Update

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METHOD 1 - Full Sample + BLB Bootstrapped SE (Wald CI Formed at End)

```
base nm <- 'blb standard error v1'
temp_dir <- file.path(base_dir, dat_path, paste0(base_nm, '_tmp'))</pre>
cblb <- as.data.table(readRDS(file.path(temp_dir, 'coverage.rds')))</pre>
cblb[, `:=`(lower_ci = tau_hat - qnorm(0.975)*boot_sd,
            upper_ci = tau_hat + qnorm(0.975)*boot_sd)][
              , .(coverage = mean(lower_ci <= te & upper_ci >= te)), by = c('n', 'subsets', 'prop_form
##
          n subsets prop_form out_form coverage
##
  1: 50000
                 10
                                           0.951
                      correct correct
##
  2: 50000
                 50
                      correct correct
                                           0.951
  3: 50000
                 1
                      correct correct
                                           0.948
##
##
   4: 50000
                 10
                                           0.953
                        wrong correct
##
  5: 50000
                 50
                        wrong correct
                                           0.955
  6: 50000
                                           0.953
                 1
                        wrong correct
  7: 50000
                 10
                                  wrong
                                           0.954
##
                     correct
   8: 50000
                 50
                      correct
                                  wrong
                                           0.955
## 9: 50000
                                           0.956
                 1
                     correct
                                  wrong
## 10: 50000
                 10
                                  wrong
                                           0.000
                        wrong
## 11: 50000
                  50
                                           0.000
                        wrong
                                  wrong
## 12: 50000
                  1
                                           0.000
                         wrong
                                  wrong
```

METHOD 2 - Bias Correct BLB Replicates in Each Set, Take the Mean for an Estimate of the ATE, Wald Interval at the End

```
base nm <- 'blb standard error v2'
temp_dir <- file.path(base_dir, dat_path, paste0(base_nm, '_tmp'))</pre>
cblb <- as.data.table(readRDS(file.path(temp_dir, 'coverage.rds')))</pre>
cblb[, `:=`(lower_ci = tau_hat - qnorm(0.975)*boot_sd,
            upper_ci = tau_hat + qnorm(0.975)*boot_sd)][
              , .(coverage = mean(lower_ci <= te & upper_ci >= te)), by = c('n', 'subsets', 'prop_form
##
           n subsets prop_form out_form coverage
   1: 50000
                  10
                       correct correct
  2: 50000
                  50
                       correct correct
                                           0.951
   3: 50000
                  1
                      correct correct
                                           0.948
## 4: 50000
                  10
                                           0.953
                         wrong correct
```

0.955

5: 50000

50

wrong correct

```
## 6: 50000
                                        0.953
                 1
                       wrong correct
## 7: 50000
                10
                                        0.954
                     correct
                               wrong
## 8: 50000
                50 correct
                                wrong
                                        0.955
## 9: 50000
                 1 correct
                                        0.956
                                wrong
## 10: 50000
                 10
                       wrong
                                wrong
                                        0.000
## 11: 50000
                50
                                        0.000
                                wrong
                       wrong
## 12: 50000
                                        0.000
                 1
                       wrong
                                wrong
```

METHOD 3 - Bias Correct BLB Replicates, Take Percentile CI In Each Subset

```
base_nm <- 'blb_standard_error_v3'</pre>
temp_dir <- file.path(base_dir, dat_path, paste0(base_nm, '_tmp'))</pre>
cblb <- as.data.table(readRDS(file.path(temp_dir, 'coverage.rds')))</pre>
cblb[, .(coverage = mean(lower_ci <= te & upper_ci >= te)), by = c('n', 'subsets', 'prop_form', 'out_f
          n subsets prop_form out_form coverage
## 1: 50000
                10 correct correct
                                         0.956
## 2: 50000
                 50
                    correct correct
                                         0.958
## 3: 50000
                 1
                    correct correct
                                         0.956
## 4: 50000
                 10
                                         0.958
                        wrong correct
## 5: 50000
                 50
                                         0.961
                        wrong correct
## 6: 50000
                                         0.959
                 1
                        wrong correct
## 7: 50000
                 10
                                         0.965
                     correct
                                wrong
## 8: 50000
                 50 correct
                              wrong
                                         0.961
## 9: 50000
                 1 correct wrong
                                         0.963
## 10: 50000
                 10
                                         0.000
                        wrong
                                 wrong
## 11: 50000
                 50
                                         0.000
                        wrong
                                 wrong
## 12: 50000
                  1
                                         0.000
                        wrong
                                 wrong
```

