

ISA, 4 + 2

64-bit	32-bit	16-bit	8-bit
rax	eax	ax	al
rbx	ebx	bx	bl
rcx	ecx	cx	cl
rdx	edx	dx	dl
rsi	esi	si	sil
rdi	edi	di	dil
rbp	ebp	bp	bpl
rsp	esp	sp	spl
r8	r8d	r8w	r8b
r9	r9d	r9w	r9b
r10	r10d	r10w	r10b
r11	r11d	r11w	r11b
r12	r12d	r12w	r12b
r13	r13d	r13w	r13b
r14	r14d	r14w	r14b
r15	r15d	r15w	r15b

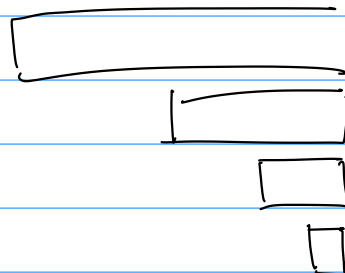
x86-64

word = 16 bit

PC = IP

rip

CISC



Tip	Zapis	Vrednost
Neposredni	Imm	Imm
Registarski	Rx	R[Rx]
Memorijski	[Rx]	$M[R[Rx]]$
Memorijski	[Rx + Imm]	$M[R[Rx] + Imm]$
Memorijski	[Rx + Ry]	$M[R[Rx] + R[Ry]]$
Memorijski	[Rx + Ry + Imm]	$M[R[Rx] + R[Ry] + Imm]$
Memorijski	[Rx + s*Ry]	$M[R[Rx] + s*R[Ry]]$
Memorijski	[Rx + s*Ry + Imm]	$M[R[Rx] + s*R[Ry] + Imm]$

intel, att

0xAB, 10, 0777, 061001

[rax], [rbx], ...

[rax + 10]

1, 2, 4, 8

[rax + 8 \* rbx]

[rax + 4 \* rbx + 17] ← 15

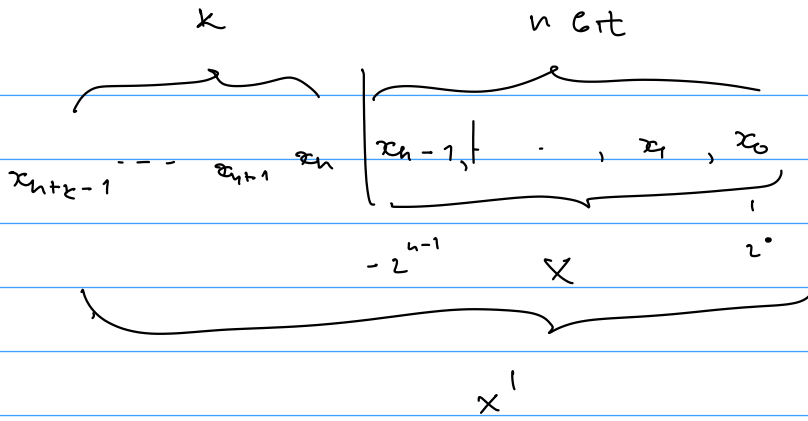
Instrukcija	Efekat	Opis
mov D, S	$D := S$	move
movsx D, S	$D := \text{signExtend}(S)$	move sign extend
movzx D, S	$D := \text{zeroExtend}(S)$	move zero extend
movabs R, Imm	$R := \text{Imm}$	mov 64-bit immediate to a register

unsigned 1 0 . 0 0 1 0 1 1 1 0 1  
 1 - - - 1 1  
 $2^5 \quad 2^1 \quad 2^0$

signed

1 1 1 1 1 0 1 1 - 5  
 $-2^7 \quad 2^5 \quad -2^3 \quad 2^1 \quad 2^0$   
 $-8 + 2 + 1 = -5$

$x_n, x_{n-1}, \dots, x_1, x_0$   
 $-2^n \quad 2^{n-1} \quad \dots \quad 2^1 \quad 2^0$



$$\text{val}(x) = -2^{n-1} \cdot x_{n-1} + \sum_{i=0}^{n-2} x_i 2^i$$

$$\text{val}(z) = -2^{n+k-1} + \sum_{i=0}^{n+k-2} x_i 2^i$$

$$x_{n-1} = 0$$

$$x_{n-1} = 1$$

$$\text{val}(z) = \sum_{i=0}^{n-2} z_i z^i$$

$$v_a'(x) = -2^{n+k-1} + \sum_{i=n-1}^{n+k-2} 2^i$$

$$\text{val}(x') = \sum_{i=0}^{h-2} x_i \cdot 2^i$$

$$+ \sum_{i=0}^{h-2} x_i 2^i$$

$$val(x) = val(x')$$

$$\text{val}(x') = -2^{n+k-1} + 2^{n-1} \sum_{i=0}^{k-1} 2^i$$

$$+ \sum_{i=0}^{n-2} z_i z^i$$

$$val(z') = -2^{h+k-1} + 2^{h-1} (2^k - 1) + \sum_{i=0}^{h-2} 2^{i+1}$$

$$= \underbrace{-2^{n-1}}_{\text{}} + \sum_{i=0}^{n-2} x_i \cdot 2^i$$

$$= -x_{n-1} z^{n-1} + \sum_{i=0}^{n-2} x_i z^i = \text{val}(x)$$

$$2^k$$

$$1 \ 0 \ \dots \ 0$$

$$1 \ \dots \ 1 \ 1 \ 1 \ 1$$

$$\underbrace{\hspace{10em}}$$

$$k$$

$$2^k - 1$$

Instrukcija	Efekat	Opis
inc D	$D := D+1$	Increment
dec D	$D := D-1$	Decrement
neg D	$D := -D$	Negate
not D	$D := \sim D$	Complement
add D, S	$D := D+S$	Add
sub D, S	$D := D-S$	Subtract
imul D, S	$D := D*S$	Multiply
xor D, S	$D := D \oplus S$	Exclusive-or
or D, S	$D := D   S$	Or
and D, S	$D := D \& S$	And
sal D, k	$D := D \ll k$	Arithmetic left shift
shr D, k	$D := D \ll_L k$	Logic left shift
sar D, k	$D := D \gg_A k$	Arithmetic right shift
shr D, k	$D := D \gg_L k$	Logic right shift

$$w = 0, 1, 2, \dots, w-1 = \lceil \log_2(w) \rceil$$

110011001

64

$$\log_2(64) = 6$$

32

$$\log_2(32) = 5$$

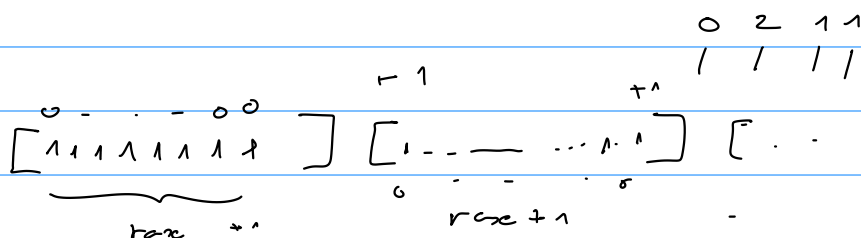
8

$$\log_2(8) = 3$$

1B, 2B, 4B.

