



ME338 – Manufacturing Process II

Lecture 5: Milling/Grinding/Drilling

Pradeep Dixit

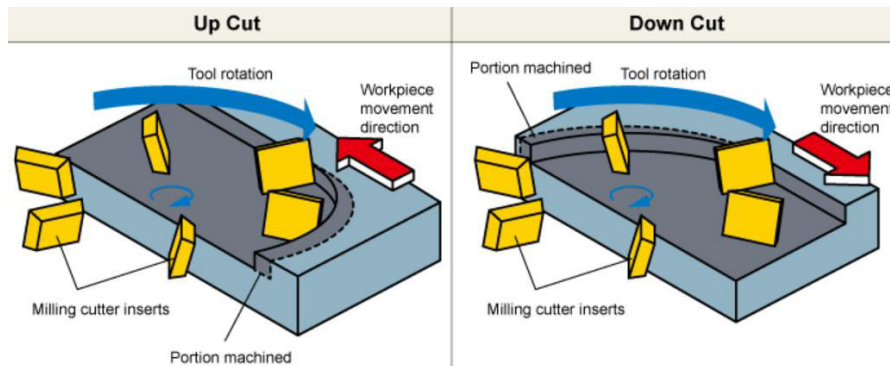
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http://www.mitsubishicarbide.com/en/technical_information
http://www.mitsubishicarbide.com/en/technical_information/tec_turning_tools/tec_external_turning

Milling techniques : Up & down



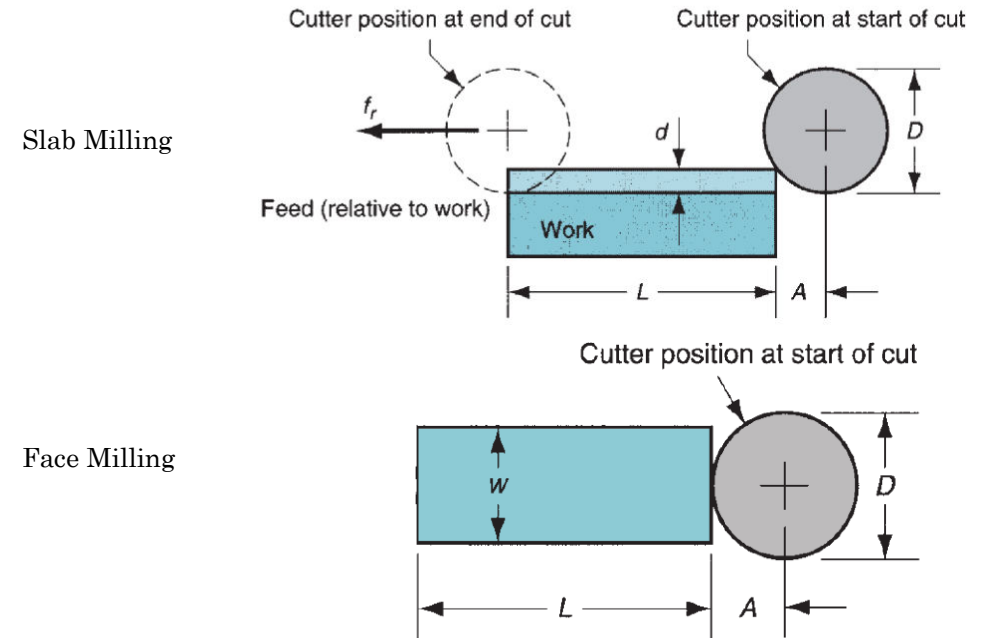
- Multiple cutting edges > higher MRR, all kinds of shapes can be generated
- Both Horizontal or vertical type : Based on the Cutter axis
- Arbor: Shaft on which milling cutter is mounted
- Up milling or down milling : decided by the conditions of the machine tool, the milling cutter and the application.
 - In terms of tool life, down cut (climb) milling is more advantageous.



