

Logistic Map

1 Setting Up The Equation

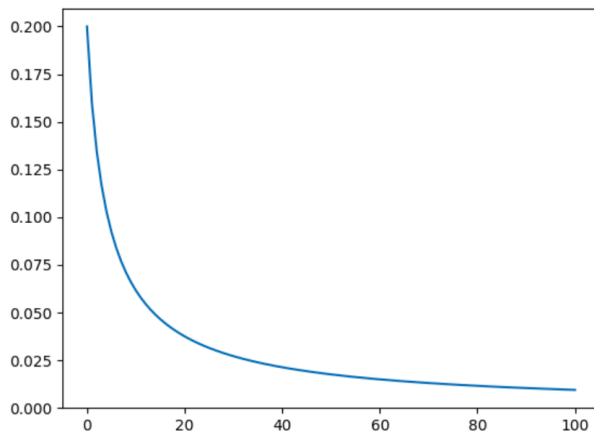
The dynamical equation is as follows: $x_{n+1} = rx_n(1 - x_n)$

where r can be considered akin to a growth rate, x_{n+1} is the population next year, and x_n is the current population.

2 Python Script

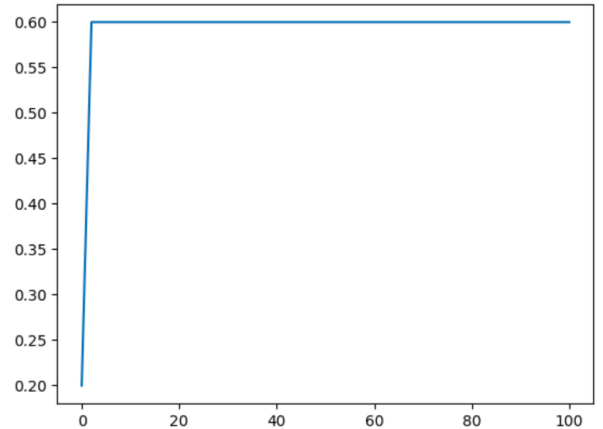
```
1 import matplotlib.pyplot as plt
2
3 def logistic_map(r, x0, n):
4     x = [x0]
5     for i in range(n):
6         x.append(r * x[-1] * (1 - x[-1]))
7     return x
8
9 # Example usage
10 r = int(input("Growth rate = "))
11 x0 = 0.2
12 n = 100
13
14 x = logistic_map(r, x0, n)
15 plt.plot(x)
16 plt.show()
```

Growth rate = 1



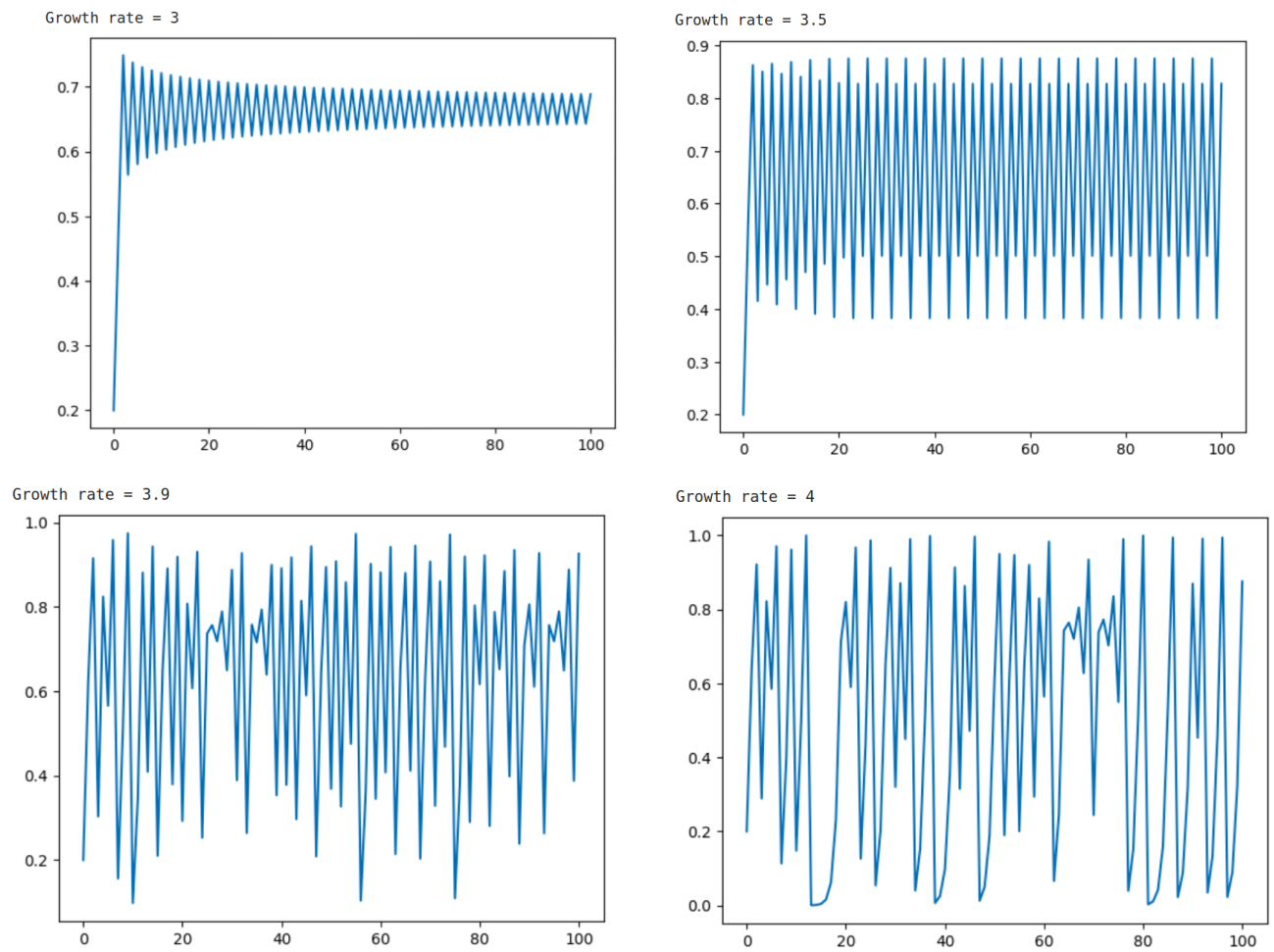
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9 # Example usage
10 r = float(input("Growth rate = "))
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12 n = 100
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14 x = logistic_map(r, x0, n)
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```

Growth rate = 2.5



When,

- $r = 1$. Population Outcome is 1.
- $r = 2.5$, two output occurs but stables into one again.
- $r = 3$, two output occurs and stabilizes.
- $r = 3.5$, four output stabilizes.



As r value increases, the number of outcomes increases. When r approaches 4, the number of outcomes becomes chaotic.