Grid and Graph based Path Planning Methods

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Lecture 04

B4M36UIR - Artificial Intelligence in Robotics

Overview of the Lecture

- Part 1 Grid and Graph based Path Planning Methods
 - Grid-based Planning
 - DT for Path Planning
 - Graph Search Algorithms
 - D* Lite
 - Path Planning based on Reaction-Diffusion Process Curiosity

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Grid-based Planning

DT for Path Planning

Graph Search Algorithms

Grid-based Planning

DT for Path Planning

Grid-based Planning

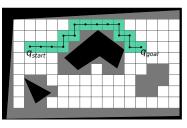
- A subdivision of C_{free} into smaller cells
- Grow obstacles can be simplified by growing borders by a diameter of the robot
- Construction of the planning graph G = (V, E) for V as a set of cells and E as the neighbor-relations
 - 4-neighbors and 8-neighbors





A grid map can be constructed from the so-called occupancy grid maps

E.g., using thresholding







Part I

Part 1 – Grid and Graph based Path Planning Methods

Grid-based Planning DT for Path Planning Graph Search Algorithms RD-based Planning Grid-based Planning DT for Path Planning RD-based Planning

Grid-based Environment Representations

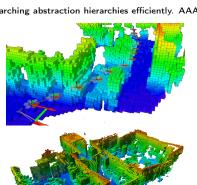
- Hiearchical planning
 - Coarse resolution and re-planning on finer resolution

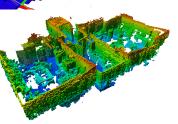
Holte, R. C. et al. (1996): Hierarchical A *: searching abstraction hierarchies efficiently. AAAI

- Octree can be used for the map representation
- In addition to squared (or rectangular) grid a hexagonal grid can be used
- 3D grid maps octomap

https://octomap.github.io

- Memory grows with the size of the environment
- Due to limited resolution it may fail in narrow passages of \mathcal{C}_{free}





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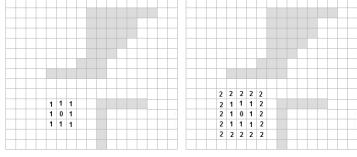
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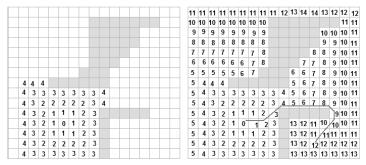
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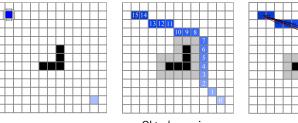
Example – Wave-Front Propagation (Flood Fill)





Path Simplification

- The initial path is found in a grid using 4-neighborhood
- The rayshoot cast a line into a grid and possible collisions of the robot with obstacles are checked
- The "farthest" cells without collisions are used as "turn" points
- The final path is a sequence of straight line segments



Example of Simple Grid-based Planning

Initial map with a robot and goal

for avoiding obstacles

■ Wave-front propagation – "flood fill"

■ Find a path using a navigation function

"Ray-shooting" technique combined

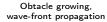
with Bresenham's line algorithm

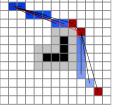
■ The path is a sequence of "key" cells

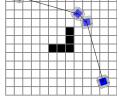
Obstacle growing

Path simplification

■ Wave-front propagation using path simplication







Ray-shooting

Simplified path

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Initial and goal locations

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Bresenham's Line Algorithm

Filling a grid by a line with avoding float numbers

```
■ A line from (x_0, y_0) to (x_1, y_1) is given by y = \frac{y_1 - y_0}{x_1 - x_0}(x - x_0) + y_0
```

```
CoordsVector& bresenham(const Coords& pt1, const 26
                                                              int twoDy = 2 * dy;
            Coords& pt2, CoordsVector& line)
                                                              int twoDyTwoDx = twoDy - 2 * dx; //2*Dy - 2*Dx
 2
                                                              int e = twoDy - dx; //2*Dy - Dx
        // The pt2 point is not added into line
                                                              int y = y0;
        int x0 = pt1.c; int y0 = pt1.r;
                                                              int xDraw, yDraw;
        int x1 = pt2.c; int y1 = pt2.r;
                                                              for (int x = x0; x != x1; x += xstep) {
                                                      32
                                                                 if (steep) {
        Coords p;
                                                      33
                                                                    xDraw = y;
 7
        int dx = x1 - x0;
        int dy = y1 - y0;
 8
                                                      34
                                                                    vDraw = x:
        int steep = (abs(dy) >= abs(dx));
                                                      35
                                                                 } else {
10
                                                      36
                                                                    xDraw = x;
        if (steep) {
                                                      37
11
           SWAP(x0, y0);
                                                                    yDraw = y;
12
           SWAP(x1, y1);
                                                      38
13
           dx = x1 - x0; // recompute Dx, Dy
                                                      39
                                                                 p.c = xDraw;
14
           dy = y1 - y0;
                                                      40
                                                                 p.r = yDraw;
15
                                                                 line.push back(p): // add to the line
16
        int xstep = 1;
                                                      42
17
        if (dx < 0) {
                                                                    e += twoDyTwoDx; //E += 2*Dy - 2*Dx
18
           xstep = -1;
                                                      44
19
           dx = -dx;
                                                      45
                                                                 } else {
20
                                                      46
                                                                     e += twoDy; //E += 2*Dy
21
                                                      47
        int ystep = 1;
22
        if (dy < 0) {
                                                      48
23
           ystep = -1;
                                                      49
                                                              return line;
24
           dy = -dy;
                                                      50
25
```

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DT for Path Planning

Graph Search Algorithms

D* Lite

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Distance Transform Path Planning

Algorithm 1: Distance Transform for Path Planning

```
for v := 0 to vMax do
    for x := 0 to xMax do
         if goal [x,y] then
             cell [x,y] := 0;
              cell [x,y] := xMax * yMax; //initialization, e.g., pragmatic of the use longest distance as <math>\infty;
repeat
    for y := 1 to (yMax - 1) do
         for x := 1 to (xMax - 1) do
              if not blocked [x,y] then
                  cell [x,y] := cost(x, y);
    for y := (yMax-1) downto 1 do
         for x := (xMax-1) downto 1 do
              if not blocked [x,y] then
                   cell[x,y] := cost(x, y);
until no change;
```

Distance Transform based Path Planning

- For a given goal location and grid map compute a navigational function using wave-front algorithm, i.e., a kind of potential field
 - The value of the goal cell is set to 0 and all other free cells are set to some very high value
 - For each free cell compute a number of cells towards the goal cell
 - It uses 8-neighbors and distance is the Euclidean distance of the centers of two cells, i.e., EV=1 for orthogonal cells or $EV = \sqrt{2}$ for diagonal cells
 - The values are iteratively computed until the values are changing
 - The value of the cell c is computed as

$$cost(c) = \min_{i=1}^{8} \left(cost(c_i) + EV_{c_i,c} \right),$$

where c_i is one of the neighboring cells from 8-neighborhood of the cell c

- The algorithm provides a cost map of the path distance from any free cell to the goal cell
- The path is then used following the gradient of the cell cost

