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Evaluating the agreement between measurements and models of net ecosystem exchange at different times and time scales using wavelet coherence: an example using data from the North American Carbon Program Site-Level Interim Synthesis

P. C. Stoy¹, M. Dietze², A. D. Richardson³, R. Vargas⁴, A. G. Barr⁵,
R. S. Anderson⁶, M. A. Arain⁷, I. T. Baker⁸, T. A. Black⁹, J. M. Chen¹⁰,
R. B. Cook¹¹, C. M. Gough¹², R. F. Grant¹³, D. Y. Hollinger¹⁴, R. C. Izaurralde¹⁵,
C. J. Kucharik¹⁶, P. Lafleur¹⁷, B. E. Law¹⁸, S. Liu¹⁹, E. Lokupitiya²⁰, Y. Luo²¹,
J. W. Munger²², C. Peng²³, B. Poulter²⁴, D. T. Price²⁵, D. M. Ricciuto¹¹,
W. J. Riley²⁶, A. K. Sahoo²⁷, K. Schaefer²⁸, C. R. Schwalm²⁹, H. Tian³⁰,
H. Verbeeck³¹, and E. Weng³²

Wavelet coherence
for multiple models

P. C. Stoy et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



¹Department of Land Resources and Environmental Sciences, Montana State University, Bozeman, MT 59717, USA

²Department of Earth and Environment, Boston University, Boston, MA 02215, USA

³Department of Organismic & Evolutionary Biology, Harvard University, Cambridge, MA, USA

⁴Department of Plant and Soil Sciences, Delaware Environmental Institute, University of Delaware, Newark, DE 19717, USA

⁵Climate Research Division, Atmospheric Science and Technology Directorate, Saskatoon, SK S7N 3H5, Canada

⁶Numerical Terradynamic Simulation Group, University of Montana, Missoula, MT 59812, USA

⁷School of Geography and Earth Sciences and McMaster Centre for Climate Change, McMaster University, Hamilton, ON L8S 4K1, Canada

⁸Department of Atmospheric Science, Colorado State University, Fort Collins, CO 80523, USA

⁹Faculty of Land and Food Systems, University of British Columbia, Vancouver, BC V6T 1Z4, Canada

¹⁰Department of Geography and Program in Planning, University of Toronto, Toronto, ON M5S 3G3, Canada

¹¹Environmental Sciences Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

¹²Department of Biology, Virginia Commonwealth University, Richmond, VA 23284, USA

¹³Department of Renewable Resources, University of Alberta, Edmonton, AB T6G 2E3, Canada

¹⁴Northern Research Station, USDA Forest Service, Durham, NH 03824, USA

¹⁵Pacific Northwest National Laboratory and University of Maryland, College Park, MD 20740, USA

¹⁶Department of Agronomy & Nelson Institute Center for Sustainability and the Global Environment, University of Wisconsin – Madison, Madison, WI 53706, USA

¹⁷Department of Geography, Trent University, Peterborough, ON K9J 7B8, Canada

¹⁸Department of Forest Ecosystems and Society, Oregon State University, Corvallis, OR 97331, USA

¹⁹US Geological Survey (USGS) Earth Resources Observation and Science (EROS) Center, Sioux Falls, SD 57198, USA

²⁰Department of Zoology, POB 1490, University of Colombo, Colombo 03, Sri Lanka

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Abstract

Earth system processes exhibit complex patterns across time, as do the models that seek to replicate these processes. Model output may or may not be significantly related to observations at different times and on different frequencies. Conventional model diagnostics provide an aggregate view of model-data agreement, but usually do not identify the time and frequency patterns of model misfit, leaving unclear the steps required to improve model response to environmental drivers that vary on characteristic frequencies. Wavelet coherence can quantify the times and frequencies at which models and measurements are significantly different. We applied wavelet coherence to interpret the predictions of twenty ecosystem models from the North American Carbon Program (NACP) Site-Level Interim Synthesis when confronted with eddy covariance-measured net ecosystem exchange (NEE) from ten ecosystems with multiple years of available data. Models were grouped into classes with similar approaches for incorporating phenology, the calculation of NEE, and the inclusion of foliar nitrogen (N). Models with prescribed, rather than prognostic, phenology often fit NEE observations better on annual to interannual time scales in grassland, wetland and agricultural ecosystems. Models that calculate NEE as net primary productivity (NPP) minus heterotrophic respiration (HR) rather than gross ecosystem productivity (GPP) minus ecosystem respiration (ER) fit better on annual time scales in grassland and wetland ecosystems, but models that calculate NEE as GPP – ER were superior on monthly to seasonal time scales in two coniferous forests. Models that incorporated foliar nitrogen (N) data were successful at capturing NEE variability on interannual (multiple year) time scales at Howland Forest, Maine. Combined with previous findings, our results suggest that the mechanisms driving daily and annual NEE variability tend to be correctly simulated, but the magnitude of these fluxes is often erroneous, suggesting that model parameterization must be improved. Few NACP models correctly predicted fluxes on seasonal and interannual time scales where spectral energy in NEE observations tends to be low, but where phenological events, multi-year oscillations in climatological drivers,

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



and ecosystem succession are known to be important for determining ecosystem function. Mechanistic improvements to models must be made to replicate observed NEE variability on seasonal and interannual time scales.

1 Introduction

- 5 Land surface models represent our understanding of how terrestrial ecosystems function in the climate system. It is critical to test, compare and improve these models as new information and methods become available, especially because numerous recent syntheses have demonstrated a considerable lack of model skill (Schwalm et al., 2010; Wang et al., 2010; Schaefer et al., 2012). Models are commonly diagnosed using statistical metrics that can be combined for a more complete view of model performance 10 (Taylor, 2001). Such model diagnostics are able to identify whether a different model, different model parameterization, or different subroutine represents an improvement (Akaike, 1974), but are not intended to identify the symptoms of model failure across time and scales in time to identify the conditions that result in poor performance. Residual analyses and detailed investigations of model performance during different time 15 periods give important insight into the mechanisms underlying model failure, but are rarely interpreted with respect to patterns of model/measurement mismatch (see however Dietze et al., 2011; Mahecha et al., 2010; Vargas et al., 2010). In this paper, we present a formal analysis of model/measurement mismatch across times and frequencies. Such an analysis may also provide insight into how improvements to model 20 structure and/or parameterization should be made (Williams et al., 2009).

Improving individual models is a noteworthy goal, but modern efforts combine multiple observations and model simulations, i.e. multiple databases, to arrive at a synthesis (Friedlingstein et al., 2006; Schwalm et al., 2010). In other words, such studies adopt an 25 data-intensive approach to scientific inference (Gray, 2009), and techniques from non-linear time series analysis and knowledge discovery in databases may provide important insights into the aggregate or divergent behavior of these model and observational

BGD

10, 3039–3077, 2013

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



databases. In this study, we quantify significant relationships among twenty ecosystem models and ten multi-year time series of eddy covariance NEE measurements from the North American Carbon Program (NACP) Site-Level Interim Synthesis (Schwalm et al., 2010) using a technique called wavelet coherence (Grinsted et al., 2004; Torrence and Webster, 1999). Wavelet coherence is conceptually similar to a measure of correlation between data series across time and time scale (related to frequency). Like correlation, significant values of wavelet coherence can be quantified, in this case by comparison against appropriate synthetic null spectra. Unlike simple correlation, statistical significance can be quantified across both time and time scales simultaneously.

We use wavelet coherence to determine the times and time scales when NACP models and measurements are significantly related and, importantly, when they are not. Notably, wavelet coherence can quantify significance in the time and time scale domains even when common power (i.e. shared variability) among time series on these scales is low (Grinsted et al., 2004), and may offer an improvement over residual analyses for this reason. Wavelet coherence has found applications in comparing ecological models and measurements for the goal of model improvement (Williams et al., 2009), but not across multiple model and observational time series to date.

Previous studies of ecosystem models in the time scale domain have demonstrated that models tend to miss patterns in flux observations on intermediate (i.e. weekly to monthly) and interannual time scales (Siqueira et al., 2006; Stoy et al., 2005). Biological responses to variability in climate often dominates flux variability on these time scales (Richardson et al., 2007), and models tend to replicate these biological responses poorly. Such responses include weekly-to-monthly shifts in leaf out/leaf drop phenology and the multitude of factors including lagged responses known to contribute to interannual carbon flux variability. With respect to the NACP, findings to date have identified superior model fit when phenology is prescribed by remote sensing observations as opposed to prognostic via a phenology model, when a sub-daily (i.e. half hourly or hourly) rather than a daily time step is used, and when net ecosystem exchange (NEE) is calculated as the difference between gross primary productivity (GPP) and

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



ecosystem respiration (ER) rather than the difference between net primary productivity (NPP) and heterotrophic respiration (HR) (Schwalm et al., 2010; Richardson et al., 2012). Schwalm et al. (2010) also found that model performance was poorer during spring and fall when phenological events dominate surface flux and during dry periods within the growing season. Less certain is how models match measurements on multiple time scales as they respond to climatic and biological forcings that act on multiple time scales (Dietze et al., 2011). Quantifying such model-measurement relationships contributes to the NACP objective to measure and understand the sources and sinks of CO₂ in North America. Following previous studies, we hypothesize that models will tend to match flux patterns on daily and annual time scales, and we focus our investigation on time scales between weeks and multiple months as well as interannual time scales, where we postulate that models will replicate observations more poorly.

2 Methods

2.1 Eddy covariance data and ecosystem models

Half hourly (or hourly) micrometeorological and eddy covariance measurements were collected by site principal investigators and research teams, and these data were provided to the AmeriFlux and Fluxnet-Canada consortia to create the NACP Site Level Interim Synthesis product (Schwalm et al., 2010). For this analysis we examine 20 ecosystem models against measurements of the net ecosystem exchange of CO₂ (NEE) from the ten eddy covariance research sites investigated by Dietze et al. (2011) (Table 1). These sites were chosen because the length of the observation period tended to be longer and more continuous, allowing us to investigate interannual (multiple year) variability, and because more models tended to be run for these ecosystems (Schwalm et al., 2010; Schaefer et al., 2012). Missing meteorological data were gap-filled using National Oceanic and Atmospheric Administration (NOAA) meteorological station data and Daymet reanalysis products (Ricciuto et al., 2009). Half-hourly

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



(or hourly) NEE values were filtered to remove periods of insufficient turbulence determined using friction velocity (u_*) thresholds, and despiked to remove outliers (Papale et al., 2006; Reichstein et al., 2005). Missing NEE data were then gap-filled following Barr et al. (2004). Model runs at each site followed a prescribed protocol for intercomparison described by Schwalm et al. (2010). Ancillary biological, disturbance, edaphic, and management data used by model runs for each site were given by the AmeriFlux BADM templates (Law et al., 2008). The ecosystem models explored here are listed in Table 2 and described in more detail in Schwalm et al. (2010) and the original publications.

