



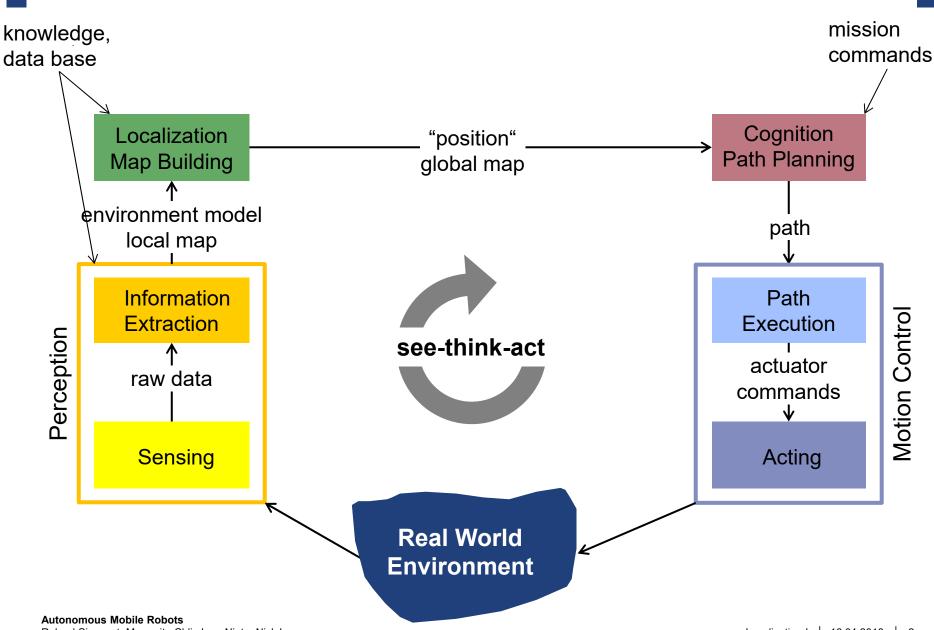


Localization I

Roland Siegwart, Margarita Chli, Juan Nieto, Nick Lawrance

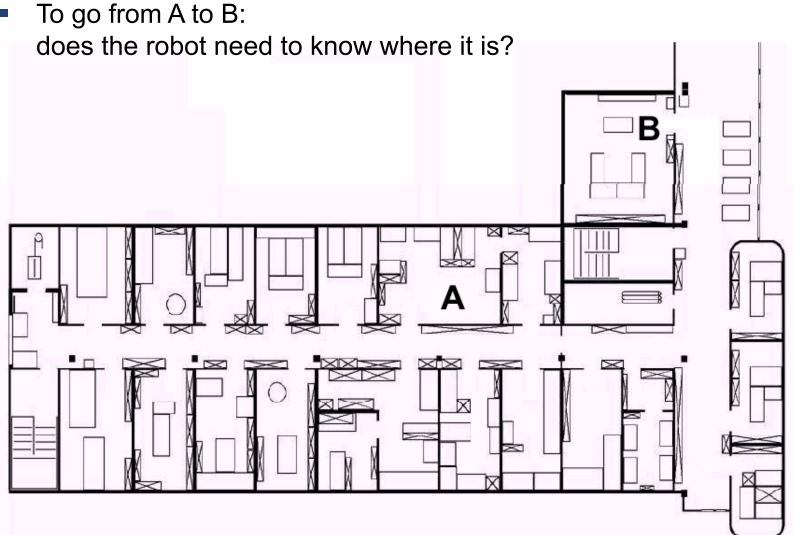
ETH zürich





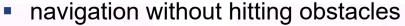


introduction | Do we need to localize of hot.

