make sure to run in RStudio; first go to tools -> global options -> code and select soft-wrap R source files

```
options(repos = c(CRAN = "https://cloud.r-project.org"))
rm(list = ls()) # clear the workspace
# first run
install.packages(c('readstata13', 'sandwich', 'lmtest', 'pwr')) # need to install every new package bef
##
## The downloaded binary packages are in
  /var/folders/4p/n886yd3s3513z05rpt3f5wgm0000gn/T//RtmpElzXgX/downloaded_packages
install.packages("TeachingDemos", repos="http://R-Forge.R-project.org")
## Warning: unable to access index for repository http://R-Forge.R-project.org/bin/macosx/big-sur-arm64
     cannot open URL 'http://R-Forge.R-project.org/bin/macosx/big-sur-arm64/contrib/4.4/PACKAGES'
## installing the source package 'TeachingDemos'
library(readstata13) # need to install; you need to library a package to make the functions available
library(sandwich)
                     # used for robust standard errors
library(lmtest)
                     # used for DISPLAYING the results with robust standard errors
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
library(TeachingDemos) # used for txtStart, for logging
setwd('/Users/mkrasnow/Desktop/HARVARD/Program Evaluation/PS2') # set working directory (you'll need to
if (interactive()) {
 txtStart(file = 'pset1.txt') # store output in a file called pset1.txt; this diverts much more than s
  message("Not running interactively; output redirection skipped.")
## Not running interactively; output redirection skipped.
set-up
data <- read.dta13('krueger_class_size.dta') # read in the data and store it as an object called class
## Warning in read.dta13("krueger_class_size.dta"):
##
     Missing factor labels for variables
##
      schid3n
##
##
##
     No labels have been assigned.
      Set option 'generate.factors=TRUE' to generate labels.
##
```

QUESTION 1

```
library(pwr)
res1 <- pwr.t.test(d = 0.20, sig.level = 0.05, power = 0.80,
                   type = "two.sample", alternative = "two.sided")
##
##
        Two-sample t test power calculation
##
##
                 n = 393.4057
##
                 d = 0.2
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
```

Q1 Interpretation:

A 0.20 SD difference requires about 393 students per group (≈ 786 total) to achieve 80% power at a 5% significance level. Because 0.20 is not a large effect, you still need several hundred participants per group to have an 80% chance (power) of detecting it, if it's really there

QUESTION 2

```
res2 <- pwr.t.test(d = 0.10, sig.level = 0.05, power = 0.80,
                   type = "two.sample", alternative = "two.sided")
res2
##
##
        Two-sample t test power calculation
##
##
                 n = 1570.733
                 d = 0.1
##
##
         sig.level = 0.05
##
             power = 0.8
       alternative = two.sided
##
##
## NOTE: n is number in *each* group
```

Q2 Interpretation:

Halfing the effect to .10 SD requires roughly 1571 students per group (≈ 3142 total). This is more than double the sample (4x) for a .20 SD difference because sample size scales with $1/(effectsize)^2$. The power formula for a simple two-sample t-test indicates that required n scales with $\frac{1}{effect \, size^2}$. So if the effect size is cut from 0.20 to 0.10, that ratio is $\frac{(0.20)^2}{(0.10)^2} = 4$. Meaning detecting a smaller effect demands a much larger sample, to ensure that you do not miss the effect due to random variation.

QUESTION 3

```
m <- 250
icc <- 0.18
clusters <- 30
n arm <- clusters * m
deff \leftarrow 1 + (m - 1) * icc
n_eff <- n_arm / deff
res3_cluster <- pwr.t.test(n = n_eff, sig.level = 0.05, power = 0.80,
                            type = "two.sample", alternative = "two.sided")
res3_indiv <- pwr.t.test(n = n_arm, sig.level = 0.05, power = 0.80,
                          type = "two.sample", alternative = "two.sided")
res3_cluster
##
##
        Two-sample t test power calculation
##
##
                 n = 163.684
                 d = 0.3106035
##
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
res3_indiv
##
##
        Two-sample t test power calculation
##
##
                 n = 7500
                 d = 0.04572422
##
##
         sig.level = 0.05
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
Q3 Interpretation:
```

$$DE = 1 + (m-1) \times ICC = 1 + (250 - 1) \times 0.18 \approx 45.82$$

With 7500 total students per arm (30 schools \times 250 students), the real sample size is:

$$n_{effective} = \frac{7500}{45.82} \approx 164 \text{ per arm}$$

This means:

- With clusters: Can detect effects of 0.31 SD at 80% power
- Without clusters: Could detect 0.046 SD at 80% power

thus School-level grouping makes it harder to find small effects when ICC is high (0.18).

With school-level randomization (30 schools per arm, 250 students each, ICC=0.18), the design effect reduces the effective sample size to ~164 per arm, yielding a minimum detectable effect of ≈ 0.31 SD. In contrast, individual randomization with 7500 students per arm would detect effects as small as ≈ 0.046 SD.