↓↓↓  
1120

inc [rax]



0x AABP

BP AA

0x 0201

00000010 00000001

DWORD PTR

add eax, [rbx]  
32 bit

Instrukcija	Efekat	Opis
imul S	R[rdx]:R[rax] := S*R[rax]	Signed full multiply
mul S	R[rdx]:R[rax] := S*R[rax]	Unsigned full multiply
idiv S	R[rax] := R[rdx]:R[rax] div S R[rdx] := R[rdx]:R[rax] mod S	Signed divide
div S	R[rax] := R[rdx]:R[rax] div S R[rdx] := R[rdx]:R[rax] mod S	Unsigned divide
cqo	R[rdx]:R[rax] := signExtend(R[rax])	Convert to oct word

[rdi] [rax]

lea rax, [rbx]      rax ← rbx  
lea rax, [rbx+10]      rax ← rbx + 10  
lea rax, [rbx+8rbx+10]      rax ← rbx + 8rbx + 10

mov rax, rcx      1  
imul rax, 8      3  
add rax, 10      1  
add rax, rcx      1

ZF, SF, OF, CF  
signed overflow  
sub eax, 10      unsigned overflow

rax, rbx

add rax, rbx  
[+, + → -]  
[-, - → +]

1  
0 1 ... 1  
0 1 ... 0  
1 0

1  
1 ... 1  
1 ... 1  
0 ... 0  
1  
0 ... 0  
1 ... 1

add rax, rbx

CF  
- ... 1 0 1 1  
>> 3

CF  
1 1 1 0  
<< 3

! < > → ≥

xor

setg D	setnle	D := ~(SF^OF)&~ZF	Greater (signed >)
setge D	setnl	D := ~(SF^OF)	Greater or equal (signed >=)
setl D	setnge	D := SF^OF	Less (signed <)
setle D	setng	D := [(SF^OF) ZF]	Less or equal (signed <=)

setg D

D ← 1

cmp a, b

a - b > 0

a > b

(+) - (-) → (-)

(-) - (+) → (+)

SF OF SF ^ OF

a < b

1	1	0
1	0	1
0	1	1
0	0	0

seta D	setnbe	D := ~CF&~ZF	Above (unsigned >)
setae D	setnb	D := ~CF	Above or equal (unsigned >=)
setb D	setnae	D := CF	Below (unsigned <)
setbe D	setna	D := CF ZF	Below or equal (unsigned <=)

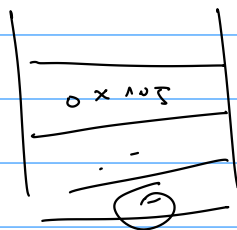
cmp a, b

a - b

a < b

≥

≤



0x100

0x105

call f

add ...

f;

push...

ret

f {

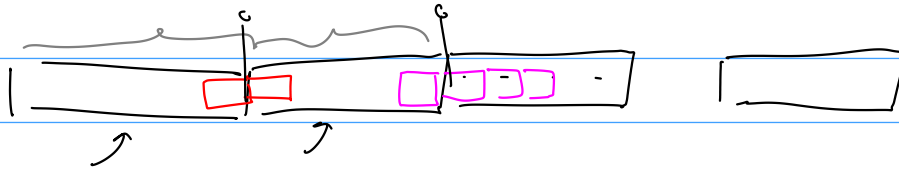
...

g();

...

}

C4 c.t = 8 B



short x; 2B

2B → align(2)

int x; 4B

4B → align(4)

8B → align(8)

struct A {

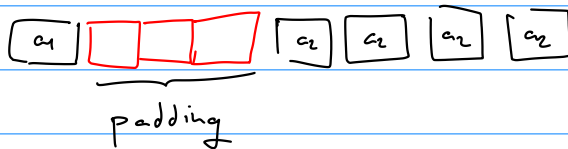
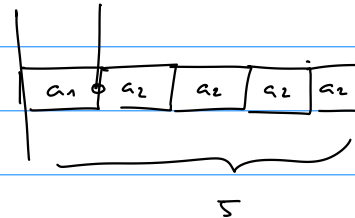
char a1; align(1)

int a2; align(4)

}

sizeof(A) = 8

align(A) = 4



struct X {  
    :  
};  
sizeof(X)  
align(X).

struct X arr[N];

$i \in \{0, 1, \dots, N-1\}$

$\text{arr} \bmod \text{align}(X) = 0$

$(\text{arr} + i \cdot \text{sizeof}(X)) \bmod \text{align}(X) = 0$

$(i \cdot \text{sizeof}(X)) \bmod \text{align}(X) = 0$

$\text{sizeof}(X) \bmod \text{align}(X) = 0$

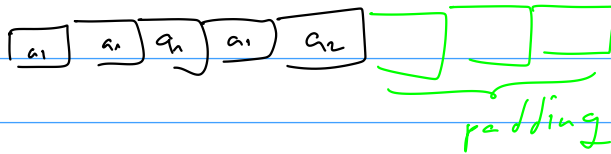
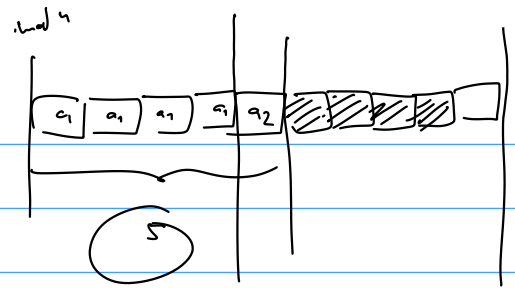
struct A {

int a1; align(4)

char a2; align(1)

