

# <sup>1</sup> pyGeo: A geometry package for multidisciplinary design optimization

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## <sup>8</sup> Summary

<sup>9</sup> In shape optimization, an algorithm modifies a body's geometry to improve its performance. <sup>10</sup> A common shape optimization example is adjusting the geometry of an aircraft wing to <sup>11</sup> minimize aerodynamic drag computed via computational fluid dynamics (CFD). Multidisciplinary <sup>12</sup> design optimization (MDO) couples multiple disciplines, such as aerodynamics and structural <sup>13</sup> mechanics, to optimize them simultaneously. In MDO, the geometry must be represented <sup>14</sup> consistently across multiple disciplines.

<sup>15</sup> pyGeo is a geometry package for three-dimensional shape manipulation tailored for aerodynamic <sup>16</sup> and multidisciplinary design optimization. It provides several methods for geometry parameterization, <sup>17</sup> geometric constraints, and utility functions for geometry manipulation. pyGeo <sup>18</sup> computes derivatives for all parameterization methods and constraints, facilitating efficient <sup>19</sup> gradient-based optimization.

## Features

### <sup>21</sup> Integrations

<sup>22</sup> pyGeo is the geometry manipulation engine within the MDO of Aircraft Configurations at <sup>23</sup> High Fidelity (MACH) framework ([Kenway et al., 2014](#); [Kenway & Martins, 2014](#)), which <sup>24</sup> specializes in high-fidelity aerostructural optimization. pyGeo is also integrated into MPhys<sup>1</sup>, a <sup>25</sup> more general framework for high-fidelity multiphysics problems built with OpenMDAO ([Gray <sup>26</sup> et al., 2019](#)). Both MACH and MPhys use pyOptSparse ([Wu et al., 2020](#)) to interface with <sup>27</sup> optimization algorithms.

<sup>28</sup> pyGeo's interface for design variables and constraints is independent of which solvers are <sup>29</sup> accessing the geometry. This means that pyGeo geometries can interact with different types <sup>30</sup> of solvers, such as structures and aerodynamics, in the same way. This also allows direct <sup>31</sup> comparison of the behavior or performance of two different solvers within the same discipline <sup>32</sup> using the same geometric parameterization for each, such as two different flow solvers ([Adler <sup>33</sup> et al., 2022](#)).

### <sup>34</sup> Geometry Parameterization with pyGeo

<sup>35</sup> pyGeo contains several options for parameterizing geometry: variations on the FFD method, <sup>36</sup> interfaces to external parametric modeling tools, and an analytic parameterization. Because

<sup>1</sup> <https://github.com/OpenMDAO/mphys>

37 each parameterization method uses a common interface for interacting with the rest of the  
 38 MACH framework, any surface parameterization can be used in place of another within an  
 39 optimization setup ([Hajdik et al., 2023](#)). The choice of parameterization depends on the user's  
 40 experience, the geometry details, and whether the user needs the final design in a specific  
 41 format.

#### 42 Free-form Deformation

43 The free-form deformation (FFD) method ([Sederberg & Parry, 1986](#)) is one of the most popular  
 44 three-dimensional geometry parameterization approaches ([Zhang et al., 2018](#)). This approach  
 45 embeds the entire reference geometry in a parameterized volume. The set of control points  
 46 that determine the shape of the volume are displaced to manipulate the points inside. The  
 47 user can have a high degree of control over the geometry by selecting different control point  
 48 densities and locations.

49 Individual control points can be moved to obtain local shape modifications. In pyGeo, these  
 50 are referred to as *local* design variables because a single control point is affected. Conversely,  
 51 it is also common to define geometric operations involving a collection of control points across  
 52 the entire FFD block. These are referred to as *global* design variables in pyGeo. For example,  
 53 wing twist variables can be defined as rotations of the control points about a reference axis  
 54 that runs along the wing. [Figure 1](#) shows a few common planform design variables for an  
 55 aircraft wing.

56 Design variables formulated from groupings of FFD control points often exhibit ill conditioning.  
 57 To alleviate this, a parameterization based on singular value decomposition is also possible  
 58 within pyGeo ([Wu et al., 2022](#)).