Question 4

```
data$cltype1 <- factor(data$cltype1, labels = c("regular", "small", "regular_aide"))</pre>
reg_read <- lm(pread1g ~ relevel(cltype1, ref = "regular") + factor(schid1n), data = data)
reg_math <- lm(pmath1g ~ relevel(cltype1, ref = "regular") + factor(schid1n), data = data)
coeftest(reg_read, vcov = sandwich)
##
  t test of coefficients:
##
##
                                                    Estimate Std. Error t value
## (Intercept)
                                                   58.335059
                                                                3.050030 19.1261
## relevel(cltype1, ref = "regular")small
                                                   -8.134632
                                                                0.817770 -9.9473
## relevel(cltype1, ref = "regular")regular_aide
                                                   -5.339605
                                                                0.837262 - 6.3775
## factor(schid1n)2
                                                  -20.220565
                                                                4.590594 -4.4048
## factor(schid1n)3
                                                   15.927128
                                                                3.829518 4.1590
## factor(schid1n)4
                                                  -12.002421
                                                                4.140817 -2.8986
## factor(schid1n)5
                                                   -5.857713
                                                                4.500806 -1.3015
## factor(schid1n)7
                                                                4.005331 1.9829
                                                    7.942041
## factor(schid1n)8
                                                   -4.821768
                                                                3.953754 -1.2195
## factor(schid1n)9
                                                    8.168932
                                                                3.839410 2.1277
## factor(schid1n)10
                                                   19.948272
                                                                4.406084
                                                                         4.5274
## factor(schid1n)11
                                                    5.712365
                                                                4.327621
                                                                         1.3200
## factor(schid1n)12
                                                    4.017987
                                                                          0.7641
                                                                5.258743
## factor(schid1n)13
                                                    4.361731
                                                                4.639339 0.9402
## factor(schid1n)14
                                                  -11.890016
                                                                4.826185 -2.4636
## factor(schid1n)15
                                                  -17.494138
                                                                3.998315 -4.3754
## factor(schid1n)16
                                                  -24.702245
                                                                3.468949 -7.1210
## factor(schid1n)17
                                                  -19.146583
                                                                3.868696 -4.9491
## factor(schid1n)19
                                                  -27.783901
                                                                3.637101 -7.6390
## factor(schid1n)20
                                                                3.994937 0.2172
                                                    0.867676
## factor(schid1n)21
                                                  -10.505290
                                                                4.260738 -2.4656
## factor(schid1n)22
                                                  -19.140803
                                                                3.644574 -5.2519
## factor(schid1n)23
                                                                3.977428 0.3855
                                                    1.533138
## factor(schid1n)24
                                                   -3.037857
                                                                3.902908 -0.7784
## factor(schid1n)25
                                                  -12.806513
                                                                4.254885 -3.0098
## factor(schid1n)26
                                                  -23.983342
                                                                4.867585 -4.9272
## factor(schid1n)27
                                                  -17.488238
                                                                3.466375 -5.0451
## factor(schid1n)28
                                                  -26.411639
                                                                3.844793 -6.8695
## factor(schid1n)29
                                                                4.381403 -2.6990
                                                  -11.825595
## factor(schid1n)30
                                                  -34.542500
                                                                3.735363 -9.2474
                                                                3.829175 -7.6955
## factor(schid1n)31
                                                  -29.467380
## factor(schid1n)32
                                                  -23.650876
                                                                3.579285 -6.6077
                                                  -15.774661
                                                                3.579756 -4.4066
## factor(schid1n)33
## factor(schid1n)34
                                                    0.899684
                                                                4.131669 0.2178
## factor(schid1n)35
                                                    0.182716
                                                                4.592485 0.0398
## factor(schid1n)36
                                                   15.308256
                                                                3.767206 4.0636
## factor(schid1n)37
                                                    6.435528
                                                                3.747274 1.7174
## factor(schid1n)38
                                                  -16.833818
                                                                4.810999 -3.4990
## factor(schid1n)39
                                                    5.571355
                                                                4.936371
                                                                         1.1286
## factor(schid1n)40
                                                    6.348667
```

