CIS 678 Machine Learning

Time series data modeling

Outline

- How are the time series problems different than non time series problems?
- Stationary vs non-stationary signals
- AR(I)MA: Autoregressive Integrated Moving Average
 - From non no-stationary to stationary
 - Auto Regression
 - Moving Average

Let's look at some time-series data

Notebook

How are the time-series problems different?

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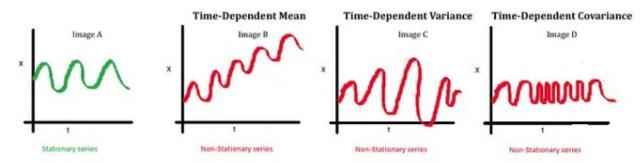
- For certain data, especially the time series, we can take advantage of the form:

 $f(y_t|X, y_{t-1}, y_{t-2}, y_0)$; essentially, here the input features are X plus the lagged instances of the target y.

Stationarity vs non-stationary signals

- A time-series is said to be stationary if it does not display any trends or seasonality.
- One more way of defining stationarity is that it is when data does not have any time-dependent mean, variance or covariance.

The Principles of Stationarity





Non stationary to stationary

- If signal is non-stationary, we can convert them into stationary signal by differencing

$$T_t = S_t - S_{t-1},$$

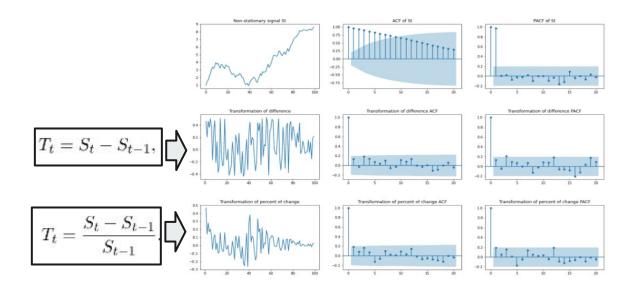
Non stationary to stationary

- If signal is non-stationary, we can convert them into stationary signal by differencing
- or calculating percent of change

$$T_t = S_t - S_{t-1},$$

$$T_t = \frac{S_t - S_{t-1}}{S_{t-1}}$$

Non stationary to stationary



- Autoregressive Models (AR)
- Moving Average (MA)
- Autoregressive Moving Average (ARMA)
- Autoregressive Moving Integrated Average (ARIMA)

$$f(y_t|y_{t-1}, y_{t-2, ..., y_0})$$

Autoregressive Models (AR)

The
$$extstyle{AR(p)}$$
 model is defined as, $X_t = \sum_{i=1}^p arphi_i X_{t-i} + arepsilon_t$ where p is the order of the model

Moving Average (MA)

MA(q): moving average model of **order q**: $X_t = \mu + arepsilon_t + heta_1 arepsilon_{t-1} + \cdots + heta_q arepsilon_{t-q}$

$$X_t = \mu + \sum_{i=1}^q heta_i arepsilon_{t-i} + arepsilon_t$$

Autoregressive Moving Average (ARMA)

ARMA(
$$p,q$$
) model $X_t = arepsilon_t + \sum_{i=1}^p arphi_i X_{t-i} + \sum_{i=1}^q heta_i arepsilon_{t-i}$

with p autoregressive terms and q moving-average terms.

AR(I)MA

 AutoRegressive Integrated Moving Average (ARIMA) is a statistical model for forecasting time series data.

A combined model with **AR**, **MA**, but first transforming the signal to stationary.

- AR (Autoregression): This emphasizes the dependent relationship between an observation and its preceding or 'lagged' observations.
- I (Integrated): To achieve a stationary time series, one that doesn't exhibit trend or seasonality, differencing is applied. It typically involves subtracting an observation from its preceding observation.
- MA (Moving Average): This component zeroes in on the relationship between an observation and the residual error from a moving average model based on lagged observations.

AR(I)MA

The parameters of the ARIMA(p,d,q) model are defined as follows:

- **p**: The lag order, representing the number of lag observations incorporated in the model.
- **d**: Degree of differencing, denoting the number of times raw observations undergo differencing.
- q: Order of moving average, indicating the size of the moving average window.

A combined model with **AR**, **MA**, but first transforming the signal to stationary.

Notebook presentation

Notebook

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