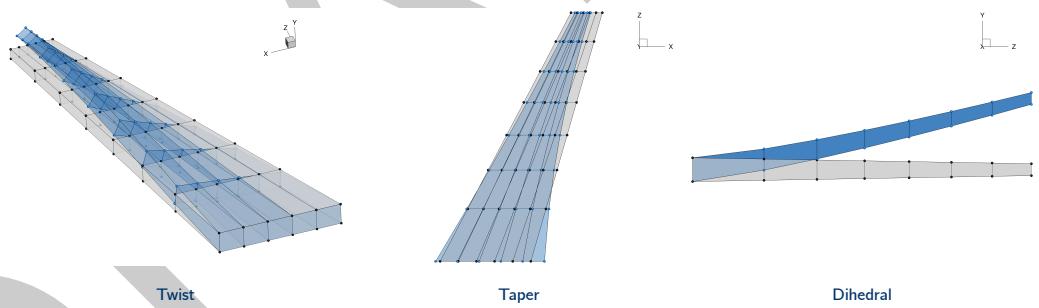
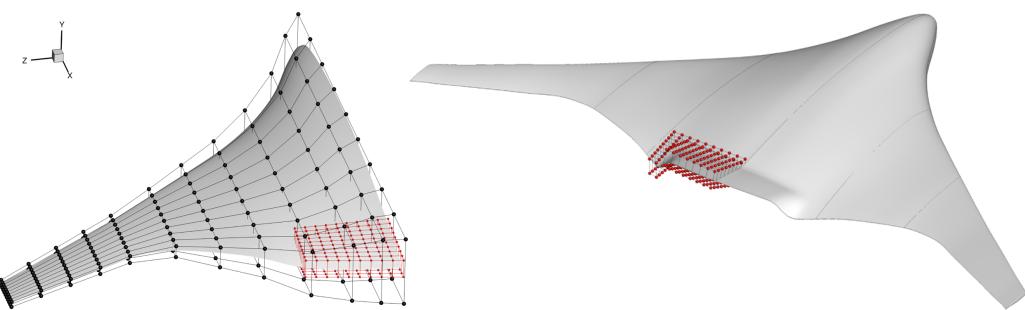


Figure 1: Examples of common wing planform design variables.

59 In addition to the basic FFD implementation, pyGeo offers two additional features: hierarchical  
 60 FFD and multi-component FFD.

#### 61 Hierarchical FFD

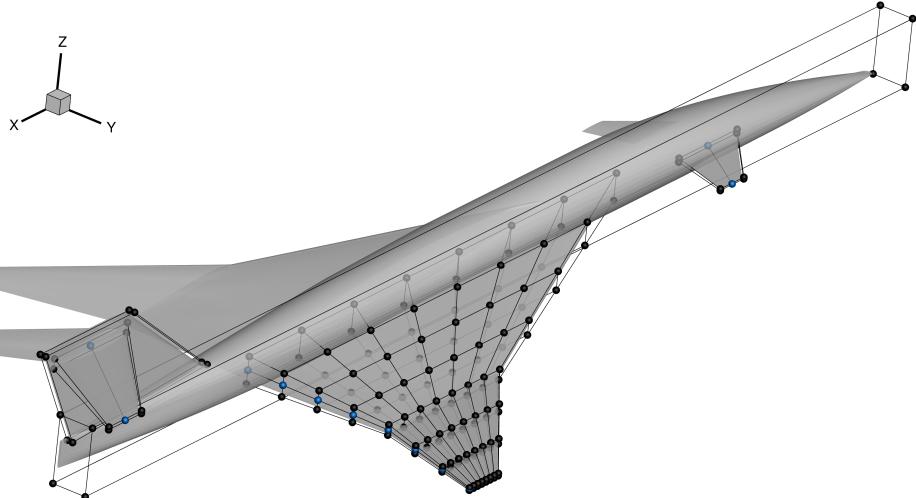
62 FFD objects can be organized in a hierarchical structure within pyGeo. Dependent, "child"  
 63 FFD blocks can be embedded in the main, "parent" FFD block to enable modifications on  
 64 a subset of the full geometry. pyGeo first propagates the parent deformations to both the  
 65 geometry and the child control points and then propagates the deformations of the child  
 66 control points to their subset of the geometry. One of the advantages of using this approach is  
 67 that each FFD block can have its own independent reference axis to be used for global design  
 68 variables such as rotations and scaling. This has facilitated the definition of control surface  
 69 deflections ([Lyu & Martins, 2014](#)) and hydrofoil design ([Liao et al., 2021](#)). [Figure 2](#) from the  
 70 former paper shows a case where the parent FFD block is used to manipulate the shape of an  
 71 entire wing of a blended wing body aircraft while the control surface on that wing is deformed  
 72 using a child FFD block.



