```
// include modII
2
   namespace number_theoretic_transform {
3
5
      // when MOD - 1 = 2<sup>m</sup> * a,
      // min_omega = root^a (try 3, 5, 7, ... to get root)
6
7
      // min_omega_depth = m
8
      // \text{ mod_half} = (MOD + 1) / 2
9
10
      modll min_omega;
11
      int min_omega_depth;
12
      modIl mod_half;
13
14
      void make_base(int mode) {
15
        switch (mode) {
16
          /*
17
        case 0:
18
          MOD = 167772161;
19
          min\_omega = 17;
20
          min_omega_depth = 25;
21
          mod_half = 83886081;
22
          break;
23
        case 1:
24
          MOD = 469762049;
25
          min\ omega = 30;
26
          min\_omega\_depth = 26;
27
          mod half = 234881025;
28
          break;
29
        case 2:
30
          MOD = 1224736769;
31
          min\_omega = 149;
32
          min\_omega\_depth = 24;
33
          mod_half = 612368385;
34
          break;
35
          */
36
        default:
37
          MOD = 924844033;
38
          min\_omega = 3597;
39
          min\_omega\_depth = 21;
40
          mod_half = 462422017;
41
      }
42
43
44
      vector < mod | | > omegas, iomegas;
45
46
      inline int bit_reverse(int x, int digit) {
47
        int ret = digit ? x & 1 : 0;
48
        Loop (i, digit - 1) { ret \leq 1; x > 1; ret |= x & 1; }
49
        return ret;
50
51
52
      inline void make_omegas(int n) {
53
        if (omegas.size() != n) {
54
          omegas.resize(n);
55
          modII omega = pow(min_omega, (1 << min_omega_depth) / n);</pre>
56
          Loop(i, n) {
57
            if (i == 0) omegas[i] = 1;
58
            else omegas[i] = omegas[i - 1] * omega;
59
          }
        }
60
      }
61
62
63
      inline void make_iomegas(int n) {
64
        if (iomegas.size() != n) {
65
          iomegas.resize(n);
66
          mod|| iomega = mod||(1) / pow(min_omega, (1 << min_omega_depth) / n);</pre>
67
          Loop(i, n) {
68
            if (i == 0) iomegas[i] = 1;
69
            else iomegas[i] = iomegas[i - 1] * iomega;
70
71
```

```
72
73
74
       // a.size() should be 2^digit
75
      vector<mod||> NTT(const vector<mod||> a, int mode = 0) {
76
         int n = int(a.size());
77
         int digit = int(rndf(log2(n)));
78
         vector<modll> ret = a;
79
         make_omegas(n);
80
         Loop(i, n) {
81
           int j = bit_reverse(i, digit);
           if (j > i) swap(ret[i], ret[j]);
82
83
84
         Loop(i, digit) {
           int j = 0, m = 1 << i, mw = (digit - i - 1);
85
86
           Loop(group_id, n \gg (i + 1)) {
87
             Loop(k, m) {
               modll x = ret[j] + omegas[k << mw] * ret[j + m];
88
               modll y = ret[j] - omegas[k << mw] * ret[j + m];
89
90
               ret[j] = x; ret[j + m] = y;
91
               ++j;
92
             }
93
             j += m;
           }
94
95
96
         return ret;
97
98
99
       // f. size() should be 2^digit
100
      vector<mod||> INTT(const vector<mod||>& f, int mode = 0) {
101
         int n = int(f.size());
102
         int digit = int(rndf(log2(n)));
103
         vector<mod||> ret = f;
104
         make_iomegas(n);
105
         Loopr(i, digit) {
           int j = 0, m = 1 << i, mw = (digit - i - 1);
106
           Loop(group_id, n \gg (i + 1)) {
107
108
             Loop(k, m) {
               modll q = (ret[j] + ret[j + m]) * mod_half;
109
               modll r = (ret[j] - ret[j + m]) * mod_half * iomegas[k \left mw];
110
111
               ret[j] = q; ret[j + m] = r;
112
               ++j;
113
114
             j += m;
           }
115
116
117
         Loop(i, n) {
118
           int j = bit_reverse(i, digit);
119
           if (j > i) swap(ret[i], ret[j]);
120
121
         return ret;
122
123
       // a.size() = b.size() should be 2^digit
124
125
       vector<mod||> mul_convolution(const vector<mod||> &a, const vector<mod||> &b) {
126
         int n = int(a.size());
127
         vector<modll> ret;
128
         make\_base(0);
         // Garner's algorithm is unsupported yet
129
130
         vector < mod | | > g = NTT(a), h = NTT(b);
131
         Loop(i, n) g[i] *= h[i];
132
         ret = INTT(g);
133
         return ret;
134
135
136
       int legal_size_of(int n) {
137
         int ret = 1 << (int) log2(n);
138
         if (ret < n) ret <<= 1;
139
         return ret;
140
      }
141
    }
142
```