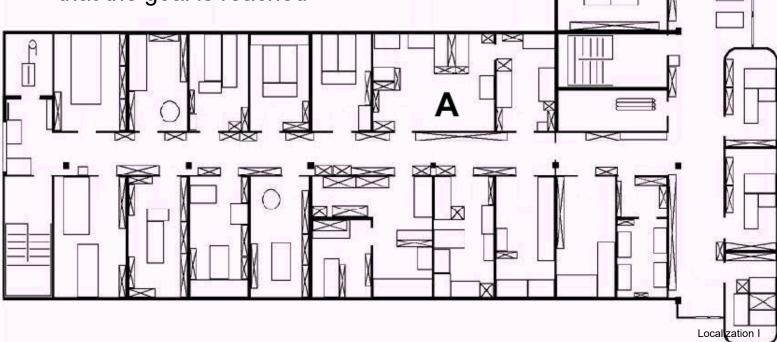




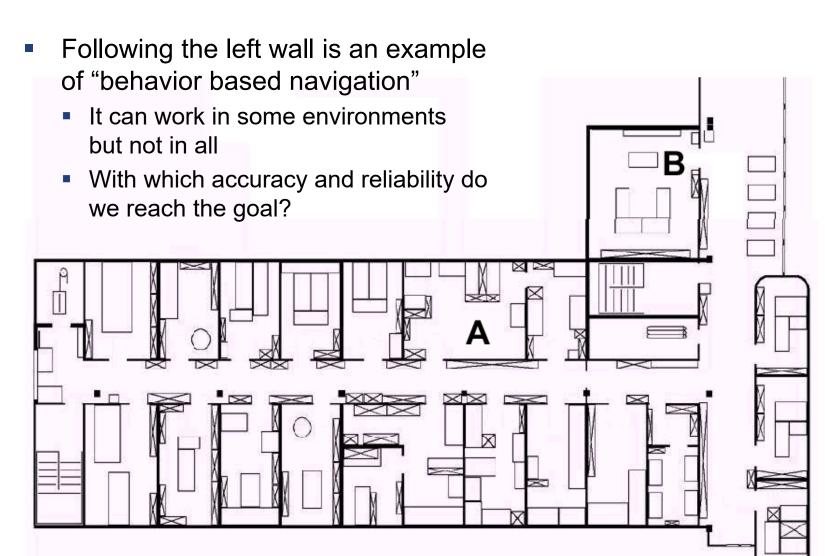




- detection of goal location
- Possible by following always the left wall
 - However, how to detect that the goal is reached



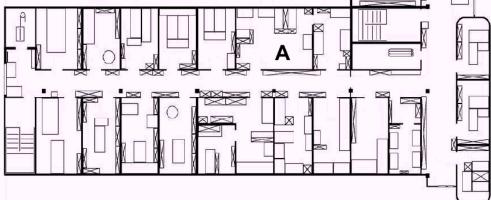






- As opposed to behavior based navigation is "map based navigation"
 - Assuming that the map is known, at every time step the robot has to know where it is How?
 - If we know the start position, we can use wheel odometry or dead reckoning. Is this enough? What else can we use?
- But how do we represent the map for the robot?
- And how do we represent the position of the

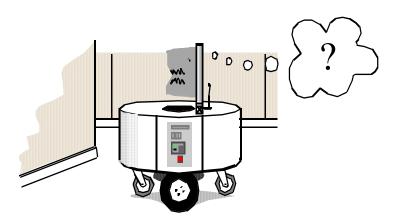
robot in the map?





Introduction | Definitions

- Global localization
 - The robot is not told its initial position
 - Its position must be estimated from scratch
- Position Tracking
 - A robot knows its initial position and "only" has to accommodate small errors in its odometry as it moves





Introduction | How to localize?

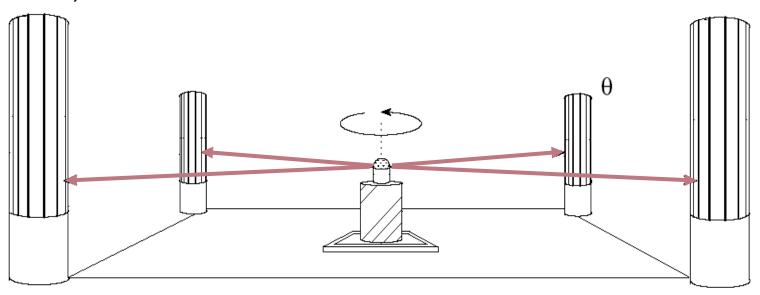
- Localization based on external sensors, beacons or landmarks
- Odometry
- Map Based Localization without external sensors or artificial landmarks, just use robot onboard sensors
 - Example: Probabilistic Map Based Localization



