

Experiment 2- Impact of Jets

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Aim - To study the impact of jets on stationary surfaces

Working and CalculationsFor table 1 \Rightarrow Using reading 4 (Flat plate)

Given - Nozzle diameter - 6 mm

Weight added $m = 0.1 \text{ kg}$ Distance of weight $L = 37.2 \text{ cm}$ Time taken $t = 18.8 \text{ s}$ Amount of water $V = 5 \text{ litres}$

$$\text{Discharge: } V/t = \frac{5 \times 10^{-3}}{18.8} = 2.66 \times 10^{-4} \text{ m}^3/\text{s}$$

$$\text{Velocity } v = \frac{Q/\pi d^2/4}{\pi/4 \times (6 \times 10^{-3})^2} = \frac{2.66 \times 10^{-4}}{\pi/4 \times (6 \times 10^{-3})^2} = 9.40 \text{ m/s}$$

$$F_{th} = \rho A v^2 = 1000 \times \frac{\pi}{4} (6 \times 10^{-3})^2 \times (9.40)^2$$

$$= 2.50 \text{ N}$$

$$F_{expt} = \frac{mgl}{0.135} = \frac{0.1 \times 9.8 \times 37.2 \times 10^{-2}}{0.135} = 2.70 \text{ N}$$

$$\text{Errors} = \frac{F_{th} - F_{expt}}{F_{th}} \times 100 = \frac{2.50 - 2.70}{2.50} \times 100 = -7.94\%$$

For table 2: (Using reading 4, Hemispherical Plate)

Given nozzle diameter = 6mm

weight added $m = 0.2 \text{ kg}$

Distance of weight $L = 39.3 \text{ cm}$

Time taken = 15.83 s

Amount of water = $V = 5 \times 10^{-3} \text{ m}^3$

$$\text{Discharge} = \frac{5 \times 10^{-3}}{15.83} = 3.283 \times 10^{-4} \text{ m}^3/\text{s}$$

$$\text{Velocity} = \frac{Q}{\frac{\pi d^2}{4}} = \frac{3.283 \times 10^{-4} \text{ m}^3/\text{s}}{\frac{\pi (6 \times 10^{-3})^2}{4}} = 11.61 \text{ m/s}$$

$$F_R = \rho S A v^2 = 2 \times 1000 \times \frac{\pi}{4} \times (6 \times 10^{-3})^2 \times (11.61)^2 = 7.62 \text{ N}$$

$$F_{\text{expt}} = \frac{mgL}{0.135} = \frac{0.1 \times 9.8 \times 39.3}{0.135} = 5.71 \text{ N}$$

$$\text{Error} = \frac{F_R - F_{\text{expt}}}{F_R} \times 100 = \frac{7.62 - 5.71}{7.62} \times 100 = 25.16\%$$

Sources of error

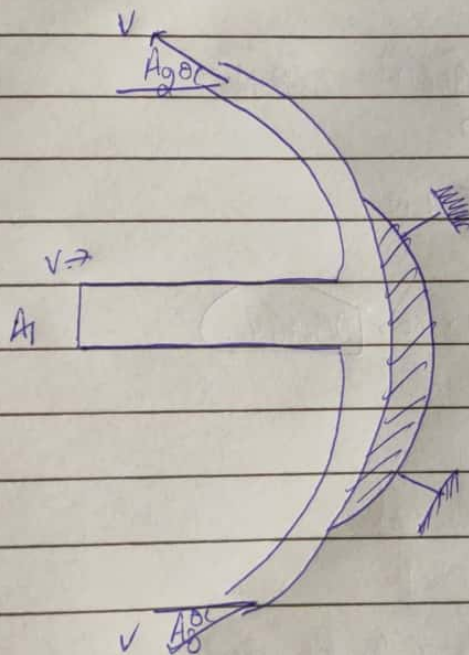
- we have neglected the frictional force in the calculation of theoretical force giving an error
- we have considered the collision to be elastic, which is not the case.
- Volume flux from the jet may not be uniform.
- Parallax error while measuring the length

