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Simulation checks

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Simulation checks

Supplemental Material 2

- In order to insure the reliability of our calculation method, for all scenarios where $G_1 = G_2 = 0$, we compared empirical means and variances of all estimators (i.e. means and variances of all estimates) with theoretical means and variances (i.e. expected means and variances, computed based on equations in Tables 1, 2 and 3 in the main article). Because we can draw exactly the same conclusions for **biased** (Cohen's d, Glass' d using either S_1 or S_2 as standardizer, Shieh's d and Cohen's d^*) and **unbiased** (Hedges' g, Glass' g using either S_1 or S_2 as standardizer, Shieh's g and Hedges' g^*) estimators, we will simultaneously present results for both categories of estimators. Results will be subdivided into 4 conditions: - When population variances and sample sizes are equal across groups (condition a; 13 see Figures A2.1 and A2.5 for respectively biased and unbiased estimators); 14 - When population variances are equal across groups and sample sizes are unequal 15 (condition b; see Figures A2.2 and A2.6 for respectively biased and unbiased estimators); 16 - When population variances are unequal across groups and sample sizes are equal 17
- When population variances are unequal across groups and sample sizes are equal (condition c; see Figures A2.3 and A2.7 for respectively biased and unbiased estimators);
- When population variances and sample sizes are unequal across groups (condition d;
 see Figures A2.4 and A2.8 for respectively biased and unbiased estimators).
- Because the equations of theoretical means and variances of Cohen's *d* and Hedges' *g*rely on the assumption of normality and equality of population variances, we expect
 empirical and theoretical parameters to be very close only in conditions a and b. For all
 other estimators, the equations of theoretical means and variances rely solely on the
 assumption of normality and therefore, we expect empirical and theoretical parameters to
 be very close in all conditions.
 - On average, empirical means (and variances) of all estimators are very close to

SIMULATION CHECKS

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theoretical expectations when population variances are equal across groups, with equal
   sample sizes (condition a; see Tables A2.1 and A2.5) or unequal sample sizes (condition b;
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   see Tables A2.2 and A2.6).
30
         When population variances are unequal across groups (conditions c and d; see Tables
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   A2.3, A2.4, A2.7 and A2.8), empirical means (and variances) of Cohen's d^* (Hedges' q^*)
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   and Shieh's d (Shieh's g) are still very close to theoretical expectations. Regarding Glass' d
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   (Glass' q), on average, while empirical variances remain very close to theoretical
   expectations, one observes larger departures between empirical and theoretical means when
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   using S_2 as standardizer. However, when looking at details in results for each scenario (see
   "biased estimator_condition C.xlsx," "biased estimator_condition D.xlsx," "unbiased
37
   estimator_condition C.xlsx" and "unbiased estimator_condition C.xlsx" in Supplemental
   Material 2), one notices that the larger the population effect size, the larger the departure
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   between empirical and theoretical means, and that relative to the population effect size,
   departures between empirical and theoretical means are always very small. On the other
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   hand, both empirical bias and variance of Cohen's d (Hedges' q) highly depart from
   theoretical expectations, even when looking at relative departures to the population effect
   size, especially when sample sizes are unequal across groups (condition d; see Table A2.4
   and A2.8), which is not surprising, as Cohen's d (Hedges' q) relies on the equality of
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population variances assumption.

Table A2.1.

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for biased estimators,

when population variances and sample sizes are equal across groups (condition a).

