Definition 0.1 ([?]). A nonassociative algebra is an algebra

$$A = \langle A; ; +, \cdot, -, \check{}, 1', 0, 1 \rangle$$

with type (2, 2, 2, 1, 1, 0, 0, 0) such that:

- $\langle A; +, \cdot, -, 0, 1 \rangle$ is a Boolean algebra,
- x = x; 1' = 1'; x for all $x \in A$. That is, 1' is an identity element,
- $(x;y) \cdot z = 0$ if and only if $(x^{\circ};z) \cdot y = 0$ for all $x,y,z \in A$,
- $(y; x) \cdot z = 0$ if and only if $(z; x) \cdot y = 0$ for all $x, y, z \in A$.

A nonassociative algebra is a relation algebra if, for all $x, y, z \in A$,

$$x;(y;z) = (x;y);z.$$

Definition 0.2 ([?]). Let X be a set. A proper relation algebra with base set X is an algebra \mathcal{A} with nonempty domain $A \subseteq \wp(X \times X)$ and signature $\{\circ, \cup, \cap, \subseteq, ^{-1}, \setminus, \operatorname{id}_X, \mathsf{U}\}$ such that the following hold:

- A together with the operations in $\{\cup, \cap, \setminus, \emptyset, \mathsf{U}\}$ form a field of sets. That is, if $R, S \in A$ then $R \cup S, R \cap S, \mathsf{U} \setminus S \in A$. It follows that $\emptyset, \mathsf{U} \in A$. Also, U is the biggest binary relation in A, and so $\mathsf{U} = \cup A$,
- $id_X := \{(x, x) : x \in X\} \in A$, the identity relation over X,
- \mathcal{A} is closed under taking converses: $R \in A$ implies $R^{-1} \in A$, where $R^{-1} = \{(y, x) : (x, y) \in R\}$,

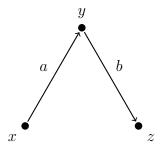
¹A more accurate term would be not-necessarily-associative algebra.

• A is closed under composition of binary relations: $R, S \in A$ implies $R \circ S \in A$ where

$$R \circ S = \{(x, y) : (\exists z)(x, z) \in R \text{ and } (z, y) \in S\}.$$

Definition 0.3. A relation algebra \mathcal{A} over a domain A is representable if there exists a proper relation algebra \mathcal{B} over a set X such that \mathcal{A} is isomorphic to \mathcal{B} . The isomorphism $h: A \to \wp(X \times X)$ is called a representation.

We can break the representation of composition down into two major components: com-position moves and $witness moves^2$. Whenever we see a situation as in Figure ?? in a representation we must see it completed to Figure ??. This makes sense intuitively, since if we can relate x to y via a, and y to z via b, then we should be able to relate x to z via a; b directly.

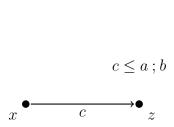


 $a \downarrow b$ a; b

Figure 1: Composition move

Figure 2: Composition response

If $c \le a$; b, then whenever we can relate x to z by c we should also be able to relate them by a; b through some third point y. This is a witness move, shown in Figures ?? and ??.



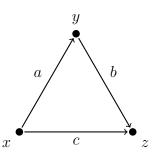


Figure 3: Witness move

Figure 4: Witness response

Hirsch, Jackson and Kowalski [?] introduce a new concept of a *qualitative representation*. Once again, we demand that there are no inconsistent triangles. Unlike a relation algebra representation, we do not require that every consistent triangle appears wherever it can. We

²The language of composition and witness moves is borrowed from [?], and will be explored in greater detail in Chapter ??.

simply demand that every consistent triangle appears at least *once* in the representation. That is, a qualitative representation is between a weak and a relation algebra representation.

Just as for weak representations, nonassociative algebras are the ideal abstract setting for qualitative representations. The main reason to prefer qualitative representations to weak representations is that a weak representation need not be isomorphic to the underlying nonassociative algebra. Indeed, different nonassociative algebras can have the same weak representation, and Hirsch et al. give examples.

As is the case for relation algebras and relation algebra representations, there does not exist a finite set of elementary axioms that characterise qualitative representability of nonassociative algebras.

The first clear definition of qualitative representations is given by Hirsch et al. [?]. We will define all of these concepts properly, but intuitively, a qualitative representation is stronger than a weak representation but weaker than a relation algebra representation. In a relation algebra representation, every composition must be seen wherever it can be seen; that is, composition must be represented through both composition moves and witness moves. In a weak representation, we require only composition moves. In a qualitative representation, we require composition moves, and that every composition appear at least *once* in the representation. That is, if $c \leq a$; b, then in a qualitative representation we should see a triangle representing this composition *somewhere*. However, we do not need to witness a; b above every c.

We survey the qualitative representability of all nonassociative algebras on 4 atoms. For each algebra we provide a possible atom table showing composition. Atoms are represented by 1' if atomic, or e_1, e_2, \ldots, e_n otherwise. We also note whether or not the algebra is a relation algebra; if so, we give the number used by Maddux [?], if applicable. If the algebra is qualitatively representable, we give an example of a representation. The representation is on the smallest number of vertices, but it is not necessarily the only representation up to isomorphism with that property.

If the representation is on too many points to draw in any useful manner, it is represented by a matrix with entries from the atoms of the algebra. To interpret these representations, we interpret the rows and columns of the matrix as vertices of a representation, such that the uv-th entry of the matrix is the relation from u to v.

1 Atoms: two fragment identity and two symmetric

			_ ;	aton	n table	R	A	Q	RNA
#1	e_1	e_2	\overline{a}	b					
e_1	e_1	0	a	b					not simple:
e_2	0	e_2	0	0			n	Ο.	not simple:
a	a	0	e_1	0					$#2_{\leq 3} \times #22_{\leq 3}$
b	b	0	0	e_1					
			_						

			aton	ı table	RA	. C	RNA
#2	e_1	e_2	a b				
e_1	e_1	0	0 b				
$ e_2 $	0	e_2	a = 0			yes	not simple:
$\mid a \mid$	0	a	$e_2 0$				$\#4_{\leq 3} \times \#4_{\leq 3}$
b	b	0	$0 e_1$				
#3	e_1	e_2	a b				
e_1	e_1	0	a b				
e_2	0	e_2	a 0			no	no
a	a	a	1' 0				
b	b	0	$0 e_1$				
	I		7				
#4	e_1	e_2	$\begin{array}{c c} a & b \\ \hline \end{array}$				
e_1	e_1	0	$\begin{bmatrix} a & b \\ 1 \end{bmatrix}$				
e_2	0	e_2	$\begin{bmatrix} a & b \\ 1/ & 0 \end{bmatrix}$			no	no
	$\begin{vmatrix} a \\ b \end{vmatrix}$	a	$\begin{bmatrix} 1' & 0 \\ 0 & 1' \end{bmatrix}$				
b	b	b	0 1'				
#5	e_1	e_2	\overline{a}	b			
e_1	e_1	0	\overline{a}	\overline{b}			1
$ e_2 $	0	e_2	0	0		no	not simple:
$\mid a \mid$	a	0	$e_1 + a$	0			$\#2_{\leq 3} \times \#23_{\leq 3}$
b	b	0	0	e_1			
#6	e_1	e_2	a	b			
e_1	e_1	0	0	b			not simple:
e_2	0	e_2	a	0		yes	$\#4_{\leq 3} \times \#5_{\leq 3}$
$\mid a \mid$	0	a	$e_2 + a$	0			11 70 11 - 70
b	b	0	0	e_1			
<i>#7</i>	0	0	a b	7			
#7	e_1	$\frac{e_2}{0}$	$\begin{array}{c c} a & b \\ \hline a & b \end{array}$	-			
$\begin{array}{ c c } e_1 \\ e_2 \end{array}$	$\begin{array}{c c} e_1 \\ 0 \end{array}$	e_2	$\begin{bmatrix} a & b \\ a & 0 \end{bmatrix}$			no	no
$\begin{vmatrix} c_2 \\ a \end{vmatrix}$	$\begin{vmatrix} a \end{vmatrix}$	$\frac{c_2}{a}$	-b 0			110	
$\begin{vmatrix} a \\ b \end{vmatrix}$	$\begin{vmatrix} a \\ b \end{vmatrix}$	0	$0 e_1$				
			<u> </u>	_			

atom table	RA QRNA	
$ #8 e_1 e_2 a b$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$	no no	
$\begin{vmatrix} a & a & 0 & e_1 + a & 0 \end{vmatrix}$		
$\begin{vmatrix} b & b & b & 0 & 1' \end{vmatrix}$		
$\begin{array}{ c cccccccccccccccccccccccccccccccccc$		
e_1 e_1 0 a b		
$\mid e_2 \mid 0 \mid e_2 \mid a \mid b \mid$	no no	
$\begin{vmatrix} a & a & a & -b & 0 \end{vmatrix}$		
$\begin{vmatrix} b & b & b & 0 & 1' \end{vmatrix}$		
$ #10 e_1 e_2 a b$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	not simple:	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$yes \qquad #2_{\leq 3} \times #12_{\leq}$. 9
$\begin{vmatrix} a & a & 0 & e_1 + b & a \end{vmatrix}$	// - <u>></u> 3 // // <u>></u>	:J
$\begin{bmatrix} b & b & 0 & a & e_1 \end{bmatrix}$		
$\begin{bmatrix} #11 & e_1 & e_2 & a & b \end{bmatrix}$		
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
$\left \begin{array}{c cccc} e_1 & e_1 & e_2 & e_2 & a & 0 \end{array}\right $	no no	
$\begin{bmatrix} a & 0 & a & e_2 + b & a \end{bmatrix}$		
$\left \begin{array}{c cccccccccccccccccccccccccccccccccc$		
3 3 3 31		
$\begin{bmatrix} #12 & e_1 & e_2 & a & b \end{bmatrix}$	e_2	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	75	
$\left \begin{array}{c cccc} e_1 & e_1 & 0 & a & 0 \\ e_2 & 0 & e_2 & a & 0 \end{array}\right $	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	
$\begin{bmatrix} c_2 & 0 & c_2 & a & 0 \\ a & a & a & -a & a \end{bmatrix}$		
$\left \begin{array}{c cccccccccccccccccccccccccccccccccc$	e_1 b)
	$e_1 \cup e_2 \cup e_3 \cup e_4 \cup e_4 \cup e_5 \cup e_6 $	$/e_1$
$\boxed{#13 \mid e_1 e_2 a b}$		
e_1 e_1 0 a b		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	no no	
$\begin{vmatrix} a & a & 0 & e_1 + b & a \end{vmatrix}$		
$\begin{bmatrix} b & b & b & a & 1' \end{bmatrix}$		

no

no

no

#14	e_1	e_2	\overline{a}	b
e_1	e_1	0	a	b
e_2	0	e_2	a	b
a	$\mid a \mid$	a	-a	a
b	b	b	a	1'

α		α	-a	a	
b	b	b	a	1'	
					_
#15	e_1	e_2	a	b	
e_1	$\begin{bmatrix} e_1 \\ 0 \end{bmatrix}$	0	a	b	
e_2	0	e_2	0	0	

#16	e_1	e_2	a	b
e_1	e_1	0	0	b
e_2	0	e_2	a	0
a	0	a	$-e_1$	a
b	b	0	a	e_1

0

a

b = 0

a

b

 $-e_2$

a

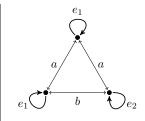
a

 e_1

#17	e_1	e_2	\overline{a}	b
e_1	e_1	0	a	b
e_2	0	e_2	a	0
a	$\mid a \mid$	a	1	a
b	b	0	a	e_1

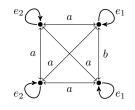
#18	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	b
a	a	0	$-e_2$	a
b	b	b	a	1'

#19	e_1	e_2	\overline{a}	b
e_1	e_1	0	\overline{a}	b
e_2	0	e_2	a	b
a	$\mid a \mid$	a	1	a
b	b	b	a	1'

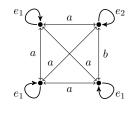


yes	not simple: $\#2_{\leq 3} \times \#14_{\leq 3}$
-----	---

no	no



no no



atom table	RA	QRNA

yes

#20	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	0
a	a	0	$e_1 + a$	b
b	b	0	b	$e_1 + a$

not simple: $\#2_{\leq 3} \times \#13_{\leq 3}$

#21	e_1	e_2	a	b
e_1	e_1	0	0	b
e_2	0	e_2	a	0
a	0	a	$e_2 + a$	b
b	b	0	b	$e_1 + a$

no no

#22	e_1	e_2	\overline{a}	b
e_1	e_1	0	a	b
e_2	0	e_2	a	0
a	$\mid a \mid$	a	-b	b
b	b	0	b	$e_1 + a$

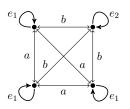
no no

#23	e_1	e_2	a	b
e_1	e_1	0	\overline{a}	b
e_2	0	e_2	0	b
a	a	0	$e_1 + a$	b
b	b	b	b	-b

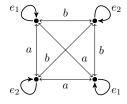


no

yes



#24	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	a	b
a	a	a	-b	b
b	b	b	b	-b



#25	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	0
a	a	0	$e_1 + b$	a+b
b	b	0	a + b	$e_1 + a$

 $\begin{array}{l} \text{not simple:} \\ \#2_{\leq 3} \times \#16_{\leq 3} \end{array}$

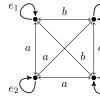
atom table	RA	ORNA
atom table	$1 \iota \Lambda$	QIUIA

#26	e_1	e_2	a	b
e_1	e_1	0	0	b
e_2	0	e_2	a	0
a	0	a	$e_2 + b$	a+b
b	b	0	a + b	$e_1 + a$

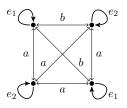
no	

n	\cap

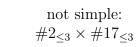
#27	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	a	0
a	a	a	-a	a+b
b	b	0	a+b	$e_1 + a$



#28	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	a	b
a	a	a	-a	a+b
b	b	b	a+b	-b