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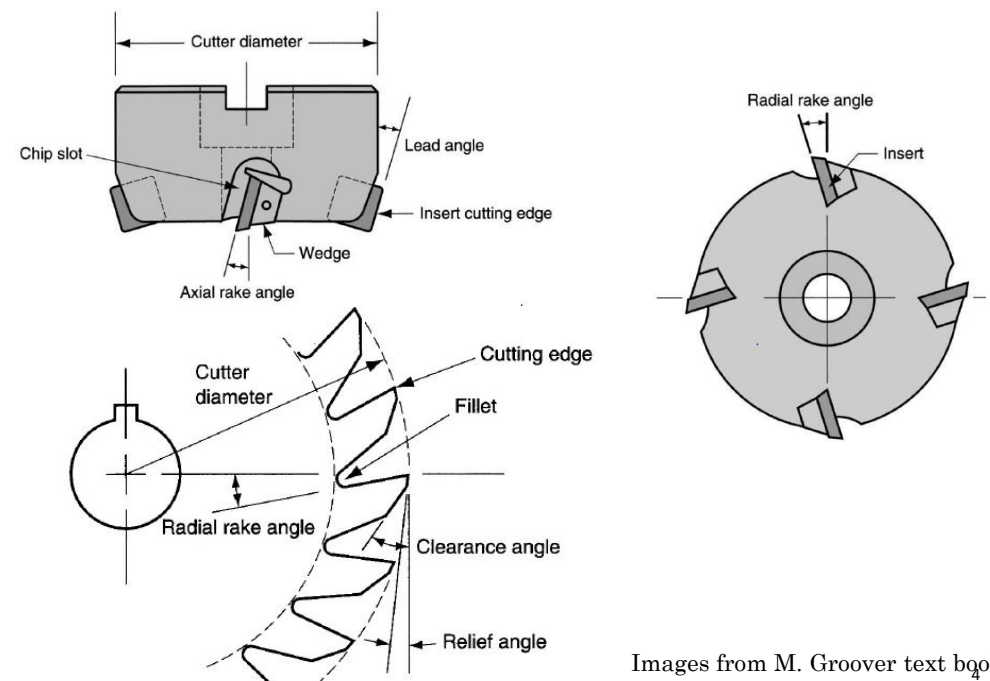
Milling process : Slab & face milling



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Geometry of milling cutter

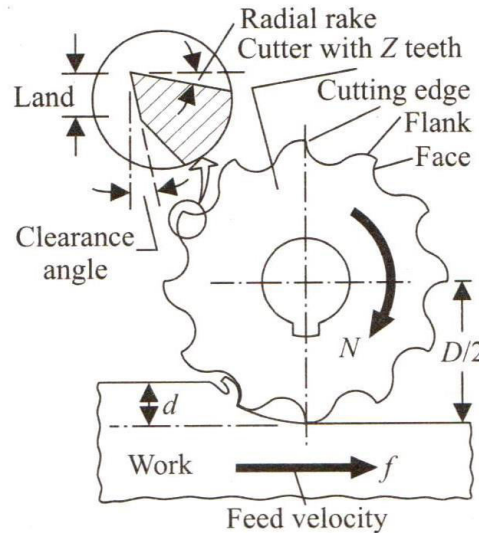


Images from M. Groover text book

Basic mechanics of slab milling process



- Milling has straight cut teeth
- Orthogonal machining
- Given feed f (mm/min),
- All teeth are participating in cutting action
- No of teeth: Z ,
- Rotation speed: N
- Effective feed/tooth: f/NZ
- Material removal rate per **unit width** of the job: $f \cdot d$



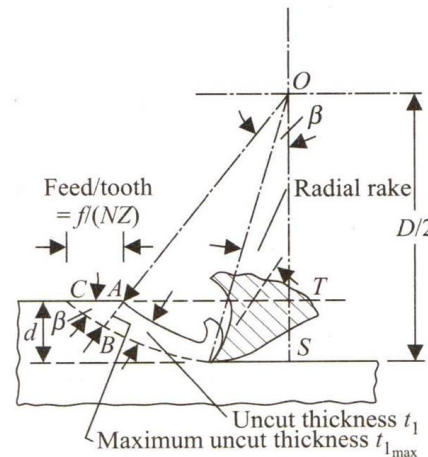
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Basic mechanics of slab milling process



- $AB \sim AC$. $\sin \beta$
– β angle included by the contact arc at the center
- $t_{1\max} = AC \cdot \sin \beta$
- From triangle OAT: $\cos \beta = OT/OA$
- $OT = D/2 - d$, $OA = D/2$
- $\sin \beta = 2(d/D)^{1/2}$
- $t_{0\max} = \frac{2f}{NZ} \sqrt{\frac{d}{D}}$ $t_{0\text{avg}} = \frac{f}{NZ} \sqrt{\frac{d}{D}}$
- Since, uncut chip thickness varies, F_c and F_t also changes as the cutting edge moves along the cut surface



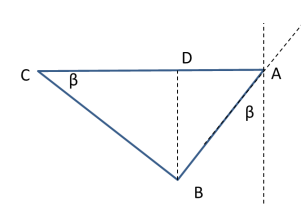
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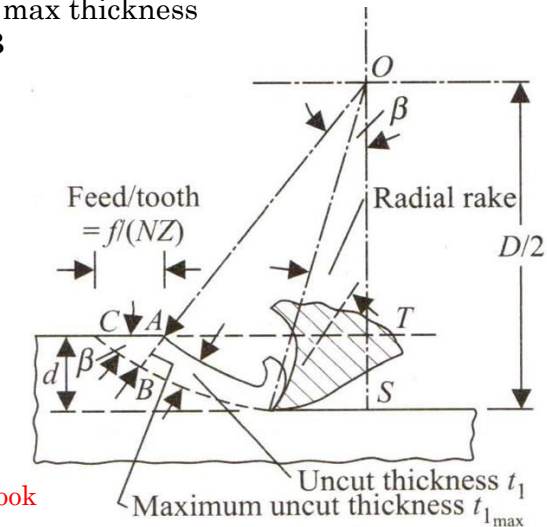
Basic mechanics of slab milling process



