




# CIS 678 Machine Learning

**ML Introduction:** Linear Regression (part 1)

# What we'd like to accomplish today

- 
- General Concepts: ***Straight Line to Linear Regression***
  - Gradient Descent Algorithm
    - A simple two parameter **Linear Regression** model
    - Hands on **Notebook implementation**
  - QA

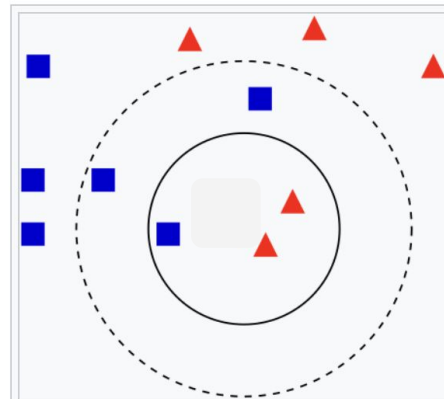


## What we have learned so far!

- k-Nearest neighbors (k-NN)

# Our first ML Model

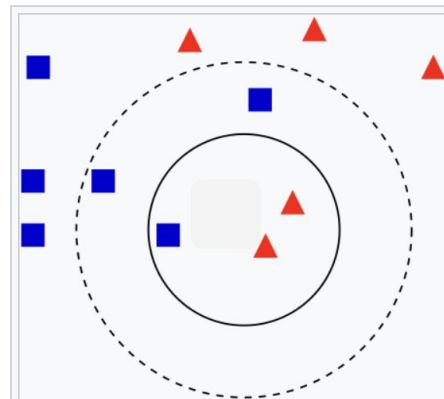
- You are given a set of data points of two classes: red triangles, and blue squares



Example of  $k$ -NN classification. The test sample (green dot) should be classified either to blue squares or to red triangles. If  $k = 3$  (solid line circle) it is assigned to the red triangles because there are 2 triangles and only 1 square inside the inner circle. If  $k = 5$  (dashed line circle) it is assigned to the blue squares (3 squares vs. 2 triangles inside the outer circle).

# Our first ML Model

- You are given a set of data points of two classes: red triangles, and blue squares
- And asked to develop a ML model that can classify (a new data point )between these two classes.

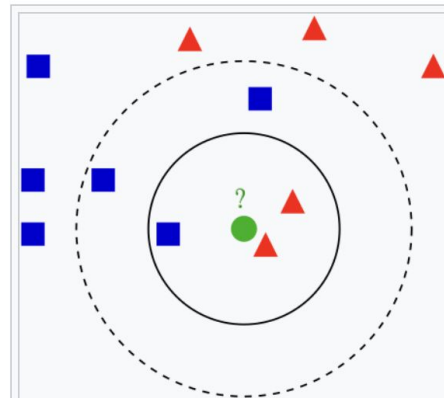


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# Our first ML Model

- k-Nearest neighbors (k-NN)
  - Supervised learning
  - Non parametric (*Distance based method*)
  - Both for Classification and Regression solutions



Circles are drawn using L2/Euclidean Distance

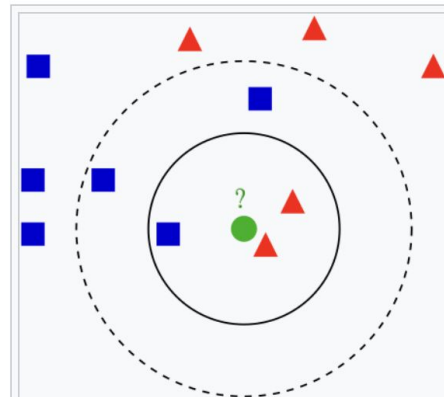



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# Our first ML Model

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*This is a red triangle  vs blue square  classification problem*

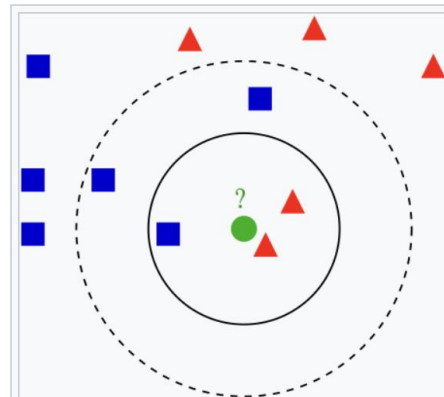



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# Our first ML Model

*What other classification problem you can think of?*

- Email Spam filter:  $y \in \{0,1\}$
- Face recognition:  $y \in \{\text{you, your friend, ...}\}$
- Cancer detection:  $y \in \{0, 1\}$
- News topic detection:  $y \in \{\text{politics, sports, ...}\}$
- Sentiment classification:  $y \in \{\text{happy, sad, ...}\}$