10 2.2 Wavelet coherence

The times and time scales at which two corresponding data series (here time series) have high common power can be quantified using the wavelet cospectrum. Wavelet coherence uses wavelet spectral and cospectral calculations to quantify correlations in the time and time scale domains (Grinsted et al., 2004; Torrence and Webster, 1999).

15 Briefly, following Grinsted et al. (2004), wavelet coherence is defined in a similar manner to the coefficient of determination (r^2) using instead wavelet coefficients:

$$r_n^2 = \frac{|S(s^{-1}W_n^{XY}(s))|^2}{S(s^{-1}|W_n^X(s)|)^2 S(s^{-1}|W_n^Y(s)|)^2} \quad (1)$$

where $W_n^X(s)$ and $W_n^Y(s)$ are the wavelet coefficients from the model (Y) and measurement (X) time series at time n on time scale s , $W_n^X Y(s)$ is the cross wavelet transform ($W_n^X(s)$ times the complex conjugate of $W_n^Y(s)$), and S is a smoothing operator for the Morlet wavelet following Torrence and Webster (1999) and Grinsted et al. (2004).

20 Grinsted et al. (2004) noted that many geophysical time series are characterized by red (Brownian) noise, which can be modeled as a first-order autoregressive process (AR1). These patterns can be used as a null model by simulating synthetic data that were simulated with AR1 coefficients to quantify significant wavelet coherence at the

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

95 % confidence level. Eddy covariance time series approximate pink noise ($1/f$ noise) (Richardson et al., 2008), which is a class of autoregressive noise, and Grinsted et al. (2004) demonstrated that the color of noise has little impact on the determination of the significance level. Wavelet coherence values above 0.7 were found by Grinsted et al. 5 (2004) to be significant against synthetic data sets across a wide range of scales when 10 scales per octave (i.e. per a doubling or halving of frequency) were chosen in the scale-wise smoothing, although a higher coherence values (ca. 0.8 or higher) should be chosen at very high and low frequencies. We used 10 scales per octave and also chose the commonly used 0.7 wavelet coherence threshold for determining significance. We 10 de-emphasize the interpretation of high frequency coherence (e.g. on hourly and sub-daily time scales) to focus on the longer time scales (i.e. > one day) where models often fail. Wavelet coefficients on very long time scales (years to multiple years) often exceed the so-called cone of influence beyond which the coherence calculation is dominated by edge effects because of incomplete time-locality across frequencies (Torrence et al., 15 1998). Wavelet coefficients outside the cone of influence are unreliable and will not be interpreted here. Also for consistency with Grinsted et al. (2004), we chose the Morlet wavelet basis function with a wavenumber of six. Time series were truncated to powers of two for spectral calculations.

Results are presented with two different representations of time scale in mind. For 20 the demonstration of the wavelet coherence technique, we interpret all relevant scales from twice the observation time step (usually 1 to 2 h) to $\frac{1}{2}$ the length of the truncated time series. For the comparison of model output against flux observations, we interpret wavelet coherence on time scales longer than one day to enable the comparison of models that operate on daily and sub-daily time steps and to focus our analysis on 25 the longer time scales (e.g. seasonal or interannual time scales) on which models often fail. By definition, some wavelet coherence values will exceed the significance threshold by chance. To avoid over-interpreting the outcome, we discuss only large regions in the time/time scale wavelet half-plane for which the coherence between

Wavelet coherence
for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



model and measurements is adjudged to be statistically significant or not significant following Grinsted et al. (2004).

Combined wavelet coherence significance analysis

A wavelet half-plane of significance values can be created for each model-
5 measurement combination for each site. As such, significance values from wavelet half-planes that represent different models run for a single site can be combined for an aggregate view of model performance. The approach that we explore is to sum wavelet half-planes that represent significance values (i) for models that possess a given attribute A (A_i), divide by the number of models with A (N_A), then subtract the sum of the
10 wavelet half-planes of significance values for models that possess the opposing model attribute B (B_i) divided by the number of models with B (N_B), using:

$$\frac{1}{N_A} \sum_{i=1}^{N_A} A_i - \frac{1}{N_B} \sum_{i=1}^{N_B} B_i \quad (2)$$

The purpose of this calculation is to provide a simple metric between –1 and 1 for cases where N_A and N_B may be different but are weighted equally to simplify comparison.
15 The goal is to identify regions in time and time scale at different sites where a certain model attribute outperforms the other (or others) across all models investigated here, with the goal of interpreting the success or failure of different model formulations across time and time scale for different ecosystem types. To avoid over-interpreting results, we only plot absolute values of Eq. (2) that exceed 0.5 to focus our study on
20 times and time scales where the first and second terms of Eq. (2) differ by more than 50 %.

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



3 Results and discussion

3.1 Wavelet coherence

We begin by demonstrating significance testing using wavelet coherence with a single site/model combination. The time series of NEE from the Harvard Forest (US-Ha1) site encompasses 140 256 potential hourly observations from 1991 until the end of 2006 (Urbanski et al., 2007). We interpret the 2^{17} (= 131 072) NEE measurements between 18 January 1992 and the end of the time series and NEE simulations from the Ecosystem Demography model version 2 (ED2, Medvigy et al., 2009). The wavelet coherence between US-Ha1 and ED2 tends to be large (> 0.7) on the daily time scale (24 h, ca. $10^{1.38}$) during growing seasons and on the annual time scale (8760 h, ca. $10^{3.94}$) across the entire measurement period (Fig. 1). Measured NEE from US-Ha1 and modeled NEE from ED2 demonstrate common power on these time scales. Some multi-day to multi-month (seasonal) periods likewise have high wavelet coherence, but wavelet coherence is generally low (< 0.7) on time scales longer than one year.

3.2 Wavelet coherence significance testing

Wavelet coherence coefficients were converted to binary significance values as demonstrated in Fig. 2. Here, regions in the time/scale wavelet half-plane that have significant coherence at the 95 % level (i.e. wavelet coherence coefficients > 0.7 following Grinsted et al., 2004) are given the value of one and appear in white in the figure, and non-significant regions are given the value of zero and appear in black in the figure. Figure 2 reveals that ED2-modeled NEE is significantly related to the NEE measurements on daily time scales during the growing season (i.e. the white areas in Fig. 2), on the annual time scale, and on seasonal time scales during the earlier part of the measurement period, but not during most of the remaining times and time scales. Smaller regions of the wavelet half-plane with significant coherence should not be over-interpreted as these occur in some 5 % of cases by chance.

BGD

10, 3039–3077, 2013

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



3.3 Wavelet coherence significance testing of multiple models at a single site

Comparing significant wavelet coherence among US-Ha1 NEE and the output of multiple models (choosing SiBCASA, ED2, LoTEC, and ORCHIDEE, Fig. 3) reveals that the observed annual variability of NEE tends to be well-replicated by models. This finding is expected given the dominant role of orbital motions in controlling climate and flux in the temperate zone on these time scales. We note that Fig. 3 and subsequent figures ignore time scales smaller than one day to facilitate comparison between models that run on the daily and sub-daily time steps, and to emphasize longer time scales in the wavelet coherence significance tests.

Figure 3 also demonstrates that results from some models are significantly related to measurements from different regions of the time/scale half-plane. LoTEC in particular is frequently related to observations on weekly and monthly time scales, but LoTEC is the only NACP model that implemented a data assimilation procedure, and should be expected to have a stronger relationship to measurements (Schwalm et al., 2010).

LoTEC results are discussed further in Appendix A. Significant wavelet coherence exists among US-Ha1 NEE measurements and the SiBCASA, ED2 and LoTEC models, but not ORCHIDEE, on the seasonal time scale (one to several months) before 2002. Such findings question whether common model attributes (Table 2) are responsible for good fit or poor fit during these times and time scales.

A major advantage of converting the wavelet coherence half-planes into binary significance maps is that the output of different models for the different measurement sites can be averaged or summed to explore aggregate model performance (e.g. via Eq. (2) or other metrics). We can begin by summing the significance patterns of all 15 models that were run for US-Ha1 (Fig. 4, see Dietze et al., 2011). Figure 4 demonstrates that

all models are related to NEE on the annual time scale for at least part of the measurement period. More than ten models are significantly related to the measurements on seasonal time scales, and frequent periods when multiple models are significantly related to measurements appear on weekly and monthly time scales. These features may

BGD

10, 3039–3077, 2013

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



be related to model structural attributes that can guide model testing and interpretation. We demonstrate such an approach by first exploring further the NEE observations and model output for US-Ha1. We then proceed to interpret results from the other nine research sites evaluated in this analysis (Table 1).

5 3.4 The role of common model features in determining significant wavelet coherence

Models in the NACP synthesis share features in common (Table 2, Schwalm et al., 2010). The role of these features in model performance across time and scale can be explored using the binary wavelet coherence significance approach demonstrated in 10 Figs. 2 and 3. Logical model attributes to explore follow the findings of Schwalm et al. (2010) and include comparisons between prescribed versus prognostic canopy phenology, the calculation of NEE as GPP ecosystem respiration (ER) or as net ecosystem productivity (NEP) heterotrophic respiration (HR), and the inclusion of foliar nitrogen in the model (Table 2).

15 The results of the combined wavelet coherence significance analysis for US-Ha1 are shown in Fig. 5. In Fig. 5a, regions in the wavelet half-plane for which coherence between NEE measurements from US-Ha1 and all models with prognostic phenology is significant are given the value of 1 (see Eq. 2). From this, significant regions in the half-plane for which all models with prescribed phenology are subtracted. If all models 20 with prognostic phenology are significantly related to NEE measurements for a given region in time and scale, and none with prescribed phenology are significant, the value of Eq. (2) equals $1 - 0 = 1$ (dark blue). If the opposite holds, then the region equals negative 1 and is shown in dark red. This procedure is repeated for the different model attributes investigated (Table 2).

