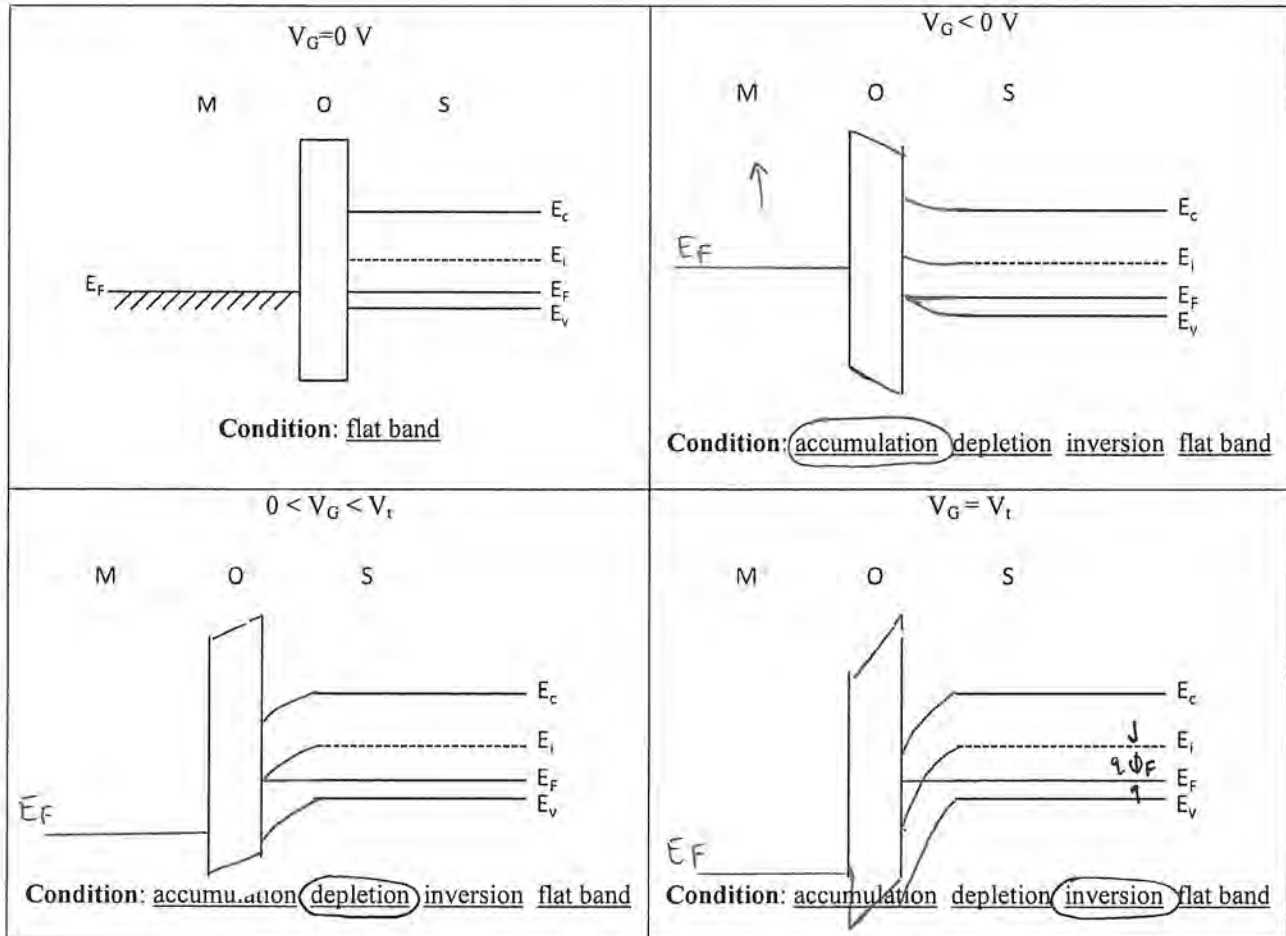


Name Solution

Section _____

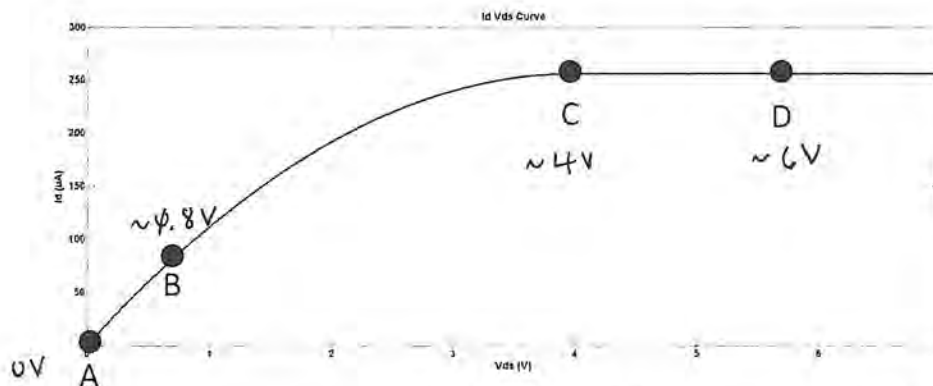
1. (25 points) The MOS-Cap energy band for $V_G=0$ V is given below. Sketch the energy band diagram for the remaining cases of V_G and circle the resulting condition.