Jarvis, R. (2004): Distance Transform Based Visibility Measures for Covert Path Planning in Known but Dynamic Environments

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Grid-based Planning DT for Path Planning Graph Search Algorithms

Distance Transform based Path Planning - Impl. 1/2

```
1 Grid& DT::compute(Grid& grid) const
                                                                      for (int r = H - 2; r > 0; --r) {
                                                                      for (int c = W - 2; c > 0; --c) {
                                                        36
                                                        37
                                                                         if (map[r][c] != FREESPACE) {
        static const double DIAGONAL = sqrt(2);
        static const double ORTOGONAL = 1;
                                                        38
                                                                            continue;
        const int H = map.H;
                                                        39
                                                                         } //obstacle detected
        const int W = map.W;
                                                        40
                                                                         double t[4];
        assert(grid.H == H and grid.W == W, "size");
                                                        41
                                                                         t[1] = grid[r + 1][c] + ORTOGONAL;
                                                        42
        bool anyChange = true;
                                                                         t[0] = grid[r + 1][c + 1] + DIAGONAL
 9
        int counter = 0;
                                                        43
                                                                         t[3] = grid[r][c + 1] + ORTOGONAL;
10
        while (anyChange) {
                                                        44
                                                                         t[2] = grid[r + 1][c - 1] + DIAGONAL;
                                                                         double pom = grid[r][c];
           anyChange = false;
           for (int r = 1; r < H - 1; ++r) {
                                                        46
                                                                         bool s = false;
13
              for (int c = 1; c < W - 1; ++c) {
                                                        47
                                                                         for (int i = 0; i < 4; i++) {
                 if (map[r][c] != FREESPACE) {
14
                                                        48
                                                                            if (pom > t[i]) {
15
                     continue;
                                                                               pom = t[i];
16
                 } //obstacle detected
                                                                                s = true;
17
                 double t[4];
18
                 t[0] = grid[r - 1][c - 1] + DIAGONAL; 52
19
                 t[1] = grid[r - 1][c] + ORTOGONAL;
                                                                         if (s) {
20
                 t[2] = grid[r - 1][c + 1] + DIAGONAL; 54
                                                                            anyChange = true;
21
                 t[3] = grid[r][c - 1] + ORTOGONAL;
                                                                            grid[r][c] = pom;
                 double pom = grid[r][c];
22
                                                        56
23
                 for (int i = 0; i < 4; i++) {</pre>
                                                        57
24
                    if (pom > t[i]) {
                                                        58
25
                        pom = t[i];
                                                        59
                                                                   counter++:
26
                                                        60
                                                                } //end while any change
                        anyChange = true;
27
                                                        61
                                                                return grid;
28
                 if (anyChange) {
                                                     A boundary is assumed around the rectangular map
30
                     grid[r][c] = pom;
31
32
33
```

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Grid-based Planning DT for Path Planning Graph Search Algorithms RD-based Planning Grid-based Planning DT for Path Planning Graph Search Algorithms RD-based Planning

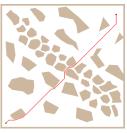
Distance Transform based Path Planning – Impl. 2/2

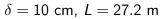
■ The path is retrived by following the minimal value towards the goal using min8Point()

```
Coords& min8Point(const Grid& grid, Coords& p)
                                                               CoordsVector& DT::findPath(const Coords& start,
 2
                                                                      const Coords& goal, CoordsVector& path)
        double min = std::numeric_limits<double>::max(); 23
        const int H = grid.H;
                                                                  static const double DIAGONAL = sqrt(2);
        const int W = grid.W;
                                                                  static const double ORTOGONAL = 1:
                                                                  const int W = map.W;
        for (int r = p.r - 1; r \le p.r + 1; r++) {
                                                                  Grid grid(H, W, H*W); // H*W max grid value
                                                          29
                                                                  grid[goal.r][goal.c] = 0;
           if (r < 0 \text{ or } r >= H) \{ \text{ continue}; \}
10
           for (int c = p.c - 1; c <= p.c + 1; c++) {
                                                         30
                                                                  compute(grid);
11
              if (c < 0 or c >= W) { continue; }
12
              if (min > grid[r][c]) {
                                                                  if (grid[start.r][start.c] >= H*W) {
13
                 min = grid[r][c];
                                                                     WARN("Path has not been found");
14
                                                                  } else {
                 t.r = r; t.c = c;
15
                                                                     Coords pt = start;
16
                                                                     while (pt.r != goal.r or pt.c != goal.c) {
17
                                                                        path.push_back(pt);
                                                                        min8Point(grid, pt);
                                                          39
20
                                                                     path.push_back(goal);
                                                          41
                                                          42
                                                                  return path;
```

DT Example











 $\delta = 30 \text{ cm}. \ L = 42.8 \text{ m}$

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Graph Search Algorithms

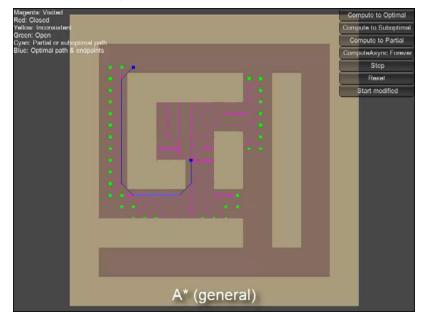
- The grid can be considered as a graph and the path can be found using graph search algorithms
- The search algorithms working on a graph are of general use, e.g.
 - Breadth-first search (BFS)
 - Depth first search (DFS)
 - Dijsktra's algorithm,
 - A* algorithm and its variants
- There can be grid based speedups techniques, e.g.,
 - Jump Search Algorithm (JPS) and JPS+
- There are many search algorithm for on-line search, incremental search and with any-time and real-time properties, e.g.,
 - Lifelong Planning A* (LPA*)

Koenig, S., Likhachev, M. and Furcy, D. (2004): Lifelong Planning A*. AlJ.

E-Graphs – Experience graphs

Phillips, M. et al. (2012): E-Graphs: Bootstrapping Planning with Experience Graphs. RSS.

Examples of Graph/Grid Search Algorithms

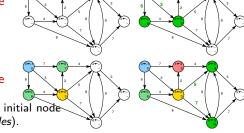


https://www.youtube.com/watch?v=U2XNjCoKZjM.mp4

Edsger W. Dijkstra, 1956

Dijkstra's Algorithm

- Dijsktra's algorithm determines paths as iterative update of the cost of the shortest path to the particular nodes
 - Let start with the initial cell (node) with the cost set to 0 and update all successors
 - Select the node
 - with a path from the initial node
 - and has a lower cost
 - Repeat until there is a reachable node
 - I.e., a node with a path from the initial node
 - has a cost and parent (green nodes).



The cost of nodes can only decrease (edge cost is positive). Therefore, for a node with the currently lowest cost, there cannot be a shorter path from the initial node.