4.574088 1.3880

```
## factor(schid1n)41
                                                   22.081072
                                                                3.805993 5.8017
                                                   11.740830
## factor(schid1n)43
                                                                4.573710 2.5670
## factor(schid1n)44
                                                  -24.521558
                                                                3.828911 -6.4043
## factor(schid1n)45
                                                   -7.344571
                                                                4.613987 -1.5918
## factor(schid1n)46
                                                    -8.891334
                                                                4.097983 -2.1697
## factor(schid1n)47
                                                                4.482016 -2.2712
                                                  -10.179403
## factor(schid1n)48
                                                                4.114267 -2.6886
                                                  -11.061502
                                                                4.395954 -0.3671
## factor(schid1n)49
                                                   -1.613575
## factor(schid1n)50
                                                    -5.380313
                                                                4.278403 -1.2576
## factor(schid1n)51
                                                    0.023572
                                                                3.501574 0.0067
## factor(schid1n)52
                                                    0.612521
                                                                4.329775 0.1415
## factor(schid1n)53
                                                   -9.552150
                                                                4.294547 -2.2243
## factor(schid1n)54
                                                     2.108895
                                                                4.285761 0.4921
## factor(schid1n)55
                                                  -13.084009
                                                                4.222168 -3.0989
## factor(schid1n)56
                                                   -21.180345
                                                                3.896129 -5.4363
## factor(schid1n)57
                                                   -4.729673
                                                                4.135537 -1.1437
## factor(schid1n)58
                                                                3.750400 3.2228
                                                   12.086820
## factor(schid1n)59
                                                     9.405810
                                                                4.416507 2.1297
## factor(schid1n)60
                                                  -17.982013
                                                                4.717290 -3.8119
## factor(schid1n)61
                                                    14.069397
                                                                3.941900 3.5692
## factor(schid1n)62
                                                   -9.748619
                                                                4.327830 -2.2525
## factor(schid1n)63
                                                   13.451130
                                                                3.617799 3.7180
## factor(schid1n)64
                                                   10.718620
                                                                3.878751 2.7634
## factor(schid1n)65
                                                                4.077130
                                                                         4.1881
                                                   17.075467
## factor(schid1n)66
                                                    3.222854
                                                                4.100440 0.7860
## factor(schid1n)67
                                                   -3.840541
                                                                4.992227 -0.7693
## factor(schid1n)68
                                                   -1.531106
                                                                3.898353 -0.3928
## factor(schid1n)69
                                                                4.088313 5.5288
                                                   22.603445
## factor(schid1n)71
                                                                4.252211 -0.7873
                                                   -3.347735
## factor(schid1n)72
                                                   18.864523
                                                                3.872736 4.8711
## factor(schid1n)73
                                                   17.483214
                                                                4.453236
                                                                          3.9260
## factor(schid1n)74
                                                   17.737916
                                                                3.756031
                                                                          4.7225
## factor(schid1n)75
                                                    5.450844
                                                                4.094022
                                                                          1.3314
## factor(schid1n)77
                                                                3.838834 1.0918
                                                    4.191158
## factor(schid1n)78
                                                    -2.191122
                                                                4.572641 -0.4792
## factor(schid1n)79
                                                   -3.128870
                                                                4.394804 -0.7119
## factor(schid1n)80
                                                    2.893535
                                                                4.703076 0.6152
##
                                                   Pr(>|t|)
## (Intercept)
                                                   < 2.2e-16 ***
## relevel(cltype1, ref = "regular")small
                                                  < 2.2e-16 ***
## relevel(cltype1, ref = "regular")regular aide 1.928e-10 ***
## factor(schid1n)2
                                                   1.076e-05 ***
## factor(schid1n)3
                                                   3.238e-05 ***
## factor(schid1n)4
                                                  0.0037617 **
## factor(schid1n)5
                                                  0.1931413
## factor(schid1n)7
                                                  0.0474255 *
## factor(schid1n)8
                                                  0.2226842
## factor(schid1n)9
                                                  0.0334045 *
## factor(schid1n)10
                                                  6.080e-06 ***
## factor(schid1n)11
                                                  0.1868902
## factor(schid1n)12
                                                  0.4448609
## factor(schid1n)13
                                                  0.3471704
## factor(schid1n)14
                                                  0.0137796 *
## factor(schid1n)15
                                                  1.232e-05 ***
```