Carefully detail the band bending at the oxide interface and relative positioning of E_F to E_i .



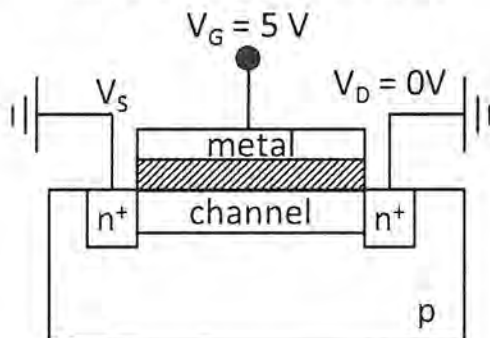
$$E_i - E_{i,bulk} = 2(E_F - E_{i,bulk})$$

2. (25 points) Suppose an nMOS transistor ($V_t = 1\text{ V}$) is biased with $V_G = 5\text{ V}$ with the resulting I_D vs V_{DS} curve below. Sketch the cross section of the conducting channel at the four points given. Circle the resulting mode of operation. Point A is already sketched for you!



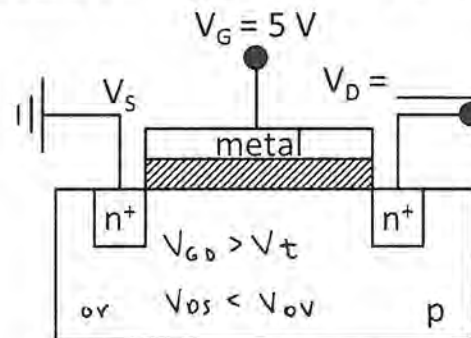
$$V_{ov} = V_{GS} - V_t = 4\text{ V for all cases}$$