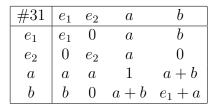
#29	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	0
a	a	0	$-e_2$	a+b
b	b	0	a+b	$e_1 + a$

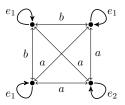


#30	e_1	e_2	a	b
e_1	e_1	0	0	b
e_2	0	e_2	a	0
a	0	a	$-e_1$	a+b
b	b	0	a+b	$e_1 + a$

no

yes





			atom table	RA	QRNA
#32	e_1	$\overline{e_2}$	a b		
e_1	e_1	0	a b		
e_2	0	e_2	$0 \qquad b$	no	no
a	a	0	$-e_2$ $a+b$		
b	b	b	a+b $-b$		
#33	e_1	e_2	a b		$e_1 \longrightarrow a \longrightarrow e_2$
e_1	e_1	0	a b		
e_2	0	e_2	a b	no	$a \mid a \mid a$
a	a	a	1 $a+b$		
b	b	b	a+b $-b$		e_2 b e_1
#34	e_1	e_2	a b		
e_1	e_1	0	$\begin{array}{cccc} a & b \\ \vdots & \vdots & \vdots \end{array}$		not simple:
e_2	0	e_2	0 0	no	$#2_{\leq 3} \times #24_{\leq 3}$
a	a	0	$e_1 + a \qquad 0$		11 70 11 70
b	b	0	$0 \qquad e_1 + b$		
#35	0	0.	a b		
	e_1	$\frac{e_2}{0}$	$\begin{array}{c c} a & b \\ \hline 0 & b \end{array}$		
$\begin{array}{ c c } e_1 \\ e_2 \end{array}$	$\begin{vmatrix} e_1 \\ 0 \end{vmatrix}$	e_2	$\begin{bmatrix} 0 & 0 \\ a & 0 \end{bmatrix}$	yes	not simple:
$\begin{vmatrix} c_2 \\ a \end{vmatrix}$	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	a	$e_2 + a \qquad 0$	yes	$\#5_{\leq 3} \times \#5_{\leq 3}$
$\begin{vmatrix} a \\ b \end{vmatrix}$	$\begin{vmatrix} b \end{vmatrix}$	0	$\begin{vmatrix} 0 & e_1 + b \end{vmatrix}$		
			- 11 , 1		
#36	e_1	e_2	a b		
e_1	e_1	0	a b		
e_2	0	e_2	a = 0	no	no
a	a	a	-b 0		
b	b	0	$0 e_1 + b$		
#37	e_1	e_2	$\begin{array}{c c} a & b \\ \hline \end{array}$		
e_1	e_1	0	$\begin{bmatrix} a & b \end{bmatrix}$		
e_2	0	e_2	$\begin{bmatrix} a & b \\ 1 & 0 \end{bmatrix}$	no	no
a	$\begin{vmatrix} a \\ 1 \end{vmatrix}$	a	-b 0		
b	b	b	0 - a		

atom table	RA	ORNA
atom table	$1 \iota \Lambda$	WILLIA

yes

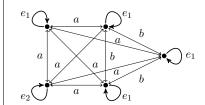
#38	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	0
a	a	0	$-e_2$	a
b	b	0	a	$e_1 + b$

not	si	mple:
$\#2_{\leq 3}$	X	$\#15_{\leq 3}$

#39	e_1	e_2	\overline{a}	b
e_1	e_1	0	0	b
e_2	0	e_2	a	0
a	0	a	$-e_1$	a
b	b	0	a	$e_1 + b$

no	no

#40	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	a	0
a	a	a	1	a
b	b	0	a	$e_1 + b$



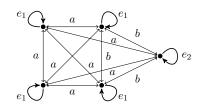
#41	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	b
a	$\mid a \mid$	0	$-e_2$	a
b	b	b	a	-a

no	
----	--

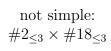
no

yes

#42	e_1	e_2	\overline{a}	b
e_1	e_1	0	a	b
e_2	0	e_2	a	b
a	a	a	1	a
b	b	b	a	-a



#43	e_1	e_2	a	b
e_1	e_1	0	a	b
e_2	0	e_2	0	0
a	a	0	$-e_2$	a+b
b	b	0	a + b	$-e_2$



			_8	atom ta	ble	RA	QRNA
$ \begin{array}{ c c c } \hline #44 \\ \hline e_1 \end{array} $	e_1	e_2	0 0	$\frac{b}{b}$			
$egin{bmatrix} e_2 \\ a \\ b \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ b \end{bmatrix}$	$egin{array}{c} e_2 \\ a \\ 0 \end{array}$	$a \\ -e_1 \\ a+b$	$0 \\ a+b \\ -e_2$		no	no
$ \begin{array}{c c} #45 \\ e_1 \\ e_2 \\ a \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_2 \\ 0 \\ e_2 \\ a \end{array} $	a a a 1	$\begin{array}{c} b \\ b \\ 0 \\ a+b \end{array}$		no	e_1 b e_1 a b b e_2
$ \begin{array}{c c} b \\ \hline & 46 \\ e_1 \\ e_2 \\ a \\ b \end{array} $	$\begin{array}{c c} b \\ \hline e_1 \\ e_1 \\ 0 \\ a \\ b \end{array}$	$ \begin{array}{c} e_2 \\ 0 \\ e_2 \\ a \\ b \end{array} $	$ \begin{array}{c} a + b \\ \hline a \\ a \\ a \\ 1 \\ a + b \end{array} $	$ \begin{array}{c c} -e_2 \\ \hline b \\ b \\ a+b \\ 1 \end{array} $		no	e_1 e_1 e_1 e_1 e_1 e_2 e_1 e_2 e_1 e_2

2 Atoms: two fragment identity and one nonsymmetric

				atom table	RA	QRNA
$ #47 \epsilon$	e_1	e_2	r	r°		
e_1 e_1	e_1	0	r	r		not simple:
e_2	0	e_2	0	0	no	# $2_{<3} \times #21_{<3}$
			0	e_1		$\#^{2} \leq 3 \land \#^{2} 1 \leq 3$
r	r $$	0	e_1	0		
#48 6	e_1	e_2	r	r		
	e_1	0	0	r°		$r \sim$
e_2	0	e_2	r	0	yes	$e_2 \longrightarrow \bullet \longrightarrow e_1$
	r	0	0	e_2		
r	0	r	e_1	0		

				atom	table	RA	QRNA	
#49	e_1	$\overline{e_2}$	r	r°				-
e_1	e_1	0	r	r°				
e_2	0	e_2	r	0		no		no
r	r	0	0	1'				
r	$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle \vee}$	e_1	0				
#50	e_1	e_2	r	$r^{\scriptscriptstyle \smile}$				
e_1	e_1	0	r	$r^{\scriptscriptstyle \smile}$				
e_2	0	e_2	r	$r^{\scriptscriptstyle \smile}$		no		no
r	r	r	0	1'				
r	r	$r^{\scriptscriptstyle{\smallsmile}}$	1'	0				
#51	e_1	e_2	r	r				
e_1	e_1	0	r	r $$			1	not simple:
e_2	0	e_2	0	0		yes		$2_{\leq 3} \times \#10_{\leq 3}$
r	r	0	r	$-e_2$			// ·	
r	r	0	$-e_2$	r				
// 50	l _				ا ۱			
#52	e_1	e_2	r	r°				
e_1	e_1	0	0	r°		TO 0		7 0.0
e_2	0	e_2	r	0		no		no
$\begin{vmatrix} r \\ r \end{aligned}$	$\begin{bmatrix} r \\ 0 \end{bmatrix}$	r°	r	$-e_1$ r				
<i>T</i>	U	T	$-e_2$	2 T	J			
								e_1
#53	e_1	e_2	r	r $^{\circ}$				\bigcirc
e_1	e_1	0	r	r $^{\circ}$				•
e_2	0	e_2	r	0		no		r
r	r	0	r	1			.	
$r^{\scriptscriptstyle \smallsmile}$	r	r	$-e_2$	$r^{\scriptscriptstyle \smile}$			e_2	$r \qquad \bigcirc e_1$
#54	e_1	$\overline{e_2}$	r	r				$\stackrel{e_1}{\bigcirc}$
e_1		$\frac{0}{2}$		r				,
e_2	0	e_2		r°		no		r
r	r	r		1		-		
r^{\smile}	$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle{\smile}}$		r^{\smile}			e_2	$r \longrightarrow e_2$
	L							J -

		atom table	RA	QRNA
$ \begin{array}{c c} #55 \\ e_1 \\ e_2 \\ r \\ r \\ \end{array} $	$\begin{array}{ccc} e_1 & e_2 \\ e_1 & 0 \\ 0 & e_2 \\ r & 0 \\ r & 0 \end{array}$	r r	yes	not simple: $\#2_{\leq 3} \times \#9_{\leq 3}$
$ \begin{array}{c c} #56 \\ e_1 \\ e_2 \\ r \\ r \\ \end{array} $	$egin{array}{cccc} e_1 & e_2 \\ e_1 & 0 \\ 0 & e_2 \\ r & 0 \\ 0 & r \end{array}$	$egin{array}{c c} 0 & r\ \hline r & 0\ \hline r\ & e_2 \end{array}$	no	no
$ \begin{array}{c} #57 \\ e_1 \\ e_2 \\ r \\ r \\ \end{array} $	$egin{array}{cccc} e_1 & e_2 \\ e_1 & 0 \\ 0 & e_2 \\ r & 0 \\ r\cdot & r\cdot \end{array}$	$\left[egin{array}{ccc} r & r\ r & 0\ r\ 1' \end{array} ight]$	no	no
$ \begin{array}{c} \#58 \\ e_1 \\ e_2 \\ r \\ r \\ r \\ \end{array} $	$egin{array}{cccccccccccccccccccccccccccccccccccc$	$\left[egin{array}{ccc} r & r\ r & r\ r & 1' \end{array} ight]$	no	e_1 r r e_2
$ \begin{array}{c c} #59 \\ \hline e_1 \\ e_2 \\ r \\ r \\ r \\ \end{array} $	$\begin{array}{ccc} e_1 & e_2 \\ e_1 & 0 \\ 0 & e_2 \\ r & 0 \\ r & 0 \end{array}$	$\left(\begin{array}{ccc} r & r \\ 0 & 0 \\ r+r & -e_2 \end{array}\right)$	yes	not simple: $\#2_{\leq 3} \times \#11_{\leq 3}$
$ \begin{array}{c c} #60 \\ \hline e_1 \\ e_2 \\ r \\ r \\ \end{array} $	$\begin{array}{c cccc} e_1 & e_2 \\ e_1 & 0 \\ 0 & e_2 \\ r & 0 \\ 0 & r \end{array}$	$ \begin{array}{ccc} 0 & r \\ r & 0 \\ r + r & -e_1 \end{array} $	no	no

			ato	om table	RA	QRNA
$ \begin{array}{c c} \#61 \\ e_1 \\ e_2 \\ r \\ r \\ \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ r \\ r \\ \end{array}$	$\begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ r \\ \end{array}$	r r r $r+r$ $-e_2$	$ \begin{array}{c c} r \\ \hline 0 \\ 1 \\ r+r \\ \end{array} $	no	$\begin{array}{c c} e_1 & r & e_1 \\ \hline r & r & r \\ \hline e_2 & r & e_1 \end{array}$
$ \begin{array}{c c} #62 \\ e_1 \\ e_2 \\ r \\ r \\ r \\ \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ r \\ r\check{} \end{array}$	$\begin{array}{c} e_2 \\ 0 \\ e_2 \\ r \\ r \\ \end{array}$	$r \\ r \\ r \\ r + r $	$ \begin{array}{c c} r \\ r \\ r \\ 1 \\ r + r \\ \end{array} $	no	e_1 r e_2 r

3 Atoms: three fragment identity

			a	tom table	RA	QRNA
$ \begin{array}{c c} #63 \\ \hline e_1 \\ e_2 \end{array} $	$egin{array}{c} e_1 \\ e_1 \\ 0 \end{array}$	e_2 0 e_2	$e_3 \\ 0 \\ 0$	$\begin{bmatrix} a \\ a \\ 0 \end{bmatrix}$	yes	not simple:
e_3 a	$\begin{bmatrix} 0 \\ a \end{bmatrix}$	0 0	e_3 0	$\begin{bmatrix} 0 \\ e_1 \end{bmatrix}$		$#2_{\leq 3} \times #2_{\leq 3} \times #4_{\leq 3}$
$ \begin{array}{c c} #64 \\ e_1 \\ e_2 \\ e_3 \\ a \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ a \end{array} $	e_3 0 0 e_3 0	$ \begin{array}{c} a \\ a \\ a \\ 0 \\ e_1 + e_2 \end{array} $	no	not simple: $\#2_{\leq 3} \times \#19_{\leq 3}$
$ \begin{array}{c} \#65 \\ e_1 \\ e_2 \\ e_3 \\ a \end{array} $	$\begin{array}{c} e_1 \\ e_1 \\ 0 \\ 0 \\ a \end{array}$	$\begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_3 \\ 0 \\ 0 \\ e_3 \\ a \end{array} $	a a a a 1'	no	no

			a	tom tabl	e	RA	QRNA
$ \begin{array}{c} #66 \\ e_1 \\ e_2 \\ e_3 \\ a \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ 0 \end{array} $	e_3 0 0 e_3 0	$ \begin{array}{c} a \\ 0 \\ 0 \\ e_1 + a \end{array} $		yes	not simple: $\#2_{\leq 3} \times \#2_{\leq 3} \times \#5_{\leq 3}$
$ \begin{array}{c} #67 \\ e_1 \\ e_2 \\ e_3 \\ a \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ a \end{array} $	$ \begin{array}{c} e_3 \\ 0 \\ 0 \\ e_3 \\ 0 \end{array} $	$ \begin{array}{c} a \\ a \\ a \\ 0 \\ -e_3 \end{array} $		no	not simple: $\#2_{\leq 3} \times \#20_{\leq 3}$
$ \begin{array}{c} \#68 \\ e_1 \\ e_2 \\ e_3 \\ a \end{array} $	$\begin{array}{c c} e_1 \\ e_1 \\ 0 \\ 0 \\ a \end{array}$	$\begin{array}{c} e_2 \\ 0 \\ e_2 \\ 0 \\ a \end{array}$	$ \begin{array}{c} e_3 \\ 0 \\ 0 \\ e_3 \\ a \end{array} $	$egin{array}{c} a \\ a \\ a \\ a \\ 1 \end{array}$		no	e_1 a a e_2 a a e_3

