

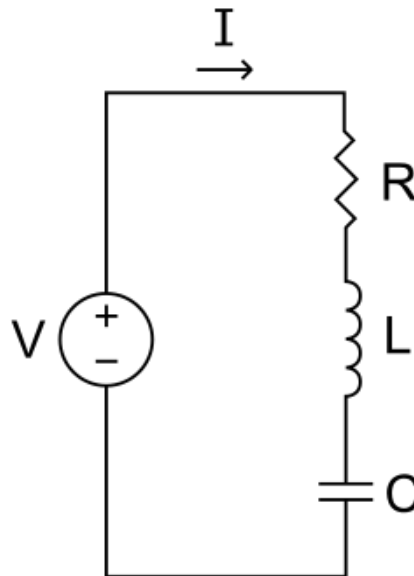
Mathematical Modelling - Assignment 6: Solving a 2nd-order DE with Matlab and Simulink.

Extra information: Sometimes you would like to select a single row or a single column from a matrix. Matlab offers a way to do it.

```
Try: M = rand(2,5)
      row1 = M(1,:)
      column2 = M(:,2)
```

Assignment 1: Solving a 2nd-order DE with Matlab

Given is the following RLC-circuit:



[reference: https://en.wikipedia.org/wiki/RLC_circuit]

In case of a DC-Voltage source, the differential equation belonging to this circuit is equal to

$$\frac{d^2 I(t)}{dt^2} + \frac{R}{L} \frac{dI(t)}{dt} + \frac{1}{LC} I(t) = 0$$

The theoretical derivation of this differential equation can be found in the Wikipedia reference given above.

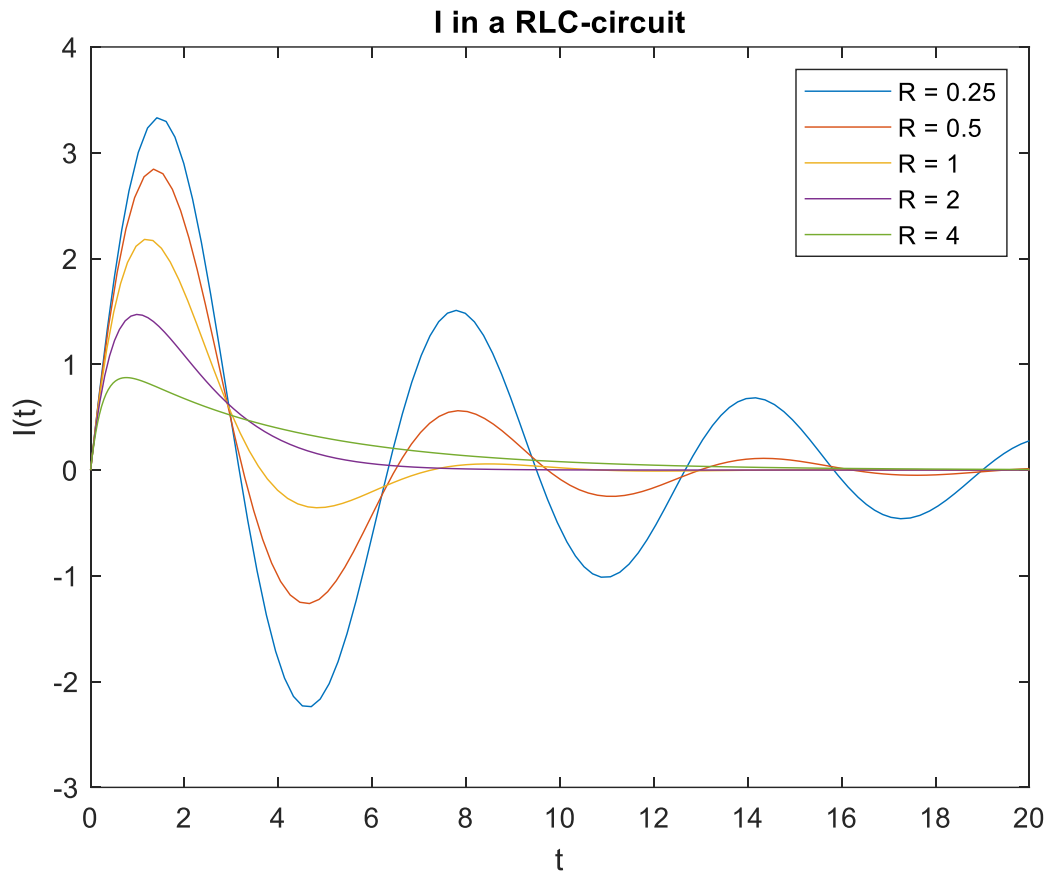
(a) Rewrite this second-order differential equation to a system of two first-order equations.

