

Programming Languages: Homework #8

Due on May 7, 2019 at 9:00am

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Problem 1

Solution

Problem 2

(14pts) Write the rules for a predicate `tally(E,L,N)`, which succeeds if `N` is the number of occurrences of element `E` in list `L`. The following query shows an example of using this predicate:

```
?-tally(3, [1,2,3,1,2,3],N).  
N = 2
```

Solution

```
tally(_, [], 0).  
tally(E, [E|L], N) :- tally(E, L, M), N is M+1.  
tally(E, [F|L], N) :- not(E=F), tally(E, L, N).
```

Problem 3

(15pts) Define predicates `and/2`, `or/2`, `nand/2`, `nor/2`, `xor/2`, and `equ/2` (for logical equivalence) which succeed or fail according to the result of their respective operations; e.g. `and(A,B)` will succeed, if and only if both A and B succeed. Note that A and B can be Prolog goals (not only the constants `true` and `fail`).

```
?-and(true, true).  
true
```

Solution

```
and(A,B) :- call(A), call(B).
```

```
or(A,_) :- A, !.  
or(_,B) :- B.
```

```
nand(A,B) :- not(and(A,B)).  
nor(A,B) :- not(or(A,B)).  
equ(A,B) :- or(and(A,B), and(not(A),not(B))).  
xor(A,B) :- not(equ(A,B)).
```

Problem 4

(15pts) Write the rules for a predicate $\text{gcd}(X,Y,G)$, which determines the greatest common divisor of two positive integer numbers. Use Euclid's algorithm:

<https://www.khanacademy.org/computing/computer-science/cryptography/modarithmetic/a/the-euclidean-algorithm?gcd>

$(36, 63, G)$.

$G = 9$

Solution

$\text{gcd}(0,X,X) :- X > 0, !.$

$\text{gcd}(X,Y,G) :- X \geq Y, X1 \text{ is } X-Y, \text{gcd}(X1,Y,G).$

$\text{gcd}(X,Y,G) :- X < Y, X1 \text{ is } Y-X, \text{gcd}(X1,X,G).$

Problem 5

(Extra Credit -10 pts) Write the rules for a predicate `flatten(A,B)`, which succeeds if `A` is a list (possibly containing sublists), and `B` is a list containing all elements in `A` and its sublists, but all at the same level. The following query shows an example of using this predicate:

```
?-flatten([1, [2, [3, 4]], 5], L).  
L = [1, 2, 3, 4, 5]
```

Solution

```
flatten(A,B) :- flatten(A,[],B).  
flatten(Var, T, [Var|T]) :- var(Var), !.  
flatten([],T,T) :- !.  
flatten([H|T],TailList,List) :- !, flatten(H,FlatTail,List), flatten(T,TailList,FlatTail).  
flatten(NonList,T,[NonList|T]).
```