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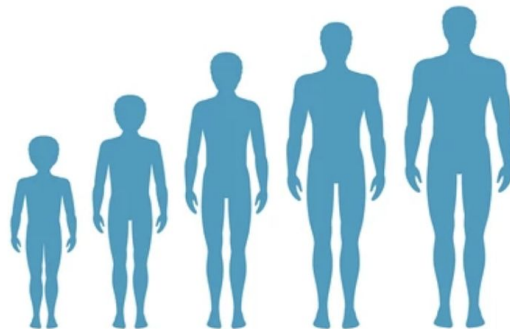
# We will be learning today about Regression

- *Insurance cost :  $y \in R$*
- *House price:  $y \in R$*
- *Weather prediction:  **$Y \in R$***
- *Energy consumption:  $y \in R$*
- *Sales forecasting:  $y \in R$*

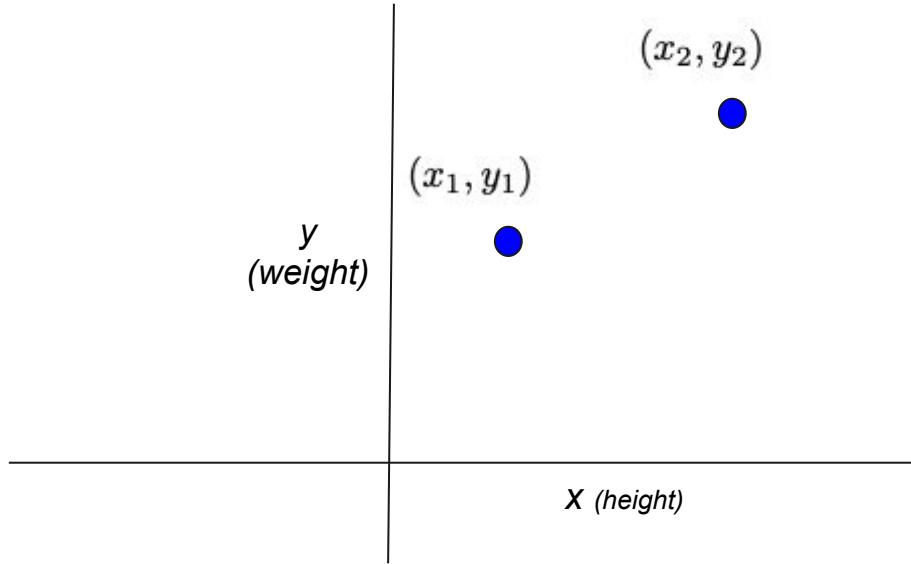
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- *Person's weight :  $y \in \mathbb{R}$*