25 For example, from Fig. 5a, all (or most) models with prognostic phenology are often significantly related to NEE observations from US-Ha1 during seasonal time scales, especially earlier in the measurement period. These results suggest that phenology models are working well in simulating the seasonal patterns that they seek to replicate,



but prescribing phenology using remote sensing observations results in model fits at these times and time scales that are not significant. Schwalm et al. (2010) found that models with prognostic phenology and (to a lesser degree) those that calculate NEE as GPP – ER tend to show better performance across sites (Fig. 5a, b). When this holds at US-Ha1, it is on time scales between ca. $10^{2.9}$ h (i.e. one month) and $10^{3.5}$ h (i.e. 3 months), which are the intermediate time scales on which model performance tends to diverge as identified by Dietze et al. (2011). This analysis reveals that the model attributes identified by Schwalm et al. (2010) as advantageous, prognostic phenology and $\text{NEE} = \text{GPP} - \text{ER}$, correspond to better performance on monthly to seasonal time scales at US-Ha1. Interestingly, including foliar N in the model did not result in unambiguous model improvement (Fig. 5c), and there were times and time scales when excluding N from the model resulted in improved model fit. Interpreting significance across all sites and model attributes at all times and time scales is beyond the scope of this analysis, and we focus the remainder of our comparison on the dominant features of the combined wavelet coherence significance analysis for different models and sites (Tables 1 and 2).

3.5 Phenology

Ecosystem models often fail to replicate the timing of spring green up and autumn leaf senescence (Richardson et al., 2012) and, interestingly, incorporating satellite remote sensing data (i.e. prescribing phenology in models) may not represent an improvement in capturing phenological events (Fisher et al., 2007). However, NACP model results from the ten study sites indicate that prescribing the phenology of leaf area index (LAI) often improves modeled carbon fluxes on seasonal and annual time scales at the cold, non-forest sites (i.e. CA-Let and CA-Mer, the deciduous forests US-UMB and US-Ha1, and the agricultural ecosystem US-Ne1 (Figs. 5 and 6). The creation of effective prognostic phenology models for grasslands and croplands remains challenging, especially when cropping systems often depend on manager decisions. Remote sensing is often unsuccessful for capturing grassland phenology (Reed et al., 1994), due in part

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

to the fact that the shift from green to brown biomass is critical for modeling NEE but can be subtle and difficult to ascertain remotely (Sus et al., 2010). Despite many successes, prescribing phenology resulted in erroneous model fit in some ecosystems, times, and time scales (Fig. 6), in agreement with Richardson et al. (2012) who found that model biases of two weeks or more for were common for deciduous forests. Predicting phenology in the coniferous forests (CA-Obs and US-Ho1) is a superior strategy for modeling NEE on seasonal time scales. This makes sense given the difficulty of using remote sensing to detect seasonal changes in leaf area and photosynthetic activity in evergreen canopies.

10 3.6 NEE calculation

Models calculate ecosystem carbon uptake and loss in different ways and the NACP models can roughly be categorized as those that calculate NEE as GPP – ER and those that calculate NEE as NPP – HR (Schwalm et al., 2010). Models that calculate NEE as NPP – HR tend to fit better than models that calculate NEE as GPP – ER on the

15 annual time scale at the Canadian grassland (CA-Let) and bog (CA-Mer) sites, which are characterized by short-statured vegetation and pronounced seasonality (Fig. 7).

Models that calculate NEE as NPP – HR also represent an improvement on seasonal and annual time scales at the deciduous forests Ca-Oas and US-UMB, and at daily to weekly time scales at the coniferous forests Ca-Obs, US-Ho1, and US-Me2. Models

20 that calculate NEE as GPP – ER tend to be better on monthly to seasonal time scales at the coniferous forests CA-Obs and US-Ho1. In general, simulating NEE and HR results in poorer NEE model fit at seasonal and annual time scales in coniferous stands, and simulating GPP and ER presents more of a challenge in grasslands, wetlands, and

deciduous forests. Many of the wavelet half-planes in Fig. 7 show a scale-wise shift (from red to blue or vice versa) as one moves to longer scales in time, suggesting that the response of GPP, NPP, ER and HR to environmental drivers that act on different

25 time scales need to be examined carefully for proper frequency response.

3.7 Nitrogen

Models utilizing measurements of foliar N show improved fits on interannual time scales than models that exclude N at a coniferous forest (US-Ho1; Fig. 8f) and to a lesser degree at a deciduous forest (CA-Oas, Fig. 8d). This finding supports the incorporation of canopy N as an important component for accurately modeling spatial and temporal patterns in NEE (Hollinger et al., 2009; Ollinger et al., 2005, 2008). However, it is discouraging that incorporating N improves interannual model fit for only a couple of sites rather than for all sites; note for example the poor fit of models that include N on time scales shorter than the interannual time scale at Ca-Oas (Fig. 8d). Climatic variables tend to be unrelated or poorly related to observed NEE on interannual time scales (Stoy et al., 2009), and variability in biological drivers like canopy N are thought to be a principle drivers of NEE variability on interannual time scales (Richardson et al., 2007). The role of biological lags (e.g. growth and NPP lagging behind C uptake) tend to be poorly represented in the current generation of ecosystem models (Keenan et al., 2012), as are the dynamics of the non-structural carbohydrates that can contribute to such lags (Gough et al., 2009, 2010). Modeling the biological responses to interannual climatic variability continues to be a major research challenge (Richardson et al., 2007; Siqueira et al., 2006), and it appears that modeling N improves models of NEE, but only in certain instances. Including foliar N improves model fit on certain time scales for different sites; for example including N appears to improve models in CA-Let, CA-Oas and CA-Obs, during summer months in 2006. The summer of 2006 was at the time the second warmest on record in Canada, but the role of N in improving modeled NEE during these conditions is difficult to interpret.

3.8 The analysis of models at multiple time scales

We used wavelet coherence as a criterion for model/measurement comparison in this study. Spectral analyses can also be used to discriminate among model subroutines and inputs (Stoy et al., 2005) or demonstrate model improvement (Williams et al.,

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



2009), and it is for these purposes that wavelet coherence may find the most application in the biogeosciences. Wang et al. (2011) recently used wavelet analysis to quantify patterns of CABLE model output (Kowalczyk et al., 2006) and demonstrated how model improvements improved predictions of NEE, latent heat and sensible heat on multiple time scales, although observed patterns in interannual variability in NEE remained difficult for CABLE to resolve. We suggest that any comprehensive model diagnostic toolkit should explore model frequency response, and we demonstrate the application of wavelet coherence as a model-measurement comparison technique that is also visually intuitive. It is important to note that wavelet coherence tests for matches in patterns, rather than magnitudes, and by itself is an incomplete metric for model fidelity. Future research efforts should compare wavelet-based approaches with other time series decomposition techniques including singular systems analysis (Mahecha et al., 2010), spectral analysis of model residuals (Dietze et al., 2011; Vargas et al., 2010), and/or to quantify causal relationships among measurements and models across time and spectra using the Granger definition (Detto et al., 2012).

4 Conclusions

We demonstrated an application of wavelet coherence for testing significant relationships between flux observation and the output of multiple ecosystem models run at multiple different study sites. Models with prognostic phenology were often significantly related to NEE measurements on seasonal time scales in coniferous sites, but models with prescribed phenology improved seasonal and annual model fit in grassland and wetland study sites, and to a lesser degree in the deciduous forests US-Ha1 and US-UMB. The inclusion of foliar N improved model performance on interannual time scales at US-Ho1.

Model pattern tended to match observed NEE on diurnal time scales during the growing season and on annual time scales (e.g. Figs. 1 and 2), but previous analyses indicate that models often misrepresent the magnitude of fluxes on these highly-energetic

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



time scales (Dietze et al., 2011). Despite correct frequency responses on growing-season diurnal and annual time scales as we find here, Dietze et al. (2011) demonstrated that proper parameterization of flux magnitude on these scales should remain a focus of modeling efforts. LoTEC results (Fig. 2) hint that data assimilation can improve model fit on the intermediate weekly to seasonal time scales during many periods, but modeled flux variability on diurnal and interannual time scales was not significantly related to measurements, suggesting that mechanistic model responses still need improvement. Mechanistic explanations for describing interannual NEE variability still elude most models, although correctly modeling N dynamics may be a strategy for progressing on this problem in some ecosystems (Fig. 8).

Wavelet coherence adds an additional diagnostic tool to a modeler's conceptual toolbox for evaluating the performance of single models or suites of models (Grinsted et al., 2004; Torrence et al., 1998; Williams et al., 2009). Future efforts should determine the benefits and drawbacks of wavelet, Fourier, and Singular Systems Analysis approaches for model/measurement comparisons (Katul et al., 2001; Mahecha et al., 2010; Siqueira et al., 2006; Vargas et al., 2010), use the outcomes of multiple spectral analyses to provide insight into how and why models fail, and use this information to improve model performance at the multiple times and time scales at which biogeochemical fluxes vary.

20 Appendix A

Data assimilation for formally fusing observations and models has gained increased attention in the Biogeosciences (Hill et al., 2011; Rastetter et al., 2010; Raupach et al., 2005; Williams et al., 2005). LoTEC applied a data assimilation procedure in the NACP modeling exercise, and output in many instances represented a striking improvement against the aggregate output of other models (Fig. 9). Namely, LoTEC output is significantly related to (and other models on average not significantly related to) NEE

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



measurements across many time scales at the deciduous forests CA-Oas and US-UMB. LoTEC also demonstrated improved fit compared to other models at annual time scales at the coniferous forests CA-Obs and US-Ho1 and the crop US-Ne1. LoTEC was not significantly related to NEE measurements (and the average of other models were) across many times and time scales at CA-Ca1, CA-Let, CA-Mer, CA-Obs, and US-Me2. Results suggest that the optimized parameters computed in the LoTEC data assimilation procedure can improve fit across times and time scales, especially for some of the ecosystems that exhibit pronounced seasonality in canopy dynamics (i.e. some deciduous forests, and the agricultural ecosystem). Results also demonstrate that the data assimilation routine does not always result in significant relationships between measurements and models; there are many periods, often time scales between a day and about a month and a half (10^3 h, Fig. 3), where LoTEC is not significantly related to measurements. Such findings demonstrate the importance of data assimilation, but also demonstrate that data assimilation should not take the place of efforts to improve model structure.