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node 2 is over the node 3

3: After the expansion, there is a new path to the node 5

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4: The path does not improve for further

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1: After the expansion, the shortest path to the 2: There is not shorter path to the node 2 over the

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Dijkstra's Algorithm

Algorithm 2: Dijkstra's algorithm

```
/* g(s) := \infty; g(s_{start}) := 0 */
Initialize(s_{start});
PQ.push(s_{start}, g(s_{start}));
while (not PQ.empty?) do
   s := PQ.pop();
   foreach s' \in Succ(s) do
       if s'in PQ then
           if g(s') > g(s) + cost(s, s') then
              g(s') := g(s) + cost(s, s');
              PQ.update(s', g(s'));
       else if s' \notin CLOSED then
           g(s') := g(s) + cost(s, s');
          PQ.push(s', g(s'));
   CLOSED := CLOSED \bigcup \{s\};
```

Dijkstra's Algorithm – Impl.

```
1 dij->nodes[dij->start_node].cost = 0; // init
   void *pq = pq_alloc(dij->num_nodes); // set priority queue
    int cur_label;
    pq_push(pq, dij->start_node, 0);
    while ( !pq_is_empty(pq) && pq_pop(pq, &cur_label)) {
       node_t *cur = &(dij->nodes[cur_label]); // remember the current node
       for (int i = 0; i < cur->edge_count; ++i) { // all edges of cur
          edge_t *edge = &(dij->graph->edges[cur->edge_start + i]);
          node_t *to = &(dij->nodes[edge->to]);
          const int cost = cur->cost + edge->cost;
          if (to->cost == -1) { // node to has not been visited
11
12
             to->cost = cost:
13
             to->parent = cur_label;
             pq_push(pq, edge->to, cost); // put node to the queue
          } else if (cost < to->cost) { // node already in the queue
16
             to->cost = cost; // test if the cost can be reduced
17
             to->parent = cur_label; // update the parent node
             pq_update(pq, edge->to, cost); // update the priority queue
18
19
       } // loop for all edges of the cur node
    } // priority queue empty
   pq_free(pq); // release memory
```

A* Algorithm

■ A* uses a user-defined h-values (heuristic) to focus the search Peter Hart, Nils Nilsson, and Bertram Raphael, 1968

• Prefer expansion of the node n with the lowest value

$$f(n) = g(n) + h(n),$$

where g(n) is the cost (path length) from the start to n and h(n)is the estimated cost from n to the goal

- h-values approximate the goal distance from particular nodes
- Admissibility condition heuristic always underestimate the remaining cost to reach the goal
 - Let $h^*(n)$ be the true cost of the optimal path from n to the goal
 - Then h(n) is admissible if for all n: $h(n) \le h^*(n)$
 - E.g., Euclidean distance is admissible
 - A straight line will always be the shortest path
- Dijkstra's algorithm h(n) = 0

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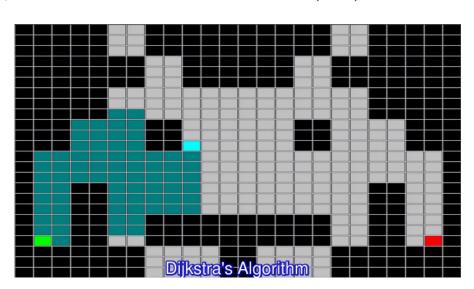
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Dijsktra's vs A* vs Jump Point Search (JPS)



https://www.youtube.com/watch?v=ROG4Ud081LY

A* Implementation Notes

- The most costly operations of A* are
 - Insert and lookup an element in the closed list
 - Insert element and get minimal element (according to f() value) from the open list
- The closed list can be efficiently implemented as a hash set
- The open list is usually implemented as a priority queue, e.g.,
 - Fibonacii heap, binomial heap, k-level bucket
 - binary heap is usually sufficient (O(logn))
- Forward A*
 - 1. Create a search tree and initiate it with the start location
 - 2. Select generated but not yet expanded state s with the smallest f-value, f(s) = g(s) + h(s)
 - 3. Stop if s is the goal
 - 4. Expand the state s
 - 5. Goto Step 2

Similar to Dijsktra's algorithm but it used f(s) with heuristic h(s) instead of pure g(s)

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Jump Point Search Algorithm for Grid-based Path Planning

■ Jump Point Search (JPS) algorithm is based on a macro operator that identifies and selectively expands only certain nodes (jump points)

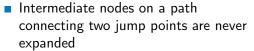
Harabor, D. and Grastien, A. (2011): Online Graph Pruning for Pathfinding on Grid Maps. AAAI.

■ Natural neighbors after neighbor prunning with forced neighbors because of obstacle













■ No preprocessing and no memory overheads while it speeds up A*

https://harablog.wordpress.com/2011/09/07/jump-point-search/

■ JPS+ – optimized preprocessed version of JPS with goal bounding

https://github.com/SteveRabin/JPSPlusWithGoalBounding http://www.gdcvault.com/play/1022094/JPS-Over-100x-Faster-than

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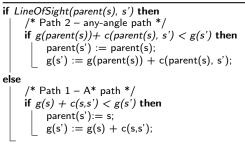
Theta* - Any-Angle Path Planning Algorithm

- Any-angle path planning algorithms simplify the path during the search
- Theta* is an extension of A* with LineOfSight()

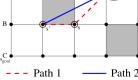
Nash, A., Daniel, K, Koenig, S. and Felner, A. (2007): Theta*: Any-Angle Path Planning on Grids. AAAI.

--- Path 1

Algorithm 3: Theta* Any-Angle Planning



Path 2: considers path from start to parent(s) and from parent(s) to s' if s' has line-of-sight to parent(s)



http://aigamedev.com/open/tutorials/theta-star-any-angle-paths/

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Path 2

A* Variants – Online Search

- The state space (map) may not be known exactly in advance
 - Environment can dynamically change
 - True travel costs are experienced during the path execution
- Repeated A* searches can be computationally demanding
- Incremental heuristic search
 - Repeated planning of the path from the current state to the goal
 - Planning under the **free-space** assumption
 - Reuse information from the previous searches (closed list entries):
 - Focused Dynamic A* $(D^*) h^*$ is based on traversability, it has been used, e.g., for the Mars rover "Opportunity"

Stentz, A. (1995): The Focussed D* Algorithm for Real-Time Replanning. IJCAI.

D* Lite – similar to D*

Koenig, S. and Likhachev, M. (2005): Fast Replanning for Navigation in Unknown Terrain. T-RO.

- Real-Time Heuristic Search
 - Repeated planning with limited look-ahead suboptimal but fast
 - Learning Real-Time A* (LRTA*)

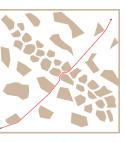
Korf, E. (1990): Real-time heuristic search. JAI

■ Real-Time Adaptive A* (RTAA*)

Koenig, S. and Likhachev, M. (2006): Real-time adaptive A*. AAMAS.