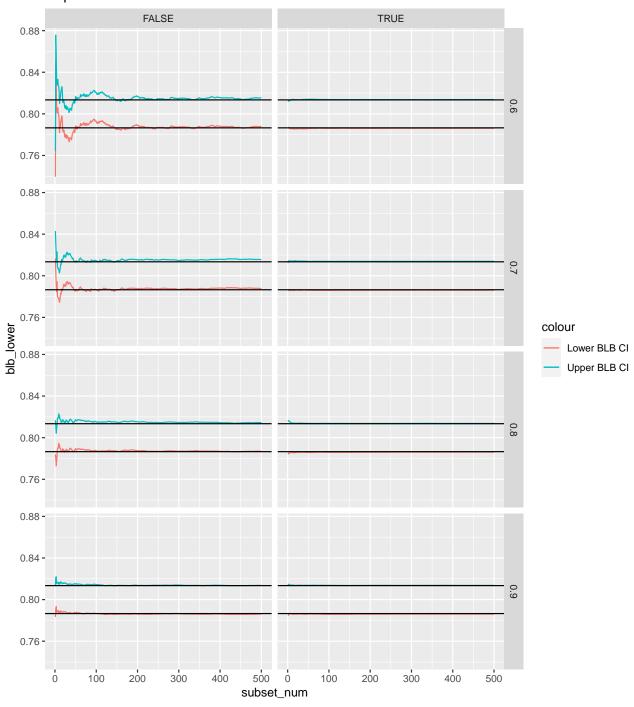
Convergence of Each Replicate

```
base_nm <- 'convergence'</pre>
temp_dir <- file.path(base_dir, dat_path, paste0(base_nm, '_tmp'))</pre>
cblb <- as.data.table(readRDS(file.path(temp_dir, 'coverage.rds')))</pre>
cblb <- cblb[gamma != 0.5]
setorder(cblb, rep, subset_num)
cblb[, `:=`(blb_lower = cumsum(blb_lower)/subset_num, blb_upper = cumsum(blb_upper)/subset_num),
             by = c('rep', 'n', 'gamma', 'subsets', 'bias_correct')]
cblb[, `:=`(error = abs(true_lower - blb_lower)/2 + abs(true_upper - blb_upper)/2)]
trajectory <- cblb[, .(mean_error = mean(error)), by = c('n', 'gamma', 'subsets', 'bias_correct', 'subs
reps <- unique(cblb$rep)
for(i in reps){
 tmp <- cblb[rep == i]</pre>
  p <- ggplot(tmp, aes(x = subset_num)) +</pre>
    geom_line(aes(y = blb_lower, color = 'Lower BLB CI')) +
    geom_line(aes(y = blb_upper, color = 'Upper BLB CI')) +
    geom_hline(aes(yintercept= true_lower)) +
```