}

align(4) = 4

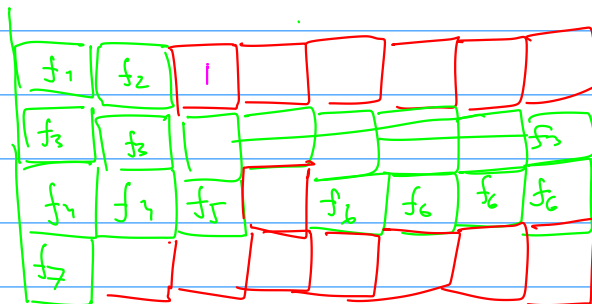


```

3 typedef struct
4 {
5     char field1;    // size: 1, alignment: 1
6     char field2;    // size: 1, alignment: 1
7     long field3;    // size: 8, alignment: 8
8     short field4;   // size: 2, alignment: 2
9     char field5;    // size: 1, alignment: 1
10    int field6;      // size: 4, alignment: 4
11    char field7;     // size: 1, alignment: 1
12 } StructType;      // size: 32, alignment: 8
13

```

mod 8



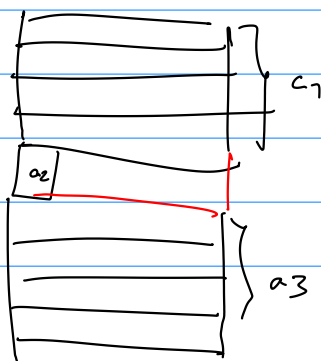
struct B {

struct A a1; a: 8

char a2; a: 1

struct A a3; a: 8

} s: 72 a: 8



72



struct A<sub>1</sub> {

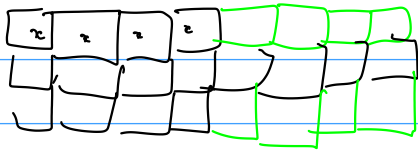
int x; 4

long y; 8

int z; 4

}

24  
8



struct A<sub>2</sub> {

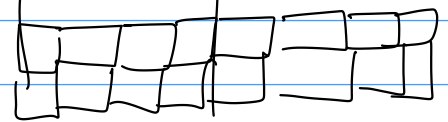
int x; 4

int z; 4

long y; 8

}

16  
8



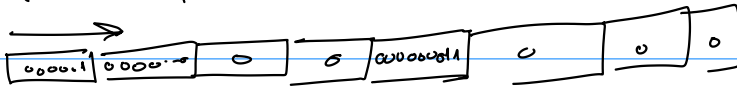
rax := 1

rax < 32:



rax += 3

.LC0



rax: [00000001] - -

long - 8B, 0

f:

push rbp

mov rbp, rsp

add rsp, 16 — sub rsp, 16

mov QWORD PTR (rbp-8), 0

mov QWORD PTR (rbp-16), 0

:

add rsp, 16 — sub rsp, 16

:

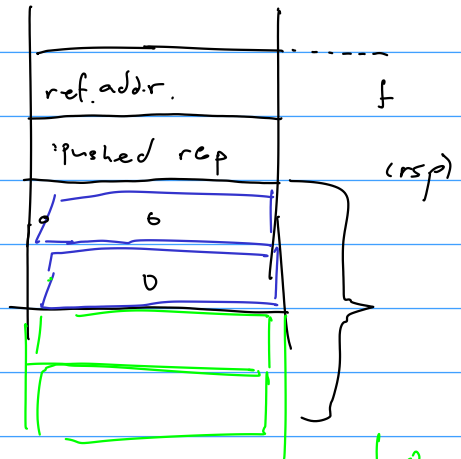
push — pop

mov rsp, rbp

pop rbp

ret

base pointer.



[enter (n), 0]

push rbp

mov rbp, rsp

sub rsp, n

leave

0xffeeddccbbaa

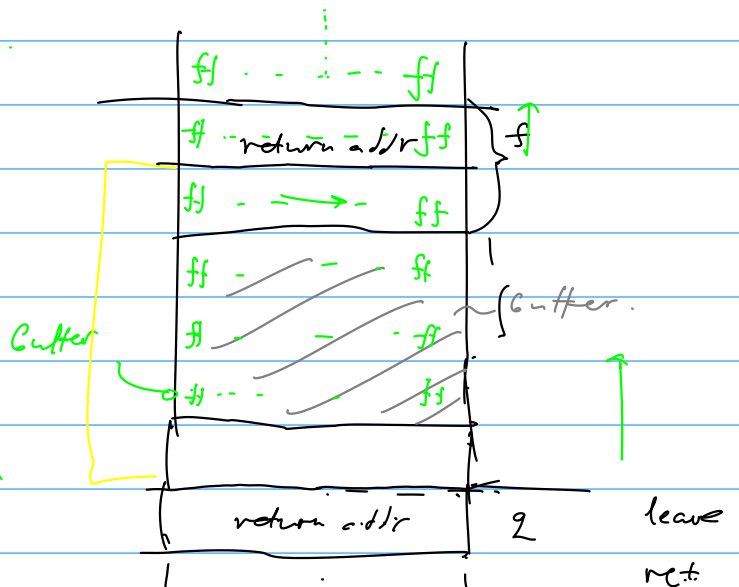
f() {

char buffer[24];

g(buffer);