Theta* Any-Angle Path Planning Examples

■ Example of found paths by the Theta* algorithm for the same problems as for the DT-based examples on Slide 16



Both algorithms implemented in C++

 $\delta = 10 \text{ cm}$. L = 26.3 m

 $\delta = 30$ cm, L = 40.3 m

The same path planning problems solved by DT (without path smoothing) have $L_{\delta=10}=27.2$ m and $L_{\delta=30}=42.8$ m, while DT seems to be significantly faster

■ Lazy Theta* – reduces the number of line-of-sight checks

Nash, A., Koenig, S. and Tovey, C. (2010): Lazy Theta*: Any-Angle Path Planning and Path Length Analysis in 3D. AAAI.

http://aigamedev.com/open/tutorial/lazy-theta-star/

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Real-Time Adaptive A* (RTAA*)

- Execute A* with limited lookahead
- Learns better informed heuristic from the experience, initially h(s), e.g., Euclidean distance
- Look-ahead defines trade-off between optimality and computational cost
 - astar(lookahead)

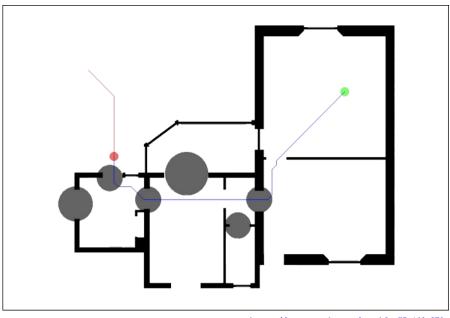
A* expansion as far as "lookahead" nodes and it terminates with the state s'

while $(s_{curr} \notin GOAL)$ do astar(lookahead); if s' = FAILURE then return FAILURE; for all $s \in CLOSED$ do H(s) := g(s') + h(s') - g(s);execute(plan); // perform one step return SUCCESS:

s' is the last state expanded during the previous A* search

Grid-based Planning DT for Path Planning Graph Search Algorithms D* Lite RD-based Planning DT for Path Planning Graph Search Algorithms D* Lite RD-based Planning

D* Lite - Demo



https://www.youtube.com/watch?v=X5a149nSE9s

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D* Lite: Cost Estimates

■ *rhs* of the node *u* is computed based on *g* of its successors in the graph and the transition costs of the edge to those successors

$$rhs(u) = \min_{s' \in Succ(u)} (g(s') + c(u, s'))$$

■ The key/priority of a node s on the open list is the minimum of g(s) and rhs(s) plus a focusing heuristic h

$$[\min(g(s), rhs(s)) + h(s_{start}, s); \min(g(s), rhs(s))]$$

- The first term is used as the primary key
- The second term is used as the secondary key for tie-breaking

D* Lite Overview

■ It is similar to D*, but it is based on Lifelong Planning A*

Koenig, S. and Likhachev, M. (2002): D* Lite. AAAI.

- It searches from the goal node to the start node, i.e., *g*-values estimate the goal distance
- Store pending nodes in a priority queue
- Process nodes in order of increasing objective function value
- Incrementally repair solution paths when changes occur
- Maintains two estimates of costs per node
 - ullet g the objective function value based on what we know
 - rhs one-step lookahead of the objective function value based on what we know
- Consistency
 - Consistent -g = rhs
 - Inconsistent $-g \neq rhs$
- Inconsistent nodes are stored in the priority queue (open list) for processing

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Lite RD-based Pla

D* Lite Algorithm

■ Main – repeat until the robot reaches the goal (or $g(s_{start}) = \infty$ there is no path)

```
Initialize();
ComputeShortestPath();
while (s_{start} \neq s_{goal}) do
s_{start} = \operatorname{argmin}_{s' \in Succ(s_{start})}(c(s_{start}, s') + g(s'));
Move to s_{start};
Scan the graph for changed edge costs;
if any edge cost changed perform then
foreach \ directed \ edges \ (u, v) \ with \ changed \ edge \ costs \ do
Update \ the \ edge \ cost \ c(u, v);
UpdateVertex(u);
foreach \ s \in U \ do
U.Update(s, CalculateKey(s));
ComputeShortestPath();
```

Procedure Initialize

```
\begin{array}{l} \mathsf{U} = \mathsf{0}; \\ \textbf{foreach } s \in S \ \textbf{do} \\ & \  \  \, \lfloor \  \  \, rhs(s) := g(s) := \infty; \\ rhs(s_{goal}) := \mathsf{0}; \\ \mathsf{U.Insert}(s_{goal}, \ \mathsf{CalculateKey}(s_{goal})); \end{array}
```

D* Lite - Demo

D* Lite Algorithm – ComputeShortestPath()

Procedure ComputeShortestPath while $U.TopKey() < CalculateKey(s_{start}) OR rhs(s_{start}) \neq g(s_{start}) do$ u := U.Pop();if g(u) > rhs(u) then g(u) := rhs(u);**foreach** $s \in Pred(u)$ **do** UpdateVertex(s); else **foreach** $s \in Pred(u) \cup \{u\}$ **do** UpdateVertex(s);

Procedure UpdateVertex

```
if u \neq s_{goal} then rhs(u) := \min_{s' \in Succ(u)} (c(u, s') + g(s'));
if u \in U then U.Remove(u);
if g(u) \neq rhs(u) then U.Insert(u, CalculateKey(u));
```

Procedure CalculateKey

```
return [\min(g(s), rhs(s)) + h(s_{start}, s); \min(g(s), rhs(s))]
```

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RD-based Planning D* Lite

Grid-based Planning

DT for Path Planning

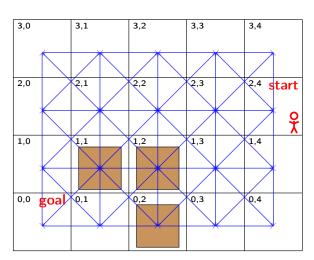
3 2

Graph Search Algorithms

RD-based Planning

Active node

D* Lite - Example



Legend

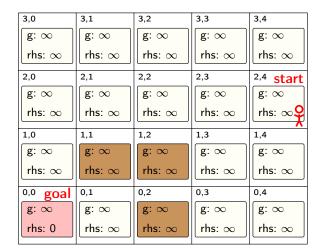
Free node Obstacle node On open list Active node

- A grid map of the environment (what is actually known)
- 8-connected graph superimposed on the grid (bidirectional)
- Focusing heuristic is not used (h = 0)

Transition costs

- Free space Free space: 1.0 and 1.4 (for diagonal edge)
- From/to obstacle: ∞

D* Lite – Example Planning (1)



Legend

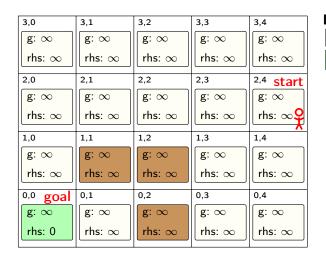
Free node Obstacle node On open list

Initialization

https://github.com/mdeyo/d-star-lite

- Set rhs = 0 for the goal
- Set $rhs = g = \infty$ for all other nodes

D* Lite – Example Planning (2)



