

Day 1:

$$X \sim \text{Binom}(0.02, 20)$$

$$E[X] = np = 0.02(20) = 0.4$$

$$P(X=0) = \binom{20}{0} (0.02)^0 (0.98)^{20} = 0.6676$$

$$P(X=1) = \binom{20}{1} (0.02)^1 (0.98)^{19} = 0.2725$$

$$P(X=2) = \binom{20}{2} (0.02)^2 (0.98)^{18} = 0.0528$$

$$P(X=3) = \binom{20}{3} (0.02)^3 (0.98)^{17} = 0.0065$$

$$P(X=4) = \binom{20}{4} (0.02)^4 (0.98)^{16} = 0.0006$$

$$E[\text{Day 2}] = 0(0.4457)$$

$$+ 1(0.1819 + 0.1856)$$

$$+ 2(0.0352 + 0.0720 + 0.0367)$$

$$+ 3(0.0043 + 0.0132 + 0.0135 + 0.0046)$$

$$+ 4(0.0004 + 0.0015 + 0.0023 + 0.0016 + 0.0001)$$

$$+ 5(0.0001 + 0.0003)$$

$$= 0.7889$$

Day 2:

Conditional Probabilities:

$$P(X_2=0 | X_1=0) = 0.6676$$

$$P(X_2=0 \cap X_1=0) = 0.6676^2 = 0.4457 \quad X=0$$

$$P(X_2=1 | X_1=0) = 0.2725$$

$$P(X_2=1 \cap X_1=0) = 0.2725(0.6676) = 0.1819 \quad X=1$$

$$P(X_2=2 \cap X_1=0) = (0.0528)(0.6676) = 0.0352 \quad X=2$$

$$P(X_2=3 \cap X_1=0) = (0.0065)(0.6676) = 0.0043 \quad X=3$$

$$P(X_2=4 \cap X_1=0) = (0.0006)(0.6676) = 0.0004 \quad X=4$$

$$P(X_2=0 | X_1=1) = \binom{19}{0} (0.02)^0 (0.98)^{19} = 0.6812 \quad X=1$$

$$P(X_2=0 \cap X_1=1) = 0.6812(0.2725) = 0.1856$$

$$P(X_2=1 | X_1=1) = \binom{19}{1} (0.02)^1 (0.98)^{18} = 0.2642 \quad X=2$$

$$P(X_2=1 \cap X_1=1) = 0.2642(0.2725) = 0.0720$$

$$P(X_2=2 | X_1=1) = \binom{19}{2} (0.02)^2 (0.98)^{17} = 0.0485 \quad X=3$$

$$P(X_2=2 \cap X_1=1) = 0.0485(0.2725) = 0.0132$$

$$P(X_2=3 | X_1=1) = \binom{19}{3} (0.02)^3 (0.98)^{16} = 0.0056 \quad X=4$$

$$P(X_2=3 \cap X_1=1) = 0.0056(0.2725) = 0.0015$$

$$P(X_2=4 | X_1=1) = \binom{19}{4} (0.02)^4 (0.98)^{15} = 0.0005 \quad X=5$$

$$P(X_2=4 \cap X_1=1) = 0.0005(0.2725) = 0.0001$$

$$P(X_2=0 | X_1=2) = \binom{18}{0} (0.02)^0 (0.98)^{18} = 0.6951$$

$$P(X_2=0 \cap X_1=2) = 0.6951(0.0528) = 0.0367 \quad X=2$$

$$P(X_2=1 | X_1=2) = \binom{18}{1} (0.02)^1 (0.98)^{17} = 0.2554 \quad X=3$$

$$P(X_2=1 \cap X_1=2) = 0.2554(0.0528) = 0.0135$$

$$P(X_2=2 | X_1=2) = \binom{18}{2} (0.02)^2 (0.98)^{16} = 0.0443 \quad X=4$$

$$P(X_2=2 \cap X_1=2) = 0.0443(0.0528) = 0.0023$$

$$P(X_2=3 | X_1=2) = \binom{18}{3} (0.02)^3 (0.98)^{15} = 0.0048 \quad X=5$$

$$P(X_2=3 \cap X_1=2) = 0.0048(0.0528) = 0.0003$$

$$P(X_3=0 | X_1=3) = \binom{17}{0} (0.02)^0 (0.98)^{17} = 0.7093 \quad X=3$$

$$P(X_3=0 \cap X_1=3) = 0.7093(0.0065) = 0.0046$$

$$P(X_3=1 | X_1=3) = \binom{17}{1} (0.02)^1 (0.98)^{16} = 0.2461 \quad X=4$$

$$P(X_3=1 \cap X_1=3) = 0.2461(0.0065) = 0.0016$$

$$P(X_3=2 | X_1=3) = \binom{17}{2} (0.02)^2 (0.98)^{15} = 0.0402 \quad X=5$$

$$P(X_3=2 \cap X_1=3) = 0.0402(0.0065) = 0.0003$$

$$P(X_2=0 | X_1=4) = \binom{16}{0} (0.02)^0 (0.98)^{16} = 0.7238$$

$$P(X_2=0 \cap X_1=4) = 0.7238(0.0006) = 0.0004$$

$X=4$