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Wavelet coherence
for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



References

- Akaike, H.: A new look at the statistical model identification, *IEEE T. Automat. Contr.*, 19, 716–723, 1974. 3043
- Arain, M. A., Yaun, F., and Black, T. A.: Soil-plant nitrogen cycling modulated carbon exchanges in a western temperate conifer forest in Canada, *Agr. Forest Meteorol.*, 140, 171–192, 2006. 3068
- Baker, I. T., Pihodko, L., Denning, A. S., Goulden, M., Miller, S., and da Rocha, H. R.: Seasonal drought stress in the Amazon: reconciling models and observations, *J. Geophys. Res.*, 113, G00B01, doi:10.1029/2007JG000644, 2008. 3068
- Barr, A. G., Black, T. A., Hogg, E. H., Kljun, N., Morgenstern, K., and Nesic, Z.: Inter-annual variability in the leaf area index of a boreal aspen-hazelnut forest in relation to net ecosystem production, *Agr. Forest Meteorol.*, 126, 237–255, 2004. 3046, 3067
- Causarano, H. J., Shaw, J. M., Franzluebbers, A. J., Reeves, D. W., Raper, R. L., Balkcom, K. S., Norfleet, M. L., and Izaurralde, R. C.: Simulating field-scale soil organic carbon dynamics using EPIC, *Soil Sci. Soc. Am. J.*, 71, 1174–1185, 2007. 3068
- Detto, M., Molini, A., Katul, G. G., Stoy, P. C., Palmroth, S., and Baldocchi, D. D.: Assessing cause and effect in ecological time series: an application of conditional Granger's spectral causality theory, *Am. Nat.*, 179, 524–535, 2012. 3055
- Dietze, M., Vargas, R., Richardson, A. D., Stoy, P. C., Barr, A. G., Anderson, R. S., Arain, A., Baker, I. T., Black, T. A., Chen, J. M., Ciais, P., Flanagan, L. B., Gough, C. M., Grant, R. F., Hollinger, D. Y., Izaurralde, C., Kucharik, C. J., Lafleur, P. M., Liu, S., Lokupitiya, E., Luo, Y., Munger, J. W., Peng, C., Poulter, B., Price, D. T., Ricciuto, D. M., Riley, W. J., Sahoo, A. K., Schaefer, K., Tian, H., Verbeeck, H., and Verma, S. B.: Characterizing the performance of ecosystem models across time scales: a spectral analysis of the North American Carbon Program site-level synthesis, *J. Geophys. Res.*, 116, G04029, doi:10.1029/2011JG001661, 2011. 3043, 3045, 3050, 3052, 3055, 3056, 3067, 3072
- Fisher, J. I., Richardson, A. D., and Mustard, J. F.: Phenology model from surface meteorology does not capture satellite-based greenup estimations, *Glob. Change Biol.*, 13, 707–721, doi:10.1111/j.1365-2486.2006.01311.x, 2007.
- Flanagan, L. B., Wever, L. A., and Carlson, P. J.: Seasonal and interannual variation in carbon dioxide exchange and carbon balance in a northern temperate grassland, *Glob. Change Biol.*, 8, 599–615, 2002. 3067

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10, 3039–3077, 2013

Wavelet coherence
for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



- Friedlingstein, P., Cox, P., Betts, R. A., Bopp, L., von Blow, W., Brovkin, V., Cadule, P., Doney, S. C., Eby, M., Fung, I. Y., Bala, G., John, J., Jones, C. D., Joos, F., Kato, T., Kawamiya, M., Knorr, W., Lindsay, K., Matthews, H. D., Raddatz, T., Rayner, P. J., Reick, C., Roeckner, E., Schnitzler, K.-G., Schnur, R., Strassmann, K., Weaver, A. J., Yoshikawa, C., and Zeng, N.: Climate-carbon cycle feedback analysis: results from the C4MIP model inter-comparison, *J. Climate*, 19, 3337–3353, 2006. 3043
- Gough, C. M., Vogel, C. S., Schmid, H. P., Su, H.-B., and Curtis, P. S.: Multi-year convergence of biometric and meteorological estimates of forest carbon storage, *Agr. Forest Meteorol.*, 148, 158–170, 2008. 3067
- Gough, C. M., Flower, C. E., Vogel, C. S., Dragoni, D., and Curtis, P. S.: Whole-ecosystem labile carbon production in a north temperate deciduous forest, *Agr. Forest Meteorol.*, 149, 1531–1540, 2009. 3054, 3067
- Gough, C. M., Flower, C. E., Vogel, C. S., and Curtis, P. S.: Phenological and temperature controls on the temporal non-structural carbohydrate dynamics of *Populus grandidentata* and *Quercus rubra*, *Forests*, 1, 65–81, 2010. 3054
- Grant, R. F., Arain, A., Arora, V., Barr, A., Black, T. A., Chen, J., Wang, S., Yuan, F., and Zhang, Y.: Intercomparison of techniques to model high temperature effects on CO₂ and energy exchange in temperate and boreal coniferous forests, *Ecol. Model.*, 188, 217–252, 2005. 3068
- Gray, J.: Jim Gray on eScience: A transformed scientific method, in: The Fourth Paradigm: Data-Intensive Scientific Discovery, edited by: Hey, T., Tansley, S., and Tolle, K., Microsoft Research, 284, 2009. 3043
- Griffis, T. J., Black, T. A., Morgenstern, K., Barr, A. G., Nesic, Z., Drewitt, G. B., Guamont-Guay, D., and McCaughey, J. H.: Ecophysiological controls on the carbon balances of three southern boreal forests, *Agr. Forest Meteorol.*, 117, 53–71, 2003. 3067
- Grinsted, A., Moore, J. C., and Jevrejeva, S.: Application of the cross wavelet transform and wavelet coherence to geophysical time series, *Nonlinear Proc. Geoph.*, 11, 561–566, 2004. 3044, 3046, 3047, 3048, 3049, 3056, 3070
- Hanson, P. J., Amthor, J. S., Wullschleger, S. D., Wilson, K. F., Grant, R. F., Hartley, A., Hui, D. F., Hunt, E. R. J., Johnson, D. W., Kimball, J. S., King, A. W. Y. L., McNulty, S. G., Sun, G., Thornton, P. E. S. W., Williams, M., Baldocchi, D. D., and Cushman, R. M.: Oak forest carbon and water simulations: model intercomparisons and evaluations against independent data, *Ecol. Monogr.*, 74, 443–489, 2004. 3068

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Hill, T. C., Quaife, T., and Williams, M.: A data assimilation method for using low-resolution Earth observation data in heterogeneous ecosystems, *J. Geophys. Res.*, 116, D08117, doi:10.1029/2010jd015268, 2011. 3056

Hollinger, D. Y., Ollinger, S. V., Richardson, A. D., Meyers, T., Dail, D. B., Martin, M. E., Scott, N. A., Arkebauer, T. J., Baldocchi, D. D., Clark, K. L., Curtis, P. S., Davis, K. J., Desai, A. R., Dragoni, D., Goulden, M. L., Gu, L., Katul, G. G., Pallardy, S. G., Paw U, K. T., Schmid, H. P., Stoy, P. C., Suyker, A. E., and Verma, S. B.: Albedo estimates for land surface models and support for a new paradigm based on foliage nitrogen concentration., *Glob. Change Biol.*, 16, 696–710, 2009. 3054

Katul, G. G., Lai, C.-T., Schäfer, K. V. R., Vidakovic, B., Albertson, J. D., Ellsworth, D. S., and Oren, R.: Multiscale analysis of vegetation surface fluxes: from seconds to years, *Adv. Water Resour.*, 24, 1119–1132, 2001. 3056

Keenan, T. F., Baker, I., Barr, A., Ciais, P., Davis, K., Dietze, M., Dragoni, D., Gough, C. M., Grant, R., Hollinger, D., Hufkens, K., Poulter, B., McCaughey, H., Racza, B., Ryu, Y., Schaefer, K., Tian, H., Verbeeck, H., Zhao, M., and Richardson, A. D.: Terrestrial biosphere model performance for inter-annual variability of land-atmosphere CO₂ exchange, *Glob. Change Biol.*, 18, 1971–1987, 2012. 3054

Kowalczyk, E. A., Wang, Y. P., Law, R. M., Davies, H. L., McGregor, J. L., and Abramowitz, G.: The CSIRO atmosphere biosphere land exchange (CABLE) model for use in climate models and as an offline model, CSIRO Marine and Atmospheric Research, 2006. 3055

Krinner, G., Viovy, N., de Noblet-Ducoudré, N., Ogée, J., Polcher, J., Friedlingstein, P., Ciais, P., Sitch, S., and Prentice, I. C.: A dynamic global vegetation model for studies of the coupled atmosphere-biosphere system, *Global Biogeochem. Cy.*, 19, GB1015, doi:10.1029/2003GB002199, 2005. 3068

Kucharik, C. J. and Twine, T. E.: Residue, respiration and residuals: evaluation of a dynamic agroecosystem model using eddy flux measurements and biometric data, *Agr. Forest Meteorol.*, 146, 134–158, 2007. 3068

Lafleur, P. M., Roulet, N. T., Bubier, J. L., Moore, T. R., and Frolking, S.: Interannual variability in the peatland-atmosphere carbon dioxide exchange at an ombrotrophic bog, *Global Biogeochem. Cy.*, 17, 1036, doi:10.1029/2002GB001983, 2003. 3067

Law, B. E., Arkebauer, T. J., Campbell, J. L., Chen, J., Sun, O., Schwartz, M., van Ingen, C., and Verma, S.: Terrestrial carbon observations: protocols for vegetation sampling and data submission, Report 55, FAO, Rome, 87, 2008. 3046

Li, H., Qiu, J., Wang, L., Tang, H., Li, C., and Van Ranst, E.: Modelling impacts of alternative farming management practices on greenhouse gas emissions from a winter wheat-maize rotation system in China, *Agr. Ecosyst. Environ.*, 135, 24–33, 2010. 3068

Liu, J., Chen, J. M., Cihlar, J., and Chen, W.: Net primary productivity distribution in the BOREAS region from a process model using satellite and surface data, *J. Geophys. Res.*, 104, 27735–27754, 1999. 3068