- Feed/tooth = $AC = f/NZ$
- Uncut chip thickness is not uniform (due to radial action of cutting), starts with zero and ends with max thickness
- Max uncut chip thickness = AB



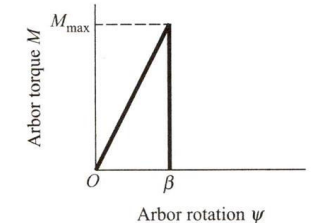
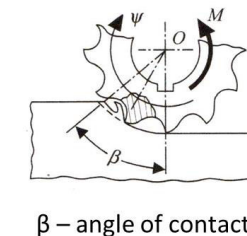
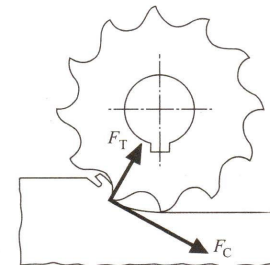
β is not friction angle here
Symbol used in Ghosh/mallick text book



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Forces & Torque in slab milling

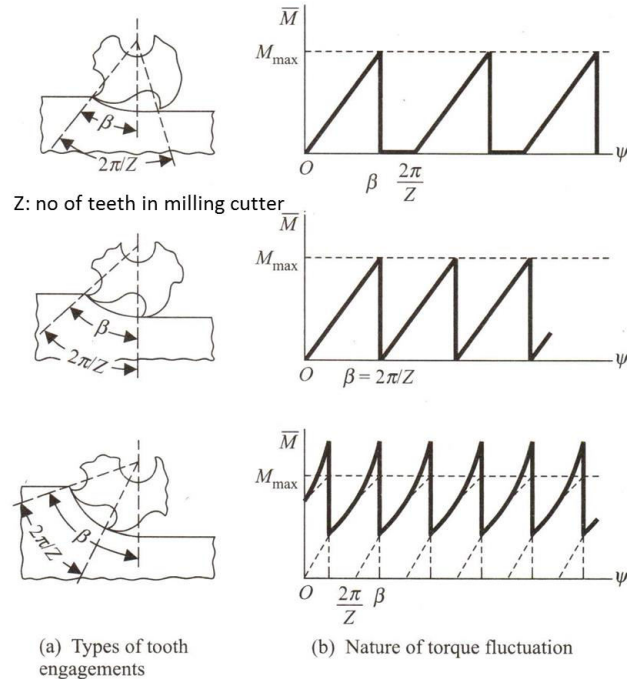


- Average uncut chip thickness (t_1) is known. Width w of cutter is known, so F_c and F_t can be calculated
- F_t acts in radial direction, so no torque due to F_t
- Torque is only generated due to cutting force F_c .
- Maximum torque $M_{\max} = (F_c \times D/2)$
- Avg Torque $M_{\text{avg}} = 0.5 \times M_{\max} \times (\text{angle of contact } \beta) / (\text{max angle allowed})$
- Max angle allowed = $2\pi / \text{No of teeth}$

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Milling torque fluctuations



Problem

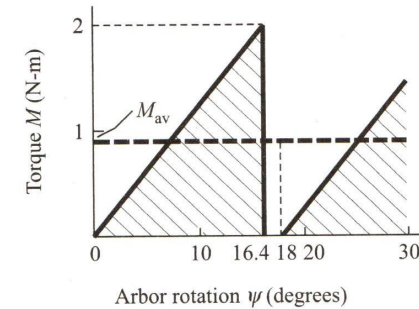
A mild steel (ms) block of 20 mm width is being milled using a straight slab milling cutter with 20 teeth, 50 mm diameter, and 10° radial rake. The feed velocity of the table is 15 mm/min and the cutter rotates at 60 rpm. If a depth of cut of 1 mm is used, what will be the power consumption?

- Assume coefficient of friction and shear strength
- Depth of cut d and cutter diameter D is known
- Angle of contact (β) can be found, $\beta=16.4^\circ$
- Total no of teeth $N = 20$, Angle per tooth = 18°
- Max uncut chip thickness t_{0max} can be found
- Shear strength τ , width w , depth of cut is known
- Cutting force F_c , F_t can be calculated

$$\sin \beta = 2 \sqrt{\frac{d}{D}}$$

$$t_{1max} = \frac{2f}{NZ} \sqrt{\frac{d}{D}}$$

Milling torque : example



- Torque is only generated due to cutting force F_c .
- Maximum torque $M_{max} = (F_c \times D/2)$
- Avg Torque $M_{avg} = 0.5 \times M_{max} \times (\text{angle of contact } \beta) / (\text{max angle allowed})$
- Max angle allowed = $2\pi/Z$, where Z no of teeth in milling cutter
- Total power consumption $P = T\omega$ $\omega = 2\pi N$