4 Atoms: four fragment identity

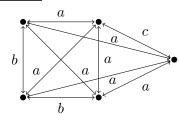
			_	aton	n table	RA	QRNA		
#69	e_1	e_2	e_3	e_4					
e_1	e_1	0	0	0			not s	simple:	
e_2	0	e_2	0	0	yes	44.9		-	v #9
e_3	0	0	e_3	0		#4	$_3 \times \#2_{\leq 3}$	× #4≤3	× #2≤3
e_4	0	0	0	e_4					

5 Atoms: atomic identity and three symmetric

	atom table	e RA	QRNA
#70 1' a	b c		
1' $1'$ a	b c		
$a \mid a \mid 1'$	0 0	no	no
$\begin{vmatrix} b & b & 0 \end{vmatrix}$	1' 0		
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	0 1'		
· · · · · · · · · · · · · · · · · · ·	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
	$\begin{bmatrix} a & b & c \end{bmatrix}$		
	$\begin{bmatrix} +a & 0 & 0 \\ 0 & 1/ & 0 \end{bmatrix}$	no	no
	$\begin{bmatrix} 0 & 1' & 0 \\ 0 & 1' \end{bmatrix}$		
c c	0 0 1'		
#72 1'	a b c		
<u> </u>	$egin{array}{cccc} a & b & c \ a & b & c \ \end{array}$		
	$\begin{bmatrix} a & b & c \\ +b & a & 0 \end{bmatrix}$	no	no
	$\begin{bmatrix} 1 & 0 & a & 0 \\ a & 1' & 0 \end{bmatrix}$	110	
	$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1' \end{bmatrix}$		
	<u> </u>		
$\boxed{\#73 \mid 1' a}$	b c		
1' $1'$ a	b c		
$\begin{vmatrix} a & a & -a \end{vmatrix}$	c a 0	no	no
$\begin{vmatrix} b & b & a \end{vmatrix}$			
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	0 1'		
#74 1' a	b c		$\stackrel{\bullet}{\longrightarrow} \stackrel{a}{\longrightarrow}$
1' $1'$ a	b c		
$\begin{vmatrix} a & a & -a \end{vmatrix}$		no	$\begin{vmatrix} a & c \\ c & b \end{vmatrix} a$
$\begin{vmatrix} b & b & a \end{vmatrix}$			
c c a	0 1'		$a \xrightarrow{\bullet \overset{\sim}{\iota}} a$
#75 1'a	b c		
1' $1'$ a	b c		
$\begin{vmatrix} a & a & 1 \end{vmatrix}$	$\begin{bmatrix} a & a \end{bmatrix}$	no	
$\begin{vmatrix} b & b & a \end{vmatrix}$	1' 0		
c c a	0 1'		$a \longrightarrow a$

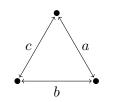
atom table	RA	QRNA
$\boxed{\#76 \mid 1' a b c \mid}$		
1' $1'$ a b c		
$\begin{vmatrix} a & a & 1'+a & b & 0 \end{vmatrix}$	no	no
$\begin{vmatrix} b & b & b & 1'+a & 0 \end{vmatrix}$		
$egin{array}{ c c c c c c c c c c c c c c c c c c c$		
$\lceil \#77 \mid 1' a b c \rceil$		
"		
	no	no
$\begin{bmatrix} a & a & 1'+b & a+b & 0 \\ b & a+b & 1'+a & 0 \end{bmatrix}$	no	no
$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$		
#78 1' a b c		
1' $1'$ a b c		
$\begin{vmatrix} a & a & -c & a+b & 0 \end{vmatrix}$	no	no
$\begin{vmatrix} b & b & a+b & 1'+a & 0 \end{vmatrix}$		
$\begin{bmatrix} c & c & 0 & 0 & 1' \end{bmatrix}$		
#79 1' a b c		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
$\begin{bmatrix} a & a & 1'+c & b & a \\ 1 & 1 & 1'+c & 0 \end{bmatrix}$	no	no
$\begin{vmatrix} b & b & b & 1'+a & 0 \\ 0 & 1' & 0 & 1' \end{vmatrix}$		
$\begin{bmatrix} c & c & a & 0 & 1' \end{bmatrix}$		
$\boxed{\#80 \mid 1' a b c}$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
$\begin{bmatrix} a & a & b & a \end{bmatrix}$	no	no
$\begin{bmatrix} b & b & b & 1'+a & 0 \end{bmatrix}$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
#81 1' a b c		
$\begin{array}{ c c c c c }\hline 1' & 1' & a & b & c \\\hline \end{array}$		
$\begin{bmatrix} a & a & -a & a+b & a \end{bmatrix}$	no	no
$\begin{vmatrix} b & b & a+b & 1'+a & 0 \end{vmatrix}$		
$\begin{vmatrix} c & c & a & 0 & 1' \end{vmatrix}$		

#82	1'	\overline{a}	b	c
1'	1'	a	b	c
a	$\mid a \mid$	1	a + b	a
b	b	a+b	1' + a	0
c	c	a	0	1'



#83	1'	a	b	c
1'	1'	a	b	c
a	a	1'	c	b
b	b	c	1'	a
c	c	b	a	1′

yes	
25_{65}	
RRA	



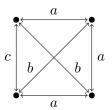
#84	1'	\overline{a}	b	c
1'	1'	a	b	c
a	$\mid a \mid$	1' + a	c	b
b	b	c	1'	a
c	c	b	a	1'

no

n	0	

#85	1'	a	b	c
1'	1'	a	b	c
a	a	1' + b	a + c	b
b	b	a + c	1'	a
c	c	b	a	1'

no



#86	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	-c	a+c	b
b	b	a + c	1'	a
c	c	b	a	1'

no

no

#87	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a+c	a+b
b	b	a + c	1'	a
c	c	a+b	a	1'

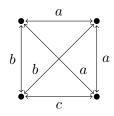
no

#88	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a+c	a+b
b	b	a+c	1'	a
c	c	a+b	a	1'

a	
	a

#89	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1' + a	b+c	b
b	b	b+c	1' + a	a
c	c	b	a	1'



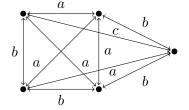


#90	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1' + b	0'	b
b	b	0'	1' + a	a
c	c	b	a	1'

no

	#91	1'	a	b	c
	1'	1'	a	b	c
	a	a	-c	0'	b
İ	b	b	0'	1' + a	a
	c	c	b	a	1'

no



#92	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b+c	a+b
b	b	1' + c $b + c$	1' + a	a
c	c	a + b	a	1'

no

#93	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-b	b+c	a+b
b	b	b+c	1' + a	a
c	c	a+b	a	1'

no

no

no

#94	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-a	0'	a+b
b	b	0'	1' + a	a
c	c	a+b	a	1'

	a
a	
•	Þ

#95	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	0'	a+b
b	b	0'	1' + a	a
c	c	a+b	a	1'

#96			b	c
1'	1'		b	c
a		1'	b	c
b	b	b	1' + a	0
c	c	c	0	1' + a

no

#97	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	b	c
b	b	b	1' + a	0
c	c	c	0	1' + a

no		
----	--	--

#98	1'	a	b	c
1'	1'	a	b	c
a	a	1' + b	a+b	c
b	b	a + b	1' + a	0
c	c	c	0	1' + a

no	no
----	----

#99	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+b	c
b	b	a+b	1' + a	0
c	c	c	0	1' + a

no no

atom table	RA	QRNA
------------	----	------

#100	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a+b	a+c
b	b	a+b	1' + a	0
c	c	a + c	0	1' + a

#101	1'	a	b	c
1'	1'	a	b	c
a	a	1	a + b	a + c
b	b	a+b	1' + a	0
c	c	a+c	0	1' + a

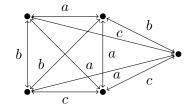
\[1'	a	a		a	a
a	1'	a	a	c	a
a	a	1'		a	a
b	a	b		a	a
a	c	a	a	1'	c
	a	a	a	c	1'

#102	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	1'	b+c	b+c
b	b	b+c	1' + a	a
$oxed{c}$	c	b+c	a	1' + a

no	c
	¥\(\nu\)

#103	1'	a	b	c
1'	1'	a	b	c
a	$\mid a \mid$	1' + a	b+c	b+c
b	b	1' + a $b + c$	1' + a	a
c	c		a	1' + a

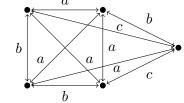
yes
28_{65}
RRA



#104	1'	a	b	c
1'	1'	a	b	c
a	$\mid a \mid$	1' + b	0'	b+c
b	b	0'	1' + a	a
c	c	b+c	a	1' + a

no	

#105	1'	a	b	c
1'	1'	a	b	c
a	a	-c	0'	b+c
b	b	0'	1' + a	a
c	c	b+c	a	1' + a



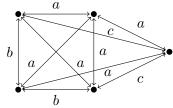
no

	#106	1'	a	b	c
ĺ	1'	1'	a	b	c
	a	a	-a	0'	0'
	b	b	0'	1' + a	a
	c	c	0 ′	a	1' + a

$a \longrightarrow a$	
	> •
a	

#107	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	0'	0'
b	b	0'	1' + a	a
c	c	0'	a	1' + a





#108	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	0	0
b	b	0	1' + b	0
c	c	0	0	1'

no	

#109	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a	0
b	b	a	1' + b	0
c	c	0	0	1'

no

#110	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	1' + c	0	a
b	b	0	1' + b	0
c	c	a	0	1'

no

#111	1'	a	b	c
1'	1'	a	b	c
a	a	-b	0	a
b	b	0	1' + b	0
c	c	a	0	1'

no

no

#112	1'	\overline{a}	b	c
1'	1'	a	b	c
a	$\mid a \mid$	-a	a	a
b	b	a	1' + b	0
c	c	a	0	1'

1′	a	b	c	
a	-a	a	a	
b	a	1' + b	0	
c	a	0	1′	

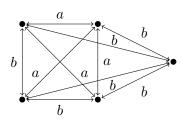
$a \longrightarrow \bullet_{\kappa}$	
b a	
	•
b	

#113	1'	a	b	c
1'	1'	a	b	c
a	a	1	a	a
b	b	a	1' + b	0
c	c	a	0	1'

1'	a	a	b	a	b
a	1'	a	a	c	a
a	a	1'	a	a	a
$\begin{bmatrix} 1' \\ a \\ b \\ a \end{bmatrix}$	a	a	1'	a	b
a	c	a	a	1'	a
b	a	a	b	a	1'

#114	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+b	0
b	b	a+b	-c	0
c	c	0	0	1'





#115	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b	a
b	b	b	-c	0
c	c	a	0	1'

no		no
----	--	----

#116	1'	a	b	c
1'	1'	a	b	c
a	$\mid a \mid$	-b	b	a
b	b	b	-c	0
c	c	a	0	1'

no	no

#117	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	a+b	a
b	b	a+b	-c	0
c	c	a	0	1'

no	no

			at	tom table	RA	QI	RNA					
#118	1'	\overline{a}	<i>b</i>	c			1'	a	a	b	a	b
1'	1'	$\frac{a}{a}$	$\frac{b}{b}$	$\frac{c}{c}$				1'	a	a	c	a
a	a	1	a+b	$\begin{bmatrix} a \\ a \end{bmatrix}$	no			a		b	a	b
b	b	a + b	-c	0				a		1'	<i>a</i>	b
c	c	a	0	1'			$\begin{vmatrix} a \\ b \end{vmatrix}$	$c \\ a$	$a \\ b$		$\frac{1'}{a}$	$\begin{bmatrix} a \\ 1' \end{bmatrix}$
<i>#</i> 110	1'		b				L '					
#119	1'	$\frac{a}{a}$	$\frac{b}{b}$	$\frac{c}{c}$								
$\begin{vmatrix} 1 \\ a \end{vmatrix}$	$\begin{vmatrix} 1 \\ a \end{vmatrix}$	1' + a	c	$\begin{bmatrix} c \\ b \end{bmatrix}$	no				n	0		
b	$\begin{vmatrix} a \\ b \end{vmatrix}$	c	1'+b		110				11	.0		
c	c	$\overset{\circ}{b}$	a	1'								
#120	1'	a	b	c								
1'	1'	a	b	c								
a			a+c	$b \mid$	no				n	Ο.		
b			1' + b	a								
c	c	<u>b</u>	\overline{a}	1'								
#121	1'	\overline{a}	b	c								
1'	1'	$\frac{a}{a}$	$\frac{b}{b}$	$\frac{c}{c}$								
a	$\begin{vmatrix} a \end{vmatrix}$	1'+c	$\stackrel{\circ}{c}$		no				n	О.		
b	b		1' + b	a								
c	c	a + b	a	1'								
#122	1'	a	<u>b</u>	c								
1'	1'	a	b	c								
a	$\begin{vmatrix} a \\ b \end{vmatrix}$	-b	C	a+b	no				n	Ο.		
<i>b</i>	b	c	1' + b	$\begin{bmatrix} a \\ 1' \end{bmatrix}$								
c	c	a+b	a	1								
#123	1'	\overline{a}	b	c								
1'		\overline{a}	b	c								
a			a + c	a+b	no				n	О.		
b		a+c		a								
c	c	a+b	a	1'								