Introduction | Beacon Based Localization



- Triangulation
 - Ex 1: Poles with highly reflective surface and a laser for detecting them
 - Ex 2: Coloured beacons and an omnidirectional camera for detecting them (example: RoboCup or autonomous robots in tennis fields)





Introduction | Beacon Based Localization

KIVA Systems, Boston (MA) (acquired by Amazon in 2011)



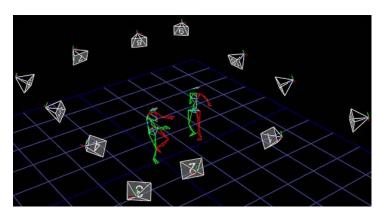
Unique marker with known absolute 2D position in the map

Prof. Raff D'Andrea, ETH



Introduction | Motion Capture Systems

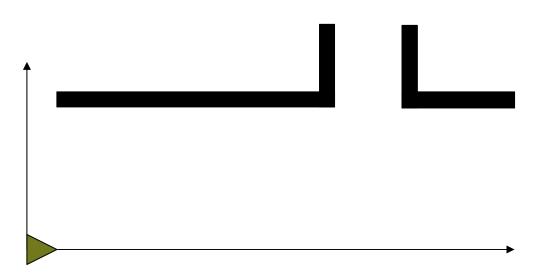
- High resolution (from VGA up to 16 Mpixels)
- Very high frame rate (several hundreds of Hz)
- Good for ground truth reference and multi-robot control strategies
- Popular brands:
 - VICON (10kCHF per camera),
 - OptiTrack (2kCHF per camera)





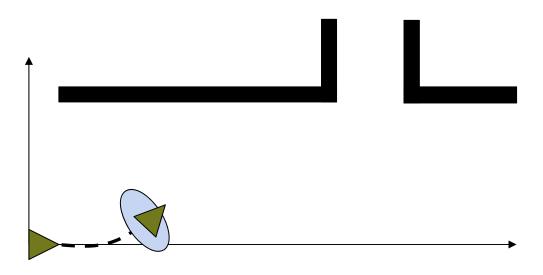


Consider a mobile robot moving in a known environment.



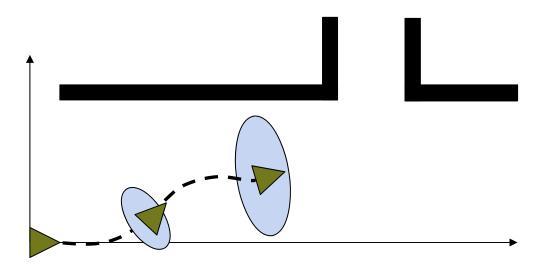


- Consider a mobile robot moving in a known environment.
- As it starts to move, say from a precisely known location, it can keep track of its motion using odometry.



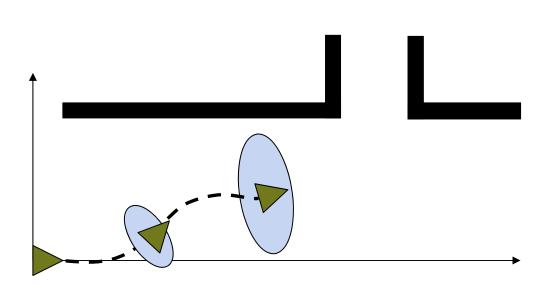


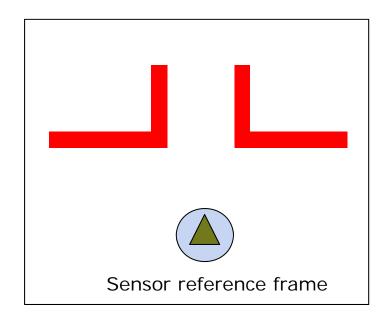
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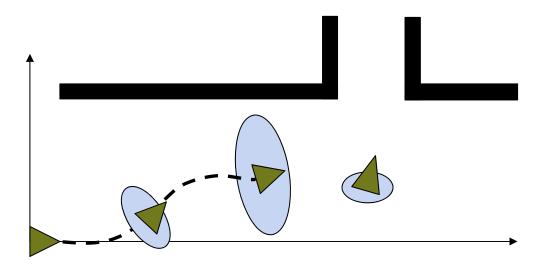


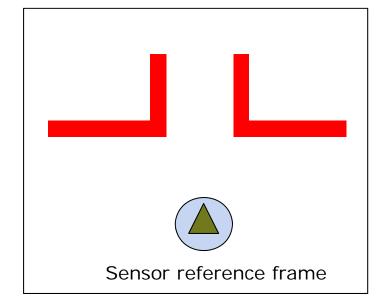
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 As it starts to move, say from a precisely known location, it can keep track of its motion using odometry.