Legend

Free node Obstacle node On open list Active node

Initialization

Put the goal to the open list It is inconsistent

D* Lite – Example Planning (3)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (goal)
- It is over-consistent (g > rhs), therefore set g = rhs

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D* Lite

RD-based Planning

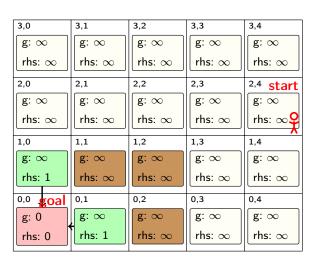
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D* Lite – Example Planning (4)



Legend

Free node Obstacle node On open list Active node

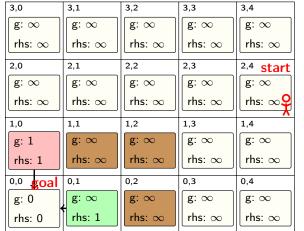
ComputeShortestPath

- node Expand popped (UpdateVertex() on all its predecessors)
- This computes the rhs values for the predecessors
- Nodes that become inconsistent are added to the open list

Small black arrows denote the node used for computing the rhs value, i.e., using the respective transition cost

■ The rhs value of (1,1) is ∞ because the transition to obstacle has cost ∞

D* Lite – Example Planning (5)



Legend

Free node Obstacle node On open list Active node

- Pop the minimum element from the open list (1,0)
- It is over-consistent (g > rhs) set g = rhs

3.0

2,0

1,0

0,0

g: 0

rhs: 0

g: 1

rhs: 1

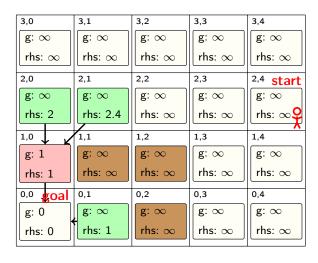
roal

g: ∞

rhs: ∞

rhs: 2

D* Lite – Example Planning (6)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Expand the popped node (UpdateVertex() on all predecessors in the graph)
- Compute rhs values of the predecessors accordingly
- Put them to the open list if they become inconsistent

- The *rhs* value of (0,0), (1,1) does not change
- They do not become inconsistent and thus they are not put on the open list

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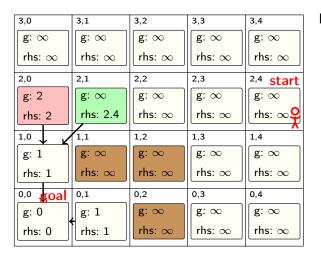
Graph Search Algorithms

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Obstacle node

Active node

D* Lite - Example Planning (8)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,0)
- It is over-consistent (g > rhs)and thus set g = rhs

D* Lite – Example Planning (9)

D* Lite – Example Planning (7)

g: ∞

g: ∞

rhs: ∞

rhs: ∞

g: ∞

rhs: ∞

2,2

1,2

0.2

rhs: ∞

g: ∞

2,3

1,3

0.3

rhs: ∞

g: ∞

g: ∞

g: ∞

rhs: ∞

rhs: ∞

rhs: ∞

g: ∞

rhs: ∞

^{2,4} start

rhs: ∞

g: ∞

g: ∞

g: ∞

rhs: ∞

rhs: ∞

1,4

g: ∞

2,1

1,1

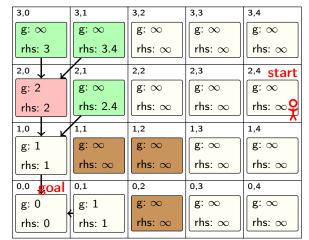
rhs: ∞

rhs: 2.4

rhs: ∞

g: 1

rhs: 1



Legend

Legend

Free node

On open list

ComputeShortestPath

from the open list (0,1)

and thus set g = rhs

■ Pop the minimum element

It is over-consistent (g > rhs)

Expand the popped element,

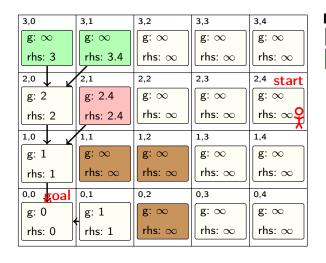
e.g., call UpdateVertex()

Free node Obstacle node On open list Active node

ComputeShortestPath

Expand the popped element and put the predecessors that become inconsistent onto the open list

D* Lite - Example Planning (10)



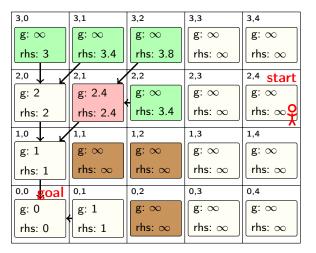
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,1)
- It is over-consistent (g > rhs) and thus set g = rhs

D* Lite – Example Planning (11)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

■ Expand the popped element and put the predecessors that become inconsistent onto the open list

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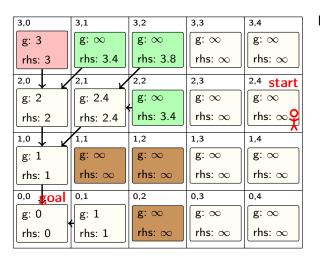
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D* Lite - Example Planning (12)



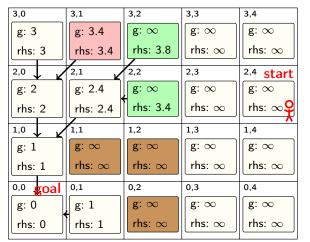
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (3,0)
- It is over-consistent (g > rhs)and thus set g = rhs
- Expand the popped element and put the predecessors that become inconsistent onto the open list
- In this cases, none of the predecessors become inconsistent

D* Lite – Example Planning (13)

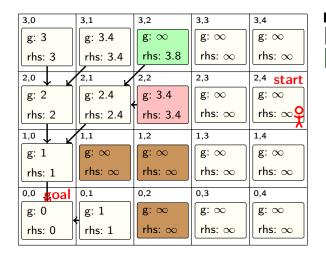


Legend

Free node Obstacle node On open list Active node

- Pop the minimum element from the open list (3,0)
- It is over-consistent (g > rhs)and thus set g = rhs
- Expand the popped element and put the predecessors that become inconsistent onto the open list
- In this cases, none of the predecessors become inconsistent

D* Lite - Example Planning (14)



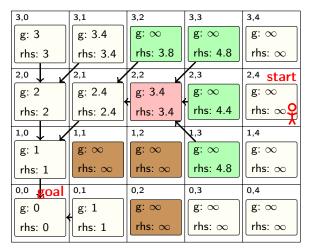
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,2)
- It is over-consistent (g > rhs)and thus set g = rhs

D* Lite – Example Planning (15)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