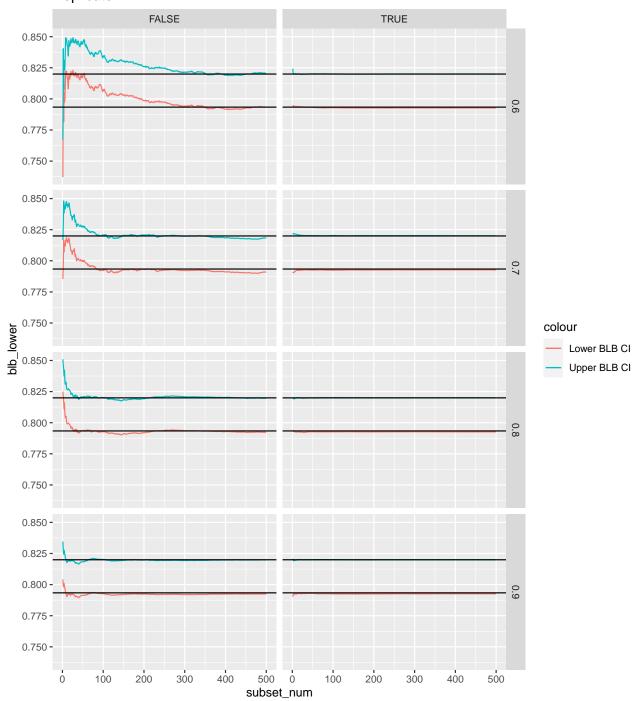
```
geom_hline(aes(yintercept = true_upper)) +
facet_grid(gamma ~ bias_correct) +
ggtitle(paste0('Replicate ', i))

print(p)
}
```