Lokupitiya, E., Denning, S., Paustian, K., Baker, I., Schaefer, K., Verma, S., Meyers, T., Bernacchi, C. J., Suyker, A., and Fischer, M.: Incorporation of crop phenology in Simple Biosphere Model (SiBcrop) to improve land-atmosphere carbon exchanges from croplands, *Biogeosciences*, 6, 969–986, doi:10.5194/bg-6-969-2009, 2009. 3068

Mahecha, M. D., Reichstein, M., Jung, M., Senevirante, S. I., Zaehle, S., Beer, C., Braakhekke, M. C., Carvalhais, N., Lange, H., Le Maire, G., and Moors, E.: Comparing observations and process-based simulations of biosphere-atmosphere exchanges on multiple timescales, *J. Geophys. Res.*, 115, G02003, doi:10.1029/2009JG001016, 2010. 3043, 3055, 3056

Medvigy, D., Wofsy, S. C., Munger, J. W., Hollinger, D. Y., and Moorcroft, P. R.: Mechanistic scaling of ecosystem function and dynamics in space and time: ecosystem demography model version 2, *J. Geophys. Res.*, 114, G01002, doi:10.1029/2008JG000812, 2009. 3049, 3068

Ollinger, S. V. and Smith, M.-L.: Net primary production and canopy nitrogen in a temperate forest landscape: an analysis using imaging spectroscopy, modeling and field data, *Ecosystems*, 8, 760–778, 2005. 3054

Ollinger, S. V., Richardson, A. D., Martin, M. E., Hollinger, D. Y., Frolking, S., Reich, P. B., Plourde, L. C., Katul, G. G., Munger, J. W., Oren, R., Smith, M.-L., Paw U, K. T., Bolstad, P. V., Cook, B. D., Day, M. C., Martin, T. A., Monson, R. K., and Schmid, H. P.: Canopy nitrogen, carbon assimilation, and albedo in temperate and boreal forests: functional relations and potential climate feedbacks, *Proc. Natl. Acad. Sci. USA*, 105, 19336–19341, doi:10.1073/pnas.0810021105, 2008. 3054

Papale, D., Reichstein, M., Aubinet, M., Canfora, E., Bernhofer, C., Kutsch, W., Longdoz, B., Rambal, S., Valentini, R., Vesala, T., and Yakir, D.: Towards a standardized processing of Net Ecosystem Exchange measured with eddy covariance technique: algorithms and uncertainty estimation, *Biogeosciences*, 3, 571–583, doi:10.5194/bg-3-571-2006, 2006. 3046

Rastetter, E. B., Williams, M., Griffin, K. L., Kwiatkowski, B. L., Tomasky, G., Potosnak, M. J., Stoy, P. C., Shaver, G. R., Stieglitz, M., Hobbie, J. E., and Kling, G. W.: Processing arctic

Wavelet coherence
for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



eddy-flux data using a simple carbon-exchange model embedded in the ensemble Kalman filter, *Ecol. Appl.*, 20, 1285–1301, doi:10.1890/09-0876.1, 2010. 3056

5 Raupach, M. R., Rayner, P. J., Barrett, D. J., DeFries, R. S., Heimann, M., Ojima, D., Quegan, S., and Schmullius, C. C.: Model-data synthesis in terrestrial carbon observation: methods, data requirements and data uncertainty specifications, *Glob. Change Biol.*, 11, 378–397, 2005. 3056

Reed, B. C., Brown, J. F., VanderZee, D., Loveland, T. R., Merchant, J. W., and Ohlen, D. O.: Measuring phenological variability from satellite imagery, *J. Veg. Sci.*, 5, 703–714, doi:10.2307/3235884, 1994. 3052

10 Reichstein, M., Falge, E., Baldocchi, D., Papale, D., Aubinet, M., Berbigier, P., Bernhofer, C., Buchmann, N., Gilmanov, T. G., Granier, A., Grünwald, T., Havrnkov, K., Ilvesniemi, H., Janous, D., Knohl, A., Laurila, T., Lohila, A., Loustau, D., Matteucci, G., Meyers, T., Miglietta, F., Ourcival, J.-M., Pumpanen, J., Rambal, S., Rotenberg, E., Sanz, M., Tenhunen, J., Seufert, G., Vaccari, F., Vesala, T., Yakier, D., and Valentini, R.: On the separation of net ecosystem exchange into assimilation and ecosystem respiration: review and improved algorithm, *Glob. Change Biol.*, 11, 1424–1439, 2005. 3046

Ricciuto, D. M., Thornton, P. E., Schaefer, K., Cook, R. B., and Davis, K. J.: How uncertainty in gap-filled meteorological input forcing at eddy covariance towers impacts modeled carbon and energy flux, *Eos Trans. AGU*, 90, Fall Meet. Suppl., Abstract B54A-03, 2009. 3045

20 Richardson, A. D., Hollinger, D. Y., Aber, J. D., Ollinger, S. V., and Braswell, B. H.: Environmental variation is directly responsible for short- but not long-term variation in forest-atmosphere carbon exchange, *Glob. Change Biol.*, 13, 788–803, 2007. 3044, 3054

Richardson, A. D., Mahecha, M. D., Falge, E., Kattge, J., Moffat, A. M., Papale, D., Reichstein, M., Stauch, V. J., Braswell, B. H., Churkina, G., Kruijt, B., and Hollinger, D. Y.: Statistical properties of random CO₂ flux measurement uncertainty inferred from model residuals, *Agr. Forest Meteorol.*, 148, 38–50, 2008. 3047

25 Richardson, A. D., Hollinger, D. Y., Dail, D. B., Lee, J. T., Munger, J. W., and O'Keefe, J.: Influence of spring phenology on seasonal and annual carbon balance in two contrasting New England forests, *Tree Physiol.*, 29, 321–331, 2009. 3067

30 Richardson, A. D., Anderson, R. S., Arain, M. A., Barr, A. G., Bohrer, G., Chen, G., Chen, J. M., Ciais, P., Davis, K. J., Desai, A. R., Dietze, M. C., Dragoni, D., Garrity, S. R., Gough, C. M., Grant, R., Hollinger, D. Y., Margolis, H. A., McCaughey, H., Migliavacca, M., Monson, R. K., Munger, J. W., Poulter, B., Racza, B. M., Ricciuto, D. M., Sahoo, A. K., Schaefer, K., Tian, H.,

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Vargas, R., Verbeeck, H., Xiao, J., and Xue, Y.: Terrestrial biosphere models need better representation of vegetation phenology: results from the North American Carbon Program Site Synthesis, *Glob. Change Biol.*, 18, 566–584, doi:10.1111/j.1365-2486.2011.02562.x, 2012. 3045, 3052, 3053

5 Riley, W. J., Still, C. J., Torn, M. S., and Berry, J. A.: A mechanistic model of $H_2^{18}O$ and $C^{18}OO$ fluxes between ecosystems and the atmosphere: model description and sensitivity analyses, *Glob. Biogeochem. Cycle*, 16, 1095, doi:10.1029/2002GB001878, 2002. 3068

10 Schaefer, K., Zhang, T., Slater, A. G., Lu, L., Etringer, A., and Baker, I.: Improving simulated soil temperatures and soil freeze/thaw at high-latitude regions in the Simple Biosphere/Carnegie-Ames-Stanford Approach model, *J. Geophys. Res.*, 114, F02021, doi:10.1029/2008JF001125, 2009. 3068

15 Schaefer, K., Schwalm, C. R., Williams, C., Arain, M. A., Barr, A., Chen, J. M., Davis, K. J., Dimitrov, D., Hilton, T. W., Hollinger, D. Y., Humphreys, E., Poulter, B., Racza, B. M., Richardson, A. D., Sahoo, A., Thornton, P., Vargas, R., Verbeeck, H., Anderson, R., Baker, I., Black, T. A., Bolstad, P., Chen, J., Curtis, P. S., Desai, A. R., Dietze, M., Dragoni, D., Gough, C., Grant, R. F., Gu, L., Jain, A., Kucharik, C., Law, B., Liu, S., Lokipitiya, E., Margolis, H. A., Matamala, R., McCaughey, J. H., Monson, R., Munger, J. W., Oechel, W., Peng, C., Price, D. T., Ricciuto, D., Riley, W. J., Roulet, N., Tian, H., Tonitto, C., Torn, M., Weng, E., and Zhou, X.: A model-data comparison of gross primary productivity: results from the North American Carbon Program site synthesis, *J. Geophys. Res.*, 117, G03010, doi:10.1029/2012jg001960, 2012. 3043, 3045

20 Schmid, H. P., Su, H. B., Vogel, C. S., and Curtis, P. S.: Ecosystem-atmosphere exchange of carbon dioxide over a mixed hardwood forest in northern lower Michigan, *J. Geophys. Res.-Atmos.*, 108, 4417, doi:10.1029/2002JD003011, 2003. 3067

25 Schwalm, C. R., Black, T. A., Morgenstern, K., and Humphreys, E. R.: A method for deriving net primary productivity and component respiratory fluxes from tower-based eddy covariance data: a case study using a 17-yr data record from a Douglas-fir chronosequence, *Glob. Change Biol.*, 13, 370–385, 2007. 3067

30 Schwalm, C. R., Williams, C. A., Schaefer, K., Anderson, R., Arain, M. A., Baker, I., Barr, A. G., Black, T. A., Chen, G., Chen, J. M., Ciais, P., Davis, K. J., Desai, A. R., Dietze, M., Dragoni, D., Fischer, M. L., Flanagan, L. B., Grant, R., Gu, L., Hollinger, D., Izaurralde, R. C., Kucharik, C. J., Lafleur, P. M., Law, B. E., Li, L., Li, Z., Liu, S., Lokupitiya, E., Luo, Y., Ma, S., Margolis, H., Matamala, R., McCaughey, J. H., Monson, R. K., Oechel, W., Peng, C.,