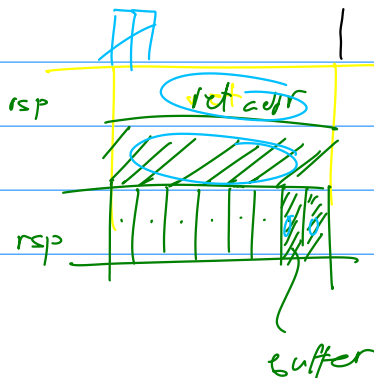
}

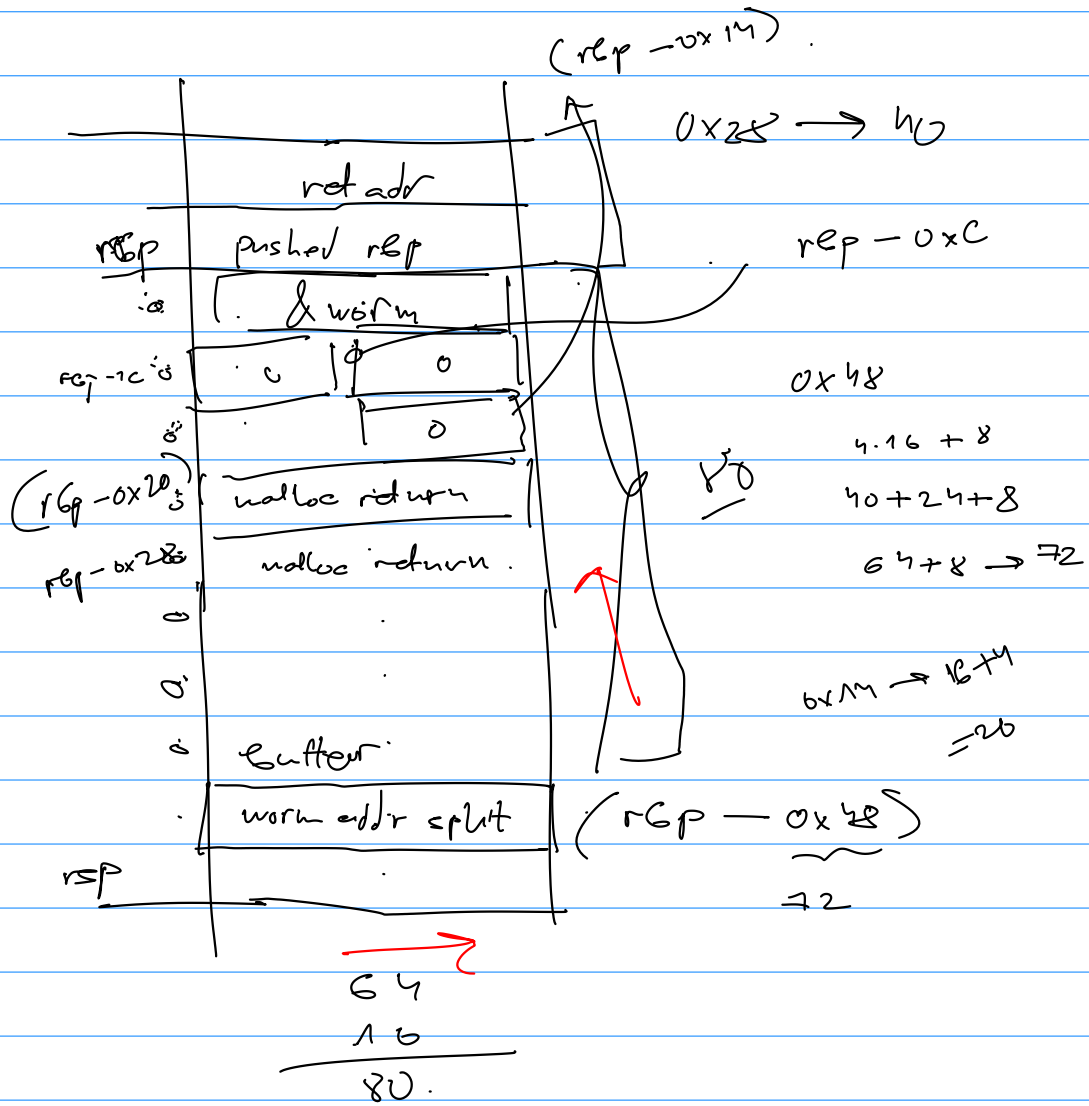
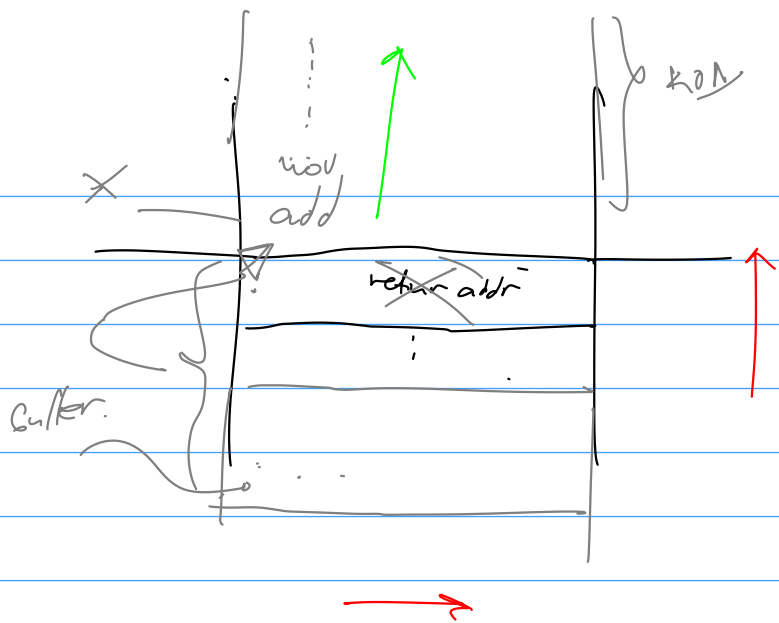
- main 0xff c4 57  
in buffer.

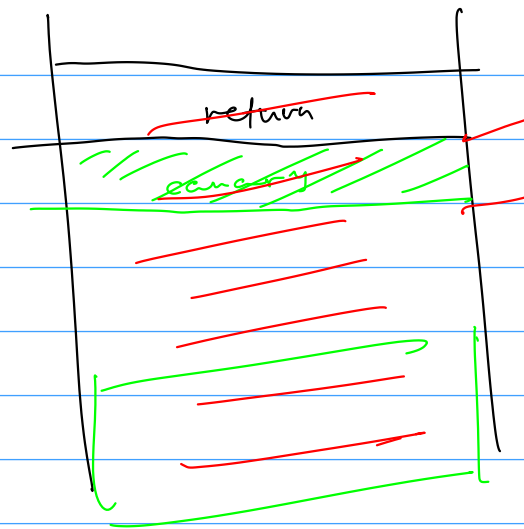


username[24]

... (username)



