

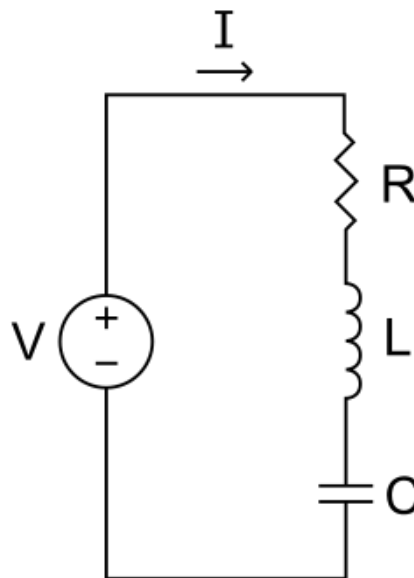
## Mathematical Modelling - Assignment 6: Solving a 2<sup>nd</sup>-order DE with Matlab and Simulink.

Extra information: Sometimes you would like to select a single row or a single column from a matrix. Matlab offers a way to do it.

```
Try: M = rand(2,5)
      row1 = M(1,:)
      column2 = M(:,2)
```

### Assignment 1: Solving a 2nd-order DE with Matlab

Given is the following RLC-circuit:



[reference: [https://en.wikipedia.org/wiki/RLC\\_circuit](https://en.wikipedia.org/wiki/RLC_circuit)]

In case of a DC-Voltage source, the differential equation belonging to this circuit is equal to

$$\frac{d^2 I(t)}{dt^2} + \frac{R}{L} \frac{dI(t)}{dt} + \frac{1}{LC} I(t) = 0$$

The theoretical derivation of this differential equation can be found in the Wikipedia reference given above.

(a) Rewrite this second-order differential equation to a system of two first-order equations.

(b) Given is  $L=1\text{ H}$ ,  $C=1\text{ F}$ ,  $I(0)=0\text{ A}$ ,  $\left. \frac{dI(t)}{dt} \right|_{t=0} = 4\text{ A/s}$

Make a plot of the current  $I(t)$  for the time period from  $t = 0$  to 20 seconds, using five different resistor values of  $R$  being  $0.25\ \Omega$ ,  $0.5\ \Omega$ ,  $1\ \Omega$ ,  $2\ \Omega$  and  $4\ \Omega$ , using the Matlab command `ode45`. Plot the results for the different resistor values together in one single graph. Don't forget to use a title, correct labels for the x- and y-axis and a legend too.

### Assignment 2: Solving a 2nd-order DE with Simulink.

Solve assignment 1 by making a Simulink model instead of solving it by Matlab code.

To implement the model, you should use summation blocks, integrating blocks and/or gain blocks as well as a scope and input sources. Plot the results for the different resistor values together in one single scope. Make use of a legend in the scope.

Finally, check if you obtain the same result as in assignment 1.