Point A: $V_{GS} = 5\text{ V}$, $V_{GD} = 5\text{ V}$, $V_{DS} = 0\text{ V}$



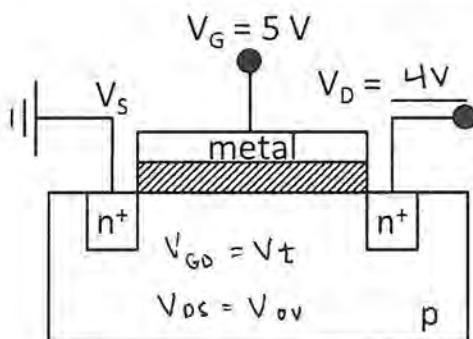
Mode: Cutoff

Point B: $V_{GS} = 5\text{ V}$, $V_{GD} = 4.2\text{ V}$, $V_{DS} = 0.8\text{ V}$



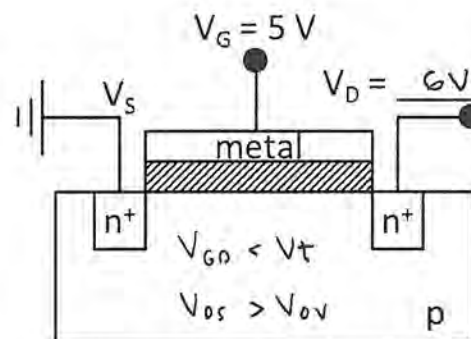
Mode: Cutoff Triode Saturation Forward

Point C: $V_{GS} = 5\text{ V}$, $V_{GD} = 1\text{ V}$, $V_{DS} = 4\text{ V}$



Mode: Cutoff Triode Saturation Forward

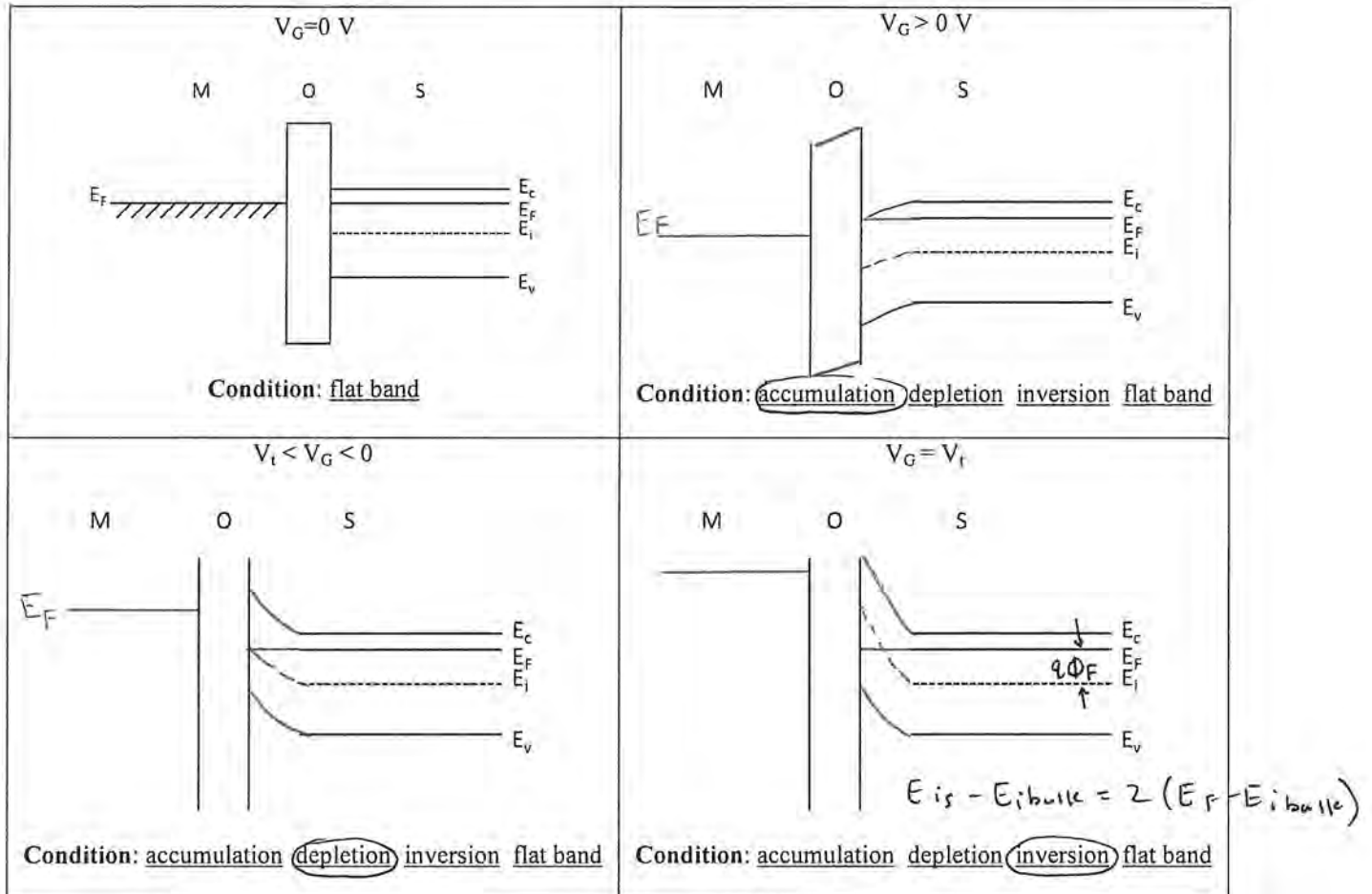
Point D: $V_{GS} = 5\text{ V}$, $V_{GD} = -1\text{ V}$, $V_{DS} = 6\text{ V}$



Mode: Cutoff Triode Saturation Forward

3. (25 points) The MOS-Cap energy band for $V_G=0$ V is given below. Sketch the energy band diagram for the remaining cases of V_G and circle the resulting condition.

Carefully detail the band bending at the oxide interface and relative positioning of E_F to E_i .



4. (25 points) Suppose the n-type Si of the MOS in part 3 is doped at 10^{15} cm^{-3} . Calculate threshold voltage V_t . Use an oxide thickness x_o of 8 nm. For Si, $K_s=11.7$. For SiO_2 , $K_o=3.9$.

$$V_t = 2\Phi_F - \frac{K_s x_o}{K_o} \sqrt{\frac{4qN_D}{K_s \epsilon_0} (-\Phi_F)} \text{ where } \Phi_F = \frac{1}{q} (E_{i,bulk} - E_F)$$

$$\begin{aligned} \Phi_F &= (E_{i,bulk} - E_F) / q \\ &= \left(\frac{1.12}{2} - 0.8478 \right) / q \\ &= -0.2878 \text{ V} \end{aligned}$$

need to calculate $E_F = E_i - kT \ln \left(\frac{N_d}{n_i} \right)$

$$\begin{aligned} &= \frac{1.12}{2} + 0.025 \ln \left(\frac{10^{15}}{10^{10}} \right) \\ &= 0.8478 \text{ eV} \end{aligned}$$

$$V_t = 2(-0.2878) - \frac{11.7(8 \cdot 10^{-9} \text{ m})}{3.9} \left[\frac{4(1.6 \cdot 10^{-19} \text{ C})(10^{15} \text{ cm}^{-3} \times (100)^3)}{11.7(8.85 \cdot 10^{-12} \text{ F/m})} \right]^{1/2} (-0.2878)$$

$$V_t = -0.6077 \text{ V}$$