**Figure 2:** Example of parameterization through parent-child FFD blocks (Lyu & Martins, 2014).

### 73 Multi-component FFD

74 The basic FFD implementation lacks flexibility when the geometry has intersecting components.  
 75 In such cases, pyGeo can parameterize each component using FFD and ensure a watertight  
 76 surface representation at the component intersections using an inverse-distance surface defor-  
 77 mation method (Yildirim et al., 2021). **Figure 3** shows an example of a component-based FFD  
 78 setup for a supersonic transport aircraft.



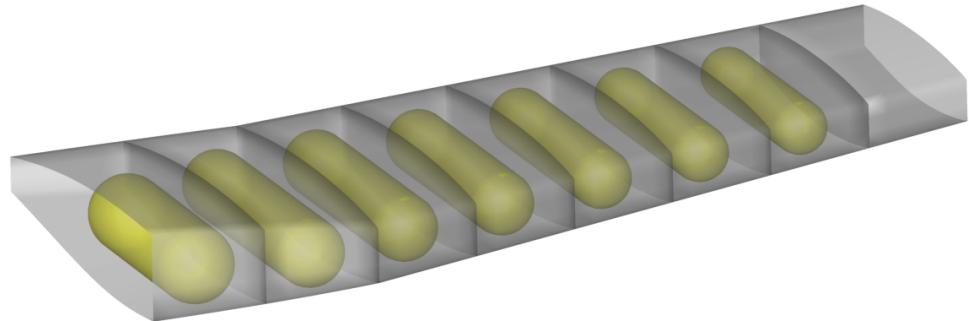
**Figure 3:** Example of FFD parameterization with intersecting components (Seraj & Martins, 2022).

### 79 Parametric Geometry Tools

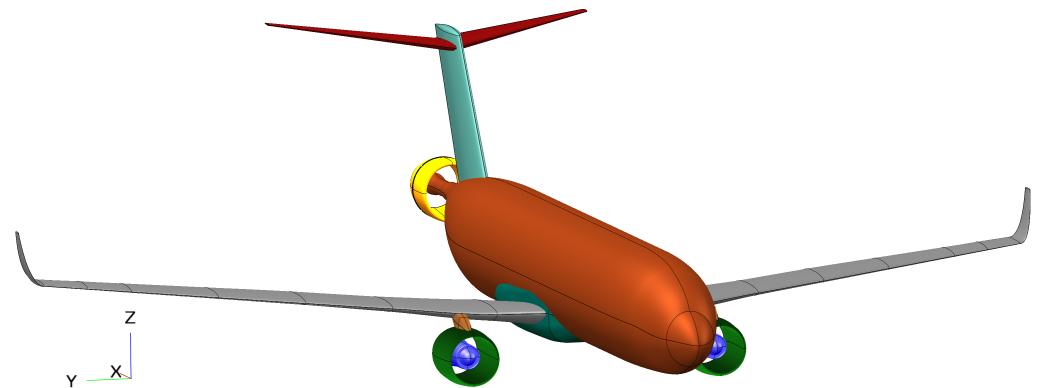
80 pyGeo contains interfaces to two parametric geometry tools, the Engineering Sketch Pad (ESP)  
 81 (Haines & Dannenhoffer, 2013) and OpenVSP (McDonald & Gloudemans, 2022). ESP is a  
 82 CAD software, while OpenVSP is a conceptual design tool. The two packages have different  
 83 capabilities, but both directly define the geometry with design variables, and the created  
 84 geometry can be used in external analysis tools.

85 pyGeo interfaces with ESP and OpenVSP in similar ways. In both cases, pyGeo takes an  
 86 instance of the model and its points are associated with coordinates in a mesh from a solver in  
 87 the MACH framework. For ESP and OpenVSP models, the pyGeo interface to the respective  
 88 software stores the model in a form usable within the MACH framework and updates it as  
 89 design variables are changed throughout the optimization. The pyGeo interface to ESP was  
 90 used by (Brelje & Martins, 2021) to parameterize hydrogen tanks (**Figure 4**) that were packaged

91 within an aircraft wing as part of an aerostructural optimization. pyGeo's OpenVSP interface  
 92 was used to parameterize the full aircraft configuration ([Figure 5](#)) studied in the aeropropulsive  
 93 optimization work in ([Yildirim et al., 2022](#)).