Problem

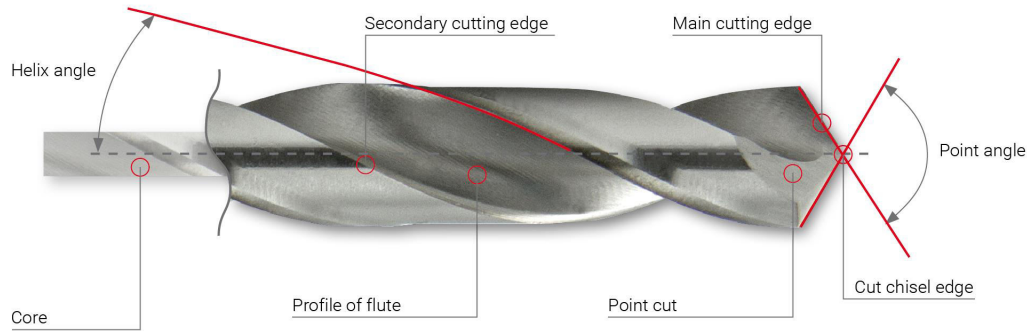
Estimate the power required during the up milling of a mild steel block of 20 mm width using a straight slab milling cutter with 10 teeth, 75 mm diameter, and 10° radial rake. The feed velocity of the table is 100 mm/min, the cutter rotates at 60 rpm, and the depth of cut is 5 mm.

- Assume coefficient of friction and shear strength
- Depth of cut d and cutter diameter D is known
- Angle of contact (β) can be found, $\beta=16.4^\circ$
- Total no of teeth $N = 20$, Angle per tooth = 18°
- Max uncut chip thickness t_{0max} can be found
- Shear strength τ , width w , depth of cut is known
- Cutting force F_c can be calculated
- Maximum torque $M_{Max} = (F_c \times D/2)$
- Avg Torque $M_{avg} = 0.5 \times M_{max} \times (\text{angle of contact } \beta) / (\text{max angle allowed})$

$$\sin \beta = 2 \sqrt{\frac{d}{D}}$$

$$t_{1max} = \frac{2f}{NZ} \sqrt{\frac{d}{D}}$$

Drilling process : Twist drill

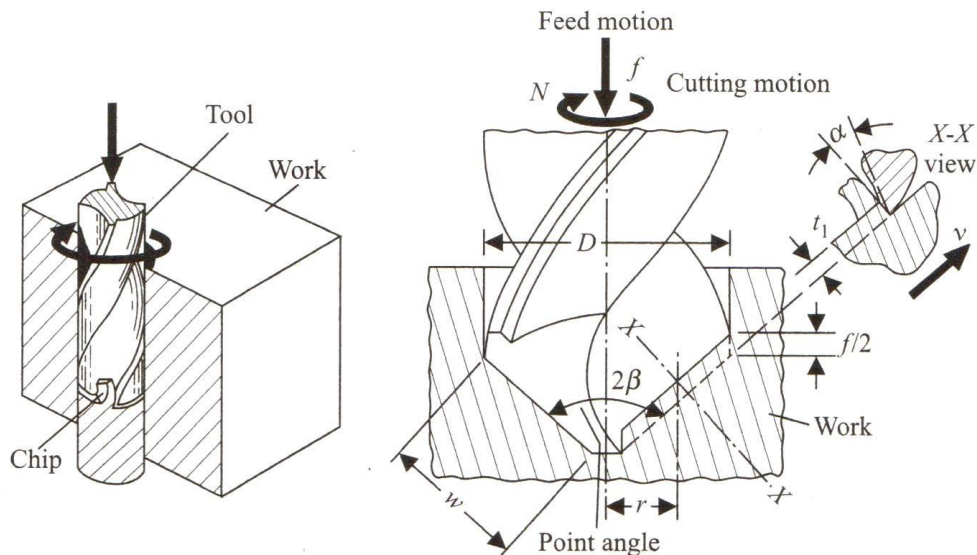


- Drill has two cutting edges, each 180° ahead of other edge
- Chip/coolant flows through the flutes

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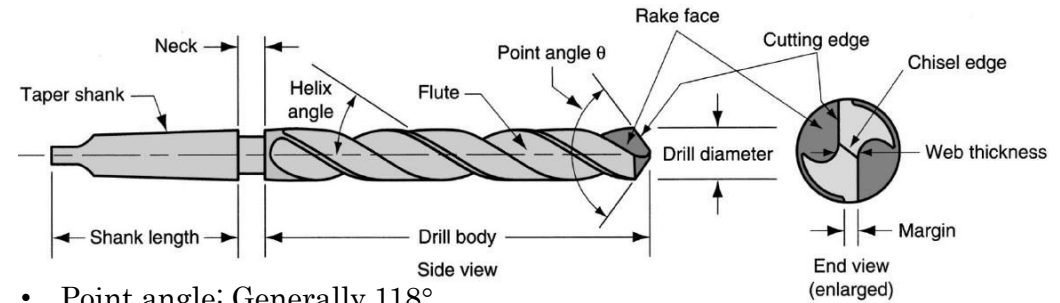
Analysis of drilling