$$f(y|x=\text{height})$$

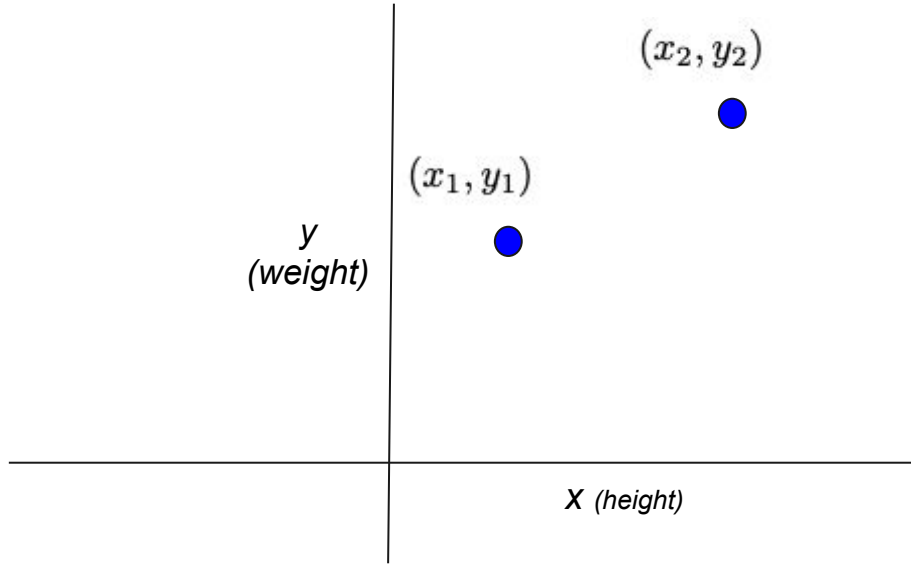


# Given these two data points



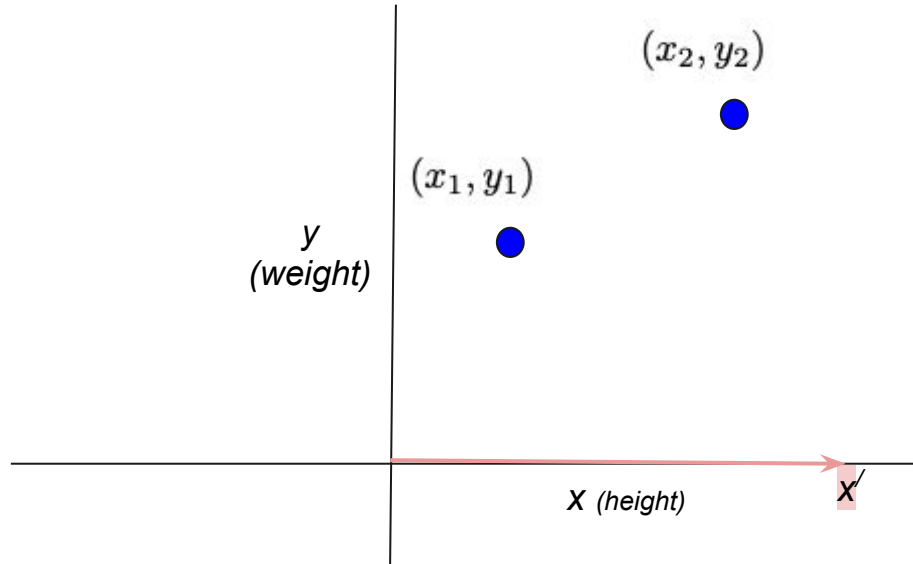
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# k-NN Regression



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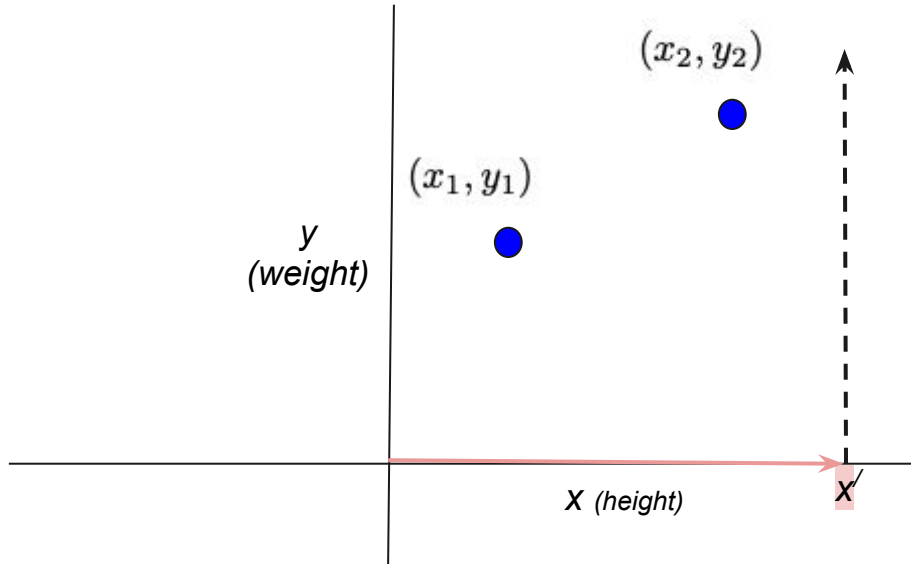
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- I.e. you have to plot  $(x', ?)$