The robot makes an observation and updates its position

and uncertainty







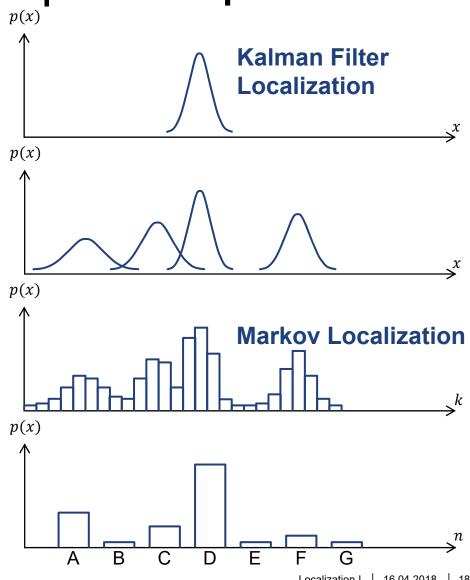
Ingredients | Probabilistic Map-based localization

- Probability theory → error propagation, sensor fusion
- Belief representation → discrete / continuous (map/position)
- Motion model → odometry model
- Sensing → measurement model



Probabilistic localization | Belief Representation

- Continuous map with single hypothesis probability distribution p(x)
- Continuous map with multiple hypotheses probability distribution p(x)
- Discretized metric map (grid k) with probability distribution p(k)
- Discretized topological map (nodes n) with probability distribution p(n)







Belief Representation | Characteristics

- Continuous
 - Precision bound by sensor data
 - Typically single hypothesis pose estimate
 - Lost when diverging (for single hypothesis)
 - Compact representation and typically reasonable in processing power.

- Discrete
 - Precision bound by resolution of discretisation
 - Typically multiple hypothesis pose estimate
 - Never lost (when diverges converges to another cell)
 - Important memory and processing power needed. (not the case for topological maps)



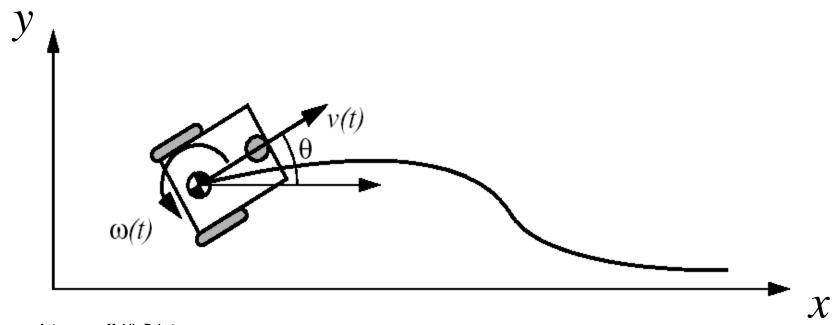
Odometry

- Definition
 - Dead reckoning (also deduced reckoning or odometry) is the process of calculating vehicle's current position by using a previously determined position and estimated speeds over the elapsed time
- Robot motion is recovered by integrating proprioceptive sensor velocities readings
 - Pros: Straightforward
 - Cons: Errors are integrated -> unbound
- Heading sensors (e.g., gyroscope) help to reduce the accumulated errors but drift remains



Odometry | The Differential Drive Robot

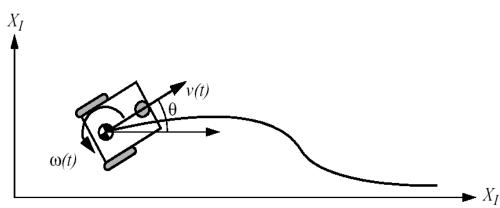
$$x = \begin{bmatrix} x \\ y \\ \theta \end{bmatrix} \qquad \hat{x}_t = x_{t-1} + \begin{bmatrix} \Delta x \\ \Delta y \\ \Delta \theta \end{bmatrix} = f(x_{t-1}, u_t)$$