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Geometry of Drill



- Point angle: Generally 118°
 - Smaller for soft / easy to machine materials
- Helix angle: determines the rake angle
 - Larger for soft materials
 - Rake angle decreases from circumference to the center
 - Chisel edge has a negative rake angle
- Web thickness: Rigidity of the tool
- Thicker for high hardness materials

Workpiece material	Point angle	Helix angle
Aluminum	90 to 135	32 to 48
Brass	90 to 118	0 to 20
Cast iron	90 to 118	24 to 32
Mild steel	118 to 135	24 to 32
Stainless steel	118 to 135	24 to 32
Plastics	60 to 90	0 to 20

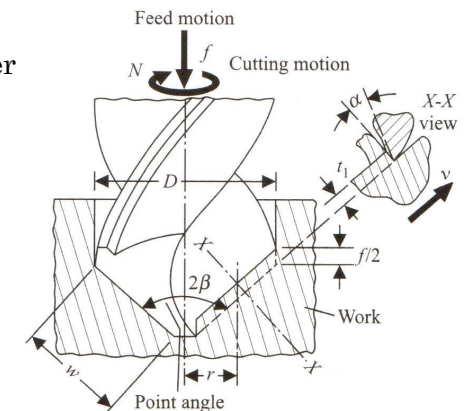
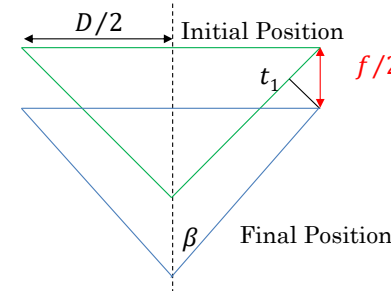
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Analysis of drilling



- Drill has two cutting edges, each 180° ahead of other edge
- In drilling, feed motion is given to drill (into the workpiece)
- If total advancement of the drill per revolution or feed is f , half of the feed motion ($f/2$) is shared by each cutting edge
 - Therefore, depth of cut is half of the feed motion
- Uncut chip thickness t_1 , width of cut w are:
 - $t_0 = (f/2) \sin \beta$, $w = (D/2) / \sin \beta$
 - β : half point angle, D : drill diameter

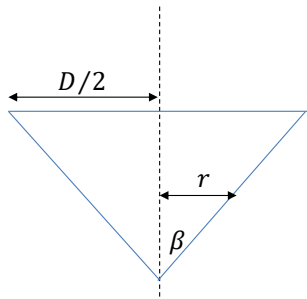


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- Normal rake angle depends upon the radial location of the sectioning plane.
- Normal rake angle depends upon the helix angle (ψ) and half-point angle (β) of the drill
- Approximate value of normal rake angle at a radial distance (r) is
 - $\alpha \approx \tan^{-1} \left[\frac{2r}{D} \tan \psi \right]$
 - r radius of the point on the cutting edge, where the normal rake angle is measured, ψ helix angle



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Example : Drilling



- Estimate the torque and the thrust force when drilling a solid block of mild steel with a normal twist drill made of HSS (point angle 118° , Helix angle: 30°). Drill diameter: 20 mm, Shear strength of mild steel: 400N/mm². Drill rotational speed: 240 rpm. Feed: 0.25 mm/rev. Friction coefficient between HSS and mild steel is 0.6.

Solution:

$$\alpha \approx \tan^{-1} \left[\frac{2r}{D} \tan \psi \right]$$

$$t_0 = (f/2) \sin \beta$$

$$w = (D/2) / \sin \beta$$

- First find normal rake angle
- Find uncut chip thickness (t_0) and width of cut (w)
- Find the friction angle (λ): $\lambda = \tan^{-1} \mu$
- Use Lee-Shaffer theory (or any given theory) and find shear plane angle ϕ
- Find shear force $F_s = \tau A_s = \tau w \frac{t_0}{\sin \phi}$
- Find cutting force (F_c) and thrust force (F_t)
- Total moment $M \approx 0.625 F_c D$
- Total thrust force $F \approx 5.4 F_t \sin \beta$

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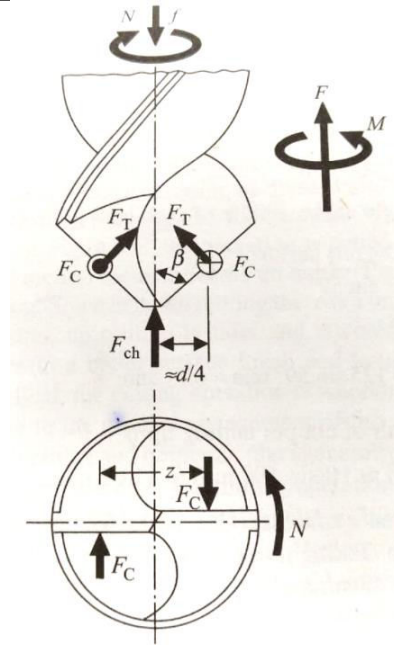
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- Total thrust force F
 - $F = 2F_T \sin \beta + F_{ch} + F_{friction}$
 - F_{ch} force from chisel edge (60% of the total thrust force $\approx 0.60F$)
 - $F_{friction}$ friction force ($\approx 0.03F$)
- $2F_T \sin \beta \approx 0.37F$, $F = 5.4 F_T \sin \beta$