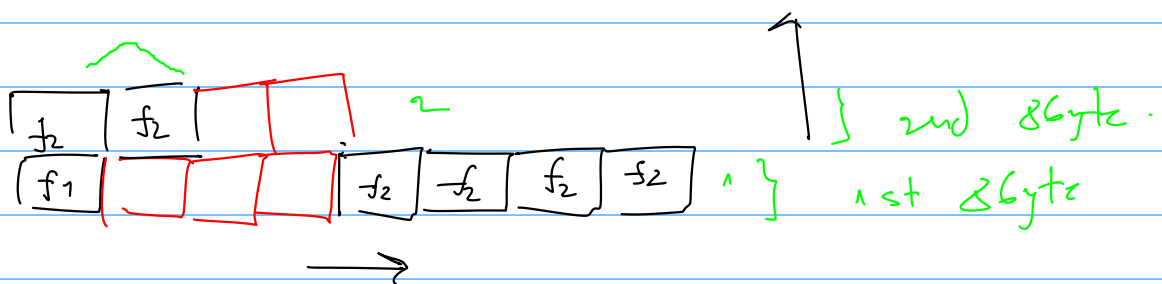




```

1
2
3 typedef struct
4 {
5     char f1;    // size: 1, alignment: 1
6     int f2;     // size: 4, alignment: 4
7     short f3;   // size: 2, alignment: 2
8 } StructType1; // size: 12, alignment: 4
9

```

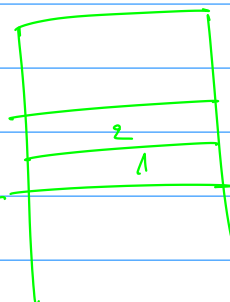


no\_class, integer

integer

integer

integer



```

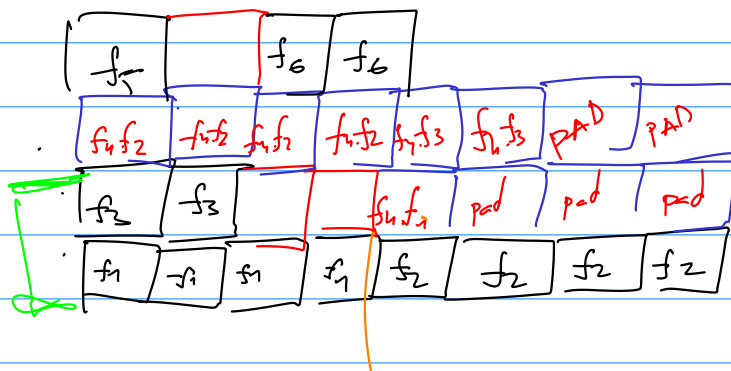
3 typedef struct
4 {
5     char f1;    // size: 1, alignment: 1
6     int f2;     // size: 4, alignment: 4
7     short f3;   // size: 2, alignment: 2
8 } StructType1; // size: 12, alignment: 4
9
10 /*

```

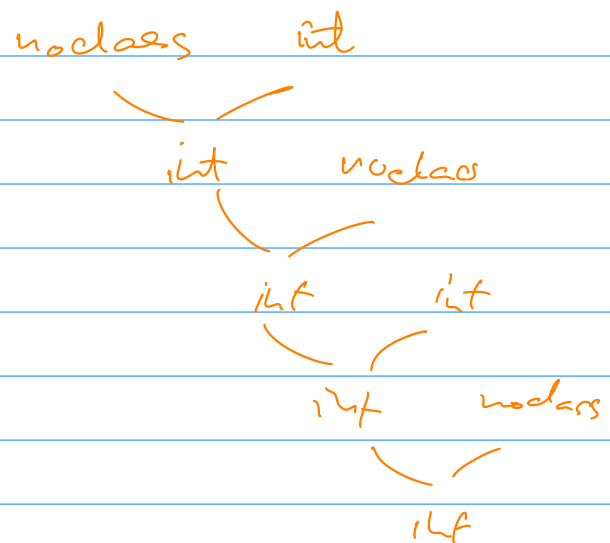
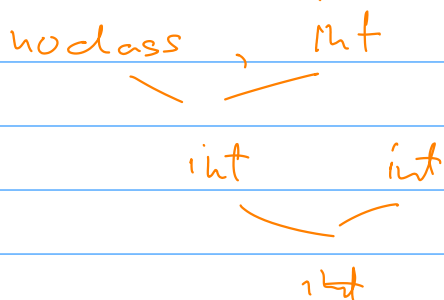
```

78 typedef struct
79 {
80     int f1;      // size: 4, alignment: 4
81     int f2;      // size: 4, alignment: 4
82     short f3;    // size: 2, alignment: 2
83     StructType1 f4; // size: 12, alignment: 4
84     char f5;     // size: 1, alignment: 1
85     short f6;    // size: 2, alignment: 2
86 } StructType2;   // size: 28, alignment: 4
87
88 /*

```



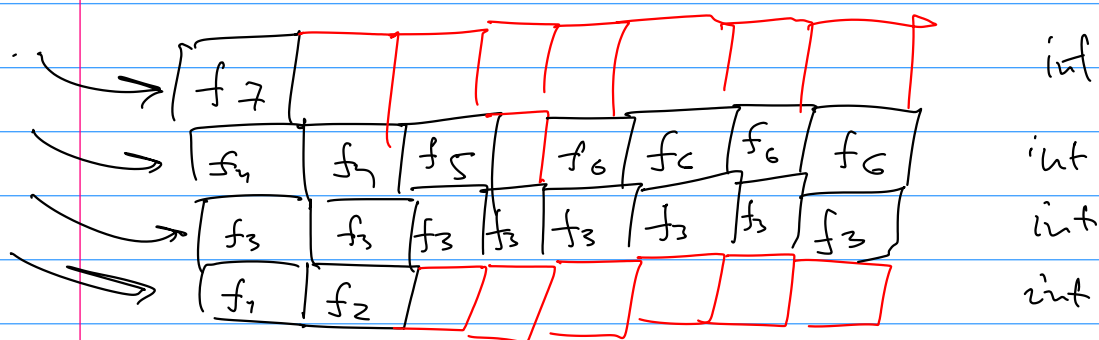
4 int  
3 int  
2 int  
1 int



```

38 typedef struct
39 {
40     char f1;    // size: 1, alignment: 1
41     char f2;    // size: 1, alignment: 1
42     long f3;    // size: 8, alignment: 8
43     short f4;   // size: 2, alignment: 2
44     char f5;    // size: 1, alignment: 1
45     int f6;     // size: 4, alignment: 4
46     char f7;    // size: 1, alignment: 1
47 } StructType3; // size: 32, alignment: 8
48

