Programming Languages: Homework #7

Due on May 2, 2019 at 9:00am

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Problem 1

(56pts) Consider an implementation of sets with Prolog lists. A set is an unordered collection of elements, without duplicates.

(a)(14pts) Write the rules for a predicate isSet(S), which succeeds if the list S is a set. The following queriesshow examplesof using this predicate:

```
?-isSet([1,2,5]).
Yes
?-isSet([1,2,1,5]).
No
```

(b)(14pts) Write the rules for a predicate subset(A,S), which succeeds if the set A is a subset of the set S. The following query shows an example of using this predicate:

```
?-subset([2,5], [1,5,3,2]).
Yes
```

(c)(14pts) Write the rules for a predicate union(A,B,C), which succeeds if the union of sets Aand Bis the set C. The following query shows an example of using this predicate:

```
?-union([2,5,4], [1,5,3,2], C).
C = [4,1,5,3,2]
```

(d)(14pts) Write the rules for a predicate intersection(A,B,C), which succeeds if the intersection of sets A and B is the set C. The following query shows an example of using this predicate:

```
?-intersection([2,5,4], [1,5,3,2], C).
C = [2,5]
```

Solution

```
(a)
isSet(L) :- duplicate(L, []),!.
duplicate([],_) :- !.
duplicate([Head|_],List) :- member(Head,List), !, fail.
duplicate([Head|Tail],List) :- duplicate(Tail,[Head|List]).
(b)
subset([],_).
subset([A|S],K) :- member(A,K), subset(S,K), !.
(c)
union([],B,B).
union([X|A],B,[X|C]) :- not(member(X,B)), union(A,B,C).
union([X|A],B,C) :- member(X,B), union(A,B,C).
(d)
intersection([],_,[]).
intersection([X|A],B,[X|C]) :- member(X,B), intersection(A,B,C).
intersection([_|A],B,C) :- intersection(A,B,C).
```

Problem 2

(14pts) Write the rules for a predicate tally(E,L,N), which succeeds if N is the number of occurrences of element E in list L. The following query shows an example of using this predicate:

```
?-tally(3, [1,2,3,1,2,3],N).
N = 2
```

Solution

```
tally(_,[],0).
tally(E,[E|L],N) :- tally(E,L,M), N is M+1.
tally(E,[F|L],N) :- not(E=F), tally(E,L,N).
```

Problem 3

(15pts) Define predicates and/2, or/2, nand/2, nor/2, xor/2, and equ/2 (for logical equivalence) which succeed or fail according to the result of their respective operations; e.g.and(A,B) will succeed, if and only if both A and B succeed. Note that A and B can be Prolog goals (not only the constants true and fail).

```
?-and(true, true).
true
```

Solution

```
and(A,B) :- call(A), call(B).

or(A,_) :- A, !.
or(_,B) :- B.

nand(A,B) :- not(and(A,B)).
nor(A,B) :- not(or(A,B)).
equ(A,B) :- or(and(A,B), and(not(A),not(B))).
xor(A,B) :- not(equ(A,B)).
```

Problem 4

(15pts) Write the rules for a predicate gcd(X,Y,G), whichdeterminesthe greatest common divisor of two positive integer numbers. Use Euclid's algorithm: https://www.khanacademy.org/computing/computer-science/cryptography/modarithmetic/a/the-euclidean-algorithm?-gcd

(36, 63, G).
G = 9

Solution

```
gcd(0,X,X) :- X > 0, !.
gcd(X,Y,G) :- X >= Y, X1 is X-Y, gcd(X1,Y,G).
gcd(X,Y,G) :- X < Y, X1 is Y-X, gcd(X1,X,G).
```

Problem 5

(Extra Credit −10 pts) Write the rules for a predicate flatten(A,B), which succeeds if A is a list (possibly containing sublists), and B is a list containing all elements in Aand its sublists, but all at the same level. The following query shows an example of using this predicate:

```
?-flatten([1, [2, [3, 4]], 5], L).
L = [1, 2, 3, 4, 5]
```

Solution

```
flatten(A,B) :- flatten(A,[],B).
flatten(Var, T, [Var|T]) :- var(Var), !.
flatten([],T,T) :- !.
flatten([H|T],TailList,List) :- !, flatten(H,FlatTail,List), flatten(T,TailList,FlatTail).
flatten(NonList,T,[NonList|T]).
```