- Poulter, B., Price, D. T., Riciutto, D. M., Riley, W., Sahoo, A. K., Sprintsin, M., Sun, J., Tian, H., Tonitto, C., Verbeeck, H., and Verma, S. B.: A model-data intercomparison of CO₂ exchange across North America: results from the North American Carbon Program Site Synthesis, *J. Geophys. Res.*, 115, G00H05, doi:10.1029/2009JG001229, 2010. 3043, 3044, 3045, 3046, 5 3050, 3051, 3052, 3053, 3068
- Siqueira, M. B. S., Katul, G. G., Sampson, D. A., Stoy, P. C., Juang, J.-Y., McCarthy, H. R., and Oren, R.: Multi-scale model inter-comparisons of CO₂ and H₂O exchange rates in a maturing southeastern US pine forest, *Glob. Change Biol.*, 12, 1189–1207, 2006. 3044, 3054, 3056
- Sitch, S., Smith, B., Prentice, I. C., Arneth, A., Bondeau, A., Cramer, W., Kaplan, J. O., Levis, S., 10 Lucht, W., Sykes, M., Thonicke, K., and Venevsky, S.: Evaluation of ecosystem dynamics, plant geography and terrestrial carbon cycling in the LPJ dynamic global vegetation model, *Glob. Change Biol.*, 9, 161–185, 2003. 3068
- Stoy, P. C., Katul, G. G., Siqueira, M. B. S., Juang, J.-Y., McCarthy, H. R., Kim, H.-S., Oishi, A. C., and Oren, R.: Variability in net ecosystem exchange from hourly to inter-annual time scales at adjacent pine and hardwood forests: a wavelet analysis, *Tree Physiol.*, 25, 887–902, 2005. 15 3044, 3054
- Stoy, P. C., Richardson, A. D., Baldocchi, D. D., Katul, G. G., Stanovick, J., Mahecha, M. D., Reichstein, M., Detto, M., Law, B. E., Wohlfahrt, G., Arriga, N., Campos, J., McCaughey, J. H., Montagnani, L., Paw U, K. T., Sevanto, S., and Williams, M.: Biosphere-atmosphere exchange of CO₂ in relation to climate: a cross-biome analysis across multiple time scales, *Biogeosciences*, 6, 2297–2312, doi:10.5194/bg-6-2297-2009, 2009.
- Sus, O., Williams, M., Bernhofer, C., Bziat, P., Buchmann, N., Ceschia, E., Doherty, R., Eugster, W., Grünwald, T., Kutsch, W., Smith, P., and Wattenbach, M.: A linked carbon cycle and crop developmental model: description and evaluation against measurements of carbon fluxes and carbon stocks at several European agricultural sites, *Agr. Ecosyst. Environ.*, 139, 20 402–418, 2010. 3053
- Taylor, K. E.: Summarizing multiple aspects of model performance in a single diagram, *J. Geophys. Res.*, 106, 7183–7192, 2001. 3043
- Thomas, C. K., Law, B. E., Irvine, J., Martin, J. G., Pettijohn, J. C., and Davis, K. J.: Seasonal hydrology explains interannual and seasonal variation in carbon and water exchange in 25 a semi-arid mature ponderosa pine forest in central Oregon, *J. Geophys. Res.*, 114, G04006, doi:10.1029/2009JG001010, 2009. 3067

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



- Williams, M., Richardson, A. D., Reichstein, M., Stoy, P. C., Peylin, P., Verbeeck, H., Carvalhais, N., Jung, M., Hollinger, D. Y., Kattge, J., Leuning, R., Luo, Y., Tomelleri, E., Trudinger, C. M., and Wang, Y.-P.: Improving land surface models with FLUXNET data, *Biogeosciences*, 6, 1341–1359, doi:10.5194/bg-6-1341-2009, 2009. 3043, 3044, 3054, 3056
- 5 Williamson, T. B., Price, D. T., Beverley, J. L., Bothwell, P. M., Frenkel, B., Park, J., and Patruquin, M. N.: Assessing potential biophysical and socioeconomic impacts of climate change on forest-based communities: a methodological case study, *Natural Resources Canada, ABIInf. Rep. NOR-X-415E*, Canadian Forest Service, Edmonton, 2008. 3068
- Zhan, X. W., Xue, Y. K., and Collatz, G. J.: An analytical approach for estimating CO₂ and heat fluxes over the Amazonian region, *Ecol. Model.*, 162, 97–117, 2003. 3068
- 10 Zhou, X. L., Peng, C. H., Dang, Q. L., Sun, J. F., Wu, H. B., and Hua, D.: Simulating carbon exchange in Canadian boreal forests I: model structure, validation, and sensitivity analysis, *Ecol. Model.*, 219, 287–299, 2008. 3068

Discussion Paper | Discussion Paper

Wavelet coherence
for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	

[Printer-friendly Version](#)

[Interactive Discussion](#)



Table 1. Measurement sites of the North American Carbon Program Site-Level Interim Synthesis investigated by Dietze et al. (2011) and explored in the present analysis. CRO: crop; DBF: deciduous broadleaf forest; ENF: evergreen needleleaf forest; PFT: plant functional type; WET: wetland.

Site ID	Name	PFT	Years	Figs. 6–8 subplot	References
CA-Ca1	Campbell River: Mature Forest Site	ENF	1998–2006	A	Schwalm et al. (2007)
CA-Let	Lethbridge	GRA	1999–2007	B	Flanagan et al. (2002)
CA-Mer	Eastern Peatland: Mer Bleue	WET	1999–2006	C	Lafleur et al. (2003)
CA-Oas	SSA Old Aspen	DBF	1997–2006	D	Barr et al. (2004)
CA-Obs	SSA Old Black Spruce	ENF	2000–2006	E	Griffis et al. (2003)
CA-Ha1	Harvard Forest	DBF	1992–2005	See Figs. 1–5	Urbanski et al. (2007)
CA-Ho1	Howland Forest	ENF	1996–2004	F	Richardson et al. (2009)
CA-Me2	Metolius: Intermediate Aged Ponderosa Pine	ENF	2002–2007	G	Thomas et al. (2009)
CA-Ne3	Mead: Rainfed Maize/Soybean Rotation	CRO	2002–2004	H	Verma et al. (2005)
CA-UMB	University of Michigan Biological Station	DBF	1999–2006	I	Schmid et al. (2003), Gough et al. (2008, 2009)

Table 2. A list of model attributes per model following Schwalm et al. (2010). Model/attribute combinations with no checked boxes indicate that a different formulation was used. These not considered here. ER: ecosystem respiration; GPP: gross primary productivity; HR: heterotrophic respiration; NEE: net ecosystem exchange; NPP: net primary productivity.

Model	NEE calc.		Phenology		Foliar N		Reference
	NPP – HR	GPP – ER	Prognostic	Prescribed	Yes	No	
AgroIBIS	X		X		X		Kucharik and Twine (2008)
BEPS	X		X		X		Liu et al. (1999)
Biome-BGC			X		X		Thornton et al. (2005)
Can-IBIS	X		X		X		Williamson et al. (2008)
CN-CLASS		X	X		X		Araian et al. (2008)
DLEM	X		X ^a		X		Tian et al. (2010)
DNDC	X		X		X		Li et al. (2010)
Ecosys		X	X		X		Grant et al. (2005)
ED2	X		X		X		Medvighy et al. (2009)
EPIC	X		X		X		Causarano et al. (2007)
ISOLSM		X		X		X	Riley et al. (2002)
LoTEC	X		X			X	Hanson et al. (2004)
LPJ-wsl	X		X			X	Sitch et al. (2003)
ORCHIDEE	X		X			X	Krinner et al. (2005)
SiB3		X		X	X ^b		Baker et al. (2008)
SibCASA	X			X		X	Schaefer et al. (2009)
SiBcrop	X		X			X	Lokupitiya et al. (2009)
SSiB2	X			X		X	Zhan et al. (2003)
TECO	X		X			X	Weng and Luo (2008)
Triplex-FLUX	X			X		X	Zhou et al. (2008)

^a Semi-prognostic phenology.

^b SiB3 includes N in the assignment of phenology from remotely-sensed products, but does not otherwise include it as a prognostic variable.

Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

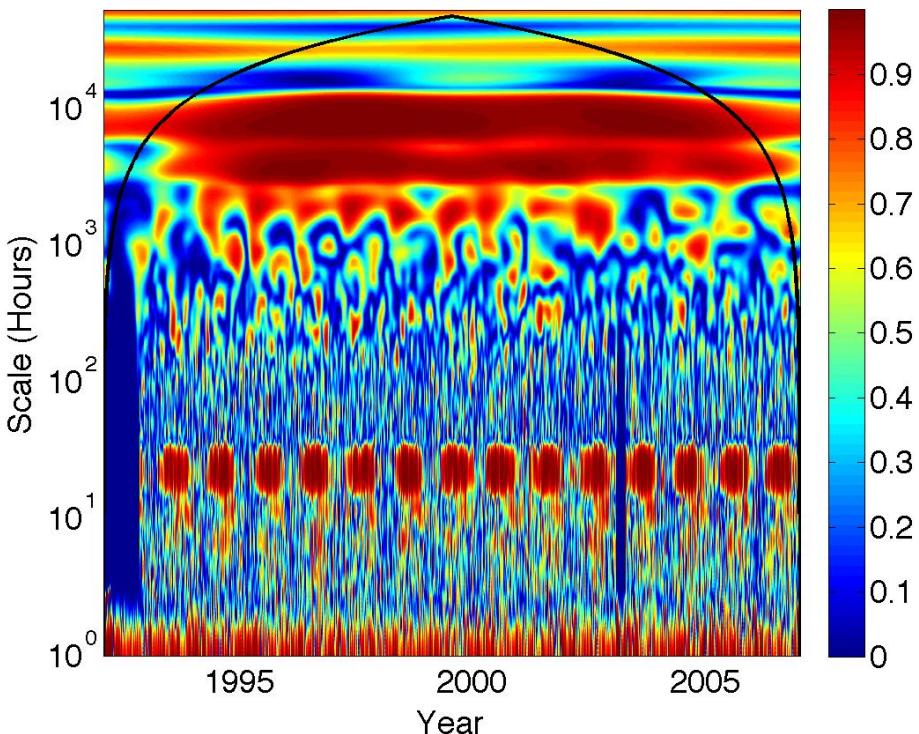


Fig. 1. Wavelet coherence between Harvard Forest (US-Ha1) net ecosystem exchange of CO₂ (NEE) observations and Ecosystem Demography 2 (ED2) model simulations along the time and scale axes in the wavelet half-plane. The model was not run for the first year of measurements for the North American Carbon Program Site-Level Interim Synthesis. The black line is the cone of influence beyond which wavelet coefficients should not be interpreted.

