition and pre-processing in studies on humans: What is not taught in statistics classes," *The American Statistician*, 67(4):235–241, which includes a series of skills: (1) get to know the study; (2) assess the validity of variable coding; (3) assess data entry accuracy; (4) perform data cleaning; and (5) edit identified data errors.

44 Although we acknowledge that Microsoft Excel is a common platform for data exchange, we do not recommend it as a primary analysis environment.

45 Appropriate environments could include R, Python, and SAS, complemented by tools including shell scripts and knitr.

46 Futschek (2006) defines algorithmic thinking as a set of abilities related to constructing and understanding algorithms: (1) the ability to analyze a given problem; (2) the ability to precisely specify a problem; (3) the ability to find the basic actions that are adequate to the given problem; (4) the ability to construct a correct algorithm to a given problem using basic actions; (5) the ability to think about all possible special and normal cases of a problem; and (6) the ability to improve the efficiency of an algorithm. Futschek, G. (2006). "Algorithmic thinking: The key for understanding computer science," in R. Mittermeir (Ed.), *Informatics Education–The Bridge Between Using and Understanding Computers* (Vol. 4226, pp. 159–168). Berlin/Heidelberg: Springer. We consider this to be a necessary, but not sufficient component of "computational thinking."

47 We define structured programming as the ability to use functions and control structures (e.g., "for" loops).

48 This recommendation is consistent with the efforts of Conrad Wolfram and the Computer-Based Math initiative, *www.computerbasedmath.org* and *www.tinyurl.com/ted-wolfram*. The incorporation of these tools may be particularly valuable at the bachelor's level, since students will generally have less technical knowledge (and need to be able to simulate to generate insights and/or check analytic results).

49 Students should develop the capacity to manipulate formats such as CSV, JSON (JavaScript Object Notation, a data-interchange format that is easy to read, parse, and generate; see Nolan and Temple Lang (2014) *XML and Web Technologies for Data Sciences with R*), XML, databases (see, for example, Ripley (2001) "Using databases with R," *R News*, 1(1):18–20 and Wickham (2011) "ASA 2009 Data Expo," *Journal of Computational and Graphical Statistics*, 20(2):281–283), and text data. Because many faculty were not trained in these technologies, continuing education in this area needs to be made a priority.

50 We are not prescriptive regarding which technologies are incorporated into the curriculum, as long as they are sufficiently flexible and powerful. Many undergraduate statistics students develop expertise in environments such as R/RStudio, Python, and SAS.

51 Multivariate calculus is recommended.

52 Markov chains are a useful topic for undergraduate majors in statistics.

53 This linkage includes topics such as the delta method. In addition, many students might benefit from exposure to modeling and simulation in their mathematics courses as a way to reinforce their computational skills.

Comprehensive Undergraduate Statistics Program (CUSP) Assessment Strategy

- 95 competencies cited in 2014 ASA Guidelines
- single assessment tool likely not sufficient

# Competencies	ASA Guidelines Topic
37	Statistical Methods & Theory
16	Data Wrangling, Computing, & Data Science
11	Mathematical Foundations
18	Statistical Practice
9	Problem Solving
4	Discipline-Specific Knowledge

Comprehensive Undergraduate Statistics Program (CUSP) Assessments

- Direct assessment–CUSP Test
  - selected response test
  - approx. 1 hour duration
  - multiple institutions w. single cohort
  - single institution w. multiple cohorts
- Indirect assessment–CUSP Survey
  - inventory of all 95 competancies cited in ASA Guidelines
  - survey data self-reported by students
  - approx. 10-15 minutes duration
  - several cohorts from single institution

CUSP Survey

- **Benefits**
  - Easy implementation
  - Can be administered multiple times if desired
  - No problem including topics we don't teach
  - Includes demographics
- **Risks/Issues**
  - Reliability of self-reporting
  - Over/Underconfidence with content exposure

Excerpt

Statistical Theory

(scale: [1] very low / never learned; [2] low; [3] fair; [4] good; [5] very good; [6] excellent; [7] exceptional)

Please rate your **current level of knowledge/competency** related to:

	1	2	3	4	5	6	7
Distributions of random variables	○	○	○	○	○	○	○
Likelihood theory	○	○	○	○	○	○	○

CUSP Test Design

- Selected response assessment tool with broad coverage
- 33 tasks; some with multiple parts
  - 9 testlets
  - 24 conventional MC questions
- several tasks/subtasks assess multiple competancies
  - diminishing weight attributed to successive competancies (1, 1/2, 1/4, ...)
  - 86 points possible
- Mix of original tasks & some from established instruments (used with permission)
  - 2 from the REGRESS assessment[2]
  - 9 from the CAOS assessment[3]

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[2]Enders, F. (2013). Do clinical and translational science graduate students understand linear regression? Development and early validation of the REGRESS quiz. *Clinical and Translational Science, 6*(6). p. 444-451.