##	factor(schid1n)16	1.191e-12	***
##	factor(schid1n)17	7.649e-07	***
##	factor(schid1n)19	2.514e-14	***
##	factor(schid1n)20	0.8280642	
##	factor(schid1n)21	0.0137047	*
##	factor(schid1n)22	1.555e-07	***
##	factor(schid1n)23	0.6999099	
##	factor(schid1n)24	0.4363875	
##	factor(schid1n)25	0.0026242	**
##	factor(schid1n)26	8.556e-07	***
##	factor(schid1n)27	4.659e-07	***
##	factor(schid1n)28	7.061e-12	***
##	factor(schid1n)29	0.0069724	
##	factor(schid1n)30	< 2.2e-16	
##	factor(schid1n)31	1.625e-14	
	factor(schid1n)32	4.222e-11	***
	factor(schid1n)33	1.067e-05	***
##	factor(schid1n)34	0.8276285	
##	factor(schid1n)35	0.9682652	
	factor(schid1n)36	4.892e-05	***
	factor(schid1n)37	0.0859571	•
	factor(schid1n)38	0.0004702	***
	factor(schid1n)39	0.2590952	
	factor(schid1n)40	0.1651971	
	factor(schid1n)41	6.884e-09	
	factor(schid1n)43	0.0102803	*
	factor(schid1n)44	1.619e-10	***
	factor(schid1n)45	0.1114783	
	factor(schid1n)46	0.0300678	
	factor(schid1n)47	0.0231704	
	factor(schid1n)48	0.0071947	**
	factor(schid1n)49	0.7135872	
	factor(schid1n)50	0.2086004	
	factor(schid1n)51	0.9946290	
	factor(schid1n)52	0.8875053	
	factor(schid1n)53	0.0261668	*
	factor(schid1n)54	0.6226868	
	factor(schid1n)55	0.0019510	
	factor(schid1n)56	5.645e-08	***
	factor(schid1n)57	0.2528055	
	factor(schid1n)58	0.0012758	
	factor(schid1n)59	0.0332354	
	factor(schid1n)60	0.0001392	
	factor(schid1n)61	0.0003607	
	factor(schid1n)62	0.0243222	
	factor(schid1n)63	0.0002025	
	factor(schid1n)64	0.0057365	
	factor(schid1n)65	2.851e-05	***
	factor(schid1n)66	0.4319100	
	factor(schid1n)67	0.4417415	
	factor(schid1n)68	0.6945121	ato ato ato
	factor(schid1n)69	3.353e-08	**
	factor(schid1n)71	0.4311401	444
##	factor(schid1n)72	1.137e-06	ጥ ጥ ጥ

```
## factor(schid1n)73
                                                   8.730e-05 ***
## factor(schid1n)74
                                                   2.380e-06 ***
## factor(schid1n)75
                                                   0.1831004
## factor(schid1n)77
                                                   0.2749719
## factor(schid1n)78
                                                   0.6318266
## factor(schid1n)79
                                                   0.4765235
## factor(schid1n)80
                                                   0.5384163
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
coeftest(reg_math, vcov = sandwich)
##
## t test of coefficients:
##
##
                                                    Estimate Std. Error t value
## (Intercept)
                                                    62.10473
                                                                3.03319
                                                                          20,4751
## relevel(cltype1, ref = "regular")small
                                                    -8.63805
                                                                0.79660 -10.8436
## relevel(cltype1, ref = "regular")regular_aide
                                                    -7.23489
                                                                0.82724
                                                                          -8.7458
## factor(schid1n)2
                                                                3.81789
                                                                         -8.2555
                                                   -31.51848
## factor(schid1n)3
                                                    13.11406
                                                                3.72168
                                                                           3.5237
## factor(schid1n)4
                                                   -10.37477
                                                                4.24834
                                                                         -2.4421
## factor(schid1n)5
                                                   -16.53495
                                                                4.15102
                                                                         -3.9834
## factor(schid1n)7
                                                     9.21771
                                                                4.05102
                                                                          2.2754
## factor(schid1n)8
                                                    -7.99894
                                                                3.87825
                                                                         -2.0625
## factor(schid1n)9
                                                    8.40709
                                                                3.80201
                                                                           2.2112
## factor(schid1n)10
                                                    18.12294
                                                                4.48519
                                                                          4.0406
## factor(schid1n)11
                                                    7.63674
                                                                4.65140
                                                                           1.6418
## factor(schid1n)12
                                                    0.83916
                                                                4.84464
                                                                           0.1732
## factor(schid1n)13
                                                    11.21947
                                                                4.57389
                                                                           2.4529
## factor(schid1n)14
                                                                4.84720
                                                   -11.14748
                                                                         -2.2998
## factor(schid1n)15
                                                   -24.10684
                                                                4.25918
                                                                         -5.6600
## factor(schid1n)16
                                                   -24.33598
                                                                3.49641
                                                                         -6.9603
## factor(schid1n)17
                                                   -25.34625
                                                                3.79431
                                                                          -6.6801
## factor(schid1n)19
                                                   -31.70696
                                                                3.57437
                                                                         -8.8707
## factor(schid1n)20
                                                    -4.89094
                                                                3.98148
                                                                         -1.2284
## factor(schid1n)21
                                                   -24.86817
                                                                3.78888
                                                                         -6.5635
## factor(schid1n)22
                                                   -26.57986
                                                                3.62624
                                                                         -7.3299
## factor(schid1n)23
                                                     1.92113
                                                                4.00630
                                                                          0.4795
## factor(schid1n)24
                                                    -2.57297
                                                                3.75423
                                                                         -0.6854
## factor(schid1n)25
                                                   -23.34056
                                                                4.09834
                                                                         -5.6951
## factor(schid1n)26
                                                   -36.40181
                                                                4.21550
                                                                         -8.6352
## factor(schid1n)27
                                                   -11.77517
                                                                3.77990
                                                                         -3.1152
## factor(schid1n)28
                                                   -28.48382
                                                                3.75534
                                                                         -7.5849
## factor(schid1n)29
                                                     3.75932
                                                                4.55934
                                                                          0.8245
## factor(schid1n)30
                                                   -34.59581
                                                                3.64288
                                                                         -9.4968
## factor(schid1n)31
                                                   -17.16659
                                                                4.18056
                                                                         -4.1063
                                                   -28.34969
                                                                3.72521
                                                                         -7.6102
## factor(schid1n)32
## factor(schid1n)33
                                                   -19.62580
                                                                3.61012
                                                                          -5.4363
## factor(schid1n)34
                                                                4.02762
                                                                         -1.5675
                                                    -6.31330
## factor(schid1n)35
                                                                4.16915
                                                                         -3.6801
                                                   -15.34276
## factor(schid1n)36
                                                     2.36806
                                                                4.03461
                                                                          0.5869
## factor(schid1n)37
                                                    -2.33818
                                                                3.87643
                                                                          -0.6032
## factor(schid1n)38
                                                   -24.51701
                                                                4.63140
                                                                         -5.2937
## factor(schid1n)39
                                                    2.55253
                                                                4.66051
                                                                          0.5477
```

```
## factor(schid1n)40
                                                      0.26482
                                                                 4.47362
                                                                            0.0592
## factor(schid1n)41
                                                                            4.6723
                                                    16.75060
                                                                 3.58509
## factor(schid1n)43
                                                      3.71049
                                                                 4.89807
                                                                            0.7575
## factor(schid1n)44
                                                   -12.97570
                                                                 4.13847
                                                                           -3.1354
## factor(schid1n)45
                                                      1.34066
                                                                 4.75676
                                                                            0.2818
## factor(schid1n)46
                                                   -11.77777
                                                                 4.09510
                                                                          -2.8761
## factor(schid1n)47
                                                    -9.65056
                                                                 4.53675
                                                                           -2.1272
## factor(schid1n)48
                                                   -15.97939
                                                                 4.01614
                                                                          -3.9788
## factor(schid1n)49
                                                    -7.31914
                                                                 4.40438
                                                                           -1.6618
## factor(schid1n)50
                                                   -10.79815
                                                                 4.03385
                                                                          -2.6769
## factor(schid1n)51
                                                    -4.69678
                                                                 3.51498
                                                                          -1.3362
## factor(schid1n)52
                                                                            1.2530
                                                     5.42704
                                                                 4.33117
## factor(schid1n)53
                                                    -7.81937
                                                                 4.13153
                                                                          -1.8926
## factor(schid1n)54
                                                      0.86513
                                                                 4.29959
                                                                            0.2012
## factor(schid1n)55
                                                                 4.23426
                                                                           -2.3787
                                                   -10.07190
## factor(schid1n)56
                                                    -20.18183
                                                                 4.04095
                                                                           -4.9943
## factor(schid1n)57
                                                    -9.98441
                                                                 4.08438
                                                                           -2.4445
## factor(schid1n)58
                                                     5.34280
                                                                 3.68753
                                                                            1.4489
## factor(schid1n)59
                                                                 4.47771
                                                                            1.2741
                                                     5.70491
## factor(schid1n)60
                                                   -20.44948
                                                                 4.32664
                                                                           -4.7264
## factor(schid1n)61
                                                    10.50992
                                                                 4.08302
                                                                            2.5741
## factor(schid1n)62
                                                    -5.25015
                                                                 4.18775
                                                                          -1.2537
## factor(schid1n)63
                                                     6.96615
                                                                 3.66323
                                                                            1.9016
## factor(schid1n)64
                                                                            0.4483
                                                      1.68301
                                                                 3.75427
                                                     1.00536
## factor(schid1n)65
                                                                 4.18407
                                                                            0.2403
## factor(schid1n)66
                                                    -6.12297
                                                                 3.94557
                                                                          -1.5519
## factor(schid1n)67
                                                    -0.97307
                                                                 4.68911
                                                                          -0.2075
## factor(schid1n)68
                                                     5.63710
                                                                 3.70156
                                                                            1.5229
## factor(schid1n)69
                                                    10.72990
                                                                 4.33810
                                                                            2.4734
## factor(schid1n)70
                                                     2.14522
                                                                 3.78536
                                                                            0.5667
## factor(schid1n)71
                                                    -8.72322
                                                                 4.13986
                                                                           -2.1071
## factor(schid1n)72
                                                     18.57793
                                                                 3.71650
                                                                            4.9988
## factor(schid1n)73
                                                    17.11958
                                                                 4.11409
                                                                            4.1612
## factor(schid1n)74
                                                                            5.5467
                                                    21.16368
                                                                 3.81553
## factor(schid1n)75
                                                     -6.05790
                                                                 4.06812
                                                                           -1.4891
## factor(schid1n)77
                                                     9.83771
                                                                 3.63383
                                                                            2.7073
## factor(schid1n)78
                                                    -8.44206
                                                                 4.75528
                                                                          -1.7753
## factor(schid1n)79
                                                    -2.51768
                                                                 4.33873
                                                                          -0.5803
## factor(schid1n)80
                                                                 4.61563
                                                    -0.99489
                                                                          -0.2155
##
                                                    Pr(>|t|)
## (Intercept)
                                                    < 2.2e-16 ***
## relevel(cltype1, ref = "regular")small
                                                    < 2.2e-16 ***
## relevel(cltype1, ref = "regular")regular_aide < 2.2e-16 ***
## factor(schid1n)2
                                                    < 2.2e-16 ***
## factor(schid1n)3
                                                    0.0004285 ***
## factor(schid1n)4
                                                    0.0146293 *
## factor(schid1n)5
                                                    6.869e-05 ***
## factor(schid1n)7
                                                   0.0229140 *
## factor(schid1n)8
                                                   0.0391985 *
## factor(schid1n)9
                                                   0.0270548 *
                                                   5.392e-05 ***
## factor(schid1n)10
## factor(schid1n)11
                                                   0.1006770
## factor(schid1n)12
                                                   0.8624889
## factor(schid1n)13
                                                   0.0141954 *
```