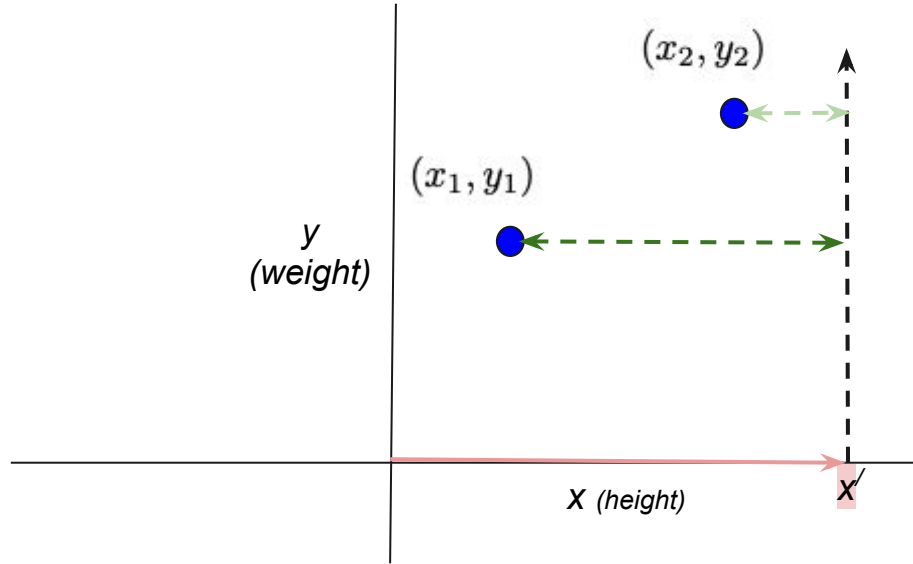
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- To estimate the distances let's draw the vertical line

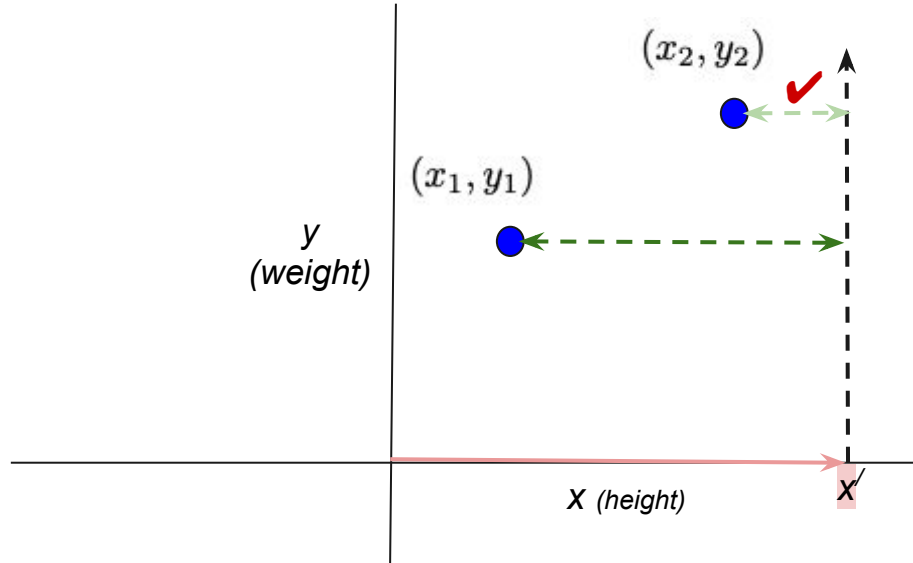
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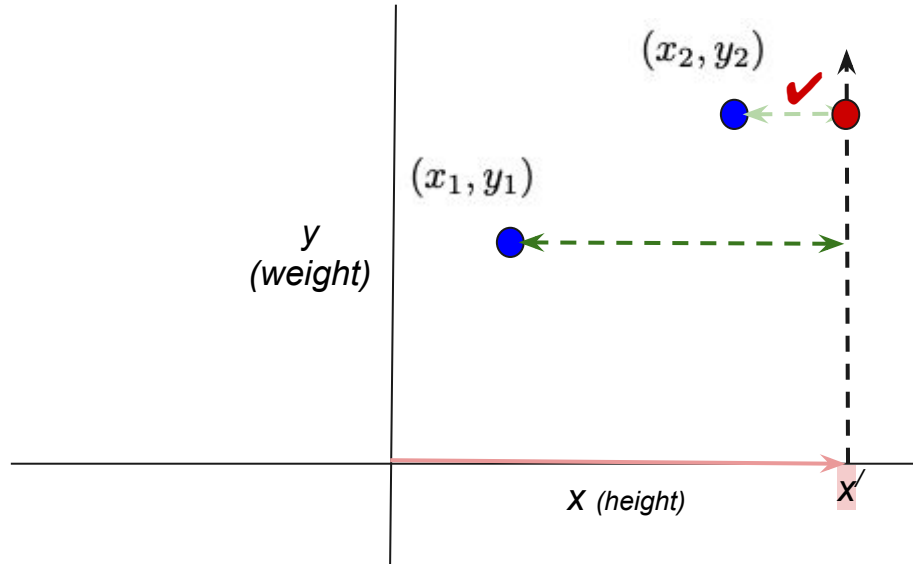