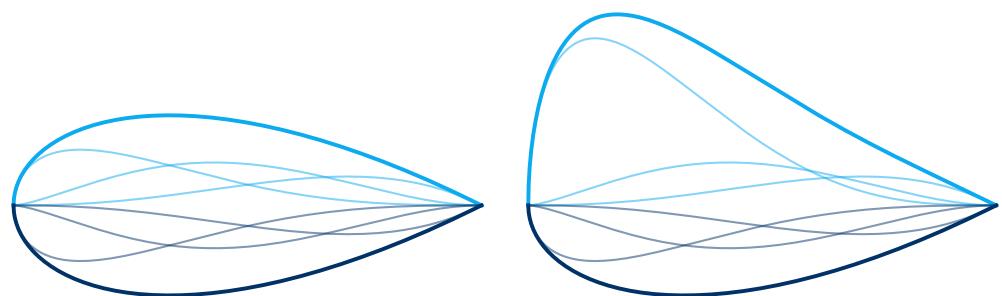
**Figure 4:** Example of ESP models of hydrogen tanks used through pyGeo ([Brelje & Martins, 2021](#)).



**Figure 5:** Example of a VSP aircraft model used through VSP's pyGeo interface ([Yildirim et al., 2022](#)).

#### 94    Class Shape Transformation

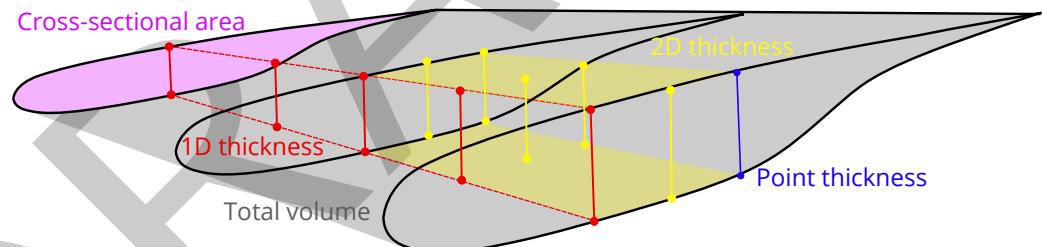
95    The class shape transformation (CST) methodology ([Kulfan, 2008](#)) is a popular airfoil pa-  
 96    rameterization. It generates a shape using Bernstein polynomials to scale a class function,  
 97    which is most often a base airfoil shape. pyGeo contains an implementation of this airfoil  
 98    parameterization that supports design variables for the Bernstein polynomial weightings, the  
 99    class function parameters, and the airfoil chord length. pyGeo's CST implementation can only  
 100   be used for 2D problems, such as airfoil optimization ([Figure 6](#)).



**Figure 6:** Airfoil defined by three CST coefficients on each surface undergoing a perturbation in one Bernstein polynomial.

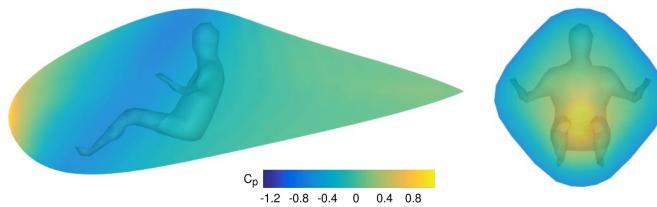
### 101 Constraints

102 pyGeo also includes geometric constraints to prevent geometrically undesirable designs. The  
 103 most commonly-used class of geometry constraints in pyGeo involves tracking one or more  
 104 linear dimensions on the optimized object's surface. These constraints are created by specifying  
 105 a single point, a line, or an array of points, along with a normal direction, then computing  
 106 two line-surface intersection points. Some commonly used geometric constraints in shape  
 107 optimization, such as thickness, area, and volume constraints ([Figure 7](#)) can be computed  
 108 using variations on this approach, which is computationally cheap and robust ([Brelje et al.,](#)  
 109 [2020](#)).