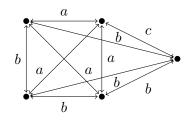
#124	1'	a	b	c
1'	1'	a	b	c
a	a	1	a + c	a+b
b	b	a+c	1' + b	a
c	c	a+b	a	1'

a
c

#125	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-c	0 ′	b
b	b	0'	-c	a
c	c	b	a	1'

yes
27
27_{65}
RRA

no



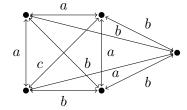
#126	1'	\overline{a}	b	c
1'	1'	a	b	c
a	$\mid a \mid$	1' + c	b+c	a+b
b	b	b+c	-c	a
c	c	a + b	a	1'

no

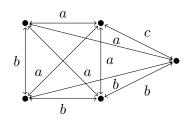
#127	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-b	b+c	a+b
b	b	b+c	-c	a
c	c	a+b	a	1'

no

#128	1'	a	b	c
1'	1'	a	b	c
a	$\mid a \mid$	-a	0 ′	a+b
b	b	0'	-c	a
c	c	a+b	a	1'



#129	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	0'	a+b
b	b	0'	-c	a
c	c	a+b	a	1'



			at	om table	RA	QRNA		
#130	1'	\overline{a}	<u></u>	c			-	
1'	1'	\overline{a}	b	\overline{c}				
a	$\mid a \mid$	1' + a	0	c	no		no	С
b	b	0	1' + b	0				
c	c	c	0	1' + a				
#131	1'	a	b	c				
1'	1'	a	b	c				
a	$\mid a \mid$	1' + b	a	c	no		no	C
b	b	a	1' + b	0				
c	c	c	0	1' + a				
// 100	1/		7					
#132	1'	a	<u>b</u>	c				
1'	1'	a	b	c	1 0.0		70.7	_
$\begin{vmatrix} a \\ b \end{vmatrix}$	$\begin{vmatrix} a \\ b \end{vmatrix}$	-c a 1		$\begin{bmatrix} c \\ 0 \end{bmatrix}$	no		no	J
$\begin{vmatrix} b \\ c \end{vmatrix}$	$\begin{vmatrix} v \\ c \end{vmatrix}$		0 1					
C		C	0 1	+a				
#133	1'	\overline{a}	b	c				
1'	1'	\overline{a}	b	c				
a	a	1' + c	0	a+c	no		no	С
b	b	0	1' + b	0				
c	c	a+c	0	1'+a				
#134	1'	a	<u>b</u>	c				
1'	1'	a	b	c				
a	$\begin{vmatrix} a \\ 1 \end{vmatrix}$	-b	0		no		no	Э
b	b		1' + b 0	0				
c	c	a+c	U	1 + a				
#135	1'	\overline{a}	b	c				
1'	1'	\overline{a}	b	c				
a	$\mid a \mid$	-a	a	a+c	no		no	С
b	b	a	1' + b	0				
c	c	a+c	0	1' + a				

		atom table	RA QI	RNA
#136	1'	a b c		
1'	1'	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
a	a	$\begin{bmatrix} 1 & a & a+c \end{bmatrix}$	no	$\begin{bmatrix} b & a & 1' & a & a & b \end{bmatrix}$
b	b	a 1'+b 0		$\begin{bmatrix} a & c & a & 1' & c & a \end{bmatrix}$
c	c	a+c 0 $1'+a$		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
#137	1'	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
1'	1′	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
a	a	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	no	no
b	b	b - c 0		
c	c	c 0 1' + a		
#138	1'	a b c		
1'	1'	a b c		
a	a	1' + a b c	no	no
b	b	b -c 0		
c	c	c 0 1' + a		
#139	1'	a b c		
1'	1'	a b c		
a	a	1' + b a + b c	no	no
b	b	a+b $-c$ 0		
c	c	c 0 1' + a		
// 1.40	11	7		
#140	1′	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
1'	1'	a b c		
	$\begin{vmatrix} a \\ b \end{vmatrix}$	-c $a+b$ c	no	no
b	b	a+b $-c$ 0		
c	c	$c \qquad 0 \qquad 1'+a$		
#141	1'	a b c		
1'	1'	a b c		
a	a	1' + c b $a + c$	no	no
b	b	b - c = 0		
c	c	a+c 0 $1'+a$		

			a	tom table	RA	QF	RNA
#142	1'	\overline{a}	b	c			
1'	1'	\overline{a}	b	\overline{c}			
a	a	-b	b = a	a+c	no		no
b	b	b	-c	0			
c	c	a+c	0 1	'+a			
#143	1'	a	b	c			
1'	1'	a	b	c			
a	$\mid a \mid$	-a	a+b	a+c	no		no
b	b		-c				
c	c	a+c	0	1' + a			
#144	1'	\overline{a}	b	c			$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	\overline{a}	\overline{b}	\overline{c}			$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
a		1			no		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b		-c				a a 1' b a a b b a b 1' a a b a c a a 1' c a a a a a c 1' a
c		a+c					
				·			
#145	1'	\overline{a}	b	c			
1'	1'	\overline{a}	b	c			
a	a	1' + a	c	b+c	no		no
b	b	c	1' + b	a			
c	c	b+c	a	1' + a			
#146	1'	a	b	c			
1'	1'	a	b	c			
a	$\mid a \mid$		a+c		no		no
b	b	a+c		l			
c	c	b+c	a	1' + a			
#147	1'	\overline{a}	b	c			$a \longrightarrow a$
1'	1'	\overline{a}	b	c			b c
a	a	-c	a + c	b+c	no		
b	b	a + c	1' + b	a			
c	c	b+c	a	1' + a			$a \xrightarrow{b} c$
	-						a

atom table	R.A	ORNA
atom table	1011	$ $ $\alpha_{1}\alpha_{1}\alpha_{1}$

#148	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	c	0'
b	b	c	1' + b	a
c	c	0'	a	1' + a

no		no
	1	

#149	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-b	c	0'
b	b	c	1' + b	a
c	c	0'	a	1' + a

no	nc

#150) 1'	a	b	c
1'	1'	a	b	c
a	$\mid a \mid$	-a	a+c	0'
b	b	a+c	1' + b	a
c	c	0'	a	1' + a

	<i>a</i> → • • • • • • • • • • • • • • • • • •
	$\begin{array}{c c} & b & c \\ \hline \end{array}$
no	
	b
	c

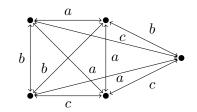
#151	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a + c	0'
b	b	a+c	1' + b	a
c	c	0'	a	1' + a

	[1'	a	a	b	c	b
MOG	$\begin{bmatrix} 1' \\ a \\ a \\ b \\ c \\ b \end{bmatrix}$	1'	a	a	a	c
yes 30_{65}	a	a	1'	a	b	c
30 ₆₅ RRA	b	a	a	1'	a	b
ши	c	a	b	a	1'	a
	b	c	c	b	a	1'

#	152	1'	a	b	c
	1'	1'	a	b	c
	a	a	1'	b+c	b+c
	b	b	b+c	-c	a
	c	c	b+c	a	1' + a

no	no

#153	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a $b + c$	b+c	b+c
b	b	b+c	-c	a
c	c	b+c	a	1' + a



no

no

 $\begin{array}{c} \mathrm{yes} \\ 33_{65} \\ \mathrm{RRA} \end{array}$

#154	1'	a	b	c
1'	1'	a	b	c
a	a	1' + b	0'	b+c
b	b	0'	-c	a
c	c	b+c	a	1' + a

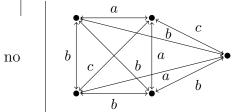
#155	1'	a	b	c
1'	1'	a	b	c
a	a	-c	0'	b+c
b	b	0'	-c	a
c	c	b+c	a	1' + a

#156	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b+c	0'
b	b	b+c	-c	a
c	c	0'	a	1' + a

#157	1'	a	b	c
1'	1'	a	b	c
a	a	-b	b+c	0'
b	b	b+c	-c	a
c	c	0'	a	1' + a

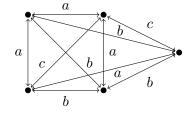
#158	$\mid 1' \mid$	a	b	c
1'	1'	a	b	c
a	a	-a	0'	0'
b	b	0 ′	-c	a
c	c	0'	a	1' + a

#159	1'	a	b	c
1'	1'	a	b	c
a	a	1	0'	0'
b	b	0'	-c	a
c	c	0 ′	a	1' + a



Γ 1'	a	a	b	c	b
a	1'	a	a	b	c
a	a	1'	b	c	b
b	a	b	1'	a	b
c	b	c	a	1'	a
b	c	b	b	a	1'

no	no



\[1'	a	a	b	c	b
a	1'	a	a	a	c
a	a	1'	b	c	b
b	a	b	1'	a	$\begin{bmatrix} b \\ c \\ b \\ b \end{bmatrix}$
c	a	c	a		a
b	c	b	b	a	
 _					_

#160	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a	a
b	b	a	1' + c	b
c	c	a	b	1'

#161	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	1	a	a
b	b	a	1' + c	b
c	c	a	b	1'

#162	1'	a	b	c
1'	1'	a	b	c
a	a	-b	b	a
b	b	b	-b	b
c	c	a	b	1'

#163	1'	\overline{a}	b	c
1'	1'	a	b	c
a	$\mid a \mid$	-a	a+b	a
b	b	a+b	-b	b
c	c	a	b	1'

#164	1'	a	b	c
1'	1'	a	b	c
a	a	1	a+b	a
b	b	a+b	-b	b
c	c	a	b	1'

#165	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	a + c	a+b
b	b	a+c	1' + c	a+b
c	c	a + b	a + b	1'

 $yes \\ 1_{65} \\ RRA$

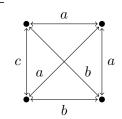


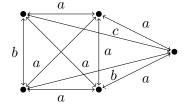


 $yes \\ 15_{65} \\ RRA$

 $yes \\ 16_{65} \\ RRA$

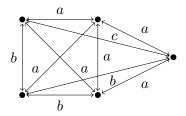


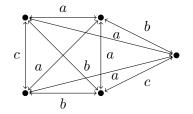




a	

,





no

no

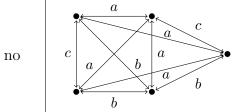
#166	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a+c	a+b
b	b	a + c	a + c $1' + c$ $a + b$	a + b
c	c	a+b	a+b	1'

a
C

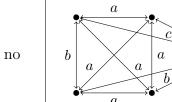
#167	1'	a	b	c
1'	1'	a	b	c
a	a	-b		a+b
b	b	b+c	-b	a+b
c	c	a+b	a+b	1'

a	
	•
a	

#168	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-a	0'	a+b
b	b	0'	-b	a+b
c	c	a+b	a+b	1'



#169	1'	a	b	c
1'	1'	a	b	c
a	a	1	0'	a+b
b	b	0'	-b	a+b
c	c	a+b	a + b	1'



#170	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	1' + b	a	c
b	b	a	1' + c	b
c	c	c	b	1' + a

no	no

#171	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a	c
b	b	a	1' + c	b
c	c	c	b	1' + a

no no

atom table	RA	QRNA
------------	----	------

#172	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a	a+c
b	b	a	1' + c	b
c	c	a + c	b	1' + a

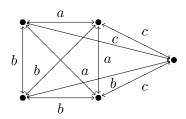
no	

#173	1'	a	b	c
1'	1'	a	b	c
a	a	1	a	a + c
b	b	a	1' + c	b
c	c	a + c	b	1' + a

\[1'	a	a	b	c	a
a	1'	a	a	a	c
a	a	1'	a	a	c
b	a	a	1'	b	a
c	a	a	b	1'	a
$\lfloor a \rfloor$	c	c	a	a	1'

#174	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	b	c
b	b	b	-b	b
c	c	c	b	1' + a

yes
2_{65}
RRA



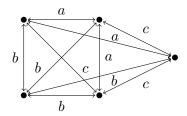
#175	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+b	c
b	b	a+b	-b	b
c	c	c	b	1' + a

no

n	O	

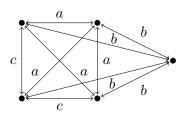
#176	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b	a + c
b	b	b	-b	b
c	c	a + c	b	1' + a

yes
9_{65}
RRA



#177	1'	a	b	c
1'	1'	a	b	c
a	a	-b	b	a + c
b	b	b	-b	b
c	c	a+c	b	1' + a

 $\begin{array}{c} {\rm yes} \\ 10_{65} \\ {\rm RRA} \end{array}$



atom table	RA	QRNA
acom casic	1011	Q-1-1-1-

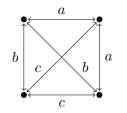
#178	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a+b	a+c
b	b	a+b	-b	b
c	c	a + c	b	1' + a

#179	1'	a	b	c
1'	1'	a	b	c
a	a	1	a+b	a+c
b	b	a+b	-b	b
c	c	a+c	b	1' + a

a

#180	1'	a	b	c
1'	1'	a	b	c
a	a	1' + b	a + c	b+c
b	b	a + c	1' + c	a + b
c	c	b+c	a + b	1' + a





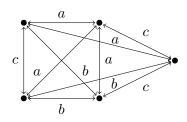
#181	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+c	b+c
b	b	a+c	1'+c	a+b
c	c	b+c	a+b	1' + a

yes
40_{65}
∉ RRA

a	
	c c
a	

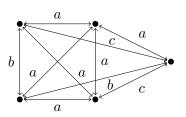
#182	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-a	a+c	0'
b	b	a+c	1' + c	a+b
c	c	0'		

yes	
43_{65}	
$\notin RRA$	



#183	1'	a	b	c
1'	1'	a	b	c
a	a	1	a+c	0'
b	b	a+c	1' + c	a+b
c	c	0'	a+b	1' + a

 $\begin{array}{c} \text{yes} \\ 44_{65} \\ \notin \text{RRA} \end{array}$



no

#184	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1' + a	b+c	b+c
b	b	b+c	-b	a+b
c	c	b+c	a + b	1' + a

u

#185	1'	a	b	c
1'	1'	a	b	c
a	a	-c	0'	b+c
b	b	0'	-b	a + b
c	c	b+c	a + b	1' + a

	a
yes 45 ₆₅ RRA	

#186	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b+c	0'
b	b	b+c	-b	a+b
c	c	0'	a + b	1' + a