[3]delMas, R., Garfield, J., Ooms, A., Chance, B. (2007). Assessing students' conceptual understanding after a first course in statistics. *Statistics Education Research Journal, 6*. p. 28-58.

CUSP Test

Excerpt (partial item)

driver or passenger side.

Study design dictates appropriate statistical analysis, but often there is more than one reasonable approach to the analysis. Evaluate whether each of the following analysis suggestions is VALID or NOT VALID for testing and estimating the difference in durability for the two brake pad materials:

	Valid	NOT Valid
paired t-test for brake pad difference of each car (DriverSide - PassengerSide)	○	○
paired t-test for brake pad difference of each car (Experimental - Standard)	○	○
ANOVA with car as a blocking variable	○	○

CUSP Test

- **Benefits**
  - test statistical "reflexes" of students
  - built-in "CAOS" subtest
  - objective measure of student competancies
    - for individual students
    - for a cohort of students
    - aggregate useful for program evaluation
  - Easy implementation
- **Risks/Issues**
  - Variable use conditions may jeopardize comparisons
  - Scope constrained by test fatigue
  - Includes topics we don't necessarily teach
  - Longer to implement

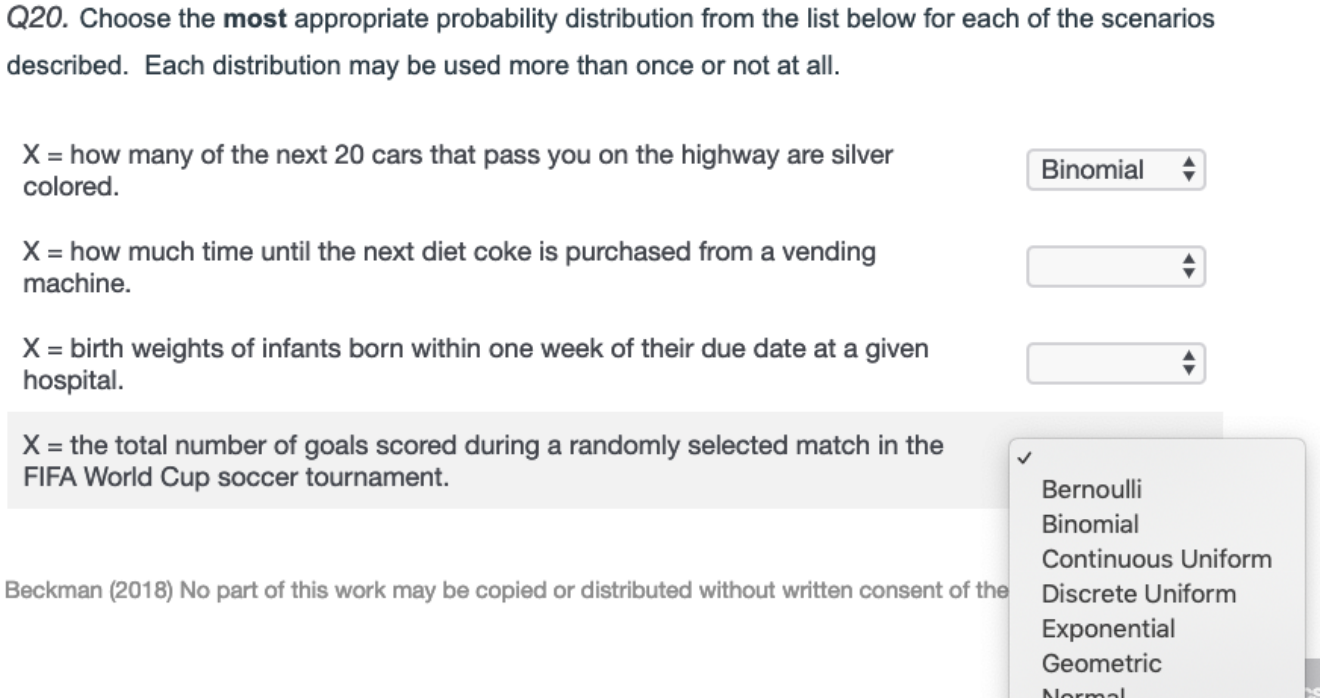
Preliminary Item Functioning Analysis

- Benchmarks for item statistics[4]
  - Unidimensionality assumed by common methods of assessment evaluation
  - Cronbach alpha (reliability)
  - descrimination > 0.15 preferred
  - $0.6 <$ proportion correct < 0.9
- Results
  - PCA evidence supports unidimensionality
  - Cronbach alpha $= 0.81$
  - $30/33$ items with discrimination > 0.15
  - $9/33$ items in recommended difficulty range
  - $21/33$ items with $> 50\%$ correct

[4] Haladyna, T. M., & Rodriguez, M. C. (2013). *Developing and validating test items*. Routledge: New York.

Item discrimination

- Item discrimination < 0.15
  - (21% correct) Validity of models aligned to a study design
  - (3.6% correct) Strategies to maximize likelihood
  - (40% correct) CAOS task about CI interpretation
- Best item discrimination
  - (discrim $= 0.59$) Probability distributions task
  - (discrim $= 0.50$) Histograms & std deviation task
  - (discrim $= 0.46$) OLS regression assumptions task



Future work

Shorter term goals

- Streamline logistics for wider implementation
- Link CUSP Survey data to CUSP Test outcomes
- Expand item bank

Longer term goals

- Experimentation with short/long forms
- Alternative or additional tools for more complete alignment to ASA Guidelines

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Discussion

Backup slides

CUSP Test blueprint alignment to ASA Guidelines

Section	Subsection	Target Weight (%)
Statistical Methods and Theory	Statistical Theory	18.0