Shieh's d	Cohen's d*	Glass' d ₂	Glass' d_1	Cohen's d	Estimator $(\widehat{\delta})$	
0.006	0.012	0.023	0.022	0.012	Max	Absolute o
0.000	0.000	0.000	0.000	0.000	Min	deviation betv
0.1	0.002	0.005	0.004	0.002	Mean	veen empirica $ E(\widehat{\delta}) extcolor{pt}{\mu_{\delta}} $
0.002	0.003	0.007	0.006	0.003	Standard deviation	Absolute deviation between empirical and theoretical means $ \operatorname{E}(\widehat{\delta}) \cdot \mu_{\delta} $
1.006	1.006	1.005	1.006	1.006	Max	Rati
0.910	0.910	0.889	0.897	0.910	Min	o between en
0.976	0.976	0.966	0.966	0.976	Mean	npirical and th $S^2_{\ \delta}/\sigma_\delta$
0.028	0.028	0.035	0.033	0.028	Standard deviation	Ratio between empirical and theoretical variances $S^2_{\ \delta}/\sigma_\delta$

Table A2.2

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for biased estimators, when population variances are equal across groups and sample sizes are unequal (condition b).

Absolute deviation between empirical and theoretical means Ratio between empirical and theoretical variances $ {\sf E}(\widehat{\delta}) - \mu_\delta $	Min Mean Standard deviation Max Min Mean Standard deviation	0.000 0.001 0.001 1.017 0.951 0.985 0.017	0.000 0.004 0.006 1.006 0.891 0.966 0.037	0.000 0.005 0.007 1.015 0.881 0.968 0.036	0.000 0.003 0.002 1.007 0.902 0.965 0.034	
deviation between empirical and the $ E(\widehat{\delta}) \cdot \mu_{\delta} $	Mean					0.000 0.002
Absolute	Мах	0.005	0.019	0.027	0.010	0.008
	Estimator $(\widehat{\delta})$	Cohen's d	Glass' d_1	Glass' d_2	Cohen's d*	Shieh's d

Table A2.3

when population variances are unequal across groups and sample sizes are equal (condition c). Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for biased estimators,

Absolute deviation between empirical and theoretical means

Ratio between empirical and theoretical variances

Shieh's d	Cohen's d*	Glass' d ₂	Glass' d_1	Cohen's d	Estimator $(\widehat{\delta})$	
0.018	0.036	0.230	0.037	0.080	Max	
0.000	0.000	0.000	0.000	0.000	Min	
0.002	0.003	0.012	0.005	0.010	Mean	$ E(\widehat{\delta})\!\!-\!\!\mu_{\delta} $
0.003	0.006	0.033	0.007	0.015	Standard deviation	
1.007	1.007	1.008	1.004	1.753	Max	
0.874	0.874	0.883	0.888	1.005	Min	
0.975	0.975	0.974	0.973	1.175	Mean	$S^2_{\widehat{\delta}}/\sigma_{\delta}$
0.033	0.033	0.032	0.030	0.208	Standard deviation	

Table A2.4

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for biased estimators, when population variances and sample sizes are unequal across groups (condition d).

	Absolute de	eviation betwe	en empirical ar $ E(\widehat{\delta}) - \mu_{\delta} $	Absolute deviation between empirical and theoretical means $ E(\widehat{\delta}) ext{-} \mu_{\delta} $	Ratio	between empi	Ratio between empirical and theoretical variances $S^2{}_{\hat{\delta}}/\sigma_{\delta}$	etical variances
Estimator $(\widehat{\delta})$	Мах	Min	Mean	Standard deviation	Мах	Min	Mean	Standard deviation
Cohen's d	0.252	0.000	0.015	0.034	5.624	0.208	1.638	1.357
Glass' d ₁	0.026	0.000	0.005	0.006	1.009	0.881	0.972	0.033
Glass' d ₂	0.219	0.000	0.012	0.031	1.011	0.872	0.973	0.036
Cohen's d*	0:030	0.000	0.003	0.006	1.011	0.860	0.974	0.034
Shieh's d	0.009	0.000	0.001	0.002	1.011	0.867	0.970	0.036

Table A2.5

estimators, when population variances and sample sizes are equal across groups (condition a). Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for unbiased