```

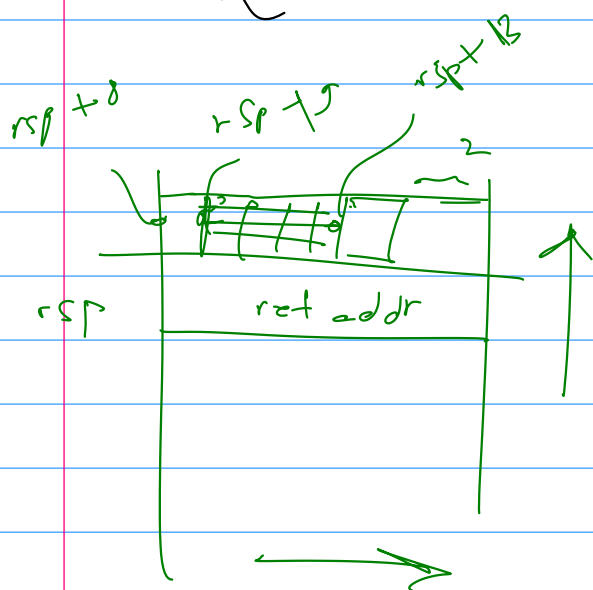


25 - 32

16B

MEM MEM

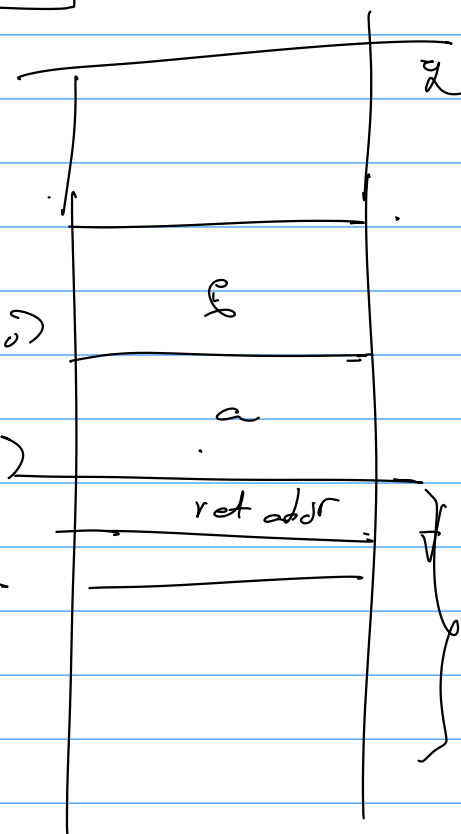
f(A, a, B, C)

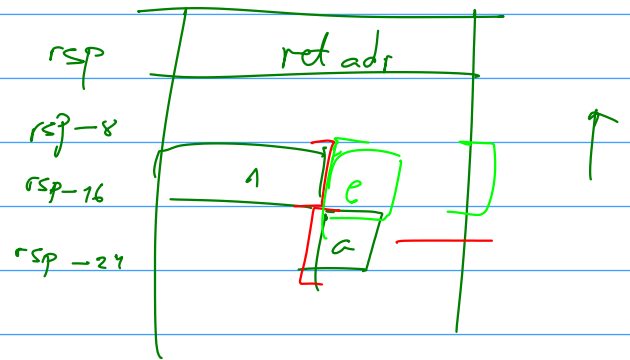


(rsp + 40)

(rsp + 8)