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- We propagate the associated label(s), i.e.

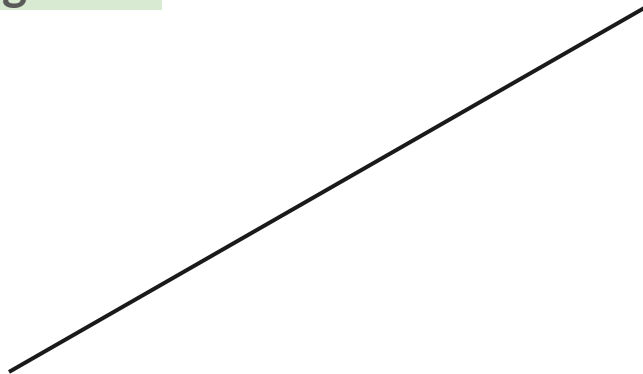
$$y(x') = y_2$$

- If we have more data points we may go for a higher  $k$ , and take the average

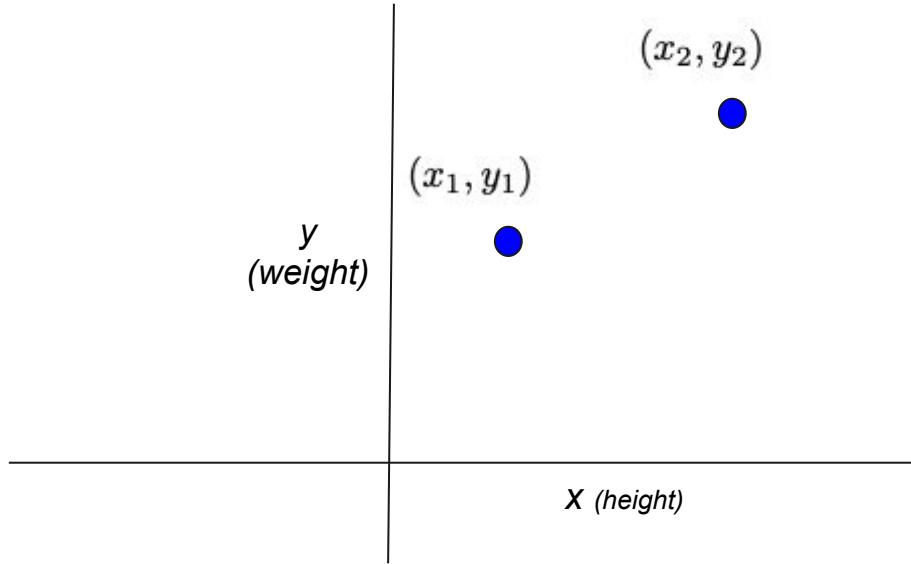


## Our Second (Supervised) Model

A simple straight line

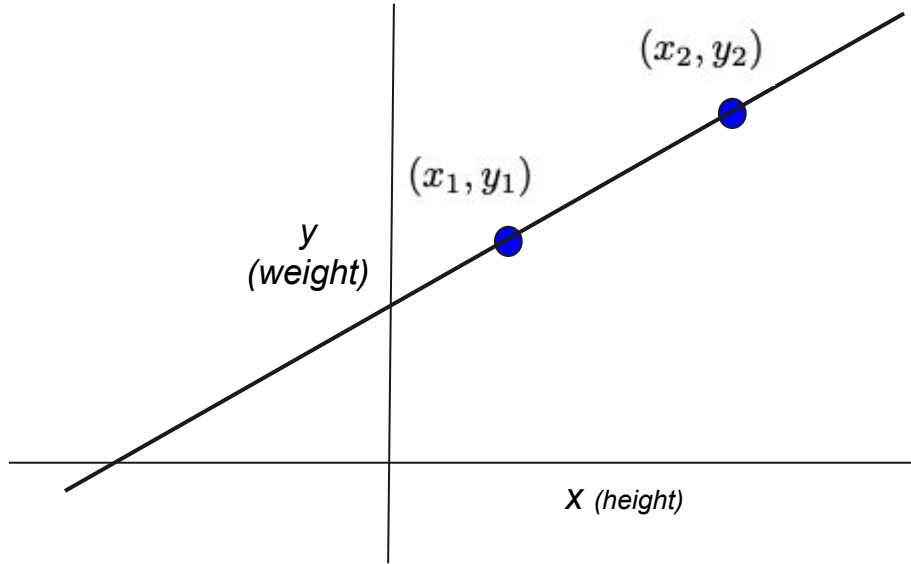


# Linear equation, a quick review



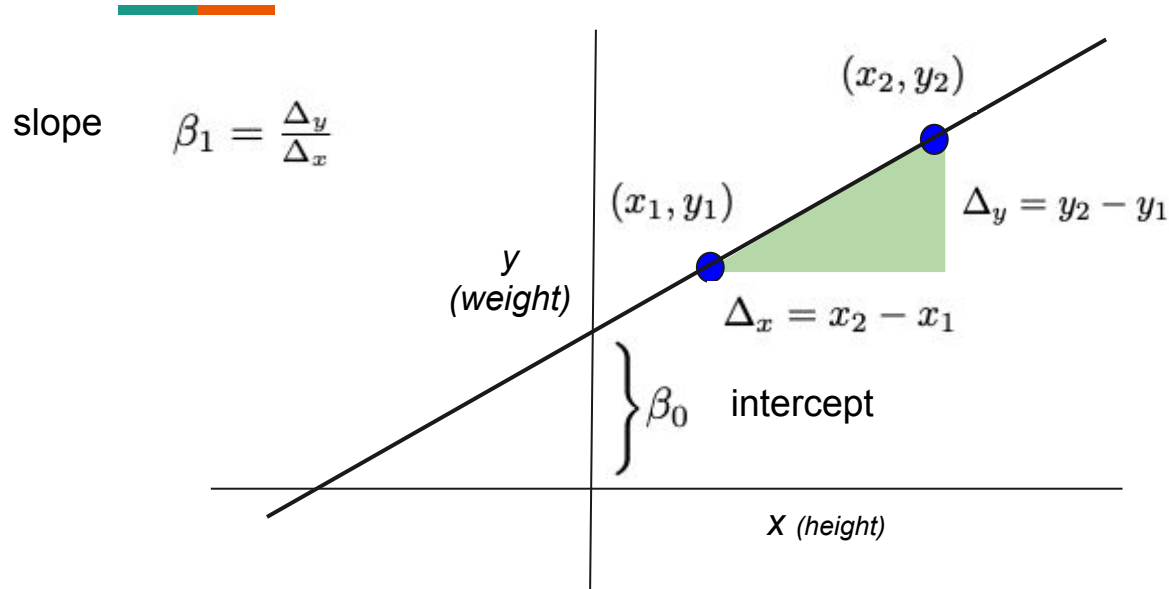