##	factor(schid1n)14	0.0214924 *	
##	factor(schid1n)15	1.578e-08 ***	
##	factor(schid1n)16	3.727e-12 ***	
##	factor(schid1n)17	2.585e-11 ***	
##	factor(schid1n)19	< 2.2e-16 ***	
##	factor(schid1n)20	0.2193325	
##	factor(schid1n)21	5.661e-11 ***	
##	factor(schid1n)22	2.582e-13 ***	
##	factor(schid1n)23	0.6315796	
##	factor(schid1n)24	0.4931454	
##	factor(schid1n)25	1.287e-08 ***	
##	factor(schid1n)26	< 2.2e-16 ***	
##	factor(schid1n)27	0.0018461 **	
##	factor(schid1n)28	3.792e-14 ***	
##	factor(schid1n)29	0.4096682	
##	factor(schid1n)30	< 2.2e-16 ***	
	factor(schid1n)31	4.070e-05 ***	
	factor(schid1n)32	3.123e-14 ***	
	factor(schid1n)33	5.636e-08 ***	
	factor(schid1n)34	0.1170460	
	factor(schid1n)35	0.0002350 ***	
	factor(schid1n)36	0.5572659	
	factor(schid1n)37	0.5464111	
	factor(schid1n)38	1.238e-07 ***	
	factor(schid1n)39	0.5839212	
	factor(schid1n)40	0.9527972	
	factor(schid1n)41	3.038e-06 ***	
	factor(schid1n)43	0.4487526	
	factor(schid1n)44	0.0017239 **	
	factor(schid1n)45	0.7780720	
	factor(schid1n)46	0.0040397 **	
	factor(schid1n)47	0.0334412 *	
	factor(schid1n)48	7.002e-05 ***	
	factor(schid1n)49	0.0966041 .	
	factor(schid1n)50	0.0074496 **	
	factor(schid1n)51	0.1815251	
	factor(schid1n)52	0.2102432	
	factor(schid1n)53 factor(schid1n)54	0.0584540 .	
	factor(schid1n)55	0.8405392 0.0174039 *	
	factor(schid1n)56	6.057e-07 ***	
	factor(schid1n)57	0.0145301 *	
	factor(schid1n)58	0.1474178	
	factor(schid1n)59	0.2026848	
	factor(schid1n)60	2.333e-06 ***	
		0.0100734 *	
	factor(schid1n)62	0.2099980	
	factor(schid1n)63	0.2099980	
	factor(schid1n)64	0.6539567	
		0.8101181	
	factor(schid1n)66	0.1207447	
	factor(schid1n)67	0.8356128	
	factor(schid1n)68	0.1278322	
	factor(schid1n)69	0.0134084 *	
ıππ	140001 (00114111/00	0.0101001	

```
## factor(schid1n)70
                                                 0.5709275
## factor(schid1n)71
                                                 0.0351443 *
## factor(schid1n)72
                                                 5.920e-07 ***
## factor(schid1n)73
                                                 3.206e-05 ***
## factor(schid1n)74
                                                 3.025e-08 ***
## factor(schid1n)75
                                                 0.1365056
## factor(schid1n)77
                                                 0.0068019 **
## factor(schid1n)78
                                                 0.0758948 .
## factor(schid1n)79
                                                 0.5617459
## factor(schid1n)80
                                                 0.8293474
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Q4 Interprtation:

The (estimated) coefficients on the treatment indicators are:

Reading Percentile Score

Small classroom: -8.13 (Estimate = -8.13, Robust SE ≈ 0.82) Regular with aide: -5.34 (Estimate = -5.34, Robust SE ≈ 0.84) Math Percentile Score

Small classroom: -8.64 (Estimate = -8.64, Robust SE ≈ 0.80) Regular with aide: -7.23 (Estimate = -7.23, Robust SE ≈ 0.83)

- The measured difference in reading and math percentiles is lower (by about 8–9 points) for small classes compared to the "regular" category.
- STAR experiment found a positive advantage for small classes, so these negative signs might reflect how the dataset is coded or labeled.

Question 5:

The treatment effects estimated in question 4 are intent-to-treat (ITT) effects.

We used the randomly assigned class type (small vs. regular vs. regular+aide) as the explanatory, regardless of any noncompliance that might have happened Thus, we are measuring the average effect of being assigned to each type, not necessarily the effect of actually attending with that assignment.

Question 6

In Table V the reduced form ITT estimates for 1st grade are consistently smaller in magnitude than the OLS estimates that use actual placement.

If we used a regression on "actual class size" (instead of "assigned class size"), we might see a larger effect, because students who remain in small classes could be higher-achieving. That leads to positive selection into the small-class group. Thus we might be measuring all students including non compliers. It probably overstates the effect since the switches aren't random

Question 7:

For AA students only, regress math scores on "teacher is African American." For white students only, regress math scores on teacher is white."

Question 7a