reg

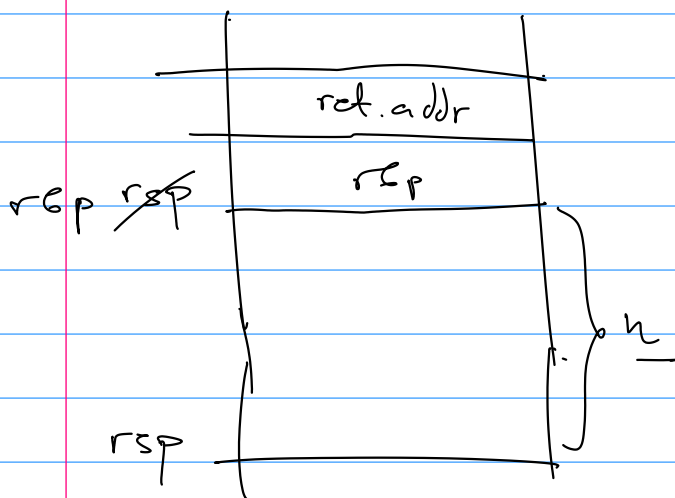




$rax : [a] \text{ , , , } [1]$   
 $edx : [e] \text{ , , , } 0000$

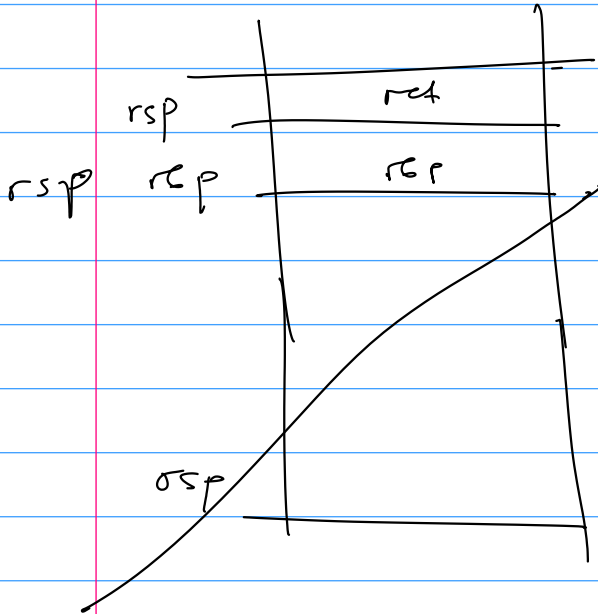
enter n, 0

push rbp  
 mov rbp, rsp  
 sub rsp, n



leave  
[ret]  
↑

mov rsp, rbp  
pop rbp

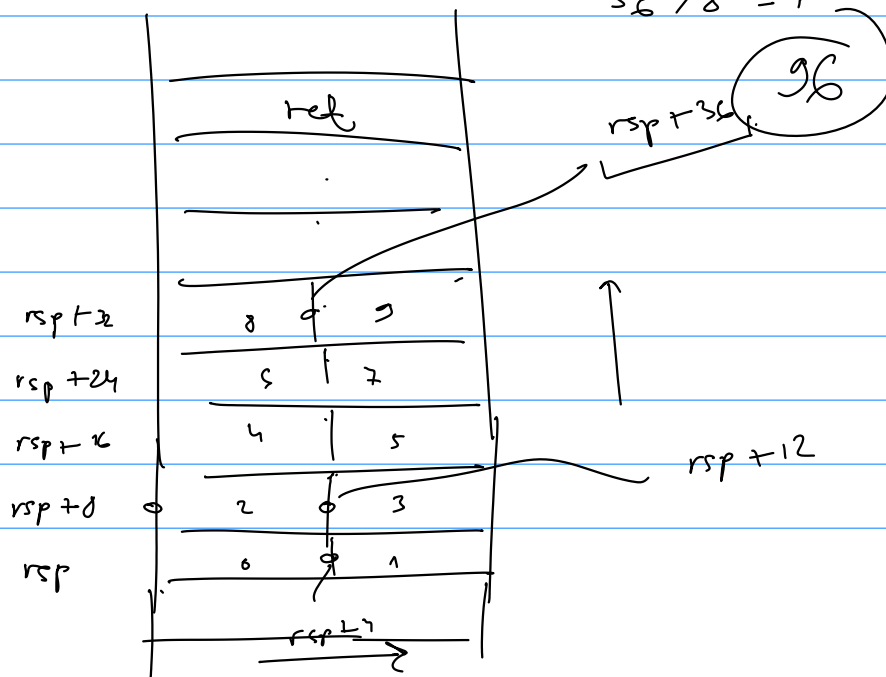


$rsp + 32$	$P_{16}$
$rsp + 24$	$P_3$
$rsp + 16$	$P_2$
$rsp + 8$	$P_7$
$rsp$	<code>ret</code>

$$\begin{array}{r} 56 + 4.8 \\ 56 + 32 \\ \hline 88 \end{array}$$

$$\begin{array}{r} 16 \\ 32 \\ \hline 48 \end{array}$$

$$56 / 8 = 7$$





```

if ( < cond > ) {
    < then >
} else {
    < else >
}

```

```

if ( < cond > ) goto then

```

```

    < else >
    goto out
then : < then >
out :

```

```

: { cond
j? then
: { < else >

```

```

    jump over
then: : { < then >
over:

```

```
do {
    <body>
} while (<cond>);
```

```
loop:
    <body>
    if (<cond>) goto loop
```

```
loop:
    {
        <body>
    }
    {
        <cond>
    }
    ? loop
```

```

      ranc
      cmov
[ x = <cond> ? (val1) : val2; ]

```

```
if (<cond>) x = val1
else x = val2
```

```
{ <cond>
```

```
mov ranc, val1
```

```
[ cmov? ranc, val2 ]
```

```

    |

```

```
while (<cond>) {
    <body>
}
```

```
if (!<cond>) goto over
```

```
loop: <body>
```

```
if (<cond>) goto loop
```

```
over:
```

```

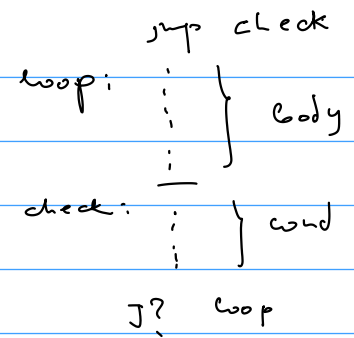
    |

```

```

      goto check
loop : < body >
check: if(< cond >) goto loop.

```



```

for (init ; cond ; inc) {
    body
}

```

```

init
while (cond) {
    body
    inc
}

```

```

init
jmp check
loop  body
     inc
check: cond
     j? loop.

```

```

switch ( <expr> ) {
    case val1: <case1> ; break;
    case val2: <case2>
    default: <default>
}

```

```

x = <expr>
if ( x == val1 ) goto case1
if ( x == val2 ) goto case2
goto def

```

```

[
    case1: <case1>
        goto over
    case2: <case2>
    def: <default>
    over:
]

```

```

      E
    -----
switch ( <expr> ) {
    case 0:
    case 1:
    case 2:
    .
    .
    case 10:

```

$L = \{ \text{case } 0, \text{case } 1, \dots, \text{case } 10 \}$

```

if ( 0 ≤ E && E ≤ 10 ) goto L[E];
goto default

```

```

case 0;
case 1;
.
.
case 10;

```

```

.intel_syntax noprefix
.text
.global foo
.type foo, @function
foo:

```

```

    push rbp
    mov rbp, rsp
    mov QWORD PTR -24[rbp], rdi
    mov QWORD PTR -32[rbp], rsi
    mov DWORD PTR -36[rbp], edx
    mov rax, QWORD PTR -32[rbp]
    mov rdx, QWORD PTR [rax]
    mov rax, QWORD PTR -24[rbp]
    add rax, rdx
    mov QWORD PTR -8[rbp], rax
    mov rax, QWORD PTR -32[rbp]
    mov rdx, QWORD PTR [rax]
    mov eax, DWORD PTR -36[rbp]
    add eax, edx
    mov DWORD PTR -12[rbp], eax
    mov eax, DWORD PTR -12[rbp]
    movsx rdx, eax
    mov rax, QWORD PTR -8[rbp]
    add rax, rdx
    pop rbp
    ret

```

(caf, 128)