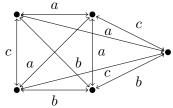
	a
no	

#187	1'	a	b	c
1'	1'	a	b	c
a	a	-b	b+c	0'
b	b	b+c	-b	a + b
c	c	0'	a + b	1' + a

A

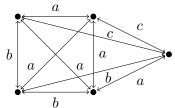
#188	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	0'	0'
b	b	0'	-b	a + b
c	c	0 ′	a+b	1' + a

yes	
54_{65}	c
∉ RRA	
·	



#189	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	0'	0'
b	b	0'	-b	a+b
c	c	0'	a + b	1' + a





atom table	RA QR	NA_
	no	no
	yes 7 ₆₅ RRA	$\begin{bmatrix} 1' & a & a & b & c & b \\ a & 1' & a & a & a & a \\ a & a & 1' & a & a & a \\ b & a & a & 1' & b & b \\ c & a & a & b & 1' & b \\ b & a & a & b & b & 1' \end{bmatrix}$
	yes 19 ₆₅ RRA	$\begin{bmatrix} 1' & a & a & b & c & b \\ a & 1' & a & a & a & b \\ a & a & 1' & b & a & b \\ b & a & b & 1' & b & b \\ c & a & a & b & 1' & b \\ b & b & b & b & b & 1' \end{bmatrix}$
	no	no
	no	$\begin{bmatrix} 1' & a & a & b & c & b \\ a & 1' & a & a & a & c \\ a & a & 1' & c & a & a \\ b & a & c & 1' & b & b \\ c & a & a & b & 1' & b \\ b & c & a & b & b & 1' \end{bmatrix}$

#195 1' 1' 1'

 $egin{array}{c} a \\ b \\ c \end{array}$

 $\frac{b}{b}$

 \overline{a}

 $c \over c$

a + b a + b 1'

		atom tab	ole F	RA	QRN	NA
#196	1'	a b c				
1'	1'	a b c				
a	a	1' + a = 0 c		no		no
b	b	0 - a b				
c	c	$c \qquad b \qquad 1' + a$				
#197	1'	a b c				
1'	1'	a b c				
a	a	-c a c		no		no
b	b	a - a b				
c	c	c b 1' + a				
<i>#</i> 108	1'	a b c				
#198 1'	1'	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
$\begin{vmatrix} 1 \\ a \end{vmatrix}$	$\begin{vmatrix} 1 \\ a \end{vmatrix}$	$\begin{bmatrix} a & b & c \\ -b & 0 & a+c \end{bmatrix}$		no		no
$\begin{vmatrix} a \\ b \end{vmatrix}$	$\begin{vmatrix} a \\ b \end{vmatrix}$	$\begin{bmatrix} -b & 0 & a+c \\ 0 & -a & b \end{bmatrix}$		110		110
$\begin{array}{ c c } \hline c \\ \hline \end{array}$	$\begin{vmatrix} c \\ c \end{vmatrix}$	a+c b $1'+a$				
#199	1'	a b c				
1'	1'	a b c				
a	a	-a a $a+c$		no		no
b	b	a -a b				
c	c	a+c b $1'+a$				
						Г1/ 1 1 -
#200	1'	a b c				$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c				$\begin{bmatrix} a & 1 & a & a & a & c & a \\ a & a & 1' & a & a & c & a \end{bmatrix}$
a	$\mid a \mid$	1 $a + c$		no		$\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b	a -a b				$\begin{bmatrix} c & a & a & b & 1' & a & b \end{bmatrix}$
c	c	a+c b $1'+a$				$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
#201	1'	a b c				$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c		yes		$\left[\begin{array}{ccccccc} a & 1' & a & b & c & b \\ a & a & 1' & b & c & b \end{array}\right]$
a	a	$1' + a b \qquad c$		6_{65}		$\left[\begin{array}{ccccccc} a & a & 1' & b & c & b \\ b & b & b & 1' & b & b \end{array}\right]$
b	b	b 1 b		RRA	A	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
c	c	$c \qquad b 1' + a$				$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$

atom table	RA	QRNA
------------	----	------

no

 $\begin{array}{c} \mathrm{yes} \\ 12_{65} \\ \mathrm{RRA} \end{array}$

 $\begin{array}{c} \mathrm{yes} \\ 13_{65} \\ \mathrm{RRA} \end{array}$

no

no

#202	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-c	a+b	c
b	b	a+b	1	b
c	c	c	b	1' + a

#203	1'	a	b	c
1'	1'	a	b	c
a	a	1' + c	b	a + c
b	b	b	1	b
c	c	a + c	b	1' + a

#204	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-b	b	a + c
b	b	b	1	b
c	c	a + c	b	1' + a

#205	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	a+b	a+c
b	b	a+b	1	b
c	c	a + c	b	1' + a

#206	1'	a	b	c
1'	1'	a	b	c
a	a	1	a+b	a + c
b	b	a+b	1	b
c	c	a + c	b	1' + a

#207	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	c	b+c
b	b	c	-a	a + b
c	c	b+c	a+b	1' + a

	I'	a	a	b	b	b	b	
	a	1'	a	a	b	b	b	
	a	a	1'	b	b	b	b	
	b	a	b	1'	b	b	b	
	$\begin{bmatrix} 1 \\ a \\ b \\ b \\ b \end{bmatrix}$	b	b	b	1'	c	a	
	b	b	b	b	c	1'	c	
	b	b	b	b	a	c	1'	

	1'	a	c	b	a	b
	a	1'	a	b	c	b
١	c	a	1'	b	c	b
İ	b	b	b	1'	b	b
	a	c	c	b	1'	b
	b	b	b	b	b	1'

\[1'	a	a	c	b	b
$\mid a \mid$	1'	a	a	b	b
$\mid a \mid$	a	1'	c	b	b
c	a	c	1'	b	b
b	b	b	b	1'	b
b	b	b	b	b	1'

Γ 1′	a	b	c	b	b	b
a	1'	a	a	b	b	b
b	a	1'	b	b	b	b
c	a	b	1'	b	b	b
b	b	b	b	1'	c	a
b	b	b	b	c	1'	c
b	b	b	b	a	c	1'

$$\begin{vmatrix} 1' & a & a & b & c & b \\ a & 1' & a & a & a & b \\ a & a & 1' & b & c & b \\ b & a & b & 1' & b & b \\ c & a & c & b & 1' & b \\ b & b & b & b & b & 1' \end{vmatrix}$$

no no

atom table	RA	QRNA
------------	----	------

#208	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	-c	a + c	b+c
b	b	a + c		a + b
c	c	b+c	a + b	1' + a

	$\mid b \mid$	a+c	-a	a+b		∉ R
	c	b+c	a + b	1' + a		
					_	
)9	1'	\overline{a}	b	c		
	1/	a	h	C		

	c	c	0' a	+b 1	'+a
	#210	1'	a	b	c
Ì	1'	1'	a	b	c
	a	a	-a	a + c	0'
	b	b	a + c		a + b
	c	c	0'	a + b	1' + a

#211	1'	a	b	c
1'	1'	a	b	c
a	a	1	a + c	0'
b	b	a + c	-a	a+b
c	c	0'	a + b	1' + a

#212	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	b+c	b+c
b	b	b+c	1	a+b
c	c	b+c	a + b	1' + a

#213	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	-c	0'	b+c
b	b	0'	1	a + b
c	c	b+c	a+b	1' + a

	yes	
	<i>1</i> 1	
	41_{65}	
#	RRA	
7	- 0- 01 1	

no

 $\begin{array}{c} \text{yes} \\ 48_{65} \\ \notin \text{RRA} \end{array}$

no

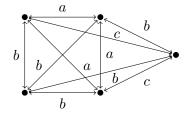
yes

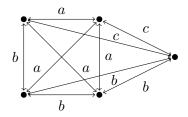
 46_{65} RRA

\[1'	a	a	b	b	b
a	1'	a	a	c	a
a	a	1'	a	c	a
b	a	a	1'	b	b
b	c	c	b	1'	c
b	a	a	b	c	1'

	1'	a	b	c	c	a	
TTOG	$\begin{bmatrix} 1' \\ a \\ b \\ c \\ c \end{bmatrix}$	1'	a	a	b	b	
yes 17 ₆₅	b	a	1'	b	a	a	
RRA	c	a	b	1'	a	c	
RRA	c	b	a	a	1'	b	
	a	b	a	c	b	1'	

\[1'	a	a	b	c	b
a	1'	a	a	a	c
a	a	1'	a	c	a
b	a	a	1'	b	b
$\begin{vmatrix} b \\ c \end{vmatrix}$	$a \\ a$	$a \\ c$	b'	$b \\ 1'$	$rac{b}{b}$





#214	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	1' + c	b+c	0'
b	b	b+c	1	a + b
c	c	0'	a + b	1' + a

	no

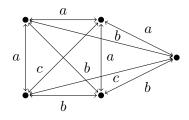
\[1'	a	c	b	b	b
a	1'	a	b	c	c
c	a	1'	b	b	b
b	b	b	1'	b	b
b	c	b	b	1'	a
b	c	b	b	a	1'

\[1'	a $1'$ a a b	a	c	b	a
a	1'	a	a	b	c
$\mid a \mid$	a	1'	c	b	a
c	a	c	1'	b	b
b	b	b	b	1'	b
	c				1'

#216	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	0'	0'
b	b	0 ′	1	a + b
c	c	0'	a + b	1' + a

yes
58_{65}
$\notin RRA$

no



#217	1'	a	b	c
1'	1'	a	b	c
a	a	1	0'	0'
b	b	0'	1	a + b
c	c	0'	a + b	1' + a

yes	
59_{65}	
RRA	

1'	a	a	b	c	a
a	1'	a	a	a	c
a	a	1'	b	b	b
b	a	b	1'	b	b
c	a	b	b	1'	c
a	c	b	b	c	1'

#218	1'	\overline{a}	b	\overline{c}
1'	1′	\overline{a}	b	c
a	a	1' + a	0	c
b	b	0	1' + b	c
c	c	c	c	-c

ſ	1'	a	a	c	c	c
	a	1'	a	c	c	c
l	a	a	1'	c	c	c
	c	c	c	1'	b	b
l	c	c	c	-	1'	b
1	c	c	c	b	b	1'

#219	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-c	a	c
b	b	a	1' + b	c
c	c	c	c	-c

$$\begin{array}{c} \text{yes} \\ 4_{65} \\ \text{RRA} \end{array}$$

				_ 6	atom tal	ole	RA	QR	NA	_						
	#220	1'	\overline{a}	b	c											
Ì	1'	1′	a	b	c											
	a	a	-b	0	a+c		no					n	О			
	b	b	0	1' + b	c											
	c	c	a+c	c	-c											
									_	٠.,					, -	,
	#221	1'	\overline{a}	b	c					1'	<i>a</i>	b	c	a	b	
Ì	1'	1′	\overline{a}	b	c		yes			$a \\ b$	1'	$a \\ 1'$	a	c	$a \\ b$	
	a	a	-a	a	a+c		17_{69}	5		c	$a \\ a$	c	$\frac{c}{1'}$	$\frac{a}{c}$	c	
	b	b	a	1' + b	c		RRA	4		a	c	a	c	1'	a	
	c	c	a+c	c	-c					b	a	b	c	a	1'	
															_]
	#222	1'	\overline{a}	b	c					1'	<i>a</i>	a	b	c	b	
Ì	1'	1'	a	b	c		yes			$a \\ a$	$\frac{1'}{a}$	$a \\ 1'$	a	$\frac{a}{c}$	a	
	a	a	1	a	a+c		18_{65}	5		$\frac{a}{b}$	$\frac{a}{a}$	a	$a \\ 1'$	$c \\ c$	$a \\ b$	
	b	b	a	1' + b	c		RRA	4		c	$\frac{a}{a}$	c	c	1'	c	
	c	c	a+c	c	-c					$\stackrel{\circ}{b}$	a	a	b	c	1'	
										•					_]
ſ	#223	1'	\overline{a}	b	c					1'	<i>a</i>	a	b	c	b	
Ì	1'	1'	a	b	c		yes		İ	a	1'	$a \\ 1'$	$a \\ b$	c	$rac{b}{b}$	
	a	a	-c	a + b	c		11_{65}	5		$a \\ b$	$a \\ a$	b	0 1'	$c \\ c$	b	
	b	b	a+b	-c	c		RRA	4		c	c	c	c	1'	c	
	c	c	c	c	-c					b h		h	h	1	1/	

#224	1'	a	b	c
1'	1'	a	b	c
a	a	-b	b	a + c
b	b	b	-c	c
c	c	a+c	c	-c

#225	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	a+b	a+c
b	b	a+b	-c	c
c	c	a + c	c	-c

no no

no

#226	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a+b	a + c
b	b	a+b	-c	c
c	c	a+c	c	-c

10	

$\begin{bmatrix} 1' \\ a \end{bmatrix}$	a	a	b	c	b
a	1'	a	a	a	a
a	a	1'	b	c	b
b	a	b	1'	c	b
c	a	c	c	1'	c
$\begin{bmatrix} a \\ b \\ c \\ b \end{bmatrix}$	a	b	b	c	1'

#227	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	c	b+c
b	b	c	1' + b	a + c
c	c	b+c	a+c	-c

no	
	•

#228	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+c	
b	b	a + c	1' + b	a + c
c	c	b+c	a + c	-c

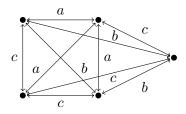
	yes
,	35_{65}
∉	RRA

#229	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	-b	c	0'
b	b	c	1' + b	a + c
c	c	0'	a + c	-c

ſ	1'	a	a	c	a	c
1	a	1'	a	a	c	c
	a	a	1'	c	c	c
1	c	a		1'	b	b
1	a	c	c	b	1'	b
1	c	c	c	b	b	1'