```
data$trace1 <- as.factor(data$trace1)</pre>
data$same race <- ifelse((data$white == 1 & data$trace1 == "White") |</pre>
                           (data$black == 1 & data$trace1 == "African American"), 1, 0)
```

Question 7b

```
reg_aa <- lm(pmath1g ~ I(trace1 == "African American") + factor(schid1n), data = data, subset = (black =
reg_white <- lm(pmath1g ~ I(trace1 == "White") + factor(schid1n), data = data, subset = (white == 1))
coeftest(reg_aa, vcov = sandwich)
## t test of coefficients:
##
##
                      Estimate Std. Error t value Pr(>|t|)
                     30.500000
                                  5.810820 5.2488 1.686e-07 ***
## (Intercept)
## factor(schid1n)2
                                  6.691217 -1.2858 0.1986621
                     -8.603448
                                11.719400 1.9057 0.0568304 .
## factor(schid1n)3
                     22.333333
## factor(schid1n)4
                     17.500000
                                 5.810820 3.0116 0.0026298 **
                                  6.571720 -1.9401 0.0524987
## factor(schid1n)5 -12.750000
                                  8.259527 2.0323 0.0422516 *
## factor(schid1n)7
                      16.785714
## factor(schid1n)9
                     31.500000
                                14.582202 2.1602 0.0308735 *
                                12.674956 2.8797 0.0040213 **
## factor(schid1n)10
                     36.500000
## factor(schid1n)11
                     -3.576923
                                 9.553126 -0.3744 0.7081268
## factor(schid1n)13
                      9.500000
                                15.289396 0.6213 0.5344403
## factor(schid1n)14
                     15.055556
                                 7.115433 2.1159 0.0344717 *
## factor(schid1n)15
                       1.372727
                                  6.478831 0.2119 0.8322223
                                  6.148710 0.2131 0.8312629
## factor(schid1n)16
                      1.310345
## factor(schid1n)17 -11.148649
                                  6.357362 -1.7537 0.0796361
## factor(schid1n)19
                                  6.185210 -0.9742 0.3300871
                     -6.025424
## factor(schid1n)20
                     21.400000
                                 6.415757 3.3355 0.0008663 ***
## factor(schid1n)21
                     -8.527778
                                 6.419205 -1.3285 0.1841656
## factor(schid1n)22
                     -0.085366
                                 6.202991 -0.0138 0.9890211
## factor(schid1n)23
                                 6.465844 4.1468 3.507e-05 ***
                     26.812500
## factor(schid1n)24
                     22.198630
                                  6.339941 3.5014 0.0004726 ***
## factor(schid1n)25
                      4.439394
                                 7.349259 0.6041 0.5458696
## factor(schid1n)26
                     -8.966667
                                 6.511096 -1.3771 0.1686182
                                 6.266903 2.1134 0.0346846 *
## factor(schid1n)27
                     13.244526
## factor(schid1n)28
                     -3.420354
                                 6.286037 -0.5441 0.5864177
## factor(schid1n)29
                     29.400000
                                 6.823645 4.3085 1.720e-05 ***
## factor(schid1n)30
                     -8.715385
                                  6.169801 -1.4126 0.1579266
                                  6.580806 1.1706 0.2418999
## factor(schid1n)31
                      7.703390
## factor(schid1n)32
                     -2.606557
                                  6.232394 -0.4182 0.6758241
## factor(schid1n)33
                      6.074074
                                  6.188751 0.9815 0.3264751
                                 22.677425 0.9922 0.3212270
## factor(schid1n)34
                     22.500000
## factor(schid1n)35
                     -4.666667
                                  7.761006 -0.6013 0.5477079
## factor(schid1n)37
                                 7.288186 1.4813 0.1386668
                     10.796296
## factor(schid1n)41
                                  5.810820 0.4302 0.6670715
                      2.500000
## factor(schid1n)44 14.209677
                                  6.612782 2.1488 0.0317637 *
## factor(schid1n)45
                     27.084615
                                  6.734308 4.0219 5.979e-05 ***
## factor(schid1n)46
                      4.333333
                                 11.043344 0.3924 0.6948079
                                 12.718712 -0.6683 0.5040120
## factor(schid1n)48 -8.500000
                                12.511557 0.2598 0.7950747
## factor(schid1n)49
                      3.250000
```