Statistical Methods and Theory	Exploratory Data Analysis	6.0
Statistical Methods and Theory	Design of Studies	18.0
Statistical Methods and Theory	Statistical Models	18.0
Data Wrangling Computation and Data Science	Software and Tools	0.0
Data Wrangling Computation and Data Science	Accessing and Wrangling Data	4.5
Data Wrangling Computation and Data Science	Basic Programming Concepts	1.5
Data Wrangling Computation and Data Science	Computationally Intensive Statistical Methods	4.0
Mathematical Foundations	Calculus	0.0
Mathematical Foundations	Linear Algebra	0.0
Mathematical Foundations	Probability	2.5
Mathematical Foundations	Connecting mathematical foundations & applications in statistics	2.5
Statistical Practice	Communication	0.0
Statistical Practice	Collaboration	0.0
Statistical Practice	Ethical Issues	5.0
Statistical Practice	Opportunities for Authentic Practice	0.0
Problem Solving	Complex open-ended problems	2.2
Problem Solving	Scientific method and statistical problem-solving cycle	12.8
Discipline-Specific Knowledge	Discipline-Specific Knowledge	5.0

Student Results (Front)

CUSP Test: Student Summary Report

Report Generated: April 02, 2019

STUDENT DEMO (demo@psu.edu)

The Capstone Undergraduate Statistics Program (CUSP) Assessment measures learning outcomes of students in undergraduate statistics programs (e.g. majors) against the competencies cited in the 2014 ASA Guidelines for Undergraduate Programs in Statistical Sciences.[1] The 2014 ASA Guidelines are aligned to 6 major sections, with several subsections.

This assessment also included items from the Comprehensive Assessment of Outcomes in Statistics (CAOS) Test which includes topics accessible to introductory statistics students. CAOS tasks were selected assess common misconceptions that persist even among advanced undergraduate statistics students.

Additional remarks about scoring

Multiple choice items were scored with 2 points possible; multiple select items (i.e. "valid" or "NOT valid") were scored 1 point for each statement/decision task. Items pertinent to more than one competency of the 2014 ASA Guidelines were applied accordingly with diminishing weight credited to secondary or tertiary competencies (e.g. 100%, 50%, 25%). Consequently, some items inform more than one competency aligned to the 2014 ASA Guidelines. This assessment seeks to expose variability among students (like a standardized test) and not to certify achievement against a fixed competency standard (like a driver's license test), so scores near 50% are typical.

CUSP Test Blueprint

By design, some sections of the 2014 ASA Guidelines were given more or less weight than others in the CUSP Test. The development team established the following weights based on (1) priority in the curriculum and (2) feasibility for a selected-response assessment design.