Total Moment

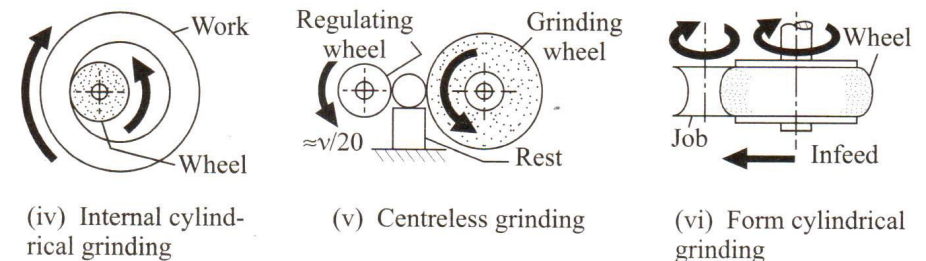
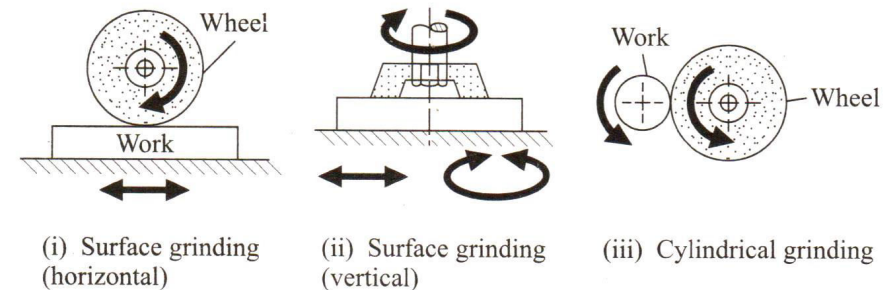
- $M = F_c z + M_{ch} + M_{friction}$
- M_{ch} moment from chisel edge ($\approx 0.08M$)
- $M_{friction}$ moment due to friction ($\approx 0.12M$)
- $\approx 80\%$ contribution of moment comes from the cutting action of the lips (i.e.,)
- $F_c z = 0.8M$, $M = 1.25 F_c z$
- At $z = \frac{D}{2}$, $M = 0.625 F_c D$



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Grinding Process : various kinds



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Grinding wheels



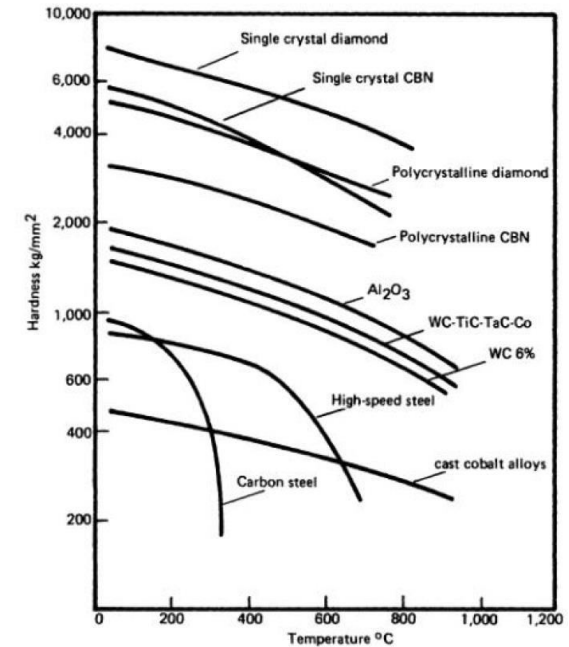
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Hardness of common abrasives used in Grinding



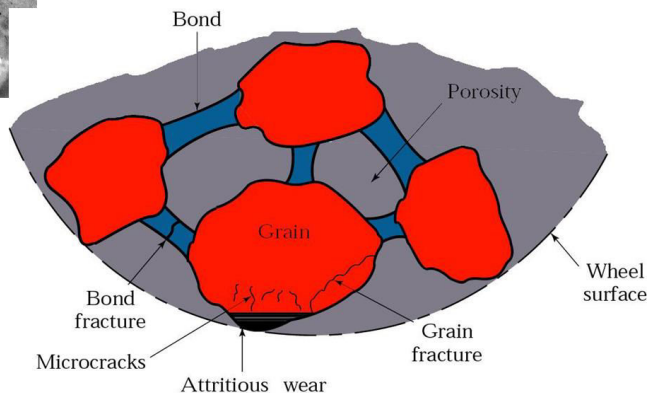
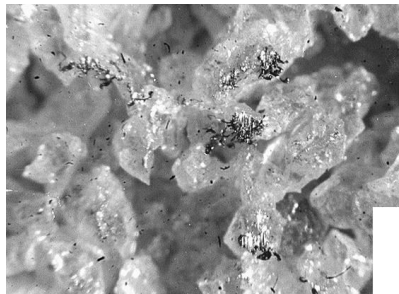
Material	N/mm ²
Common glass	300–5000
Quartz	8000
Hardened steel	7000–13,000
Emery	14,000
Tungsten carbide	18,000–24,000
Aluminium oxide	20,000–30,000
Titanium carbide	18,000–32,000
Silicon carbide	21,000–30,000
Boron carbide	28,000
Diamond	70,000–80,000