#230	1'	a	b	c
1'	1'	a	b	c
a	a	-a	a+c	0'
b	b	a + c	1' + b	a + c
c	c	0'	a+c	-c

yes	
51_{65}	
0165	
RRA	



#231	1'	a	b	c
1'	1'	a	b	c
a	a	1	a+c	0'
b	b	a+c	1' + b	a + c
c	c	0'	a+c	-c



#232	1/		h	
	1	a	<i>U</i>	C
1'	$\mid 1' \mid$	a	b	c
a	a	-c	0'	b+c
b	b	0'	-c	a + c
c	c	b+c	a + c	-c

yes	
37_{65}	
$\notin RRA$	

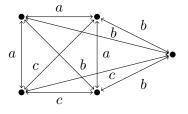
\[1'	a	a	b	c	b
a	1'	a	a	b	c
a	a	1'	b	c	b
b	a	b	1'	c	b
c	b	c	c	1'	c
b	c	b	b	c	1'
_					

yes	
49_{65}	
∉ RRA	L

\[1'	a	a	c	b	b
a	1'	a	a	b	b
a	a	1'	a	c	c
c	a	a	1'	c	c
b	b	c	c	1'	b
b	b	c	c	b	1'

#234	1'	a	b	c
1'	1'	a	b	c
a	a	-a	0'	0'
b	b	0'	-c	a + c
c	c	0'	a+c	-c

yes
56_{65}
RRA



#235	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	1	0'	0'
b	b	0'	-c	a + c
c	c	0'	a + c	-c

yes
57_{65}
RRA

\[1'	a	a	b	c	c
a	1'	a	a	a	c
a	a	1'		b	b
b	a	b	1'	a	a
c	a	b	a	1'	b
c	c	b	a	b	1'

#236	1'	\overline{a}	b	c
1'	1'	\overline{a}	b	c
a	a	-a	a+b	a + c
b	b	a+b		b+c
c	c	a+c	b+c	-c

$$yes \\ 21_{65} \\ \notin RRA$$

#237	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a+b	a + c
b	b	a+b	-b	b+c
c	c	a+c	b+c	-c

$$\begin{array}{c} \text{yes} \\ 22_{65} \\ \notin \text{RRA} \end{array}$$

$$\begin{bmatrix} 1' & a & a & b & c & b \\ a & 1' & a & a & a & a \\ a & a & 1' & b & c & b \\ b & a & b & 1' & b & c \\ c & a & c & b & 1' & c \\ b & a & b & c & c & 1' \end{bmatrix}$$

#238	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-a	0'	0'
b	b	0'	-b	0'
c	c	0 ′	0'	-c

c	c	0′	0'	-c	
#239	1'	a	b	c	
1'	1'	a	b	c	
a	a	1	0'	0 ′	
b	b	0'	-b	0'	

#240	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	-b	0	a + c
b	b	0	-a	b+c
c	c	a+c	b+c	-c

 $c \quad 0' \quad 0' \quad -c$

#241	l 1'	\overline{a}	b	\overline{c}
1'	1'	a	b	c
a	a	1	a	a+c
b	b	a	-a	b+c
c	c	a + c	b+c	-c

#242	1'	\overline{a}	b	c
1'	1'	a	b	c
a	a	1	a+b	a + c
b	b	a+b	1	b+c
c	c	a + c	b+c	-c

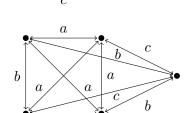
#243	1'	a	b	c
1'	1'	a	b	c
a	a	-b	c	0'
b	b	c	-a	0'
c	c	0'	0'	-c

 $\begin{array}{c} \mathrm{yes} \\ 62_{65} \\ \mathrm{RRA} \end{array}$

c



no



no

	- 1	a	1	u	α
		a	a	1'	a
no	ļ	b	a	a	$a \\ 1'$
		c	a	a	b
		a	c	c	a

 $\begin{bmatrix} 1 & a & a & b \\ a & 1' & a & a \\ a & a & 1' & b \\ b & a & b & 1' \\ c & a & c & b \\ b & a & b & b \end{bmatrix}$

 $\begin{vmatrix} 1 & a & a & c & a & c \\ a & 1' & a & a & c & c \\ a & a & 1' & c & c & b \\ c & a & c & 1' & b & b \\ a & c & c & b & 1' & b \\ c & c & b & b & b & 1' \end{vmatrix}$

 $\begin{array}{c} \text{yes} \\ 23_{65} \\ \notin \text{RRA} \end{array}$

atom table F	A QRNA
----------------	----------

#244	1'	a	b	c
1'	1'	\overline{a}	b	c
a	a	1	a + c	0'
b	b	a+c	-a	0'
c	c	0'	0'	-c

60_{65}
∉ RRA

1'	a	a	b	c	c
a	1'	a	a	a	c
a	a	1'	c	b	b
b	a	c	1'	b	c
c	a	b	b	1'	b
c	c	b	c	b	1'
_					-

$$\begin{array}{c} \text{yes} \\ 64_{65} \\ \text{RRA} \end{array}$$

\[1'	a	a	b	c	a
a	1'	a	a	a	c
a	a	1'	b	b	c
b	a	b	1'	b	c
c	a	b	b	1'	c
a	c	c	c	c	1'

#246	1'	a	b	c
1'	1'	a	b	c
a	a	1' + a	0	0
b	b	0	1' + b	0
c	c	0	0	1' + c

#249	1'	a	b	c
1'	1'	a	b	c
a	a	-c	a+b	0
b	b	a+b	-c	0
c	c	0	0	1' + c

atom table	e RA QR	NA
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	no	no
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	no	$\begin{bmatrix} 1' & a & a & b & a & b & a \\ a & 1' & a & a & c & a & c \\ a & a & 1' & b & a & b & a \\ b & a & b & 1' & a & b & a \\ a & c & a & a & 1' & a & c \\ b & a & b & b & a & 1' & a \\ a & c & a & a & c & a & 1' \end{bmatrix}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	no	no
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	no	no
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	yes 29 ₆₅ RRA	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
	no	no

			atom ta	ble	RA	QR	NA							
#256	1'	a b	\overline{c}					-						
1'	1'	a b	c											
a	a	-b $b+$	c a+b		no					n	Ο.			
b	b	b+c $-c$	a											
c	c	a+b a	1' + c											
							_							_
#257	1'	a b	c					1'	a	a	b	a	b	
1'	1'	a b	c		yes			a	1'	a	a	c	c	
a	a	1 0'	a+b		31_{68}			a	a	1'		b	a	
b	b	0' $-c$	a		RRA			b	a	$rac{b}{b}$	1′	$a \\ 1'$	b	
c	c	a+b a	1'+c					$a \\ b$	$c \\ c$	$\frac{o}{a}$	$a \\ b$	c	$\frac{c}{1'}$	
							L	U	C	a	U	C	1	J
#258	1'	a b	c											
1'	1'	a b	c											
a	a	1' + a b	c		no					n	Ο.			
b	b	b - c												
c	c	<i>c</i> 0	-b											
4250	1'	a b												
#259	1'	$ \begin{array}{c cc} a & b \\ \hline a & b \end{array} $	c											
$\begin{vmatrix} 1 \\ a \end{vmatrix}$	$\begin{vmatrix} 1 \\ a \end{vmatrix}$	-c $a +$			no					n	0			
b	$\begin{vmatrix} a \\ b \end{vmatrix}$	a+b $-c$			110					11	.0			
c	c	c 0												
#260	1'	a b	c				Γ		a a		a	a b		
1'	1'	$\frac{a}{a}$ $\frac{b}{b}$	$\frac{c}{c}$						a a a a		$\frac{c}{a}$	$\begin{array}{ccc} a & a \\ a & b \end{array}$		- 1
a	a	1 a +			no			b	a b	1'	a	a b	a	- 1
b	b	a+b $-c$			110				$\begin{pmatrix} c & a \\ a & a \end{pmatrix}$			c c $1'$ c		- 1
c	ļ	a+c 0						b	a b	b	a	a 1	' a	
	I						L	a	c a	a	c	c c	ı 1'	
#261	1'	a b	c											
1'	1'	a b												
a		1' + a b + a			no					n	Ο.			
b	l	b+c -												
c	c	b+c a	-b											

		atom table	e RA QR	NA
#262	1'	a b c		
1'	1'	a b c		
a	a	-c 0' b+c	no	no
b	b	0' -c a		
c	c	b+c a $-b$		
#263	1'	a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c	yes	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
a	a	1 0' 0'	34_{65}	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b	0' - c a	RRA	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
c	c	0' a -b		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
		_		
#264	1'	a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c	yes	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
a	a	1 a a	8 ₆₅	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b	a - a b	RRA	
c	c	a b 1' + c		
#265	1'	a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c	yes	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
a	a	1 $a+b$ a	20_{65}	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
b	b	a+b 1 b	RRA	
c	c	$a \qquad b \qquad 1'+c$		$ \left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
#266	1'	a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c	yes	$ \left \begin{array}{cccccccccccccccccccccccccccccccccccc$
a	a	1 a+c a+b	36_{65}	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b	a+c $-a$ $a+b$	$\notin RRA$	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
c	c	a+b $a+b$ $1'+c$		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
		_		
#267	1'	a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1'	1'	a b c	yes	
a	a	1 $0' a+b$	53_{65}	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b	b	0' 1 $a+b$	RRA	
c	c	a+b $a+b$ $1'+c$		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$

atom table	RA QR	NA
#268 1'abc		
1' $1'$ a b c		
$\begin{vmatrix} a & a & -c & a & c \end{vmatrix}$	no	no
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
$\boxed{\#269 \mid 1' a b c}$		$ \left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1' $1'$ a b c		
$\begin{bmatrix} a & a & 1 & a & a+c \end{bmatrix}$	no	$ \begin{array}{ c cccccccccccccccccccccccccccccccccc$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{bmatrix} c & c & a+c & b & -b \end{bmatrix}$		
$\boxed{\#270 \mid 1' a b c}$		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1' $1'$ a b c	yes	$ \left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{bmatrix} a & a & -b & b & a+c \end{bmatrix}$	14_{65}	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	RRA	b b b b 1' b b
$\begin{bmatrix} c & c & a+c & b & -b \end{bmatrix}$		$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
#271 1' a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1' $1'$ a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{bmatrix} a & a & 1 & a+b & a+c \end{bmatrix}$	no	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$b \mid b \mid a+b \mid 1 \qquad b \mid$		
c c $a+c$ b $-b$		$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
#272 1' a b c		
1' $1'$ a b c	yes	
$\begin{bmatrix} a & a & -c & a+c & b+c \end{bmatrix}$	42_{65}	$ \left \begin{array}{cccccccccccccccccccccccccccccccccccc$
b b a+c -a a+b	$\notin \mathrm{RRA}$	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$
#273 1' a b c		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
1' $1'$ a b c	yes	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
a a 1 a+c 0'	50_{65}	$ \left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
b b a+c -a a+b	$\notin RRA$	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{bmatrix} c & c & 0' & a+b & -b \end{bmatrix}$		$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$

atom table | RA | QRNA #2741' \overline{b} yes a 38_{65} b+c0' abb+c1 a + b∉ RRA b0' a+b1' #275 1' yes c 61_{65} 0' 0' aa0' RRA b1 a + b $0' \quad a+b$ #276 1' 1′ \overline{b} acyes 24_{65} 1 a+b a+caba+b1 b+cRRA a+c b+c1 #277 c1' 1' yes c 65_{65} 1 0'0'ac0' 1 0'RRA $0' \ 0'$ 1

6 Atoms: atomic identity, one symmetric and one nonsymmetric

					atom table	RA	QRNA	_
#278	1'	\overline{a}	r	r $$				
1'	1'	\overline{a}	r	r $$				
a	a	1'	0	0		no	,	no
r	r	0	0	1'				
r	r	0	1'	0				
								_

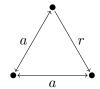
	atom table	RA	QRNA
r	r°		

#279	1'	a	r	r
1'	1'	a	r	r $\overset{\circ}{}$
a	a	1' + a	0	0
r	r	0	0	1'
r	r	0	1'	0

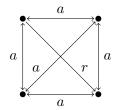
no

n	\cap

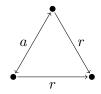
#280	1'	\overline{a}	r	r $$
1'	1'	a	r	r $^{\circ}$
a	a	-a	a	a
r	r	a	0	1'
r	$r^{\scriptscriptstyle{\smile}}$	a	1'	0



#281	1'	a	r	r°
1'	1'	a	r	r°
a	a	1	a	a
r	r	a	0	1'
r	r	a	1'	0

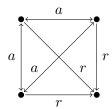


#282	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle \circ}$
a	a	1'	r	0
r	r	0	0	1' + a
$r^{\scriptscriptstyle \smile}$	r	$r^{\scriptscriptstyle{\smile}}$	1'	0



#283	1'	a	r	$r^{\scriptscriptstyle centcolor}$
1'	1'	a	r	$r^{\scriptscriptstyle \circ}$
a	a	1' + a	r	0
r	r	0	0	1' + a
r	r	r°	1′	0

no	



#284	1'	a	r	r $$
1'	1'	\overline{a}	r	r°
a	a	-a	a+r	a
r	r	a	0	1' + a
r	r	a + r	1'	0

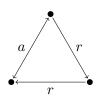
#285	1'	a	r	r $$
1'	1'	a	r	r°
a	a	1	a + r	a
r	r	a	0	1' + a
r	r	a + r	1'	0

a	
	ι

#286	1'	\overline{a}	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle{\smallsmile}}$
a	a	1'	$r^{\scriptscriptstyle{\smallsmile}}$	r
r	r	$r^{\scriptscriptstyle \smallsmile}$	a	1'
r	r	r	1'	a

yes
10
18_{37}
RRA

no



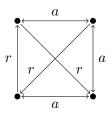
#287	1'	a	r	r $^{\circ}$
1'	1'	\overline{a}	r	r $$
a	a	1' + a	$r^{\scriptscriptstyle{\smallsmile}}$	r
r	r	$r^{\scriptscriptstyle \smile}$	a	1'
$r^{\scriptscriptstyle \vee}$	r°	r	1'	a

no

110	

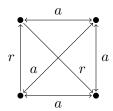
#288	1'	a	r	r $$
1'	1'	a	r	r°
a	a	-a	a + r	a+r
r	r	a + r	a	1'
$r^{\scriptscriptstyle \smile}$	r	a + r	1'	a

no	



#289	1'	a	r	r $$
1'	1'	a	r	r°
a	a	1	a + r	a + r
r	r	$a + r \overset{\circ}{}$	a	1'
r	r	a + r	1'	a

no	



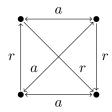
#290	1'	a	r	$r^{\scriptscriptstyle \smile}$
1'	1'	a	r	r°
a	a	1'	$r + r \check{\ }$	r
r	r	$r^{\scriptscriptstyle \smile}$	a	1' + a
r	r	$r + r^{\circ}$	1'	a

no

#291	1'	\overline{a}	r	r $$
1'	1'	a	r	r $^{\circ}$
a	a	1' + a	$r + r^{\circ}$	r
r	r	r°	a	1' + a
r	$r^{\scriptscriptstyle }$	r + r	1'	a

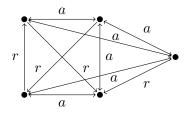
	a	
a		,
	T.	