Conclusion

- The graph of F vs v is almost parabolic - in accordance with the formula $F = \rho A v^3$
- For the flat plate, e_{loss} is negative i.e. $F_{\text{ex}} > F_{\text{th}}$ (Push) \Rightarrow This suggests that jet might not flow exactly horizontal but collides downwards, adding to the change in momentum.
- For the hemispherical plate, e_{loss} is positive i.e. $F_{\text{th}} > F_{\text{ex}}$. This may be due to the effect of friction which reduces the vertical velocity of rebounded water. Also we ^{assume} a complete 180° which might not be case. This results in a lower F_{ex}
- The magnitude of e_{loss} for hemispherical plate is much more than for the flat plate. This is mainly due to the fact that a factor of 2 is involved for calculation of the force. Also for the hemispherical plate, friction acts in both directions while it only acts in the horizontal direction for the latter case.

Questions

Q1)



From continuity
$$\frac{\partial}{\partial t} \int_V \rho dV + \int_{\partial V} \rho \vec{v} \cdot d\vec{A} = 0$$

$$\boxed{\frac{A_1}{2} = \frac{A_2}{2} = \frac{A_3}{2}}$$

Momentum equation in the horizontal direction

$$\sum \vec{F}_x = \frac{\partial}{\partial t} \int_C \rho \vec{v} dV + \int_S (\vec{v} \cdot d\vec{A}) \vec{v}$$

$$F_x = -\rho A_1 v^2 - \rho (v^2 A_2 \cos \theta + v^2 A_1 \cos \theta)$$

$$= -\rho A_1 v^2 (1 + \cos \theta)$$

Momentum equation in vertical direction

$$\sum F_y = \frac{\partial}{\partial t} \int_C \rho \vec{v} \cdot d\vec{V} + \int_S (\vec{v} \cdot d\vec{A}) \vec{v}$$

$$-\rho v_2 (A_2 \sin \theta - A_3 \sin \theta) = 0$$

Q2) We know due to friction $v_f = Kv$

from continuity eqn

$$\frac{\partial}{\partial t} \int_C \rho dV + \int_S \rho \vec{v} \cdot d\vec{A} = 0$$

$$-\rho A_1 v^2 - (\rho A_2 Kv^2 + \rho A_3 Kv^2) = 0$$

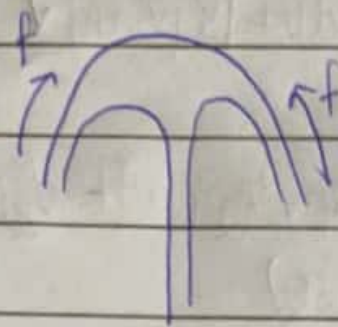
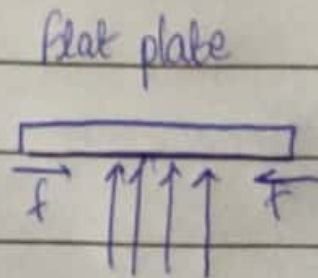
$$\boxed{\frac{A_1}{2K} = A_2 = A_3}$$

from momentum equation in horizontal direction and vertical direction

$$\boxed{F_x = -\rho A_1 v^2 (1 + K \cos \theta)}$$

$$F_y = 0$$

Q3) If we include friction, the result will change only in case of hemispherical plate. Friction in the case of the flat plate will cancel out.