**Figure 7:** Thickness and volume constraints demonstrated on an wing section ([Brelje et al., 2020](#)).

110 If a more complex geometry needs to be integrated into an optimized surface, pyGeo supports  
 111 an alternative geometric constraint formulation based on arbitrary triangulated surfaces as  
 112 described in ([Brelje et al., 2020](#)) and illustrated in [Figure 8](#).



**Figure 8:** Triangulated surface constraint used to optimize an aeroshell around a complex geometry ([Brelje et al., 2020](#)).

## <sup>113</sup> Parallelism

<sup>114</sup> pyGeo can optionally work under distributed memory parallelism using MPI, which is a  
<sup>115</sup> requirement when interfacing with large-scale CFD applications. For example, the computational  
<sup>116</sup> mesh may be partitioned and distributed among many processors by the CFD solver, and each  
<sup>117</sup> processor may be aware of only its portion of the mesh. pyGeo can handle such scenarios by  
<sup>118</sup> independently manipulating the geometry on each processor and aggregating the constraints  
<sup>119</sup> across all processors when communicating with the optimizer.

## <sup>120</sup> Derivative Computation

In addition to geometry manipulation and constraints, pyGeo can compute derivatives of these operations with respect to design variables. For the geometric deformation, pyGeo can compute the Jacobian

$$\frac{dX_s}{dx},$$

<sup>121</sup> where  $X_s$  is the vector of surface mesh coordinates, and  $x$  is the vector of geometric design  
<sup>122</sup> variables.

Similarly, pyGeo can compute the constraint Jacobian

$$\frac{dg}{dx},$$

<sup>123</sup> where  $g$  is the vector of geometric constraints.

<sup>124</sup> For the FFD parameterization, these derivatives are computed using a combination of analytic  
<sup>125</sup> methods (Martins & Ning, 2021) and the complex-step method (Martins et al., 2003). For the  
<sup>126</sup> interfaces to OpenVSP and ESP, the derivatives are computed with parallel finite differences.  
<sup>127</sup> The CST derivatives are computed analytically.

## <sup>128</sup> Statement of Need

<sup>129</sup> Few open-source packages exist with comparable functionalities. To the authors' best knowledge,  
<sup>130</sup> the only other open-source CFD-based optimization framework that contains geometry  
<sup>131</sup> parameterization is SU2 (Economou et al., 2016). It supports Hicks–Henne bump functions  
<sup>132</sup> (Hicks & Henne, 1978) for airfoil optimizations and the FFD method for three-dimensional  
<sup>133</sup> cases. However, it cannot be used with other solvers because it is tightly integrated into the  
<sup>134</sup> CFD solver.

<sup>135</sup> While both OpenVSP and ESP can be used directly in optimization without using pyGeo,  
<sup>136</sup> they lack capabilities needed for high-fidelity MDO when used as stand-alone tools. pyGeo  
<sup>137</sup> fills in these gaps through parallelism, efficient gradients, and geometric constraints. It keeps  
<sup>138</sup> OpenVSP and ESP in the optimization loop and provides a standard interface to these tools  
<sup>139</sup> for their use with external solvers.

<sup>140</sup> pyGeo has been used extensively in aerodynamic and aerostructural optimizations in aircraft,  
<sup>141</sup> hydrofoil, and wind turbine applications. The different parameterizations within pyGeo have  
<sup>142</sup> all been necessary for different optimization problems, depending on the geometry involved.  
<sup>143</sup> The interface to ESP made it possible to parameterize hydrogen tanks within a combined  
<sup>144</sup> aerostructural and packaging optimization (Brelje & Martins, 2021). pyGeo's OpenVSP  
<sup>145</sup> interface was used in aeropropulsive optimizations (Yildirim et al., 2022).

<sup>146</sup> The implementation of CST airfoil parameterization was used to compare methods for airfoil  
<sup>147</sup> optimization (Adler et al., 2022). The method for using multiple FFD volumes has been used  
<sup>148</sup> to optimize a conventional aircraft (Yildirim et al., 2021), a T-shaped hydrofoil (Liao et al.,  
<sup>149</sup> 2022), and a supersonic transport aircraft (Seraj & Martins, 2022).

150 pyGeo is maintained and developed by the MDO Lab<sup>2</sup> at the University of Michigan and is  
151 actively used for MDO applications in both research and industry. The geometry parameter-  
152 ization capabilities provided by pyGeo have facilitated the development of environmentally  
153 sustainable aircraft through design optimization.

## 154 Acknowledgements

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