CIS 635 - Knowledge Discovery & Data Mining

Time series data modeling

Outline

- How are the time series problems different than non time series problems
- Stationary vs non-stationary signals
- Signal decomposition
- AR(I)MA: Autoregressive Integrated Moving Average
 - From non no-stationary to stationary
 - Auto Regression
 - Moving Average

How are the time-series problems different?

- The models (Regression and Classification), we have learned so far are of the form:

f(y|X)

- For certain data, especially the time series, we can take advantage of the form:

 $f(y_t|X, y_{t-1}, y_{t-2,...}, y_0)$; essentially, here the input features are X plus the lagged instances of the target y.

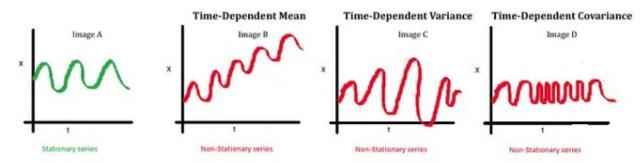
- Purely time series models are of form:

 $f(y_t|y_{t-1}, y_{t-2,...}, y_0)$, where there is no explicit, X.

Stationarity vs non-stationary signals

- A time-series is said to be stationary if it does not display any trends or seasonality.
- One more way of defining stationarity is that it is when data does not have any time-dependent mean, variance or covariance.

The Principles of Stationarity





Non stationary to stationary

- If signal is non-stationary, we can convert them into stationary signal by differencing

$$T_t = S_t - S_{t-1},$$

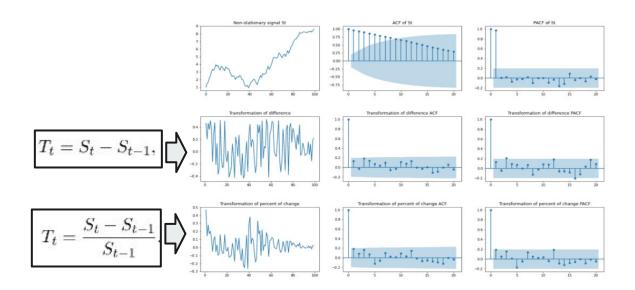
Non stationary to stationary

- If signal is non-stationary, we can convert them into stationary signal by differencing
- or calculating percent of change

$$T_t = S_t - S_{t-1},$$

$$T_t = \frac{S_t - S_{t-1}}{S_{t-1}}$$

Non stationary to stationary



Statistical time series models

- Moving Average (MA)
- Autoregressive Models (AR)
- Autoregressive Moving Average (ARMA)
- Autoregressive Moving Integrated Average (ARIMA)

$$f(y_t|y_{t-1}, y_{t-2, ...}, y_0)$$

AR(I)MA

 AutoRegressive Integrated Moving Average (ARIMA) is a statistical model for forecasting time series data.

A combined model with **AR**, **MA**, but first transforming the signal to stationary.

- AR (Autoregression): This emphasizes the dependent relationship between an observation and its preceding or 'lagged' observations.
- I (Integrated): To achieve a stationary time series, one that doesn't exhibit trend or seasonality, differencing is applied. It typically involves subtracting an observation from its preceding observation.
- MA (Moving Average): This component zeroes in on the relationship between an observation and the residual error from a moving average model based on lagged observations.

AR(I)MA

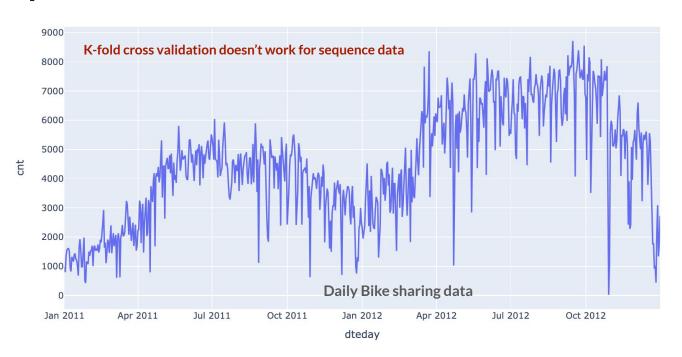
The parameters of the ARIMA(p,d,q) model are defined as follows:

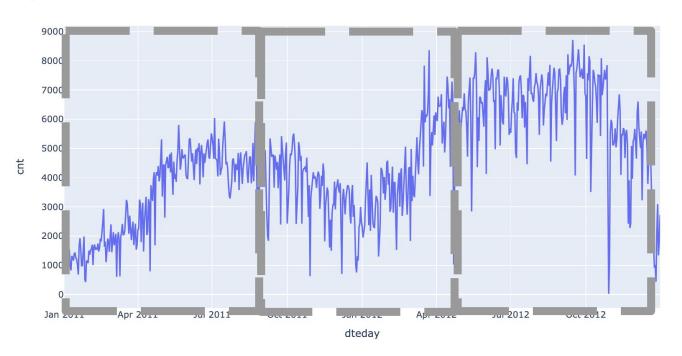
- **p**: The lag order, representing the number of lag observations incorporated in the model.
- **d**: Degree of differencing, denoting the number of times raw observations undergo differencing.
- q: Order of moving average, indicating the size of the moving average window.

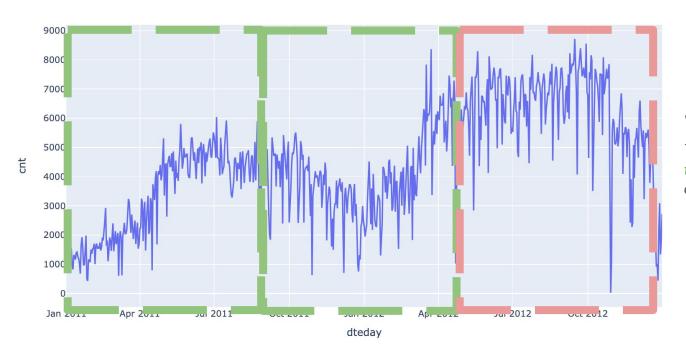
A combined model with **AR**, **MA**, but first transforming the signal to stationary.

Notebook presentation

Notebook

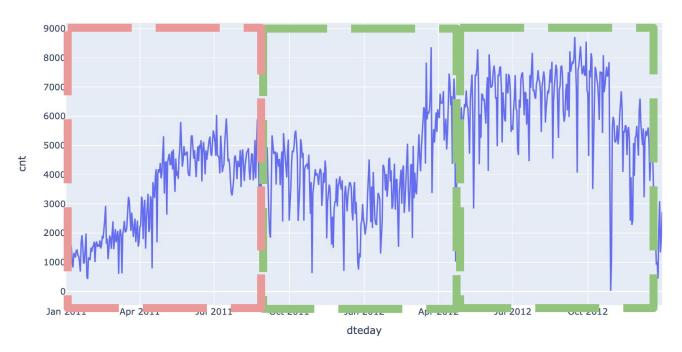






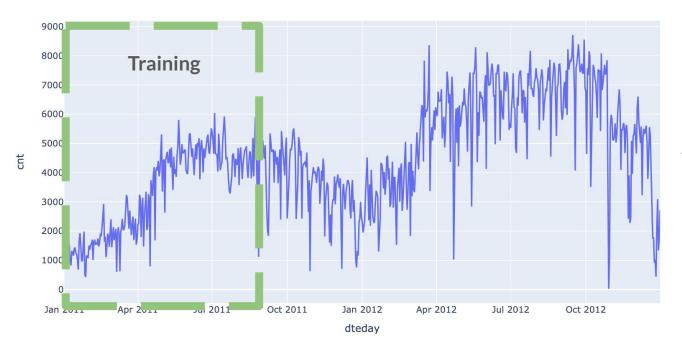
Valid configuration:

Training on first two folds, and test on the last fold



Invalid configuration:

Training on first fold, and test on the last two.









QA