```
## factor(schid1n)50 -0.100000
                                  8.246795 -0.0121 0.9903263
## factor(schid1n)51
                       7.664835
                                  6.475518 1.1837 0.2366814
## factor(schid1n)52
                       7.020000
                                  8.241724
                                            0.8518 0.3944433
                                  7.189034
                                            2.0247 0.0430268 *
## factor(schid1n)53
                      14.555556
## factor(schid1n)54
                      18.750000
                                  8.357958
                                            2.2434 0.0249777
## factor(schid1n)55
                      -4.500000
                                 10.197443 -0.4413 0.6590510
## factor(schid1n)56
                      -6.472973
                                  6.796000 -0.9525 0.3409703
## factor(schid1n)57
                       9.166667
                                  9.420568
                                           0.9730 0.3306425
## factor(schid1n)58
                       9.333333
                                  9.196007
                                            1.0149 0.3102556
## factor(schid1n)59
                       8.785714
                                 12.096503
                                            0.7263 0.4677353
## factor(schid1n)60
                       1.928571
                                  8.381503
                                            0.2301 0.8180378
## factor(schid1n)61
                      13.500000
                                  6.581883
                                            2.0511 0.0403836
## factor(schid1n)63
                      14.147059
                                  9.299356
                                            1.5213 0.1283379
                                            3.2397 0.0012153 **
## factor(schid1n)64
                      22.100000
                                  6.821556
## factor(schid1n)65
                      18.000000
                                 17.603711
                                            1.0225 0.3066576
## factor(schid1n)66 -24.500000
                                  5.810820 -4.2163 2.590e-05 ***
## factor(schid1n)68
                                  6.914001
                                            2.6551 0.0079897 **
                      18.357143
                                  5.810820
                                            0.0860 0.9314378
## factor(schid1n)70
                       0.500000
## factor(schid1n)72
                      34.750000
                                 13.050383
                                            2.6628 0.0078100 **
## factor(schid1n)73
                       0.833333
                                  6.399282
                                            0.1302 0.8964026
## factor(schid1n)74
                      26.428571
                                  8.899952 2.9695 0.0030168 **
## factor(schid1n)79
                      -8.500000
                                  5.810820 -1.4628 0.1436763
                                  7.835512 -1.5102 0.1311396
## factor(schid1n)80 -11.833333
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
coeftest(reg_white, vcov = sandwich)
##
## t test of coefficients:
##
##
                                  Std. Error t value Pr(>|t|)
                        Estimate
                                   3.2032843 18.8296 < 2.2e-16 ***
## (Intercept)
                      60.3164557
                                   4.6849735 -7.2068 6.729e-13 ***
## factor(schid1n)2
                     -33.7638241
## factor(schid1n)3
                                   3.9307830 2.6082 0.0091341 **
                      10.2521718
## factor(schid1n)4
                     -13.2584847
                                   4.6037831 -2.8799 0.0039975 **
                     -17.0477990
                                   4.3996934 -3.8748 0.0001083 ***
## factor(schid1n)5
## factor(schid1n)7
                       8.6731276
                                   4.3364202 2.0001 0.0455558 *
## factor(schid1n)8
                     -11.8273253
                                   4.1563880 -2.8456 0.0044540 **
## factor(schid1n)9
                       4.9254798
                                   3.9876756
                                             1.2352 0.2168325
## factor(schid1n)10
                     13.8687295
                                   4.7948057
                                              2.8924 0.0038417 **
## factor(schid1n)11
                      10.2147943
                                   4.5347270
                                              2.2526 0.0243363 *
## factor(schid1n)12
                      -3.2664557
                                   4.9134328 -0.6648 0.5062133
## factor(schid1n)13
                       8.4286423
                                   4.6567957
                                             1.8100 0.0703707 .
## factor(schid1n)17 -21.4686296
                                   4.5236343 -4.7459 2.143e-06 ***
                                   4.6757462 -4.4494 8.828e-06 ***
## factor(schid1n)21 -20.8042606
## factor(schid1n)23
                                   9.4461082 0.9949 0.3198461
                       9.3978300
## factor(schid1n)24 11.6835443
                                  11.0797577
                                             1.0545 0.2917157
## factor(schid1n)25 -27.4116938
                                   4.8649608 -5.6345 1.867e-08 ***
## factor(schid1n)28 -17.3164557
                                   3.2032843 -5.4058 6.799e-08 ***
                                   4.1601715 -2.6293 0.0085861 **
## factor(schid1n)34 -10.9384069
## factor(schid1n)35 -15.8395326
                                   4.5406010 -3.4884 0.0004907 ***
## factor(schid1n)36 -2.9460853
                                   4.2003169 -0.7014 0.4830938
```

4.3643356 -0.3939 0.6937111

4.7844799 -5.9514 2.870e-09 ***

factor(schid1n)37 -1.7188947

factor(schid1n)38 -28.4743504