#292	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	-a	0'	a + r
r	r	a + r	a	1' + a
r	r°	0'	1'	a



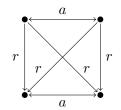
	#293	1'	a	r	r°
ſ	1'	1'	\overline{a}	r	r $^{\circ}$
	a	a	1	0'	a + r
	r	r	a + r	a	1' + a
	r^{\smallsmile}	r $^{\scriptscriptstyle \circ}$	0'	1'	a

no	



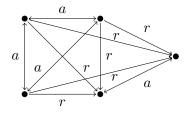
#294	1'	a	r	$r^{\scriptscriptstyle \smile}$
1'	1'	a	r	$r^{\scriptscriptstyle \smile}$
a	a	1'	r	$r^{\scriptscriptstyle \smile}$
r	r	r	0	1' + a
r	r°	$r^{\scriptscriptstyle{\smallsmile}}$	1' + a	0

no



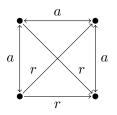
#295	1'	a	r	r°
1'	1'	a	r	r°
a	a	1' + a	r	r°
r	r	r	0	1' + a
r	$r^{\scriptscriptstyle \smile}$	r^{\smallsmile}	1' + a	0

1	10	



#296	1'	\overline{a}	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	-a	a + r	a+r
r	r	a + r	0	1' + a
r	r	a + r	1' + a	0





no

#297	1'	a	r	r $$
1'	1'	a	r	r $^{\circ}$
a	a	1	a + r	a+r
r	r	a + r	0	1' + a
r	$r^{\scriptscriptstyle \smile}$	a + r	1' + a	0

$a \rightarrow a$	
	≱•

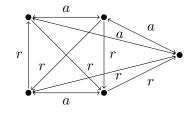
#298	1'	a	r	r°
1'	1'	a	r	r°
a	a	1'	$r + r^{\circ}$	r + r
r	r	$r + r \check{\ }$	a	1' + a
r	r	$r + r \check{\ }$	1' + a	a

a	
	r

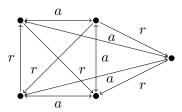
#299	1'	a	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	1' + a	$r + r \check{\ }$	$r + r \check{\ }$
r	r	$r + r \check{\ }$	a	1' + a
r	r	$r+r^{\scriptscriptstyle \vee}$	1' + a	a

yes
20_{37}
RRA

no

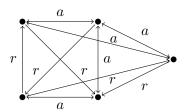


#300	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle \smile}$
a	a	-a	0'	0'
r	r	0'	a	1' + a
r	r	0'	1' + a	a



#301	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1	0'	0'
r	r	0'	a	1' + a
r	r	0'	1' + a	a

yes	
31_{37}	
RRA	



#302	1'	\overline{a}	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	1'	0	0
r	r	0	r	-a
r	r	0	-a	$r^{\scriptscriptstyle \smile}$

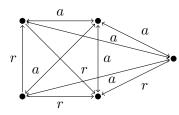
no

а	tom table	RA	QRNA	
1 ""	2			
	0	70.0		70.0
	0	no		no
	-a			
, , , , , ,				
$\lceil #304 \mid 1' a r r \rceil$]			$a \longleftrightarrow a$
1' $1'$ a r r		yes		
$\begin{vmatrix} a & a & -a & a & a \end{vmatrix}$		7_{37}		r a
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		RRA		
r r a $-a$ r				$\stackrel{\downarrow}{\bullet} \qquad \stackrel{\downarrow}{r}$
#305 1' a r r			•	$a \rightarrow a$
1' $1'$ a r r		yes		
		8_{37}		$a \nearrow r$ $a \longrightarrow r$
$\left egin{array}{c cccc} r & r & a & r & -a \ r\ \ddot{r} & a & -a & r\ \end{array} ight $		RRA		
I I a -a I				r
$\boxed{\#306 \mid 1' a r r^{\circ}}$				$a \longrightarrow a$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
$\begin{bmatrix} a & a & 1' & r & 0 \end{bmatrix}$		no		r r
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
$\begin{bmatrix} r \ \end{bmatrix} \begin{bmatrix} r \ $				$\stackrel{\longleftarrow}{\bullet} \stackrel{\longleftarrow}{r}$
	_			
$#307 \mid 1' a r r$			•	
1' $1'$ a r r	1			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		no		
				r
, , ,				r
$\lceil #308 \mid 1' a r \rceil$	r			$\bullet \longleftarrow a$
1' $1'$ a r	r			
$\begin{vmatrix} a & a & -a & a+r \end{vmatrix}$	a	no		r r
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1			
r r $a+r$ $-a$	r			$\stackrel{\checkmark}{\bullet} \stackrel{\checkmark}{\longrightarrow} \stackrel{\bullet}{\bullet}$

#309	1'	a	r	$r^{\scriptscriptstyle{\circ}}$
1'	1'	a	r	r $$
a	a	1	a + r	a
r	r	a	r	1
$r^{\scriptscriptstyle \vee}$	$r^{\scriptscriptstyle{\smallsmile}}$	a + r	-a	$r^{\scriptscriptstyle ec}$

a	a	1	a + r	a	
r	r	a	r	1	I
~ [∨]	r	$a + r\check{\ }$	-a	r°	

yes	
13_{37}	
RRA	



	#310	1'	a	r	r°
ĺ	1'	1'	\overline{a}	r	r $$
	a	a	1'	$r^{\scriptscriptstyle \circ}$	r
	r	r	$r^{\scriptscriptstyle{\smile}}$	a + r	-a
l	$r^{\scriptscriptstyle \smile}$	r	r	-a	a + r

1'	1'	a	r	r $^{\circ}$
a	a	1'	r°	r
r	r	$r^{\scriptscriptstyle{\smile}}$	a + r	-a
r°	r	r	-a	a+r

a	
	r

#311	1'	a	r	r $^{\circ}$
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	$\mid a \mid$	1' + a	$r^{\scriptscriptstyle \smile}$	r
r	$\mid r \mid$	r°	a + r	-a
r	$\mid r^{\scriptscriptstyle \smile}$	r	-a	a + r

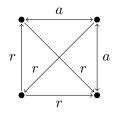
no

no

no	

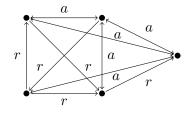
#312	1'	a	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	-a	a + r	a + r
r	r	a + r	a+r	-a
r $$	$r^{\scriptscriptstyle \circ}$	a + r	-a	a + r

yes
ດ້າ
23_{37}
RRA
1010Λ

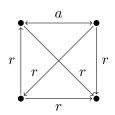


#313	1'	a	r	r $$
1'	1'	a	r	r°
a	$\mid a \mid$	1	a + r	a + r
r	r	a + r	a + r	-a
r	r	a + r	-a	$a + r \check{\ }$

	yes
	24_{37}
∉	RRA



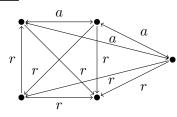
#314	1'	\overline{a}	r	r $$
1'	1'	a	r	$r^{\scriptscriptstyle \circ}$
a	a	1'	r + r	r
r	r	$r^{\scriptscriptstyle \smile}$	a + r	1
r	r	r + r	-a	$a + r \overset{\circ}{}$



atom table \mid RA \mid QRNA

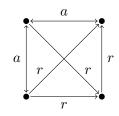
#315	1'	a	r	r $$
1'	1'	a	r	r $$
a	$\mid a \mid$	1' + a	$r + r \check{\ }$	r
r	r	r°	a + r	1
r	$\mid r$	$r + r \check{\ }$	-a	a + r

	Į	
,		
		no
		no



#316	1'	a	r	$r^{\scriptscriptstyle centcolor}$
1'	1'	a	r	r°
a	a	-a	0'	a + r
r	r	a + r	a + r	1
r $^{\circ}$	r	0'	-a	$a + r \overset{\circ}{}$

yes	
27_{37}	
∉ RRA	



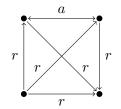
#317	1'	a	r	r^{\smallsmile}
1'	1'	a	r	$r^{\scriptscriptstyle \smile}$
a	a	1	0'	a + r
r	r	a + r	a + r	1
r	r	0'	-a	a + r

	yes
	28_{37}
∉	RRA

	a	
r	↑	

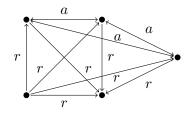
#318	1'	\overline{a}	r	r°
1'	1'	a	r	r $$
a	a	1'	r	$r^{\scriptscriptstyle{\smallsmile}}$
r	r	r	r	1
r	r°	$r^{\scriptscriptstyle{\smallsmile}}$	1	$r^{\scriptscriptstyle{\smallsmile}}$

yes	
1_{37}	
RRA	



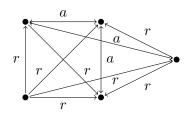
#319	1'	a	r	r $^{\circ}$
1'	1'	a	r	r $$
a	a	1' + a	r	$r^{\scriptscriptstyle \circ}$
r	r	r	r	1
r	$r^{\scriptscriptstyle{\smallsmile}}$	$r^{\scriptscriptstyle \circ}$	1	$r^{\scriptscriptstyle{\smile}}$

yes	
2_{37}	
RRA	



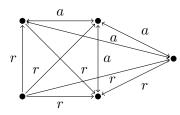
#320	1'	a	r	$r^{\scriptscriptstyle \smile}$
1'	1'	a	r	r°
a	a	-a	a + r	a+r
r	r	a + r	r	1
r	r	a + r	1	$r^{\scriptscriptstyle \smile}$

 $yes \\ 14_{37} \\ \notin RRA$



#321	1'	a	r	r°
1'	1'	a	r	r°
a	$\mid a \mid$	1	a + r	a + r
r	r	a + r	r	1
$r^{\scriptscriptstyle \smile}$	$\mid r^{\scriptscriptstyle \vee} \mid$	a + r	1	$r^{\scriptscriptstyle \smile}$

yes
15_{37}
RRA
1111L

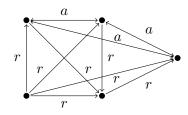


#322	1'	a	r	r $$
1'	1'	a	r	r $$
a	a	1'	$r + r \check{\ }$	$r+r\check{\ }$
r	r	r + r	a + r	1
$oxed{r}$	r	r + r	1	a + r

a	
	•

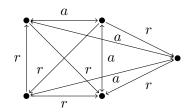
#323	1'	a	r	$r^{\scriptscriptstyle centcolor}$
1'	1'	a	r	r°
a	a	1' + a	r + r	r + r
r	r	r + r	a + r	1
r	r	r + r	1	$a + r \overset{\circ}{}$

yes
21_{37}
∉ RRA



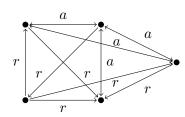
#324	1'	\overline{a}	r	r°
1'	1'	a	r	r°
a	a	-a	0'	0'
r	r	0'	a + r	1
r	r°	0'	1	a + r

	yes
;	32_{37}
∉	RRA



#325	1'	a	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	1	0'	0'
r	r	0'	a + r	1
r	r	0'	1	a + r

yes
33_{37}
RRA



#326	1'	a	r	r°
1'	1'	a	r	r°
a	a	1'	0	0
r	r	0	$r^{\scriptscriptstyle{\smallsmile}}$	1'
r	r	0	1'	r

no

atom table	RA QR	NA
	no	no
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	yes 9 ₃₇ RRA	r a r a r a r a r
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	yes 10_{37} RRA	
	no	no
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	no	no

#332	1'	a	r	r°	
1'	1'	a	r	r $^{\circ}$	
$\mid a \mid$	a	-a	a + r	a	no
$\mid r \mid$	r	a	$r^{\scriptscriptstyle \circ}$	1' + a	
$\mid r^{\circ} \mid$	$r^{\scriptscriptstyle{\smallsmile}}$	$a \\ a + r $	1'	r	

atom table	RA	QRNA
------------	----	------

#333	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1	a + r	a
r	r	a	r°	1' + a
r	r°	a + r	1'	r

U1 1	Ø101							
		$ \begin{bmatrix} 1' \\ a \\ r \\ r \\ a \\ a \end{bmatrix} $	a	r	r^{\smallsmile}	a	a	1
		a	1'	a	a	a	r	l
no		$\mid r$	a	1'	r	a	a	
по	,	$\mid r \mid$	a	r°	1'	a	a	١
		a	a	a	a	1'	r	
			r°	a	a	$r^{\scriptscriptstyle \circ}$	1'.	