Given two data points

# Linear equation, a quick review



We can fit a linear equation

# Linear equation to a linear function, a quick review



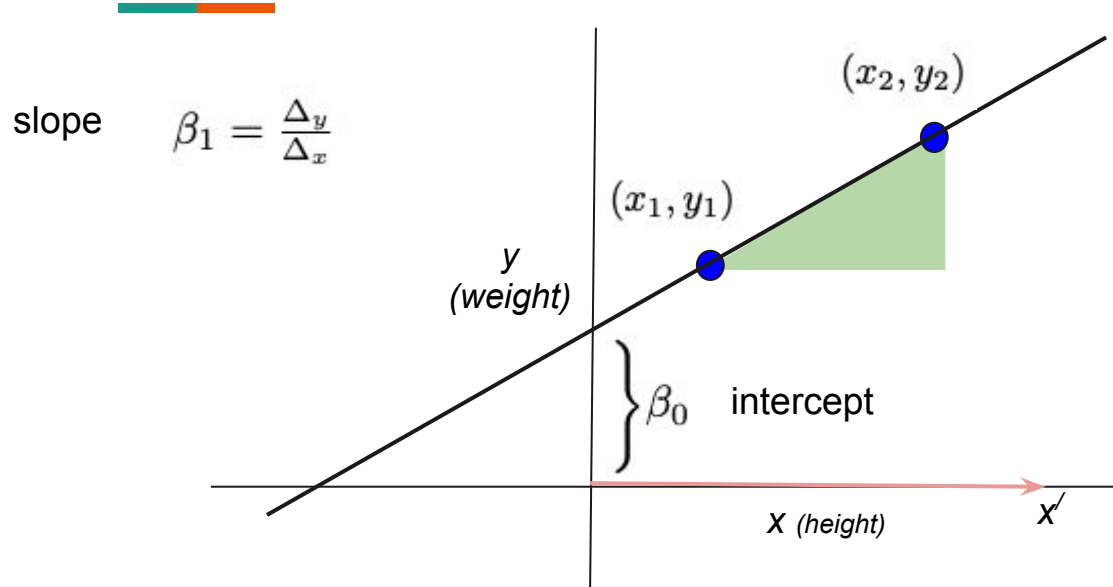
- This linear equation can be used to explain the relationship between the two axes  $x$  (independent variable) vs  $y$  (dependent variable) - as

$$y = \beta_0 + \beta_1 x$$

- A simple model with parameters: **slope**, and **intercept**