```
## factor(schid1n)39
                      -0.4341028
                                    4.8386613 -0.0897 0.9285175
## factor(schid1n)40
                      -2.8164557
                                    4.5881956 -0.6138 0.5393480
## factor(schid1n)41
                                               3.7119 0.0002083 ***
                      14.2240848
                                    3.8319754
## factor(schid1n)43
                      -0.7891830
                                    5.1013311 -0.1547 0.8770640
## factor(schid1n)44 -24.8549172
                                    8.6460118 -2.8747 0.0040636 **
## factor(schid1n)46 -14.3323287
                                    4.3121762 -3.3237 0.0008958 ***
## factor(schid1n)47 -12.5307414
                                    4.7941894 -2.6137 0.0089870 **
## factor(schid1n)48 -19.8958949
                                    4.2684056 -4.6612 3.239e-06 ***
  factor(schid1n)49
                      -9.3164557
                                    4.6098840 -2.0210 0.0433442 *
## factor(schid1n)50 -12.4683544
                                    4.2915923 -2.9053 0.0036877 **
## factor(schid1n)51
                       0.8011914
                                    3.9083364
                                               0.2050 0.8375853
## factor(schid1n)52
                      10.5790667
                                    4.6051496
                                               2.2972 0.0216536
  factor(schid1n)53
                      -8.8164557
                                    4.8127778 -1.8319 0.0670375
                      -0.0039557
                                    4.6257107 -0.0009 0.9993177
## factor(schid1n)54
## factor(schid1n)55 -12.1236846
                                    4.4464386 -2.7266 0.0064248 **
## factor(schid1n)56 -18.8748973
                                    4.7219649 -3.9973 6.515e-05 ***
## factor(schid1n)57 -12.1639133
                                    4.2856318 -2.8383 0.0045567 **
## factor(schid1n)58
                       3.0070737
                                    3.9242893
                                               0.7663 0.4435563
## factor(schid1n)59
                       4.8898935
                                    4.6976712
                                               1.0409 0.2979717
## factor(schid1n)60 -24.1800921
                                    4.7808662 -5.0577 4.420e-07
## factor(schid1n)61
                       6.9518370
                                    4.2476726
                                               1.6366 0.1017824
## factor(schid1n)62
                      -9.3010711
                                    4.3653243 -2.1307 0.0331727 *
## factor(schid1n)63
                       6.1512862
                                    3.8727858
                                               1.5883 0.1122837
## factor(schid1n)64
                      -2.2419876
                                    4.1151508 -0.5448 0.5859103
## factor(schid1n)65
                      -3.0452693
                                    4.4907357 -0.6781 0.4977304
## factor(schid1n)66 -10.7438061
                                    4.1447957 -2.5921 0.0095709
## factor(schid1n)67
                      -6.2794187
                                    4.8218286 -1.3023 0.1928869
## factor(schid1n)68
                       7.2062716
                                    3.9690072
                                               1.8156 0.0694957
## factor(schid1n)69
                       6.4335443
                                    4.6138366
                                               1.3944 0.1632680
## factor(schid1n)70
                      -2.2212176
                                    4.0735351 -0.5453 0.5855891
## factor(schid1n)71 -13.2294992
                                    4.3209313 -3.0617 0.0022142 **
## factor(schid1n)72
                      14.9286423
                                    3.9532620
                                               3.7763 0.0001613 ***
## factor(schid1n)73
                      14.2267542
                                    4.2787124
                                               3.3250 0.0008916 ***
## factor(schid1n)74
                      20.8932217
                                    3.8554013
                                               5.4192 6.313e-08 ***
## factor(schid1n)75
                      -9.3480346
                                    4.2533442
                                              -2.1978 0.0280158
## factor(schid1n)77
                       5.6746947
                                    3.8470655
                                               1.4751 0.1402665
## factor(schid1n)78
                     -12.7587634
                                    4.9835770 -2.5602 0.0104961 *
## factor(schid1n)79
                      -4.7622388
                                    4.4313892 -1.0747 0.2825869
## factor(schid1n)80
                      -3.4771700
                                    4.8427486 -0.7180 0.4727865
##
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

But is this relationship causal? we see corrlation but, that does NOT imply causation:)

• Teacher race was NOT randomized – may be some underlying factor which influences both

Question 7c

The estimated coefficients for African American students (from reg_aa) and for White students (from reg_white) showthe association between having a teacher of the same race and 1st grade math scores, controling for school fixed effects. BUT! these estimates should be interpreted with caution as causal effects. Even though school fixed effects account for between school variation teacher assignment to students is not randomized within schools so unobserved student or classroom-level factors may **confound** the relationship. So while this might be helpful to push for more research, the estimates represent correlations rather than causal effects of student-teacher race match.