

I error rate control is in general slightly better with balanced designs.

Note that the *W*-test suffers from limitations and cannot be used in all situations. First, as previously mentioned, *W*-test, as all tests based on means, does not allow researchers to compare other relevant parameters of a distribution than the mean. For these reason, we recommend to never neglect the descriptive analysis of the data. A complete description of the shape and characteristics of the data (e.g. histograms and boxplots) is important. When at least one statistical parameter relating to the shape of the distribution (e.g. variance, skewness, kurtosis) seems to vary between groups, comparing results of the *W*-test with results of a nonparametric procedure is useful in order to better understand the data. Second, with small sample sizes (i.e. less than 50 observations per group when comparing at most four groups, 100 observations when comparing more than four groups), the *W*-test will not control Type I error rate when skewness is present and detecting departures for normality is therefore especially important in small samples. Unless you have good reasons to believe that distributions underlying the data have small kurtosis and skewness, we recommend to avoid alternative tests that are based on means comparison, in favour of alternatives such as the trimmed means test (Erceg-Hurn & Miroseovich, 2008)<sup>2</sup> or nonparametric tests. For more information about robust alternatives that are based on other parameters than the mean, see Erceg-Hurn and Miroseovich (2008).

## Notes

<sup>1</sup> Note that this is a didactic example, the differences have not been tested and might not differ statistically.

<sup>2</sup> The null hypothesis of the trimmed means test assumes that trimmed means are the same between groups. A trimmed mean is a mean computed on data after removing the lowest and highest values of the distribution. Trimmed means and means are equal when data are symmetric. On the other hand, when data are asymmetric, trimmed means and means differ.

## Additional File

The additional file for this article can be found as follows:

- **Supplemental Materials.** A numerical example of the mathematical development of the *F*-test, *W*-test, and *F*\*-test (Appendix 1) and justification for the choice of distributions in simulation (Appendix 2). DOI: <https://doi.org/10.5334/irsp.198.s1>

## Competing Interests

The authors have no competing interests to declare.

## Author Contribution

The first author performed simulations. The first, second and fourth authors contributed to the design. All authors contributed to the writing and the review of the literature. The Supplemental Material, including the full

R code for the simulations and plots can be obtained from <https://github.com/mdelacre/W-ANOVA>. This work was supported by the Netherlands Organization for Scientific Research (NWO) VIDI grant 452-17-013. The authors declare that they have no conflicts of interest with respect to the authorship or the publication of this article.

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