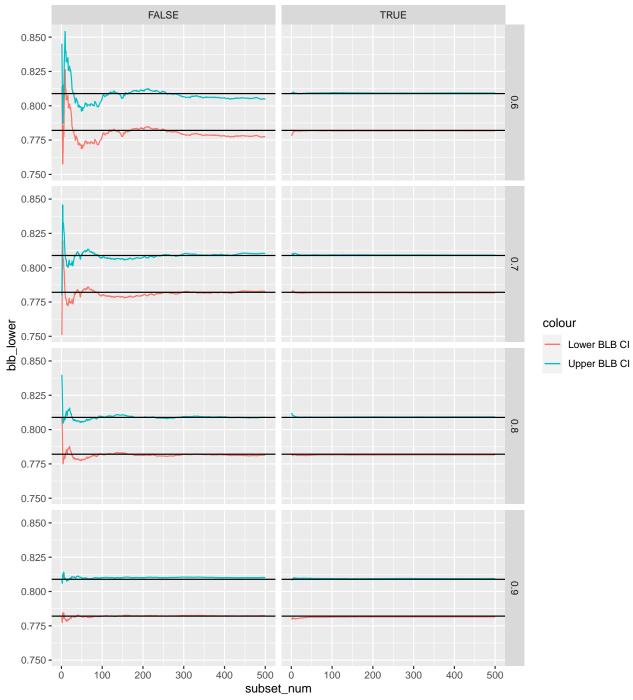
Replicate 1



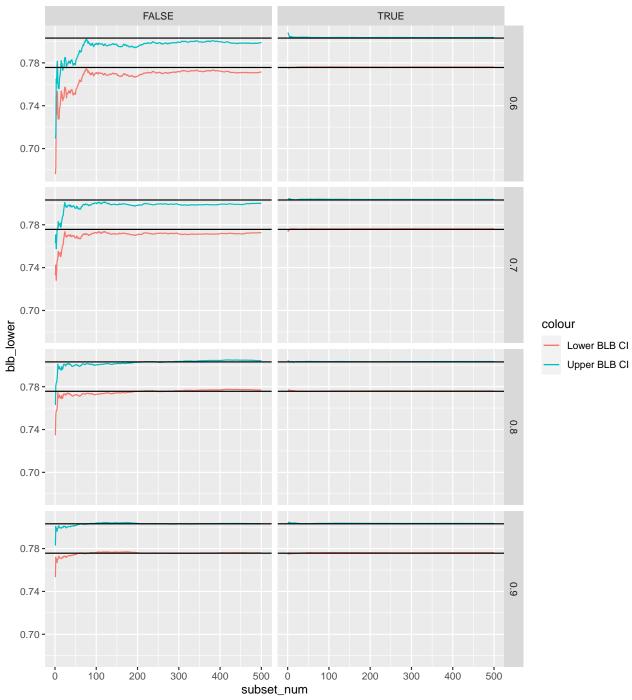




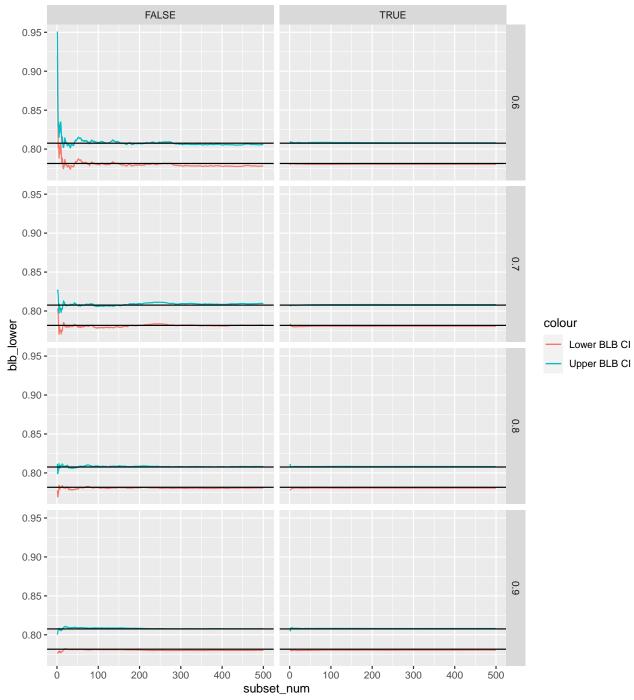


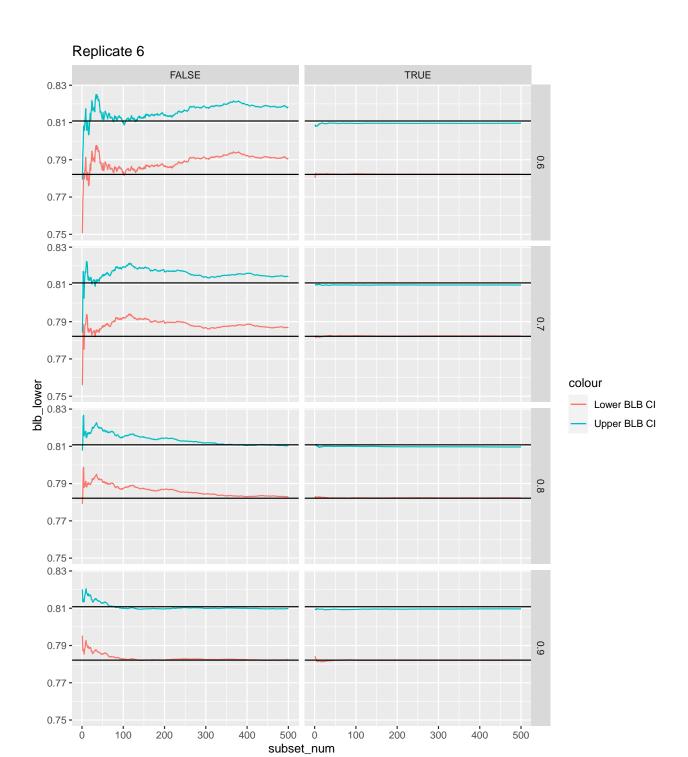




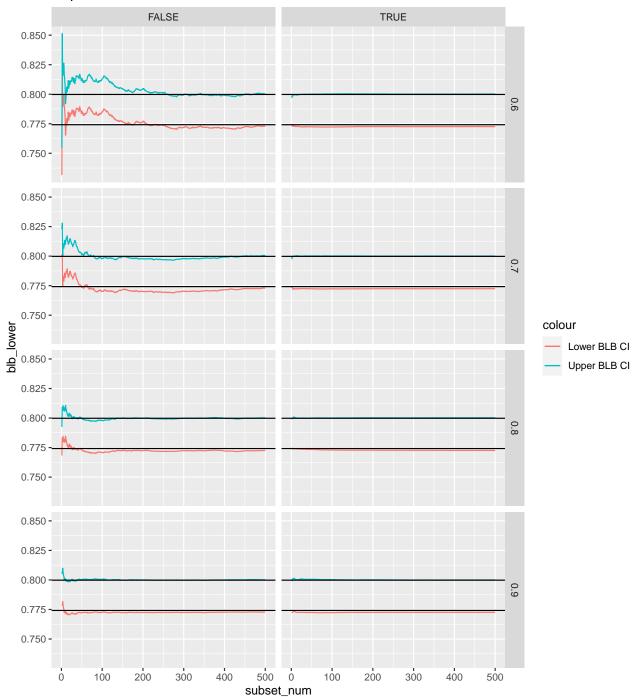




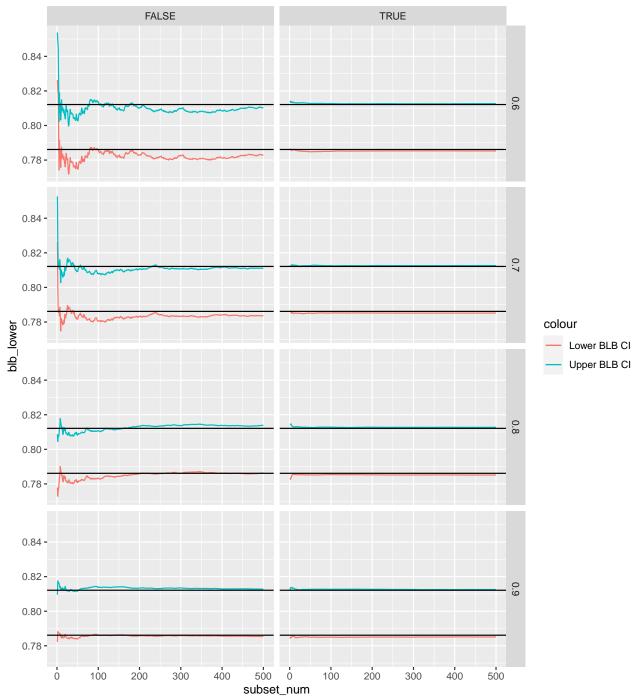




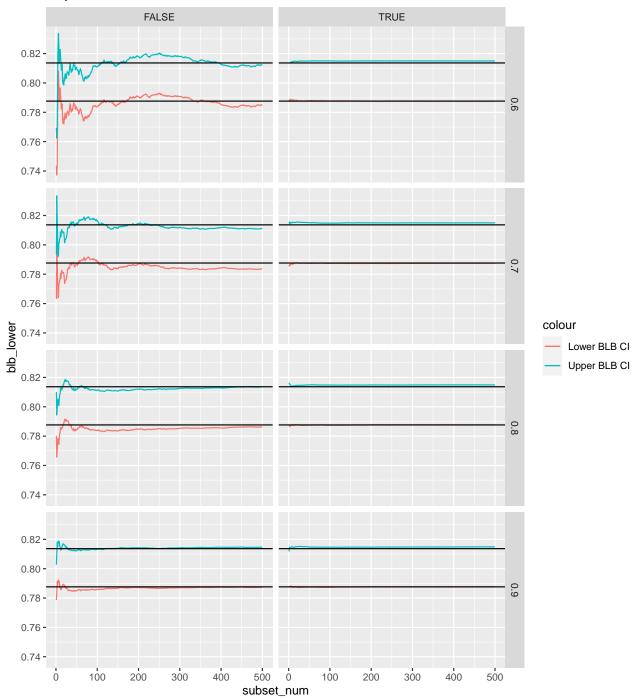


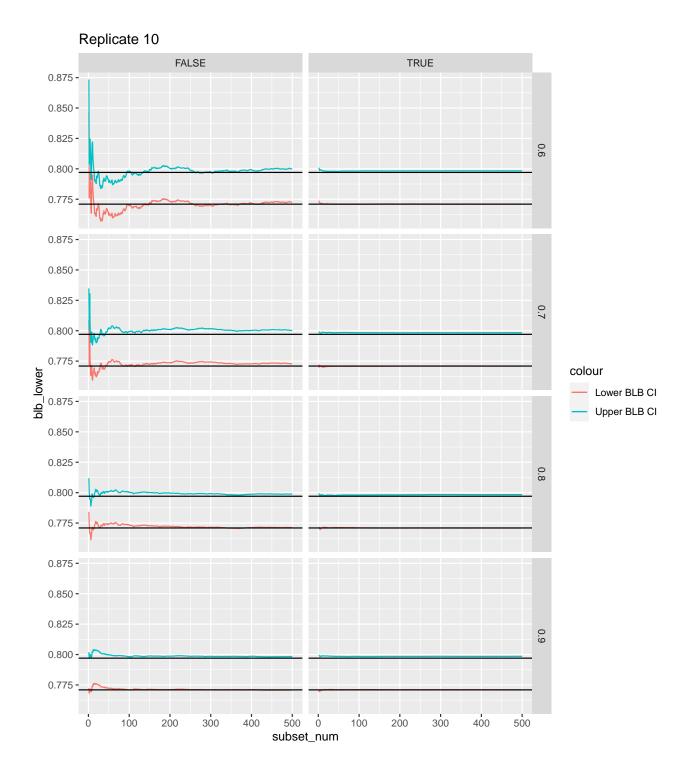






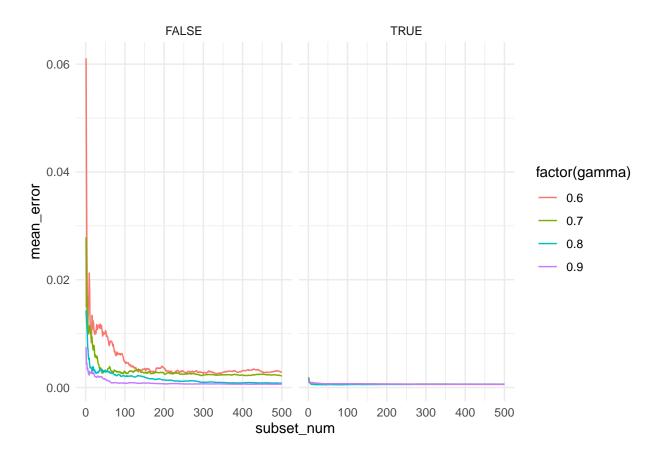






Error Convergence

```
ggplot(trajectory, aes(x = subset_num, y = mean_error, color = factor(gamma))) +
   geom_line() +
   facet_grid(~ bias_correct) +
   theme_minimal()
```



Timing

```
base_nm <- 'blb_standard_error_ml_timing_full'
temp_dir <- file.path(base_dir, dat_path, pasteO(base_nm, '_tmp'))
full <- as.data.table(readRDS(file.path(temp_dir, 'timing.rds')))
full[, `:=`(type = 'Regular bootstrap')]

base_nm <- 'blb_standard_error_ml_timing'
temp_dir <- file.path(base_dir, dat_path, pasteO(base_nm, '_tmp'))
blb <- as.data.table(readRDS(file.path(temp_dir, 'timing.rds')))
blb[, `:=`(type = pasteO('Cores: ', cores, '; Subsets = ', subsets, '; gamma = ', gamma))]
blb[, `:=`(cores = NULL, subsets = NULL, gamma = NULL)]

out <- rbindlist(list(blb, full))

ggplot(out, aes(x = type, y = time_elapsed)) +
    geom_boxplot() +
    theme(axis.text.x = element_text(angle = 90))</pre>
```