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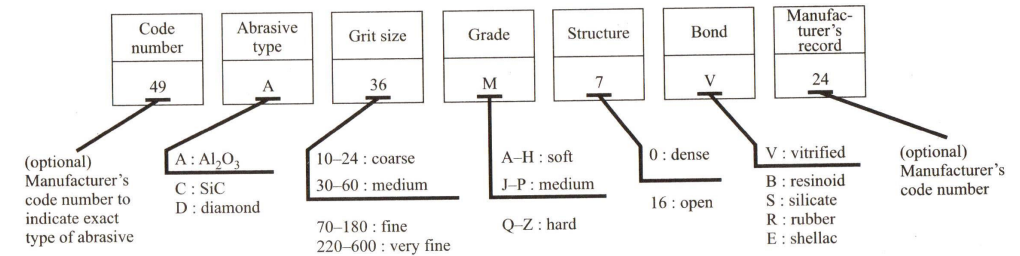
Grinding wheel surface



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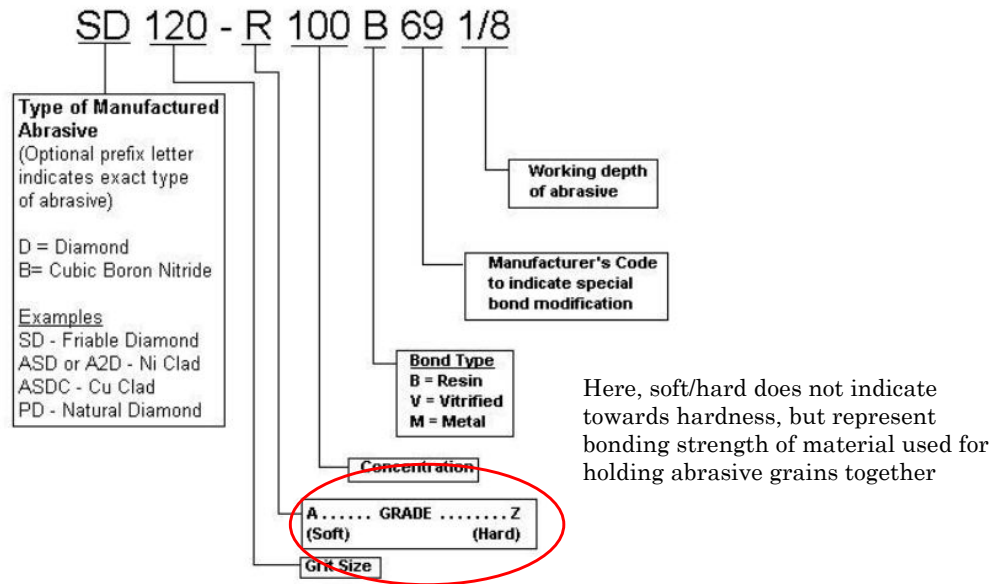
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Grinding wheels - specification



- Abrasive type:
 - A (Al₂O₃), B (cubic boron nitride), C (SiC), D (diamond). For ferrous material, Al₂O₃ used
- Grit size: higher grit number for fine polishing
 - 10-24 (coarse), 30-60 (medium), 70-180 (fine), 220-600 (super fine)
- Grade: strength of bonding materials to keep abrasive grains
 - A-I (Soft), J-P (Medium), Q-Z (Hard)
 - For harder work materials, soft bonding material, For softer work, hard bonding material
- Structure: voids/porosity in grinding wheel : 0 (dense), 16 (open)
 - Ductile material produces larger chips so open structure is recommended
 - For harder, brittle material, dense structure should be used
- Bond: V (Vitrified), B (resinoid), S (Silicate), R (Rubber), E (Shellac)
 - Vitrified bond material is the most common

