Homework 2

Answers to exercises are already provided in the text.

9-1.
$$F(s) = \frac{3}{s} - \frac{3}{s+1000} = \frac{3000}{s(s+1000)}$$
; two zeros at $s = \infty$; poles at $s = 0$; $s = -1000$.

9-3.
$$F(s) = -5 + \frac{50}{s} = \frac{-5(s-10)}{s}$$
; one zero at $s = 10$; one pole at $s = 0$.

9-7.
$$F(s) = \frac{1250000}{s(s^2 + 250000)}$$
; three zeros at $s = \infty$; poles at $s = 0$; $s = \pm j500$.

9-11. (a)
$$F_1(s) = \frac{-5s(s-10)}{(s+5)(s+10)}$$
; zeros at $s=10$; $s=\infty$; poles at $s=-5$; $s=-10$;

(b)
$$F_2(s) = \frac{20s(s^2 + 2.5 \times 10^6)}{(s^2 + 10^6)(s^2 + 4 \times 10^6)}$$
; zeros at $s = 0$; $s = \pm j1581.1$; $s = \infty$; poles at $s = \pm j1000$; $s = \pm j2000$.

9-18. (a)
$$f(t) = Au(t) - 2Au(t-T) + Au(t-2T)$$

(b)
$$F(s) = \frac{A}{s} - \frac{2A}{s}e^{-Ts} + \frac{A}{s}e^{-2Ts}$$
;

(c) apply definition

9-22. (a)
$$f_1(t) = \frac{1}{3} [-e^{-10t} + 4e^{-40t}] u(t)$$

(b)
$$f_2(t) = \left[\frac{1}{10000} - \frac{99}{10000}e^{-100t} + \frac{10989}{10000}e^{-1000t}\right]u(t)$$

9-23. (a)
$$f_1(t) = 50\delta(t) + \left[\frac{25000}{3}e^{-500t} - \frac{400000}{3}e^{-5000t}\right]u(t)$$

(b)
$$f_2(t) = 50\delta(t) + [1250e^{-100t} - 31250e^{-500t}]u(t)$$

9-30 (a)
$$f_1(t) = \left[-\frac{8}{19}e^{-t} + \frac{24}{17}e^{-3t} - \frac{320}{323}e^{-20t} \right] u(t)$$

(b)
$$f_2(t) = \left[\frac{80}{3} + \frac{100}{3}\cos(6t)\right]u(t)$$

9-32 (a)
$$f_1(t) = \left[50t - \frac{17}{3} + 6e^{-10t} - \frac{1}{3}e^{-30t}\right]u(t)$$

(b)
$$f_2(t) = \left[\frac{25000}{13}e^{-5t} + 1109.4e^{-2t}\cos(2t + 146.31^\circ)\right]u(t)$$

9-34 (a)
$$f_1(t) = \frac{1}{27}[(7+150t)e^{-50t} + (20-1200t)e^{-200t}]u(t)$$

(b)
$$f_2(t) = \frac{1}{2}[(2 - 25t)e^{-100t} - 675te^{-200t}]u(t)$$

9-55 (a)
$$\frac{d^2 v_c(t)}{dt^2} + \frac{R}{L} \frac{dv_c(t)}{dt} + \frac{1}{LC} v_c(t) = \frac{1}{LC} v_s(t)$$

(b)
$$v_c(t) = \left[1 - 20e^{-200t} + 10e^{-400t}\right]u(t) \text{ V}$$

9-65 (a)

$$f_1(\infty) = \lim_{s \to 0} s F_1(s) = 0$$

$$f_2(\infty) = \lim_{s \to 0} s F_2(s) = 10$$