■ Expand the popped element and put the predecessors that become inconsistent onto the open list, i.e., (3,2), (3,3), (2,3)

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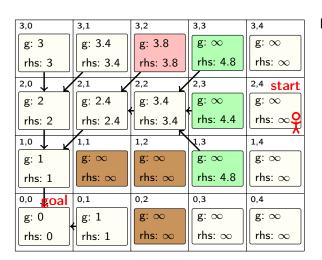
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D* Lite - Example Planning (16)



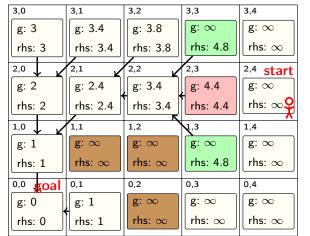
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (3,2)
- It is over-consistent (g > rhs)and thus set g = rhs
- Expand the popped element and put the predecessors that become inconsistent onto the open list
- In this cases, none of the predecessors become inconsistent

D* Lite – Example Planning (17)

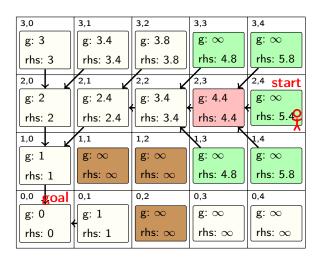


Legend

Free node Obstacle node On open list Active node

- Pop the minimum element from the open list (2,3)
- It is over-consistent (g > rhs)and thus set g = rhs

D* Lite - Example Planning (18)



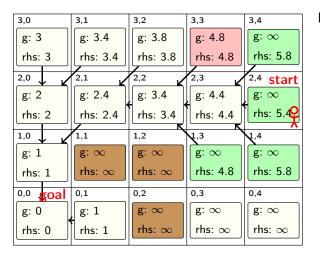
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Expand the popped element and put the predecessors that become inconsistent onto the open list, i.e., (3,4), (2,4), (1,4)
- The start node is on the open
- However, the search does not finish at this stage
- There are still inconsistent nodes (on the open list) with a lower value of rhs

D* Lite – Example Planning (19)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (3,2)
- It is over-consistent (g > rhs)and thus set g = rhs
- Expand the popped element and put the predecessors that become inconsistent onto the open list
- In this cases, none of the predecessors become inconsistent

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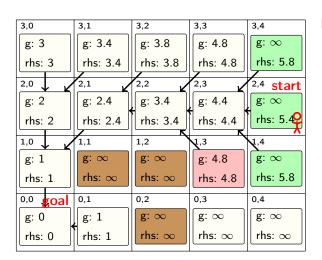
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D* Lite - Example Planning (20)



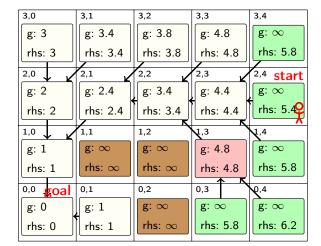
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (1,3)
- It is over-consistent (g > rhs)and thus set g = rhs

D* Lite – Example Planning (21)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

Expand the popped element and put the predecessors that become inconsistent onto the open list, i.e., (0,3) and (0,4)

3.0

2,0

1,0

0,0

g: 0

rhs: 0

g: 1

rhs: 1

roal

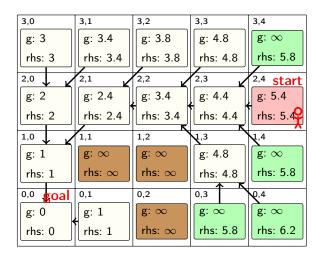
g: 2

rhs: 2

g: 3

rhs: 3

D* Lite - Example Planning (22)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,4)
- It is over-consistent (g > rhs)and thus set g = rhs
- Expand the popped element and put the predecessors that become inconsistent (none in this case) onto the open list
- The start node becomes consistent and the top key on the open list is not less than the key of the start node
- An optimal path is found and the loop of the ComputeShortestPath is breaked

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Obstacle node

Active node

■ Follow the gradient of g val-

ues from the start node

Grid-based Planning

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D* Lite

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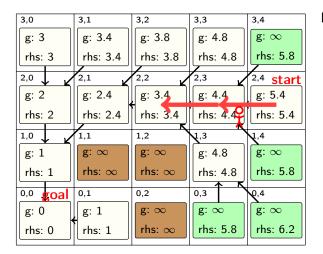
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D* Lite – Example Planning (24)



Legend

Free node Obstacle node On open list Active node

■ Follow the gradient of g values from the start node

D* Lite – Example Planning (25)

D* Lite – Example Planning (23)

g: 3.8

g: 3.4

1,2

0,2

rhs: 3.4

rhs: ∞

rhs: ∞

rhs: 3.8

g: 3.4

g: 2.4

rhs: 2.4

rhs: ∞

g: 1

rhs: 1

rhs: 3.4

g: 4.8

g: 4.4

g: 4.8

g: ∞

rhs: 5.8

0,3

rhs: 4.8

rhs: 4.4

rhs: 4.8

g: ∞

rhs: 5.8

2,4 start

rhs: 5.4

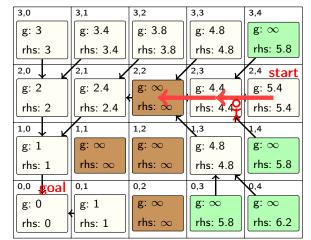
g: 5.4

g: ∞

g: ∞

rhs: 6.2

rhs: 5.8



Legend

Legend

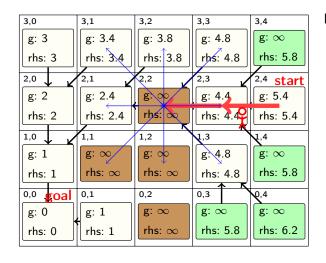
Free node

On open list

Free node Obstacle node On open list Active node

- A new obstacle is detected during the movement from (2,3) to (2,2)
- Replanning is needed!