Grinding wheels - specification

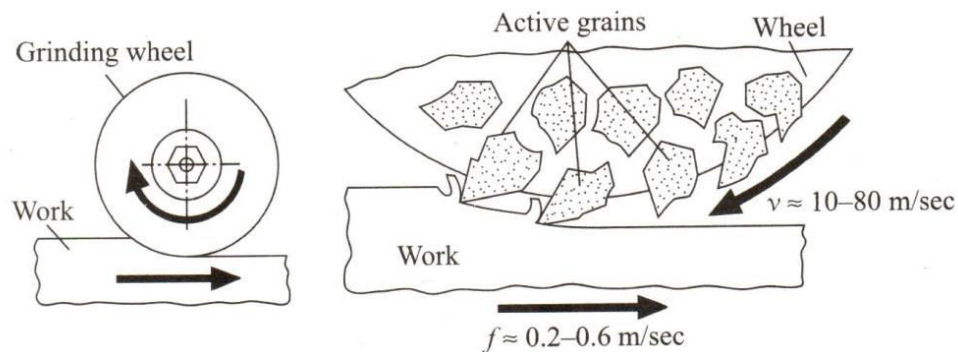


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Analysis of surface grinding



- Grinding: Rectangular cross-section is being fed radially at a rate f (mm/min)
- Assumed that active grains are uniformly distributed,
- If Z = total no of active grains, N = rpm of grinding wheel, effective feed per active grain = f/NZ
- Uncut chip thickness (t_1) is almost equal to $\sim f/NZ$

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Grinding wheel dressing



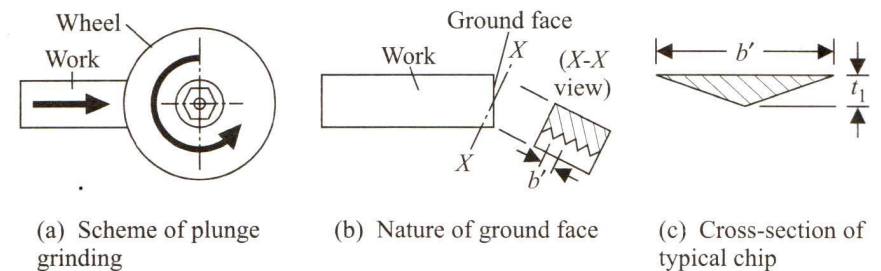
- Normally grinding wheel have self-sharpening characteristics
- Dull abrasive grains automatically removed due to fracture, and new sharpen grains are exposed
- In dense structure, chips clogg the voids between the abrasive grains
- This reduces the metal removal rate
- To avoid it, wheels are 'dressed'. It removes the clogged chips and expose the fresh abrasive grains.

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Grinding - mechanics



- If grinding wheel diameter is D and rotation speed is N rpm, then cutting speed $v = \pi DN$
- Material removal rate in grinding (MRR) = vfd ,
• where f – feed, d – depth of cut
- Chips produced in grinding have a triangular cross-section
- Ratio (r_g) of chip thickness (t_1) to chip width (b') is about 10-20,
 $b' = r_g \cdot t_1$
- No of grains/revolution $Z = \pi DCb'$, C : surface density of active grains

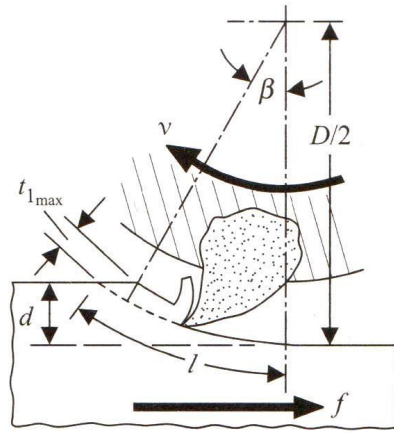
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Chip formation during grinding



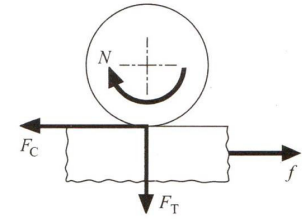
- $\cos \beta = \frac{(\frac{D}{2} - d)}{\frac{D}{2}} = 1 - 2\frac{d}{D}$
- $\cos \beta = 1 - \frac{\beta^2}{2}, \beta = 2\sqrt{\frac{d}{D}}$
- The chip length $l = \sqrt{Dd}$
- Total volume of material removed per unit time = $f \cdot d \cdot b$
- Where b is width of the cut in mm
- The chips produced during grinding have a triangular cross-section,
- and ratio (r) of chip thickness (t) to chip width (w) is about 10-20
- $t_{1max} = \sqrt{\frac{6f}{\pi D N C r_g}} \sqrt{\frac{d}{D}}$



Grinding - mechanics



- No of grains/revolution $Z = \pi D C b'$,
 - C : surface density of active grains
- Uncut chip thickness $t_0 = \sqrt{\frac{f}{\pi D N C r_g}}$
- Once t_0 is known, specific energy U_c can be determined as $U_c = U_0 t_0^{-0.4}$
- Power required to grind $W = \frac{A f U_c}{60}$,
 - A = cross-sectional area of job (mm^2)
- Force per single grit $F_c = \frac{60000 W}{\pi D A C N}$
- or $F_c = \frac{1000 f U_c}{\pi D C N}$



Material	U_0 (J/mm ³)
Steel	1.4 – 4.0
Stainless steel	1.4 - 1.6
Al alloys	0.35
Copper	1.2