#334	1'	\overline{a}	r	r $^{\circ}$
1'	1'	a	r	r°
a	a	1'	r°	r
r	r	$r^{\scriptscriptstyle \smallsmile}$	a + r	1'
r	r	r	1'	a+r

$$\begin{array}{|c|c|c|c|c|c|}\hline \#336 & 1' & a & r & r \\\hline 1' & 1' & a & r & r \\\hline a & a & -a & a+r \\\hline r & r & a+r \\\hline r' & r' & a+r & 1' & a+r \\\hline \end{array}$$

$$\begin{array}{|c|c|c|c|c|c|c|}\hline \#337 & 1' & a & r & r \\\hline 1' & 1' & a & r & r \\\hline a & a & 1 & a+r \\\hline r & r & a+r \\\hline r' & r' & a+r & 1' & a+r \\\hline \end{array}$$

no
$$\begin{bmatrix} 1' & a & r & r & a & a \\ a & 1' & a & a & a & r \\ r & a & 1' & r & a & a \\ r & a & r & 1' & a & a \\ a & a & a & a & 1' & r \\ a & r & a & a & r & 1' \end{bmatrix}$$

#338	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1'	r + r	r
r	r	r^{\smallsmile}	a + r	1' + a
r	r	$r+r^{\scriptscriptstyle \vee}$	1'	a + r

#339	1'	a	r	r°
1'	1'	a	r	r°
a	a	1' + a	r + r	r
r	r	r°	a + r	1' + a
r	r	$r + r \check{\ }$	1'	a + r

no

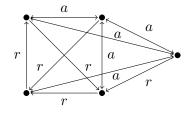
n	\mathbf{O}

#340	1'	a	r	r $$
1'	1'	a	r	r $$
a	$\mid a \mid$	-a	0'	a + r
r	r	a + r	a + r	1' + a
r°	r	0'	1'	a + r

	a	
r		
	r	

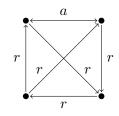
#341	1'	a	r	r $$
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	$\mid a \mid$	1	0'	a + r
r	r	a + r	a + r	1' + a
r	r	0'	1'	a + r

no



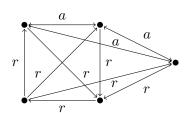
#342	1'	a	r	$r^{\scriptscriptstyle ec}$
1'	1'	a	r	r°
a	a	1'	r	r°
r	r	r	$r^{\scriptscriptstyle \smile}$	1' + a
$r^{\scriptscriptstyle \circ}$	r	r°	1' + a	r

yes
3_{37}
RRA



#343	1'	a	r	$r^{\scriptscriptstyle \vee}$
1'	1'	a	r	r°
a	a	1' + a	r	$r^{\scriptscriptstyle \smile}$
r	r	r	r^{\smallsmile}	1' + a
$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle \circ}$	r°	1' + a	r

yes
4_{37}
RRA



#344	1'	a	r	$r^{\scriptscriptstyle \smile}$
1'	1'	a	r	$r^{\scriptscriptstyle ec}$
a	a	-a	a + r	a + r
r	r	a + r	r°	1' + a
r	r	a + r	1' + a	r

no

#345	1'	a	r	r $^{\circ}$
1'	1'	a	r	r°
a	a	1	a + r	a + r
r	r	a + r	r°	1' + a
$r^{\scriptscriptstyle \smile}$	$\mid r^{\scriptscriptstyle ec} \mid$	a + r	1' + a	r

_	a	_	
Î		a	
r			•
•	r		

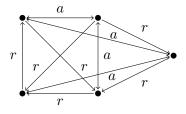
#346	1'	a	r	r°
1'	1'	a	r	r°
a	a	1'	$r + r^{\circ}$	r + r
r	r	$r+r^{\scriptscriptstyle \vee}$	a + r	
r	r	$r+r\check{\ }$	1' + a	a + r

no

no

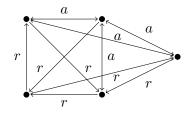
	#348	1'	\overline{a}	r	$r^{\scriptscriptstyle \smile}$
	1'	1'	a	r	$r^{\scriptscriptstyle \smile}$
İ	a	a	-a	0'	0'
	r	r	0'	a + r	1' + a
	r^{\smallsmile}	r	0'	1' + a	a+r

yes
34_{37}
$\notin RRA$



#349	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1	0'	0'
r	r	0'	a + r	1' + a
r	$r^{\scriptscriptstyle \smile}$	0'	1' + a	a + r

yes
35_{37}
RRA



#350	1'	\overline{a}	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle \circ}$
a	a	1'	0	0
r	r	0	r + r	-a
r	r	0	-a	r + r

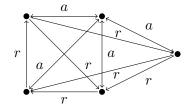
no

#351	1'	a	r	r°
1'	1'	a	r	r°
a	a	1' + a	0	0
r	r	0	$r + r^{\circ}$	-a
r	r	0	-a	r + r

n	\cap

#352	1'	\overline{a}	r	$r^{\scriptscriptstyle \vee}$
1'	1'	a	r	r $$
a	a	-a	a	a
r	r	a	r + r	-a
r	$\mid r^{\scriptscriptstyle ec} \mid$	a	-a	r + r

yes
11_{37}
RRA

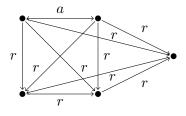


#353	1'	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1	a	a
r	r	a	$r + r \check{\ }$	-a
r	r $$	a	-a	r + r

yes	
12_{37}	
RRA	

1'	a	r	r^{-}	a	r
a	1'	a	a	a	a
$r^{\scriptscriptstyle \smile}$	a	1'	r	a	r $^{\scriptscriptstyle \circ}$
r		$r^{\scriptscriptstyle \smile}$			
a	a	a	a	1'	a
$r^{\scriptscriptstyle{\smallsmile}}$	a	r	r	a	1'

#354	1'	\overline{a}	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	$\mid a \mid$	1'	r	0
r	r	0	$r + r \check{\ }$	1
r	$\mid r^{\scriptscriptstyle \vee}$	$r^{\scriptscriptstyle{\smallsmile}}$	-a	$r+r\check{\ }$



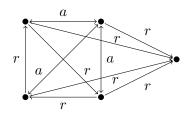
#355	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	a	1' + a	r	0
r	r	0	$r + r^{\circ}$	1
r	r	r°	-a	$r+r^{\scriptscriptstyle \vee}$

no	

$\lceil 1' \rceil$	a	r	a	r	r
a	1'	r	a	r	r
r	$r^{\scriptscriptstyle \smile}$	1'	$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle \vee}$	r
a	a	r	1'	r	r
r	$r^{\scriptscriptstyle \smallsmile}$	r	$r^{\scriptscriptstyle \smallsmile}$	1'	$r^{\scriptscriptstyle \smile}$
r°	r°	r°	$r^{\scriptscriptstyle \smallsmile}$	r	1'

#356	1'	a	r	r $$
1'	1'	a	r	$r^{\scriptscriptstyle \smile}$
a	a	-a	a + r	a
r	r	a	r + r	1
$r^{\scriptscriptstyle \smile}$	r	a + r	-a	$r+r^{\scriptscriptstyle \vee}$





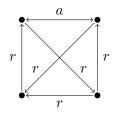
_					
	#357	1'	a	r	r°
	1'	1'	\overline{a}	r	r $^{\circ}$
	a	a	1	a + r	a
	r	r	a	r + r	1
	$r^{\scriptscriptstyle \smile}$	r	a + r	-a	$r + r \check{\ }$

\[1'	a	r	r°	a	r
a	1'	a	a	a	a
r	a	1'	r°	r°	$r^{\scriptscriptstyle \smile}$
r	a	r	1'	a	$r^{\scriptscriptstyle \smile}$
a	a	r	a	1'	a
r	a	r	r	a	1'

#358	1'	\overline{a}	r	r $^{\circ}$
1'	1'	a	r	r°
a	a	1'	$r^{\scriptscriptstyle \vee}$	r
r	r	$r^{\scriptscriptstyle{\smallsmile}}$	0 ′	-a
r	r	r	-a	0'

yes
10
19_{37}
RRA
101011

no

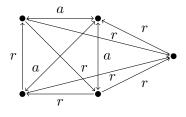


#359	1'	\overline{a}	r	r $$
1'	1'	\overline{a}	r	r $$
a	a	1' + a	$r^{\scriptscriptstyle \smile}$	r
r	r	r°	0 ′	-a
r	r	r	-a	0'

no	

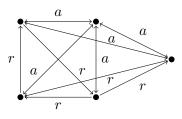
#360	1'	a	r	r°
1'	1'	a	r	r $$
a	a	-a	a + r	a + r
r	r	a + r	0'	-a
r	r	a + r	-a	0'

yes
25_{37}
$\notin RRA$

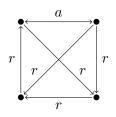


#361	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	a	1	a + r	a + r
r	r	a + r	0'	-a
r	r	a+r	-a	0'

	yes	
	26_{37}	
∉	RRA	



#362	1'	a	r	r°
1'	1'	\overline{a}	r	r $$
a	a	1'	r + r	r
r	r	r^{\smallsmile}	0'	1
$r^{\scriptscriptstyle \smile}$	r	$r+r^{\scriptscriptstyle \vee}$	-a	0'



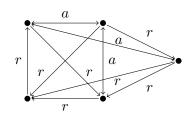
#363	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle{\smallsmile}}$
a	a	1' + a	r + r	r
r	r	r°	0'	1
r	$r^{\scriptscriptstyle{\smallsmile}}$	$r + r \check{\ }$	-a	0'

#363	1'	a	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle{\smallsmile}}$
a	a	1' + a	$r + r \check{\ }$	r
r	r	$r^{\scriptscriptstyle \vee}$	0'	1
$r^{\scriptscriptstyle \smile}$	r	$r+r^{\scriptscriptstyle \vee}$	-a	0'

a	
	•

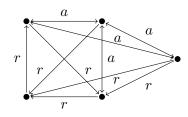
#364	1'	a	r	r $^{\circ}$
1'	1'	a	r	r $^{\circ}$
a	a	-a	0'	a + r
r	r	a + r	0'	1
r	r	0'	-a	0'

yes
29_{37}
$\notin RRA$



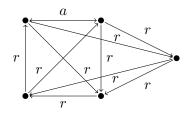
#365	1'	a	r	r°
1'	1'	a	r	r°
a	a	1	0'	a + r
r	r	a + r	0'	1
r^{\smallsmile}	r	0'	-a	0'

yes
30_{37}
RRA



#366	1'	a	r	$r^{\scriptscriptstyle \circ}$
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	a	1'	r	r°
r	r	r	r + r	1
r $$	r	$r^{\scriptscriptstyle{\smile}}$	1	r + r

yes	
5_{37}	
RRA	



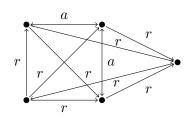
#367	1'	\overline{a}	r	r°
1'	1'	a	r	r°
a	a	1' + a	r	r°
r	r	r	$r + r \check{\ }$	1
$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle{\smile}}$	r°	1	$r+r^{\scriptscriptstyle \vee}$

yes	
6_{37}	
RRA	

\[1'	a	r	$r^{\scriptscriptstyle{\smile}}$	a	r
a	1'	r	$r^{\scriptscriptstyle{\smallsmile}}$	a	r
r	r°	1'	r	$r^{\scriptscriptstyle \smallsmile}$	$r^{\scriptscriptstyle \smile}$
r	r	r°	1'	r	$r^{\scriptscriptstyle \smile}$
a	a	r	r°	1'	r
r	r°			$r^{\scriptscriptstyle \smallsmile}$	1'

#368	1'	\overline{a}	r	r°
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	a	-a	a + r	a + r
r	r	a + r	r + r	1
r	r	a + r	1	r + r





#369	1'	\overline{a}	r	r $$
1'	1'	a	r	$r^{\scriptscriptstyle centcolor}$
a	a	1	a + r	a + r
r	r	a + r	r + r	1
r	r	a + r	1	r + r

yes
17_{37}
RRA

1'	a	r	$r^{\scriptscriptstyle \vee}$	a	r
a	1'	a	$r^{\scriptscriptstyle \vee}$	a	r
r	a	1'	$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle \smile}$	r
r	r	r	1'	r	$r^{\scriptscriptstyle \vee}$
a	a	r	$r^{\scriptscriptstyle \smallsmile}$	1'	r
$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle{\smallsmile}}$	$r^{\scriptscriptstyle \smallsmile}$	r	$r^{\scriptscriptstyle \smallsmile}$	1'

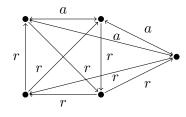
#370	1'	a	r	r $^{\circ}$
1'	1'	a	r	r°
a	$\mid a \mid$	1'	$r + r \check{\ }$	$r+r\check{\ }$
r	r	$r + r \check{\ }$	0'	1
$r^{\scriptscriptstyle \smile}$	$r^{\scriptscriptstyle \circ}$	$r+r^{\scriptscriptstyle \vee}$	1	0'

no

a	

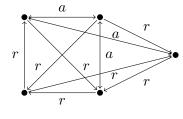
#371	$\mid 1' \mid$	a	r	r°
1'	1'	a	r	r $^{\circ}$
a	a	1' + a	$r+r\check{\ }$	$r + r \check{\ }$
r	r	$r + r \check{\ }$	0'	1
r°	r	$r + r^{\circ}$	1	0'

yes
22_{37}
RRA



#372	1'	a	r	$r^{\scriptscriptstyle{\circ}}$
1'	1'	a	r	r $$
a	a	-a	0'	0'
r	r	0 ′	0'	1
r	r	0'	1	0'

yes	
36_{37}	
R.R.A	



#373	1'	a	r	r°
1'	1'	\overline{a}	r	r
a	a	1	0'	0'
r	r	0'	0'	1
r	$r^{\scriptscriptstyle \circ}$	0'	1	0'

 $\begin{array}{c} \mathrm{yes} \\ 37_{37} \\ \mathrm{RRA} \end{array}$