Section	Subsection	Target Weight (%)
Statistical Methods and Theory	Statistical Theory	18.0
Statistical Methods and Theory	Exploratory Data Analysis	6.0
Statistical Methods and Theory	Design of Studies	18.0
Statistical Methods and Theory	Statistical Models	18.0
Data Wrangling Computation and Data Science	Software and Tools	0.0
Data Wrangling Computation and Data Science	Accessing and Wrangling Data	4.5
Data Wrangling Computation and Data Science	Basic Programming Concepts	1.5
Data Wrangling Computation and Data Science	Computationally Intensive Statistical Methods	4.0
Mathematical Foundations	Calculus	0.0
Mathematical Foundations	Linear Algebra	0.0
Mathematical Foundations	Probability	2.5
Mathematical Foundations	Connecting mathematical foundations & applications in statistics	2.5
Statistical Practice	Communication	0.0
Statistical Practice	Collaboration	0.0
Statistical Practice	Ethical Issues	5.0
Statistical Practice	Opportunities for Authentic Practice	0.0
Problem Solving	Complex open-ended problems	2.2
Problem Solving	Scientific method and statistical problem-solving cycle	12.8
Discipline-Specific Knowledge	Discipline-Specific Knowledge	5.0

[1] American Statistical Association Undergraduate Guidelines Workgroup (2014). 2014 Curriculum guidelines for undergrad-

Student Results (Back)

Penn State University Summary (n = 107 students)

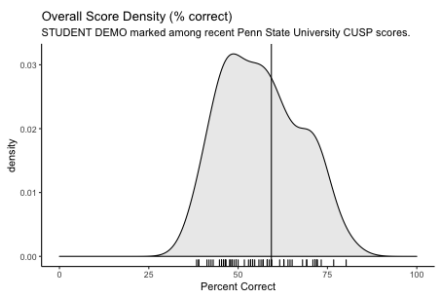
Summary Statistics

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
Overall Score (%)	31.98	48.26	56.10	57.01	66.86	84.88
CUSP Score (%; excl. CAOS items)	34.03	47.40	55.56	55.99	64.58	83.33
CAOS Score (%; excl. CUSP items)	7.14	50.00	64.29	62.24	78.57	100.00

Penn State University CUSP Test Outcomes Aligned to 2014 ASA Guidelines

Section Desc.	Subsection Desc.	% Correct	Items
Statistical Methods and Theory	Statistical Theory	64.0	5
Statistical Methods and Theory	Exploratory Data Analysis	33.8	2
Statistical Methods and Theory	Design of Studies	60.5	6
Statistical Methods and Theory	Statistical Models	58.0	11
Data Wrangling Computation and Data Science	Software and Tools	68.0	2
Data Wrangling Computation and Data Science	Accessing and Wrangling Data	53.0	1
Data Wrangling Computation and Data Science	Computationally Intensive Statistical Methods	57.8	2
Mathematical Foundations	Probability	48.3	2
Mathematical Foundations	Connecting mathematical foundations & applications in statistics	72.0	1
Statistical Practice	Ethical Issues	51.4	1
Problem Solving	Complex open-ended problems	21.5	1
Problem Solving	Scientific method and statistical problem-solving cycle	59.2	8

Results: STUDENT DEMO



Description	Result
Overall Score (%)	59
Class rank on test (62 students)	21
Rank among participating institutions (%-ile)	70
CUSP Score (%; excl. CAOS)	57
CAOS Score (%; excl. CUSP)	71

Performance Summary Aligned to 2014 ASA Guidelines (excludes CAOS Items)

Section Desc.	Subsection Desc.	% Correct	Items
Statistical Methods and Theory	Statistical Theory	73.3	5
Statistical Methods and Theory	Exploratory Data Analysis	50.0	2
Statistical Methods and Theory	Design of Studies	92.3	6
Statistical Methods and Theory	Statistical Models	47.1	11
Data Wrangling Computation and Data Science	Software and Tools	66.7	2
Data Wrangling Computation and Data Science	Accessing and Wrangling Data	100.0	1
Data Wrangling Computation and Data Science	Computationally Intensive Statistical Methods	44.4	2
Mathematical Foundations	Probability	0.0	2
Mathematical Foundations	Connecting mathematical foundations & applications in statistics	62.5	1
Statistical Practice	Ethical Issues	80.0	1
Problem Solving	Complex open-ended problems	100.0	1
Problem Solving	Scientific method and statistical problem-solving cycle	60.3	8

Scree plot of CUSP test data