- For any given  $x'$ , this model can predict  $y(x')$  using the above equation.

# Linear equation to a linear function, a quick review



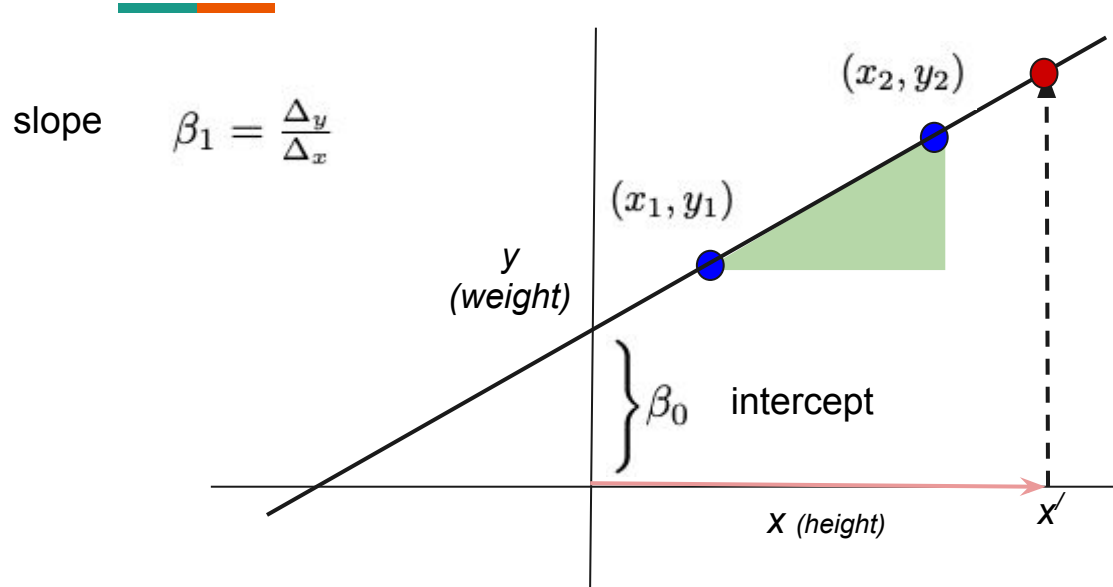
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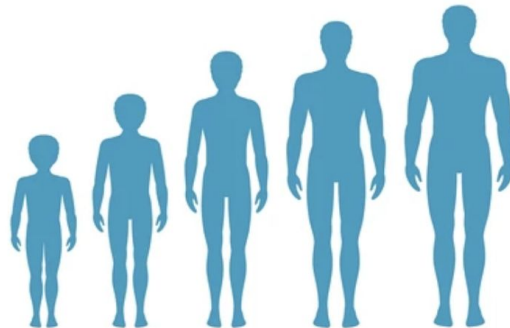
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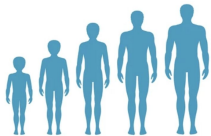
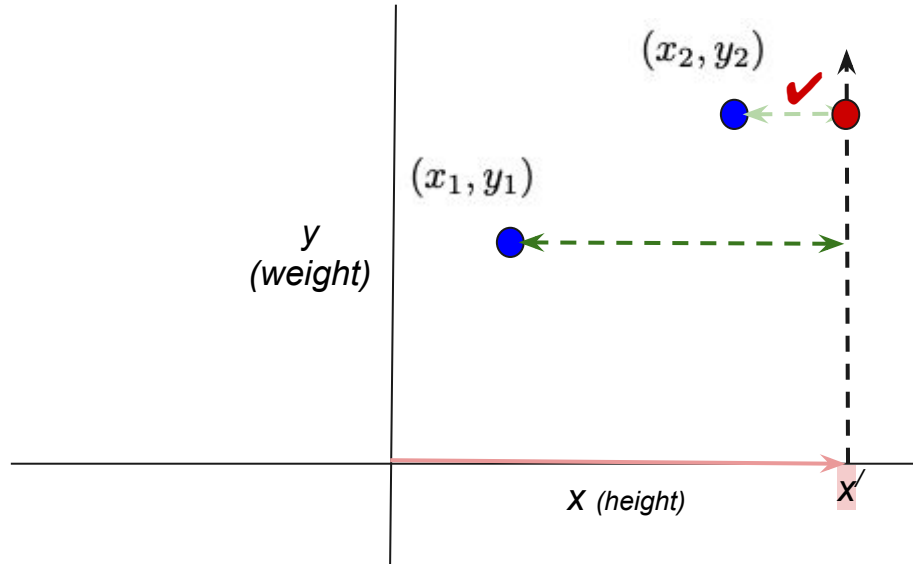
# k-NN vs. Linear Equation