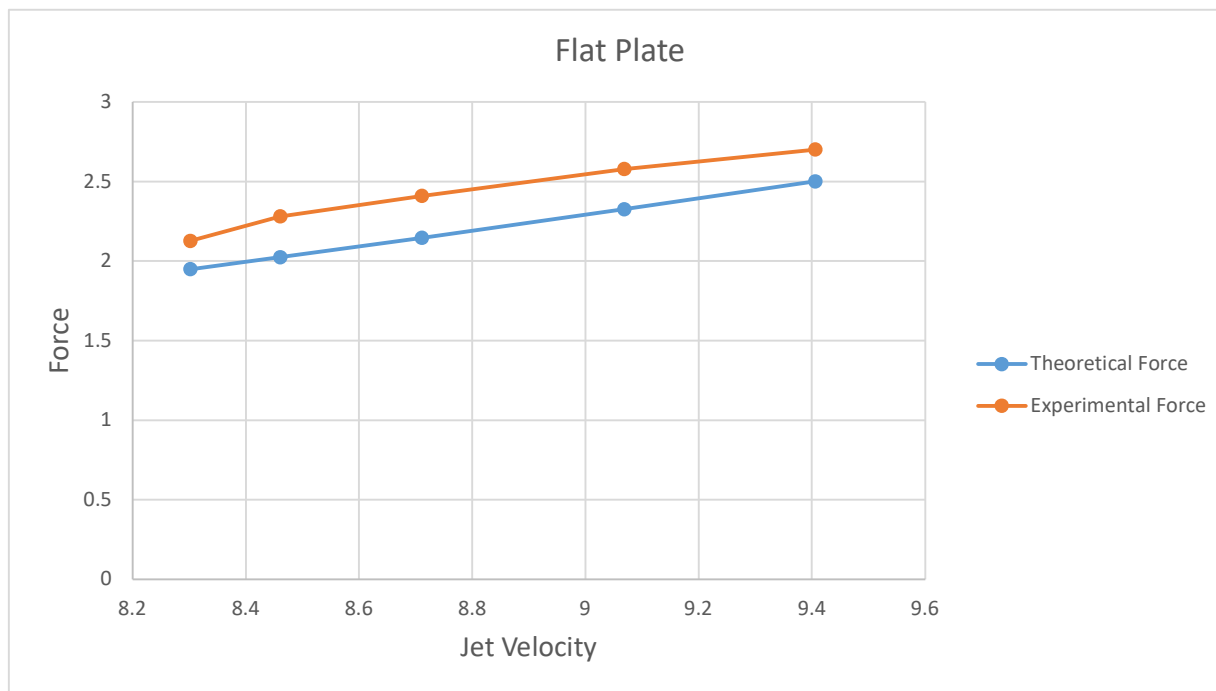


Hemispheric plate

In hemispheric plate, friction will have a vertical component as well.

$$g=9.81\text{m/s}^2$$

Sr. No.	Nozzle diameter, d (mm)	Type of vane	Weight added, m (kg)	Distance of sliding weight, L cm	Time for 5 litres rise in measuring tank, t (sec)	Discharge, Q (m^3/s)	Velocity, v (m/s)	Theoretical force, F_{th} (N)	Experimental force, F_{expt} (N)	Error (%)
0	6	Flat vanes	0.1	29.3	21.3	0.000234742	8.302292284	1.948894902	2.126962963	-9.13687343
1	6		0.1	31.4	20.9	0.000239234	8.461187831	2.024207615	2.279407407	-12.60739217
2	6		0.1	33.2	20.3	0.000246305	8.7112722	2.145633547	2.410074074	-12.32458952
3	6		0.1	35.5	19.5	0.00025641	9.068657726	2.325296853	2.577037037	-10.82615254
4	6		0.1	37.2	18.8	0.000265957	9.406320514	2.501680988	2.700444444	-7.94519596



$g=9.81\text{m/s}^2$

Sr. No.	Nozzle diameter, d (mm)	Type of vane	Weight added, m (kg)	Distance of sliding weight, L (cm)	Time for 5 litres rise in measuring tank, t (sec)	Discharge, Q (m^3/s)	Velocity, v (m/s)	Theoretical force, F_{th} (N)	Experimental force, F_{expt} (N)	Error (%)
0	6	Hemi-spherical vanes	0.2	31.8	16.9	0.000295858	10.46383584	6.191618839	4.616888889	25.43325083
1	6		0.2	33.8	16.4	0.000304878	10.78285522	6.574911721	4.907259259	25.36387609
2	6		0.2	36.2	16.1	0.000310559	10.98377799	6.822222355	5.255703704	22.96199933
3	6		0.2	37.7	15.8	0.000316456	11.19233074	7.083753632	5.473481481	22.73190506
4	6		0.2	39.3	15.23	0.000328299	11.61121639	7.62391096	5.705777778	25.15943841