Title Page

Abstract

Introduction

Conclus

s References

Table

Figures

Tables | Figures

Tables | Figures

Tables | Figures

Tables | Figures

1

1

1

Bac

Close

Full Screen / Esc

[Printer-friendly Version](#)

Interactive Discussion



Wavelet coherence for multiple models

P. C. Stoy et al.

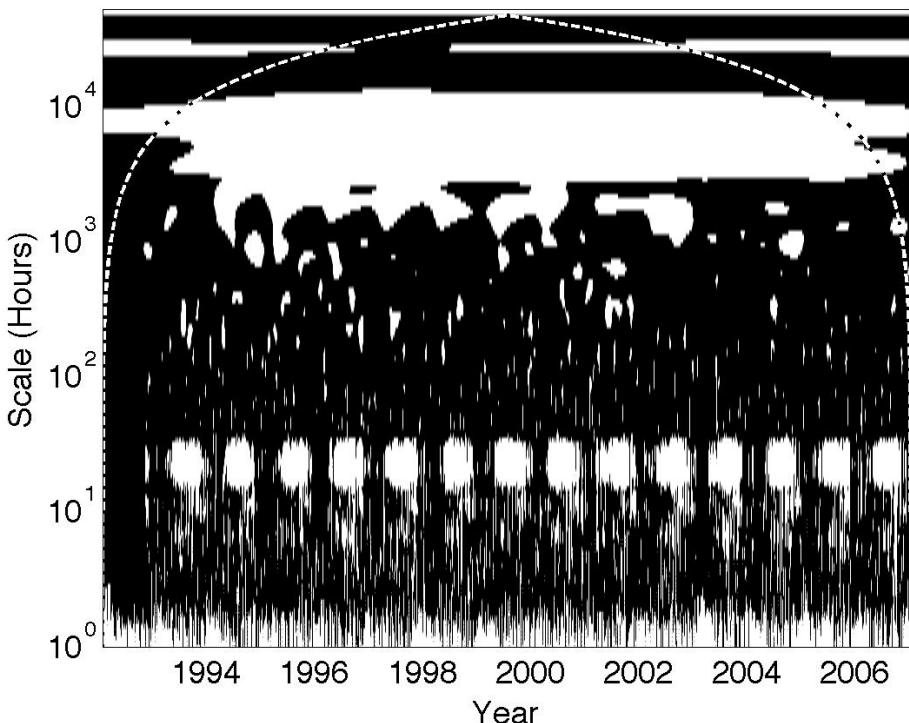


Fig. 2. Same as Fig. 1 but for regions of significant wavelet coherence between net ecosystem exchange (NEE) measurements at Harvard Forest (US-Ha1) and the Ecosystem Demography v2 (ED2) model simulations, calculated following Grinsted et al. (2004). Regions in the wavelet half-plane with significant coherence are white and given a value of unity; regions without significant coherence are black and given the null value.

Title Page

Abstract

Introduction

Conclusio

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer friendly Version

Interactive Discussion



**Wavelet coherence
for multiple models**

P. C. Stoy et al.

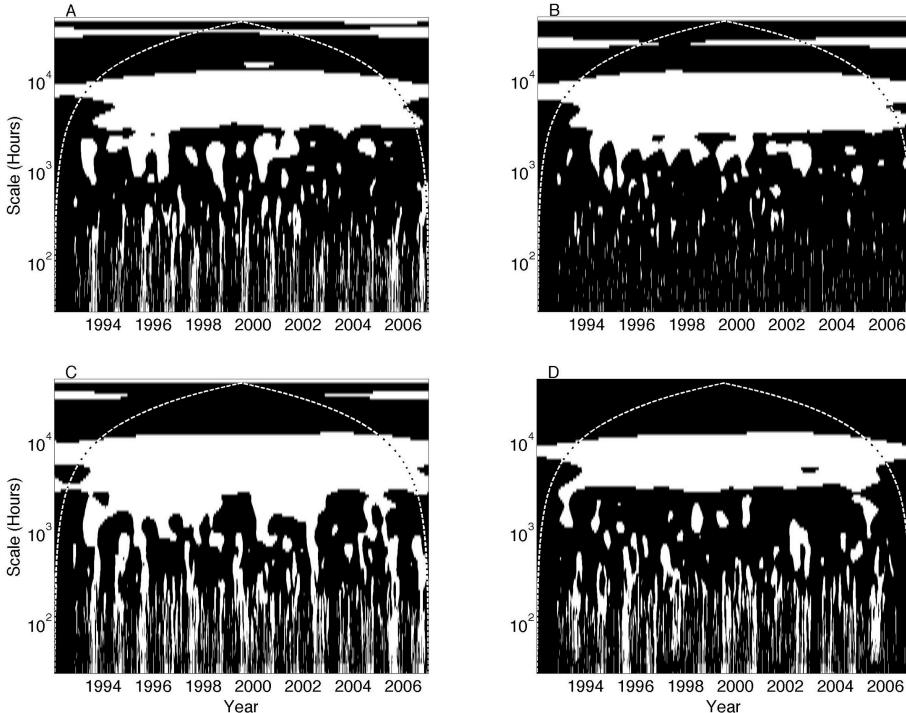


Fig. 3. Same as Fig. 2 but showing significant wavelet coherence at time scales greater than 2 days between NEE measurements at Harvard Forest (US-Ha1) and the **(A)** SiBCASA, **(B)** ED2, **(C)** LoTEC and **(D)** ORCHIDEE model simulations.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Wavelet coherence for multiple models

P. C. Stoy et al.

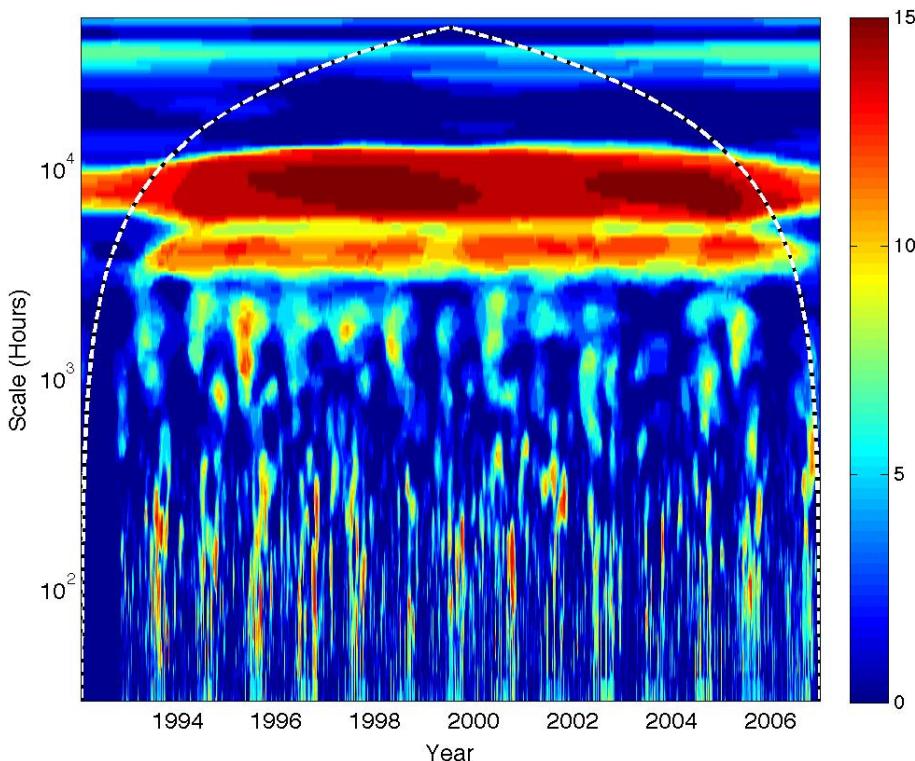


Fig. 4. The sum of significant wavelet coherence coefficients for net ecosystem exchange (NEE) observations at the Harvard forest (US-Ha1) and simulations by 15 ecosystem models (Table 2). This figure represents the sum of the subplots of Fig. 3 including the other models that were run at US-Ha1 listed in Dietze et al. (2011). A value of 15 indicates that all 15 models explored here are significantly related to NEE observations.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

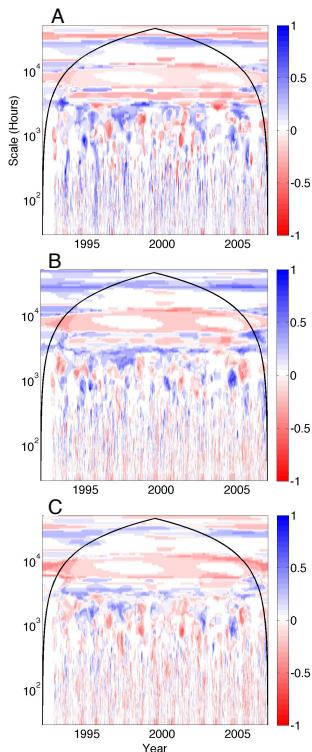


Fig. 5. The ratio of significant wavelet coherence for different model attributes for the net ecosystem exchange (NEE) observations at the Harvard Forest (US-Ha1) following Eq. (2). Areas of dark blue represent times and scales where all models that include prognostic phenology (**A**), the NEE calculation as GPP – ER (**B**), and the inclusion of nitrogen (**C**) are significantly related to NEE observations, and when none of the opposing model strategy listed in Table 2 is significant. Areas of dark red represent periods when the opposite holds.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

1

10 of 10

1

100

Full Screen / Esc

[Printer-friendly Version](#)