D* Lite - Example Planning (25 update)

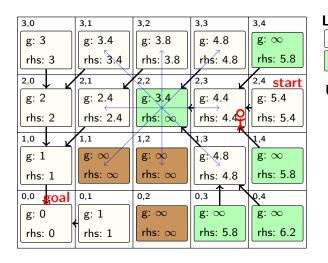


Legend

Free node Obstacle node On open list Active node

- All directed edges with changed edge, we need to call the UpdateVertex()
- All edges into and out of (2,2) have to be considered

D* Lite – Example Planning (26 update 1/2)



Legend

Free node Obstacle node On open list Active node

Update Vertex

- Outgoing edges from (2,2)
- Call UpdateVertex() on (2,2)
- The transition costs are now ∞ because of obstacle
- Therefore the $rhs = \infty$ and (2,2) becomes inconsistent and it is put on the open

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Grid-based Planning

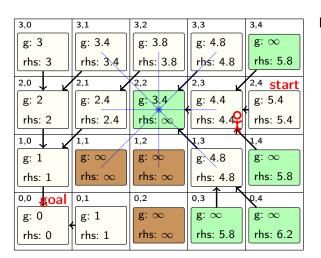
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D* Lite - Example Planning (26 update 2/2)



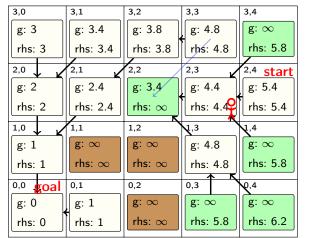
Legend

Free node Obstacle node On open list Active node

Update Vertex

- Incomming edges to (2,2)
- Call UpdateVertex() on the neighbors (2,2)
- The transition cost is ∞, and therefore, the rhs value previously computed using (2,2) is changed

D* Lite – Example Planning (27)



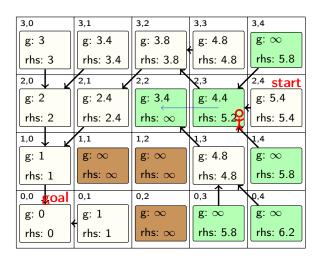
Legend

Free node Obstacle node On open list Active node

Update Vertex

- The neighbor of (2,2) is (3,3)
- The minimum possible *rhs* value of (3,3) is 4.8 but it is based on the g value of (3,2)and not (2,2), which is the detected obstacle
- The node (3,3) is still consistent and thus it is not put on the open list

D* Lite - Example Planning (28)



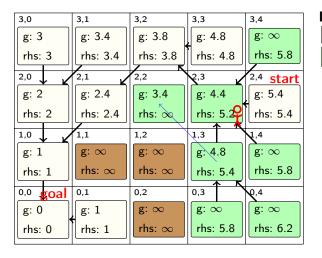
Legend

Free node Obstacle node On open list Active node

Update Vertex

- (2,3) is also a neighbor of
- The minimum possible *rhs* value of (2,3) is 5.2 because of (2,2) is obstacle (using (3,2)with 3.8 + 1.4)
- The rhs value of (2,3) is different than g thus (2,3) is put on the open list

D* Lite – Example Planning (29)



Legend

Free node Obstacle node On open list Active node

Update Vertex

- Another neighbor of (2,2) is
- The minimum possible *rhs* value of (1,3) is 5.4 computed based on g of (2,3) with 4.4 +1 = 5.4
- The *rhs* value is always computed using the g values of its successors

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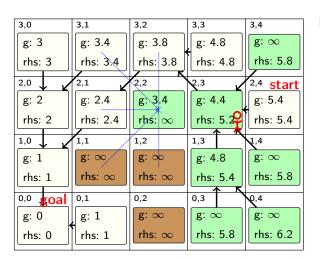
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D* Lite - Example Planning (29 update)



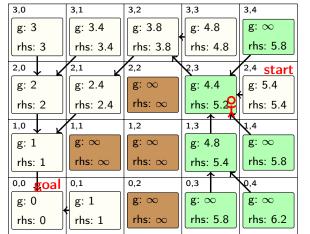
Legend

Free node Obstacle node On open list Active node

Update Vertex

- None of the other neighbor of (2,2) end up being inconsistent
- We go back to calling ComputeShortestPath() until an optimal path is determined

D* Lite - Example Planning (30)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

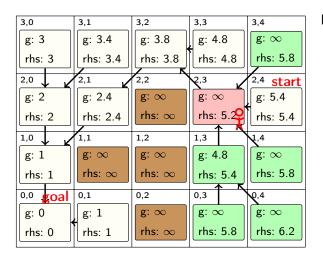
- Pop the minimum element from the open list (2,2), which is obstacle
- It is under-consistent (g <</p> *rhs*), therefore set $g = \infty$
- Expand the popped element and put the predecessors that become inconsistent (none in this case) onto the open list

- The node corresponding to the robot's current position is inconsistent and its key is greater than the minimum key on the open list
- Thus, the optimal path is not found yet

However, it has no effect as its rhs value is up to date and consistent

Because (2,2) was under-consistent (when popped), UpdateVertex() has to be called on it

D* Lite - Example Planning (31)



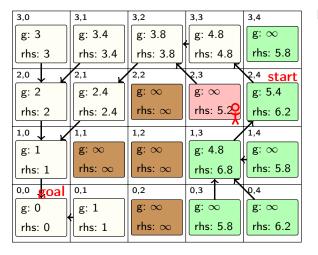
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,3)
- It is under-consistent (g < *rhs*), therefore set $g = \infty$

D* Lite – Example Planning (32)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Expand the popped element and update the predecessors
- (2,4) becomes inconsistent
- (1,3) gets updated and still inconsistent
- The *rhs* value (1,4) does not changed, but it is now computed from the g value of (1,3)

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Grid-based Planning

DT for Path Planning

Graph Search Algorithms

D* Lite

RD-based Planning

Grid-based Planning

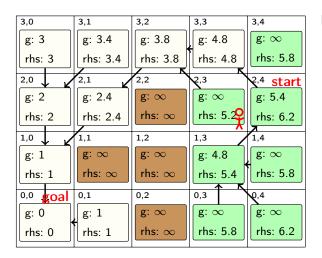
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RD-based Planning

D* Lite – Example Planning (33)



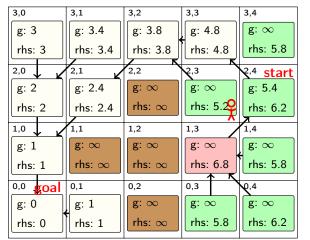
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Because (2,3) was underconsistent (when popped), call UpdateVertex() on it is needed
- As it is still inconsistent it is put back onto the open list

D* Lite – Example Planning (34)

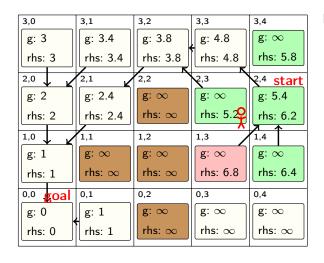


Legend

Free node Obstacle node On open list Active node

- Pop the minimum element from the open list (1,3)
- It is under-consistent (g < *rhs*), therefore set $g = \infty$

D* Lite - Example Planning (35)



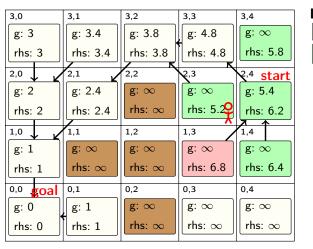
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Expand the popped element and update the predecessors
- (1,4) gets updated and still inconsistent
- (0,3) and (0,4) get updated and now consistent (both g and *rhs* are ∞)

D* Lite – Example Planning (36)



Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Because (1,3) was underconsistent (when popped), call UpdateVertex() on it is needed
- As it is still inconsistent it is put back onto the open list

