

# Quine-McCluskey

## 1- Analysis phase - Prime Implicants search & extraction

a. Visual enumeration of ALL sub-cubes (problematic if > 5 variables)

b. Tabular method

- i. Build the associated Truth Table
- ii. Group minterms according to # of 'ones' in each.  
Groups are named  $G_i$  where  $i = \# \text{'ones'}$ , they are sorted in ascending order.  
Minimum is 0 groups  $\Rightarrow F=0$ , maximum is  $n+1$  groups.
- iii. Compare Hamming distance, for each minterm of  $G_i$  and  $G_{i+1}$ .  
If H.d.=1, mark & group those minterms in  $G_i'$  using don't cares.  
If minterm is not used, it's a Prime Implicant.
- iv. Repeat ii, iii to build  $G_i''$ ,  $G_i'''$ , etc. until cannot group anymore.

Be careful! Don't cares are also considered for the H.d.

~~-000~~  
~~01-0~~

v. Remaining minterms cannot be used, so they are Prime Implicants.

Keep only one PI if, for example:

$G_0''$     -0-    (0, 1, 4, 5)  
          -0-    (0, 4, 1, 5)

PI1

If incompletely specified logic functions,

$$f(a, b, c) = \sum m(0, 1, 3, 4, 5, 7) + \sum d(2, 6)$$

$\Rightarrow$  hypothesis that all don't cares are 1 (as they were in  $\sum m$ )

## 2- Synthesis phase - Minimal cover of the logic function

a. Minimal function cover table (graphical method, not very good)

- i. Build a table from minterms -without don't cares- (lines) and found Prime Implicants.
- ii. For each PI mark all minterms covered by this PI.
- iii. Find Essential PIs (the only ones covering certain minterms)
- iv. Find PIs so that all minterms are covered.

b. Minimal cover equation (Algebraic method that generates all possible solutions and that can be automatized)

- i. For each minterm: OR all PI covering this minterm.  
So that if  $i_1, i_2$  are in the same line, we obtain  $(i_1+i_2)$
- ii. We AND all results so that if  $(i_1+i_2), (i_1+i_5)$  covers different lines:  
we have  $(i_1+i_2) \cdot (i_1+i_5)$ . Essential PIs will be isolated terms.
- iii. Drop double terms and terms containing an EPI.
- iv. Distribute terms like that:  $(i_1+i_4) (i_1+i_2) \rightarrow (i_1+i_2 \cdot i_4)$  and make sure there is no parenthesis anymore.  
The result is an OR of possible solutions (a SoP of PI).
- v. Choose the solution with the least number of smallest possible gates and rewrite it as an OR of PI:  $i_2 \cdot i_4 \rightarrow PI_2 + PI_4$