Interactive Discussion



Wavelet coherence for multiple models

P. C. Stoy et al.

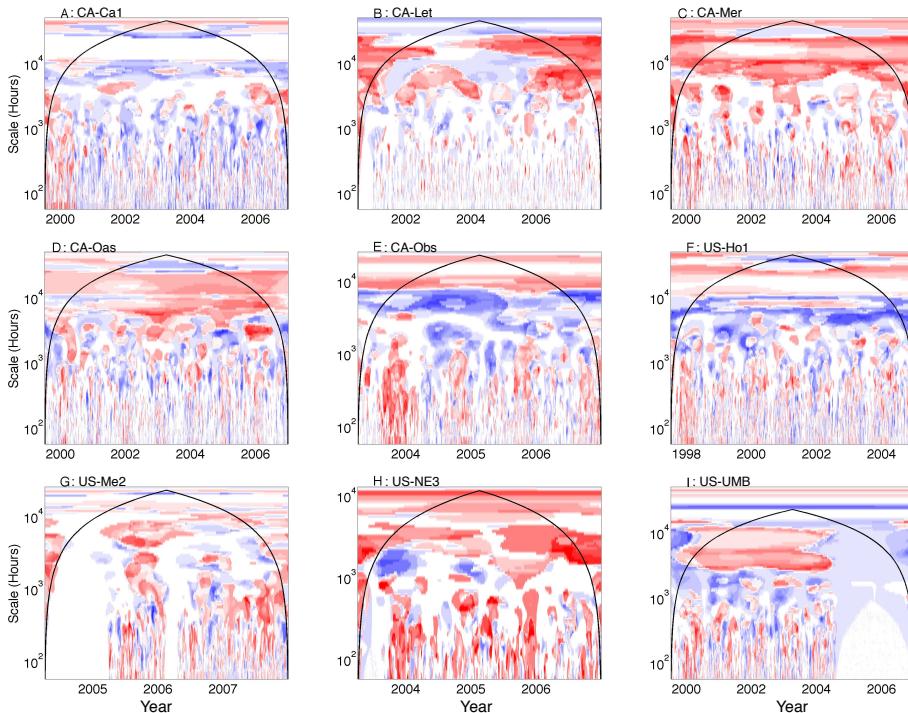


Fig. 6. The ratio of wavelet coherence significance tests for models with prognostic versus prescribed phenology for nine sites in the North American Carbon Program Interim Synthesis. The colorbar follows Fig. 5. Regions in the time/scale wavelet half-plane for which models that use prognostic leaf area index (LAI) are significantly related to NEE measurements and those that use prescribed LAI are not significantly related to NEE measurements are shown as dark blue. Regions for which models that use prescribed LAI are significant and those that use prognostic LAI are not significant are shown as dark red. The colorbar follows Fig. 5.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Wavelet coherence for multiple models

P. C. Stoy et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

◀

▶

◀

▶

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

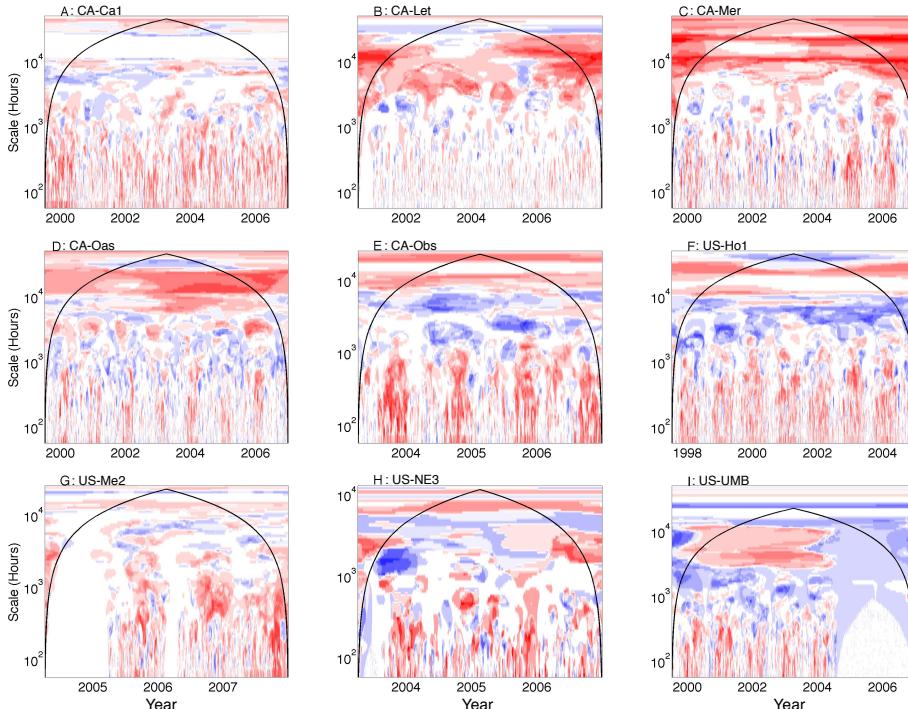


Fig. 7. The ratio of wavelet coherence significance tests for models with different calculations of the net ecosystem exchange (NEE). The colorbar follows Fig. 5. Regions in the time/scale wavelet half-plane for which models that calculate NEE as gross primary productivity (GPP) minus ecosystem respiration (ER) are significantly related to NEE measurements and models that calculate NEE as net primary productivity (NPP) minus heterotrophic respiration (HR) are not significantly related to NEE measurements are dark blue. Regions for which models that calculate NEE as NPP – HR are significant and GPP – ER are not significant are dark red. The colorbar follows Fig. 5.

Wavelet coherence for multiple models

P. C. Stoy et al.

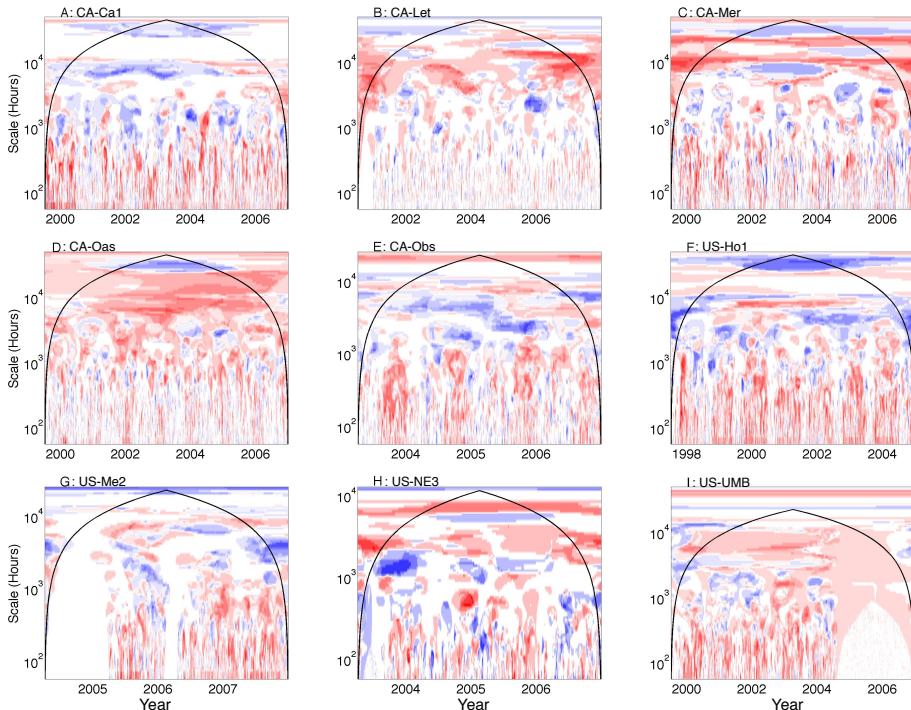


Fig. 8. The ratio of wavelet coherence significance tests for models that include or exclude foliar nitrogen (N). The colorbar follows Fig. 5. Regions in the time/scale wavelet half-plane for which models that incorporate N are significant and those that do not incorporate N are not significant are shown as dark blue. Regions for which models that do not include N are significant and those that include N are not significant are shown as dark red. The colorbar follows Fig. 5.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[◀](#)

[▶](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

Wavelet coherence for multiple models

P. C. Stoy et al.

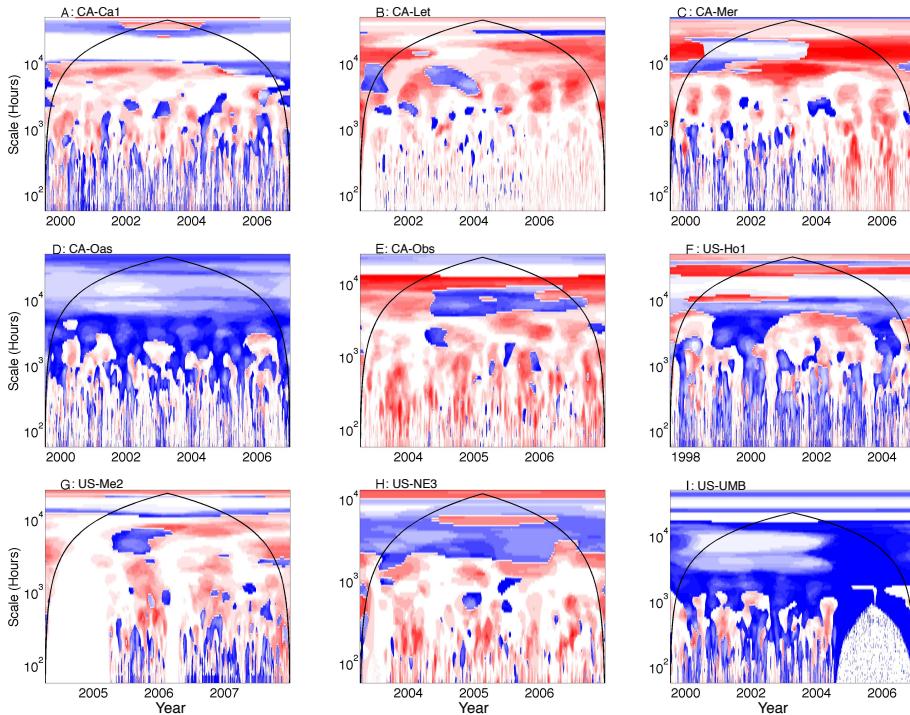


Fig. 9. The ratio of wavelet coherence significance tests for the models uses a data assimilation procedure (LoTEC) versus other models that do not use data assimilation. The colorbar follows Fig. 5. Regions in the time/scale wavelet half-plane for which LoTEC is significantly related to NEE measurements and other models are not significantly related to NEE measurements (on average) are shown as dark blue. Regions for which models other than LoTEC are significantly related to NEE measurements and LoTEC is not significantly related to NEE measurements are shown as dark red. The colorbar follows Fig. 5.

- [Title Page](#)
- [Abstract](#) [Introduction](#)
- [Conclusions](#) [References](#)
- [Tables](#) [Figures](#)
- [◀](#) [▶](#)
- [◀](#) [▶](#)
- [Back](#) [Close](#)
- [Full Screen / Esc](#)
- [Printer-friendly Version](#)
- [Interactive Discussion](#)