Model (class) comparison!





# k-NN Regression



Failed to capture the LR relationship

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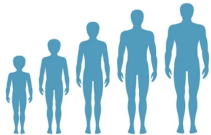
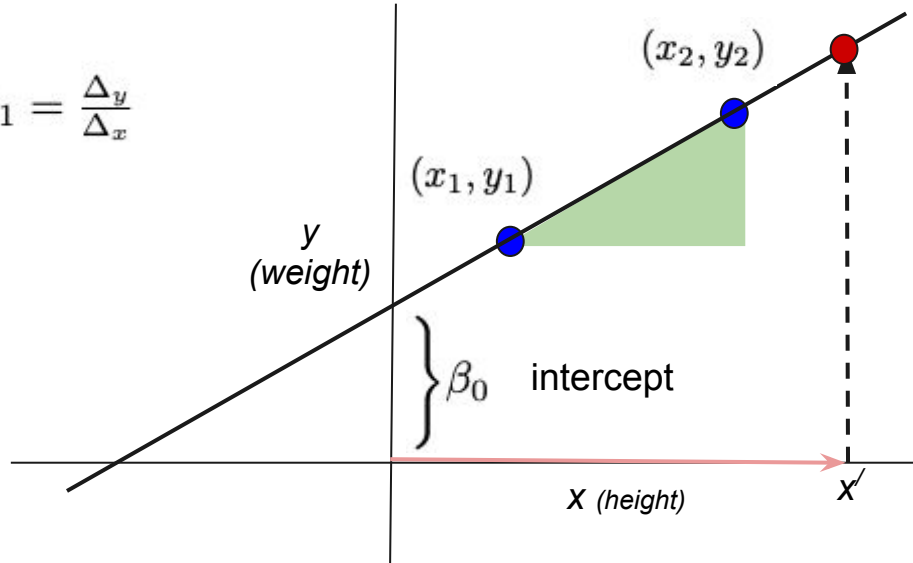
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- If we have more data points we may go for a higher  $k$ , and take the average

# Linear equation to a linear function, a quick review

slope

$$\beta_1 = \frac{\Delta y}{\Delta x}$$



Was able to capture the LR relationship

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**QA**