Odometry | Wheel Odometry

Kinematics



$$\hat{x}_{t} = f(x_{t-1}, u_{t}) = \begin{bmatrix} x_{t-1} \\ y_{t-1} \\ \theta_{t-1} \end{bmatrix} + \begin{bmatrix} \Delta s \cos(\theta + \frac{\Delta \theta}{2}) \\ \Delta s \sin(\theta + \frac{\Delta \theta}{2}) \\ \Delta \theta \end{bmatrix}$$
This term comes from the application of the Instantaneous Center of Rotation
$$\Delta s_{t} + \Delta s_{t}$$
Can you demonstrate these equations?

$$\Delta s = \frac{\Delta s_r + \Delta s_l}{2}$$

$$\Delta\theta = \frac{\Delta s_r - \Delta s_l}{b}$$



Odometry | Error Propagation

Error model
$$P_{t} = F_{x_{t-1}} \cdot \Sigma_{x_{t-1}} \cdot F_{x_{t-1}}^{T} + F_{\Delta S} \cdot \Sigma_{\Delta S} \cdot F_{\Delta S}^{T}$$

$$\Sigma_{\Delta S} = \begin{bmatrix} k_r |\Delta s_r| & 0\\ 0 & k_l |\Delta s_l| \end{bmatrix}$$

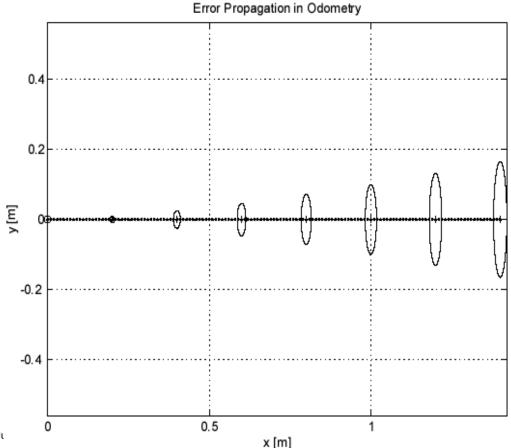
$$F_{x_{t-1}} = \nabla f_{x_{t-1}} = \begin{bmatrix} \frac{\partial f}{\partial x} & \frac{\partial f}{\partial y} & \frac{\partial f}{\partial \theta} \end{bmatrix} = \begin{bmatrix} 1 & 0 & -\Delta s \sin(\theta + \Delta \theta/2) \\ 0 & 1 & \Delta s \cos(\theta + \Delta \theta/2) \\ 0 & 0 & 1 \end{bmatrix}$$

$$F_{\Delta S} = \begin{bmatrix} \frac{1}{2}\cos\left(\theta + \frac{\Delta\theta}{2}\right) - \frac{\Delta s}{2b}\sin\left(\theta + \frac{\Delta\theta}{2}\right) \frac{1}{2}\cos\left(\theta + \frac{\Delta\theta}{2}\right) + \frac{\Delta s}{2b}\sin\left(\theta + \frac{\Delta\theta}{2}\right) \\ \frac{1}{2}\sin\left(\theta + \frac{\Delta\theta}{2}\right) + \frac{\Delta s}{2b}\cos\left(\theta + \frac{\Delta\theta}{2}\right) \frac{1}{2}\sin\left(\theta + \frac{\Delta\theta}{2}\right) - \frac{\Delta s}{2b}\cos\left(\theta + \frac{\Delta\theta}{2}\right) \\ \frac{1}{b} - \frac{1}{b} \end{bmatrix}$$



Odometry | Growth of Pose uncertainty for Straight Line Movement

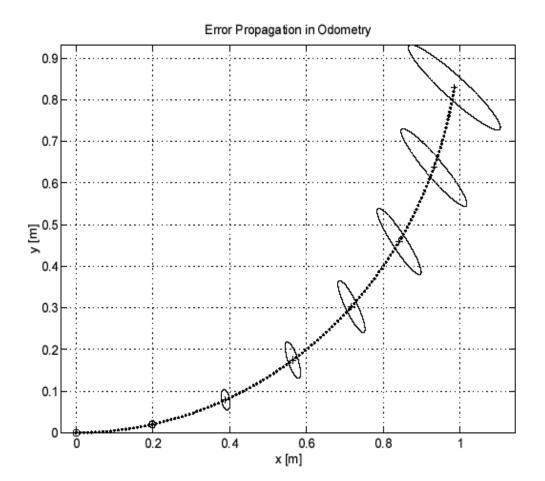
Note: Errors perpendicular to the direction of movement are growing much faster!