$rax := 2nd\ arg$   
 $rdx := *2nd\ arg$   
 $rax := 1st\ arg$

# MOVE with Sign eXtend

$rax := 2nd\ arg$

$edx := *(2nd\ arg + 8)$

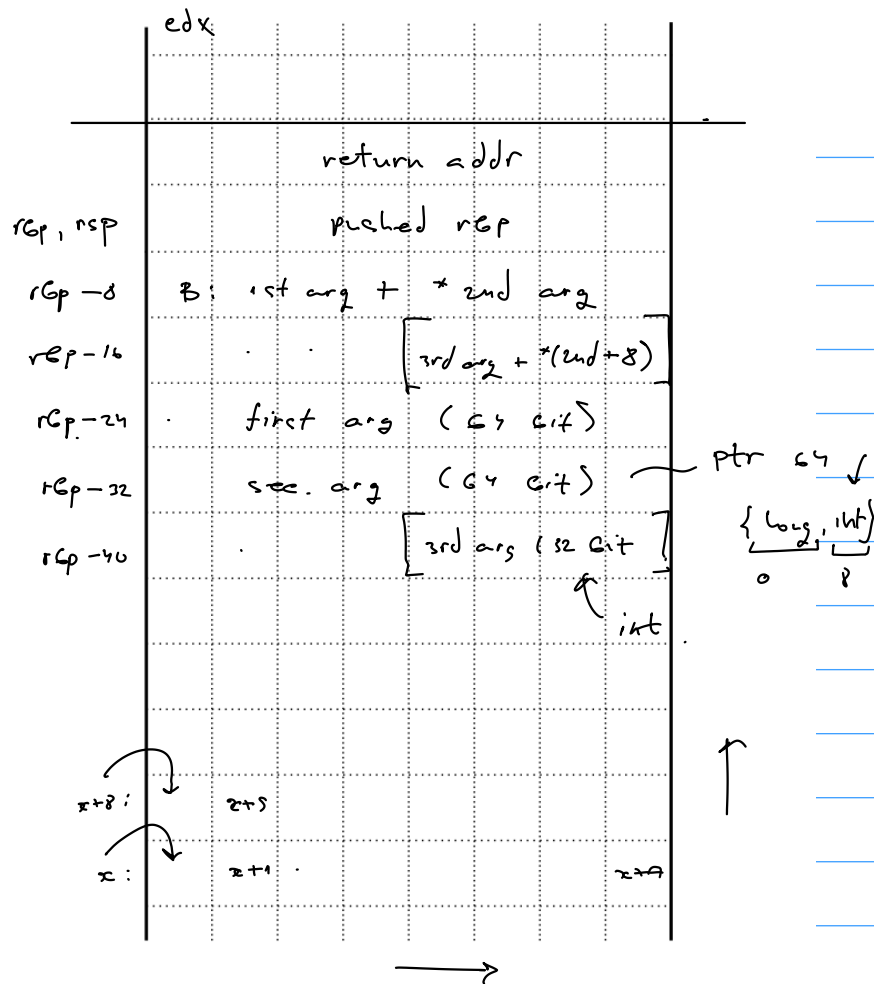
$eax := 3rd\ arg$

$A = 3rd\ arg + *(2nd\ arg + 8)$

$rdx := signExtend(A)$

$rax := A + B$

(rdi, rsi, rdx, rcx, r8, r9)



```

long foo ( long x, struct A *p, int y ) {
    long A = y + p -> a2;
    long B = x + p -> a1;
    return A + B;
}

```

```

struct A {
    long a1;
    int a2;
}

```

(rdi, rsi, rdx, rcx, r8, r9)

```

.intel_syntax noprefix
.text
.global foo
.type foo, @function

foo:
    push rbp
    mov rbp, rsp
    mov QWORD PTR -24[rbp], rdi
    mov QWORD PTR -32[rbp], rsi
    mov rax, QWORD PTR -24[rbp]
    mov rax, QWORD PTR 16[rbp+rax*8]
    mov QWORD PTR -8[rbp], rax
    mov rax, QWORD PTR -32[rbp]
    mov rdx, QWORD PTR [rax]
    mov rax, QWORD PTR -8[rbp]
    add rdx, rax
    mov rax, QWORD PTR -32[rbp]
    mov QWORD PTR [rax], rdx
    mov rax, QWORD PTR -8[rbp]
    pop rbp
    ret
    
```

		xs[2]	
		xs[1]	
rcp+16		xs[0]	
rcp+8		ret addr	foo
rcp, rsp		pushed rbp	
rcp-8		xs[1st arg]	
rcp-16			
rcp-24		1st arg (64 bit) = long	
rcp-32		2nd arg (64 bit) ptr long	

$*2nd = xs[1st] \text{ rax} = 1st$   
 $\text{rax} = 2nd$   
 $rdx := *2nd. \quad \text{rax} := xs[1st]$   
 $val := *2nd + xs[1st] = A$   
 $*2nd = A \quad \text{xs}[1st]$   
 $\text{rax} := xs[1st \text{ arg}]$

struct A {

long xs[3];

};

```

long foo(struct A a, long idx, long *p) {
    long val = a.xs[idx];
    *p += val;
    return val;
}
    
```

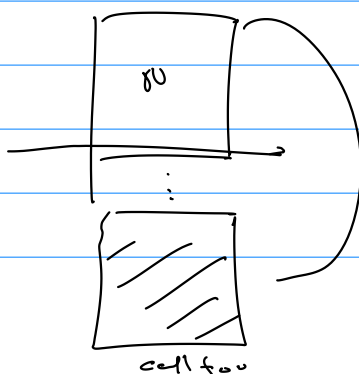
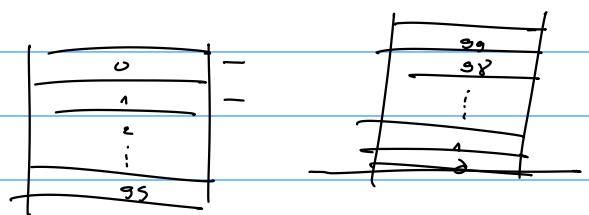
int xs[100] struct X {

foo(xs)

int xs[100];

} s;

400 foo(s)



```

.intel_syntax noprefix
.text
.globl foo
.type foo, @function
foo:

```

```

    push rbp
    mov rbp, rsp
    sub rsp, 16
    mov QWORD PTR -8[rbp], rdi
    cmp QWORD PTR -8[rbp], 0
    je label_1
    mov rax, QWORD PTR -8[rbp]
    sub rax, 1
    push QWORD PTR 88[rbp]
    push QWORD PTR 80[rbp]
    push QWORD PTR 72[rbp]
    push QWORD PTR 64[rbp]
    push QWORD PTR 56[rbp]
    push QWORD PTR 48[rbp]
    push QWORD PTR 40[rbp]
    push QWORD PTR 32[rbp]
    push QWORD PTR 24[rbp]
    push QWORD PTR 16[rbp]
    mov rdi, rax
    call foo
    add rsp, 80
    # imul reg64, mem64
    # signed multiply
    # reg64 ← truncate(reg64 * mem64)
    imul rax, QWORD PTR -8[rbp]
    jmp label_2
label_1:
    mov rax, QWORD PTR 16[rbp]
label_2:
    leave
    ret

```

if (1st == 0)  
goto lab1

10 x 8

lab1:

foo(n-1,

(rdi, rsi, rdx, rcx, r8, r9)

rbp+16

rcp+8

rcp

rsp

return addr

pushes rcp

[1st arg (call)]

10

9

8

7

6

5

4

3

2

1

27

foo

0 80

struct A {

long xs[10];

}

long foo ( long n, struct A a ) {

if ( n == 0 ) {

return a.xs[0];

} else {

return n \* foo ( n-1, a );

}