$$\begin{pmatrix} \frac{dz1}{dt} \\ \frac{dz2}{dt} \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ -\frac{1}{LC} & -\frac{R}{L} \end{pmatrix} \begin{pmatrix} z1 \\ z2 \end{pmatrix}$$

(b)

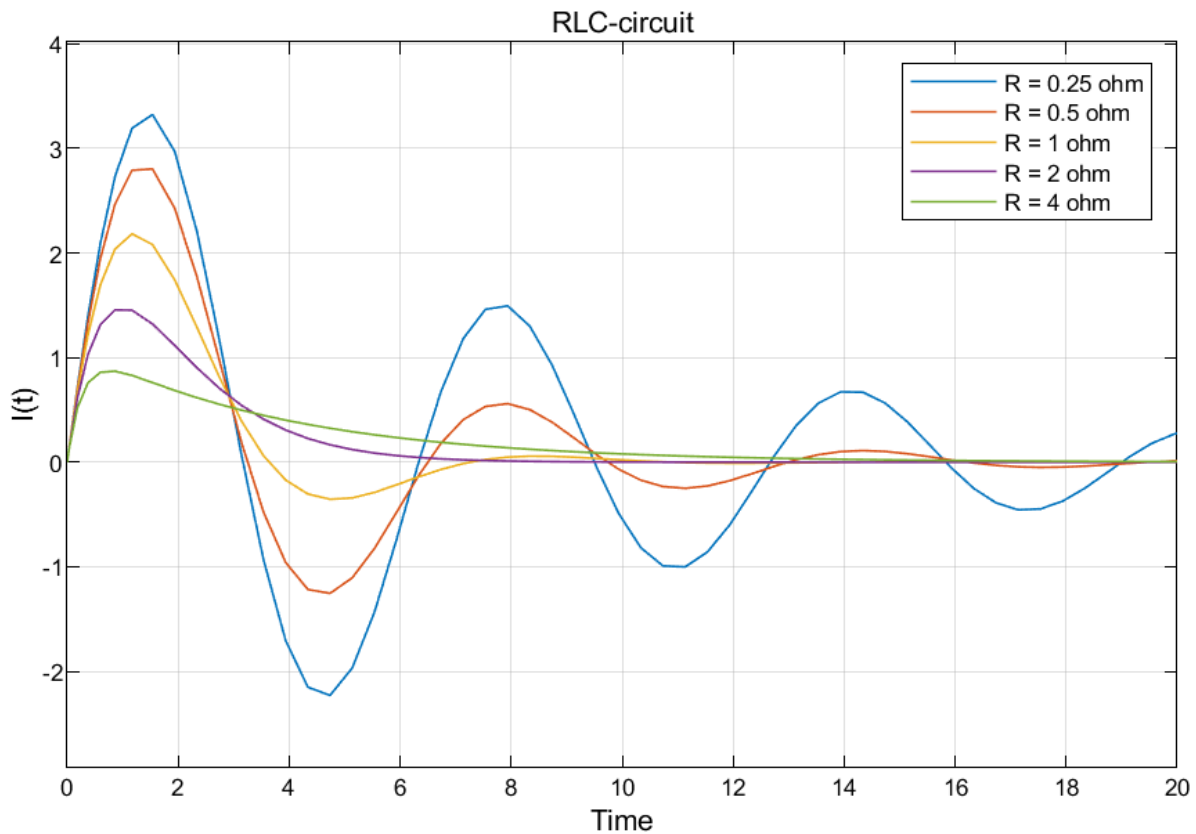
Given is $L=1\text{ H}$, $C=1\text{ F}$, $I(0) = 0\text{ A}$, $\left. \frac{dI(t)}{dt} \right|_{t=0} = 4\text{ A/s}$

Make a plot of the current $I(t)$ for the time period from $t = 0$ to 20 seconds, using five different resistor values of R being $0.25\ \Omega$, $0.5\ \Omega$, $1\ \Omega$, $2\ \Omega$ and $4\ \Omega$, using the Matlab command `ode45`. Plot the results for the different resistor values together in one single graph. Don't forget to use a title, correct labels for the x- and y-axis and a legend too.



Assignment 2: Solving a 2nd-order DE with Simulink.

Solve assignment 1 by making a Simulink model instead of solving it by Matlab code. To implement the model, you should use summation blocks, integrating blocks and/or gain blocks as well as a scope and input sources. Plot the results for the different resistor values together in one single scope. Make use of a legend in the scope. Finally, check if you obtain the same result as in assignment 1.



The Simulink graphs are the same as the Matlab graphs.