Absolute deviation between empirical and theoretical means

Ratio between empirical and theoretical variances

Shieh's g	Cohen's g*	Glass' g_2	Glass' g_1	Hedges' g	Estimator $(\widehat{\delta})$	
0.008	0.015	0.022	0.021	0.011	Max	
0.000	0.000	0.000	0.000	0.000	Min	
0.002	0.003	0.004	0.004	0.002	Mean	$ E(\widehat{\delta})$ - $\mu_{\delta} $
0.002	0.004	0.007	0.006	0.003	Standard deviation	
1.006	1.006	1.005	1.006	1.006	Max	
0.908	0.908	0.889	0.897	0.911	Min	
0.975	0.975	0.966	0.966	0.976	Mean	$S^2_{\ \widehat{\delta}}/\sigma_{\delta}$
0.029	0.029	0.035	0.033	0.028	Standard deviation	

Table A2.6

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for unbiased estimators. when population variances are equal across groups and sample sizes are unequal (condition b).

	Absolute de	eviation betwe	en empirical and $ E(\widehat{\delta}) - \mu_{\delta} $	Absolute deviation between empirical and theoretical means $ E(\widehat{\delta}) \cdot \mu_{\delta} $	Ratio	between empi	Ratio between empirical and theoretical variances $S^2_{\ \widehat{\delta}}/\sigma_{\delta}$	ical variances
Estimator (δ)	Мах	Min	Mean	Standard deviation	Мах	Min	Mean	Standard deviation
Hedges' g	0.005	0.000	0.001	0.001	1.017	0.951	0.985	0.017
Glass' g_1	0.018	0.000	0.004	0.005	1.006	0.891	9960	0.037
Glass' g ₂	0.026	0.000	0.004	0.006	1.015	0.881	0.968	0.036
Cohen's g*	0.010	0.000	0.003	0.003	1.007	0.925	0.972	0.027
Shieh's g	0.007	0.000	0.002	0.002	1.007	0.900	0.959	0.037

Table A2.7

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for unbiased

estimators, when population variances are unequal across groups and sample sizes are equal (condition c).

Absolute deviation between empirical and theoretical means

Ratio between empirical and theoretical variances

Shieh's g	Cohen's g*	Glass′ g₂	Glass' g_1	Hedges' g	Estimator $(\widehat{\delta})$	
0.017	0.034	0.221	0.036	0.079	Max	
0.000	0.000	0.000	0.000	0.000	Min	
0.002	0.003	0.012	0.005	0.010	Mean	$ E(\widehat{\delta})$ - $\mu_{\delta} $
0.003	0.006	0.032	0.007	0.015	Standard deviation	
1.008	1.008	1.008	1.004	1.753	Max	
0.890	0.890	0.883	0.888	1.005	Min	
0.978	0.978	0.974	0.973	1.175	Mean	$S^2_{\ \widehat{\delta}}/\sigma_{\delta}$
0.029	0.029	0.032	0.030	0.208	Standard deviation	

Table A2.8

Absolute deviation between empirical and theoretical means as well as ratio between empirical and theoretical variances for unbiased estimators, when population variances and sample sizes are unequal across groups (condition d).

		tion					
Ratio between empirical and theoretical variances		Standard deviation	1.357	0.033	0.036	0.029	0.032
mpirical and t	$S^2_{\hat{\delta}}/\sigma_{\delta}$	Mean	1.638	0.972	0.973	0.977	0.973
tio between e		Min	0.208	0.881	0.872	0.882	0.881
Ra		Мах	5.624	1.009	1.011	1.011	1.011
Absolute deviation between empirical and theoretical means		Standard deviation	0.034	0.006	0.030	0.005	0.002
ween empiric	$ E(\delta)$ - $\mu_{\delta} $	Mean	0.015	0.004	0.012	0.003	0.001
edeviation bet		Min	0.000	0.000	0.000	0.000	0.000
Absolute		Мах	0.250	0.025	0.210	0.029	0.008
		Estimator $(\hat{\delta})$	Hedges' g	Glass' g_1	Glass' g ₂	Cohen's g*	Shieh's g