Odometry | Growth of Pose uncertainty for Movement on a Circle

 Note: Errors ellipse does not remain perpendicular to the direction of movement!

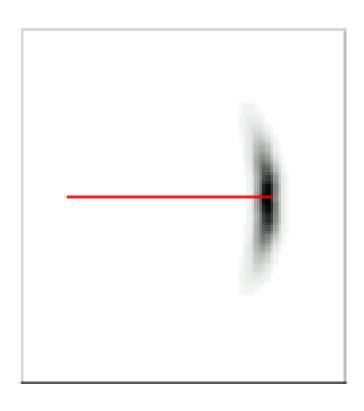


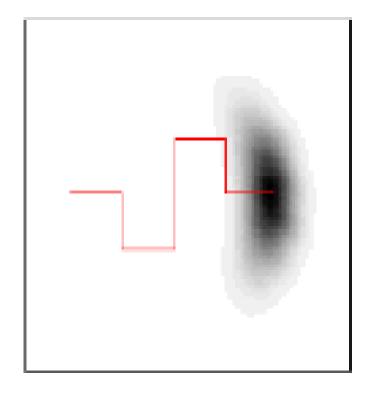


Odometry | Example of non-Gaussian error model

Note: Errors are not shaped like ellipses!

Courtesy Al Lab, Stanford





[Fox, Thrun, Burgard, Dellaert, 2000]



Odometry | Error sources

- Deterministic

Non-Deterministic

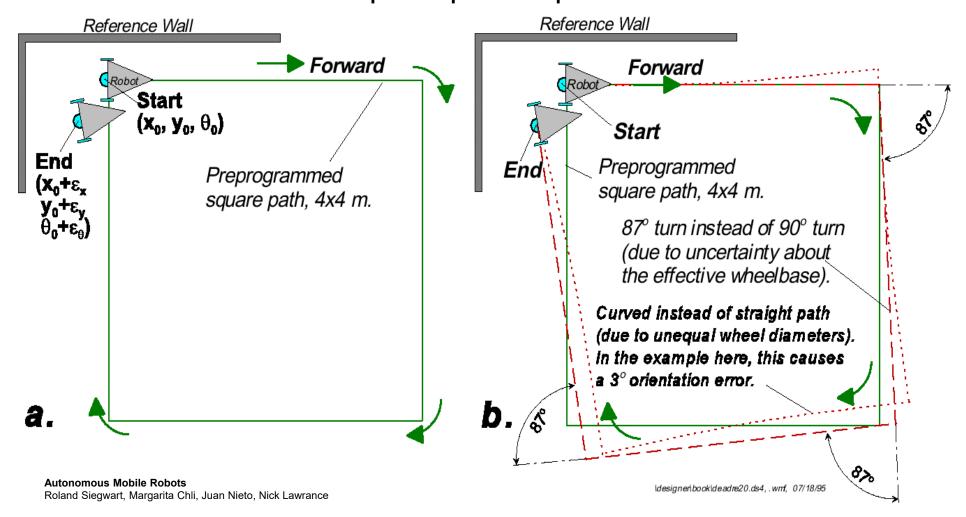
(Non-Systematic)

- (Systematic)
- Deterministic errors can be eliminated by proper calibration of the system.
- Non-Deterministic errors are random errors. They have to be described by error models and will always lead to uncertain position estimate.
- Major Error Sources in Odometry:
 - Limited resolution during integration (time increments, measurement resolution)
 - Misalignment of the wheels (deterministic)
 - Unequal wheel diameter (deterministic)
 - Variation in the contact point of the wheel (non deterministic)
 - Unequal floor contact (slippage, non planar ...) (non deterministic)



Odometry | Calibration of systematic errors [Borenstein 1996]

The unidirectional square path experiment





Odometry | Calibration of Errors II [Borenstein 1996]

The bi-directional square path experiment

Reference Wall