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Grid-based Planning

DT for Path Planning

Graph Search Algorithms

D* Lite

RD-based Planning

Grid-based Planning

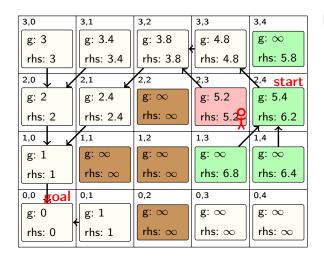
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Graph Search Algorithms

RD-based Planning

D* Lite – Example Planning (37)



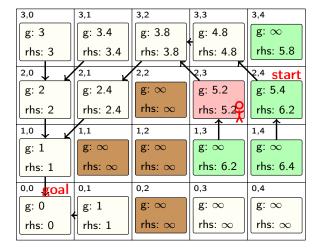
Legend

Free node Obstacle node On open list Active node

ComputeShortestPath

- Pop the minimum element from the open list (2,3)
- It is over-consistent (g > rhs), therefore set g = rhs

D* Lite – Example Planning (38)



Legend

Free node Obstacle node On open list Active node

- Expand the popped element and update the predecessors
- (1,3) gets updated and still inconsistent
- The node (2,3) corresponding to the robot's position is consistent
- Besides, top of the key on the open list is not less than the key of (2,3)
- The optimal path has been found and we can break out of the loop

D* Lite - Comments

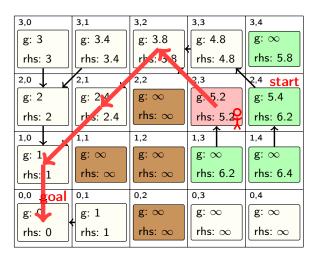
(free/obstacle)

time

shown in the example)

entire open list

D* Lite - Example Planning (39)



Legend

Free node Obstacle node On open list Active node

■ Follow the gradient of g values from the robot's current position (node)

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be added to the g and rhs values

RD-based Planning

Reaction-Diffusion Processes Background

- Reaction-Diffusion (RD) models dynamical systems capable to reproduce the autowaves
- Autowaves a class of nonlinear waves that propagate through an active media

At the expense of the energy stored in the medium, e.g., grass combustion.

■ RD model describes spatio-temporal evolution of two state variables $u = u(\vec{x}, t)$ and $v = v(\vec{x}, t)$ in space \vec{x} and time t

$$\dot{u} = f(u,v) + D_u \triangle u
\dot{v} = g(u,v) + D_v \triangle v$$

where \triangle is the Laplacian.

This RD-based path planning is informative, just for curiosity

Reaction-Diffusion Background

■ FitzHugh-Nagumo (FHN) model

FitzHugh R, Biophysical Journal (1961)

$$\dot{u} = \varepsilon \left(u - u^3 - v + \phi \right) + D_u \triangle u
\dot{v} = \left(u - \alpha v + \beta \right) + D_v \triangle u$$

■ D* Lite works with real valued costs, not only with binary costs

■ The final version of D* Lite includes further optimization (not

■ The search can be focused with an admissible heuristic that would

Updating the rhs value without considering all successors every

• Re-focusing the serarch as the robot moves without reordering the

where α, β, ϵ , and ϕ are parameters of the model.

Dynamics of RD system is determined by the associated nullcline configurations for $\dot{u}=0$ and $\dot{v}=0$ in the absence of diffusion, i.e.,

$$\varepsilon (u - u^3 - v + \phi) = 0,$$

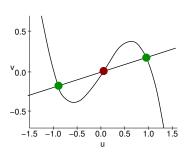
$$(u - \alpha v + \beta) = 0,$$

which have associated geometrical shapes

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Grid-based Planning RD-based Planning Grid-based Planning **RD-based Planning**

Nullcline Configurations and Steady States



Nullclines intersections represent

- Stable States (SSs)
- Unstable States

■ Bistable regime

The system (concentration levels of (u, v) for each grid cell) tends to be in SSs.

■ We can modulate relative stability of both SS

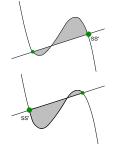
"preference" of SS+ over SS-

System moves from SS^- to SS^+ ,

if a small perturbation is introduced.

■ The SSs are separated by a mobile frontier

a kind of traveling frontwave (autowaves)



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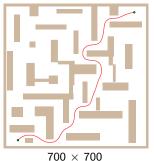
Grid-based Planning

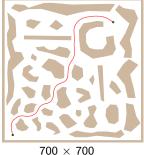
RD-based Planning

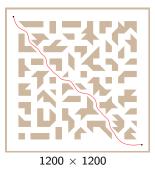
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Grid-based Planning

Example of Found Paths







■ The path clearance maybe adjusted by the wavelength and size of the computational grid.

Control of the path distance from the obstacles (path safety)

RD-based Path Planning – Computational Model

■ Finite difference method on a Cartesian grid with Dirichlet boundary conditions (FTCS) $discretization \rightarrow grid\ based\ computation \rightarrow grid\ map$

■ External forcing — introducing additional information i.e., constraining concentration levels to some specific values

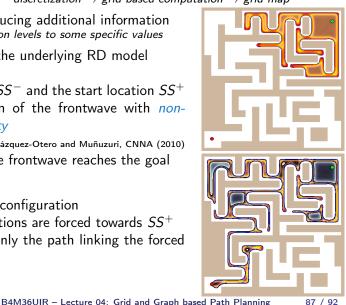
- Two-phase evolution of the underlying RD model
 - 1. Propagation phase
 - Freespace is set to SS^- and the start location SS^+
 - Parallel propagation of the frontwave with nonannihilation property

Vázquez-Otero and Muñuzuri, CNNA (2010)

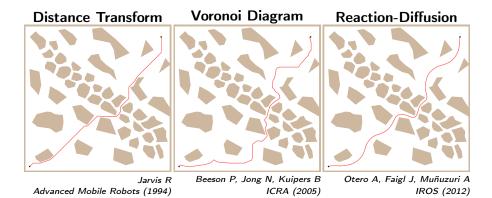
■ Terminate when the frontwave reaches the goal

2. Contraction phase

- Different nullclines configuration
- Start and goal positions are forced towards SS⁺
- SS⁻ shrinks until only the path linking the forced points remains



Comparison with Standard Approaches



 RD-based approach provides competitive paths regarding path length and clearance, while they seem to be smooth

Grid-based Planning DT for Path Planning Graph Search Algorithms D* Lite RD-based Planning Topics Discussed

Robustness to Noisy Data





Vázquez-Otero, A., Faigl, J., Duro, N. and Dormido, R. (2014): Reaction-Diffusion based Computational Model for Autonomous Mobile Robot Exploration of Unknown Environments. International Journal of Unconventional Computing (IJUC).

Summary of the Lecture

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Topics Discussed

Topics Discussed

- Front-Wave propagation and path simplification
- Distance Transform based planning
- Graph based planning methods: Dijsktra's, A*, JPS, Theta*
- D* Lite
- Reaction-Diffusion based planning (informative)
- Next: Randomized Sampling-based Motion Planning Methods