Boosting

AdaBoost, Gradient Boosting, XGboost

DS 6030 | Fall 2024

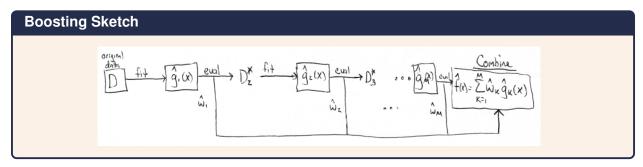
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1 Boosting

Boosting is a *sequential* ensemble method.



- A boosting model can be written as a generic ensemble
 - *M* is the number of base learners
 - \hat{a}_k is the weight for the kth base learner ($\hat{a}_k \ge 0$).
 - $\hat{g}_k(x)$ is the prediction from the kth base learner

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \, \hat{g}_k(x)$$

• The key distinction of boosting models is that the base learners are **fitted sequentially**, and the best model at stage m+1 is dependent on all models fit up to stage m.

$$\hat{f}_{m+1}(x) = \underset{a, g(x)}{\operatorname{arg \, min}} \sum_{i=1}^{n} L(y_i, \hat{f}_m(x_i) + a g(x_i))$$

- Boosting is primarily a bias reducer
 - The base models are often simple/weak (low variance, but high bias) models (like shallow trees)
- The complexity of the final model is based on i) the complexity of the base learners, ii) the number of iterations M, and iii) the magnitude of the ensemble weights a_k
 - Boosting models will overfit as the number of iterations increases
 - * Early stopping is necessary
 - * Less of a problem for hard classification problems with balanced data
 - Can apply shrinkage (making a_k smaller), to reduce complexity
- There are two main versions of boosting:
 - Gradient Boosting: fits the next model in the sequence $\hat{g}_k(x)$ to the (pseudo) residuals calculated from the predictions on the previous models
 - AdaBoost: fits the next model to sequentially weighted observations. The weights are proportional to the how poorly the current models predict the observation.

2 AdaBoost

AdaBoost was motivated by the idea that many *weak* leaners can be combined to produce a *strong* aggregate model.

- AdaBoost is for binary classification problems
- Trees are a popular base learner
 - Weak learners are usually used. For trees, this means shallow depth.
- At each iteration, the current model is evaluated.
 - The *ensemble weight* of model k is based on its performance (on all the training data)
 - The observation weight of observation i is increased if it is mis-classified and decreased if it is correctly classified.
 - Thus, at each iteration, those observations that are mis-classified are weighted higher and get extra attention in the next iteration.
- Because Adaboost uses hard-classifiers, it is sensitive to unbalanced data and unequal misclassification costs.
 - Because the thresholds are set at p > .50
 - There are, of course, ways to account for unbalance and unequal costs in the algorithm
 - An improvement to AdaBoost, *LogitBoost* explicitly attempts to estimate the class probability during each iteration which will allow easier post-fitting adjustments for unequal costs

Weighted Loss Functions (with observations weights)

Let $w_i \ge 0$ be a weight associated with observation i. The weighted loss for predictions $\hat{\mathbf{y}} = \hat{y}_1, \hat{y}_2, \dots, \hat{y}_n$ is

$$L(\mathbf{y}, \mathbf{\hat{y}}, \mathbf{w}) = \sum_{i=1}^{n} w_i L(y_i, \hat{y}_i)$$

2.1 Adaboost Algorithm

Algorithm: AdaBoost (Discrete)

Inputs:

- $D = \{(x_i, y_i)_{i=1}^n, \text{ where } y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M or other stopping criteria

Algorithm:

- 1. Initialize observation weights $w_i = 1/n$ for all i
- 2. For k = 1 to M:
 - a. Fit a classifier $\hat{g}_k(x)$ that maps (x_i, w_i) to $\{-1, 1\}$. In other words, the classifier must make a hard classification using weighted observations.
 - b. Compute the weighted mis-classification rate

$$e_k = \frac{\sum_{i=1}^n w_i \, \mathbb{1}(y_i \neq \hat{g}_k(x_i))}{\sum_{i=1}^n w_i}$$

Note: $0 \le e_k \le .5$ since model fit and evaluated on same training data.

c. Calculate the *coefficient* for model *k* (*ensemble weight*)

$$\hat{a}_k = \log\left(\frac{1 - e_k}{e_k}\right)$$

Note: $0 \le a_k < \infty$.

d. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

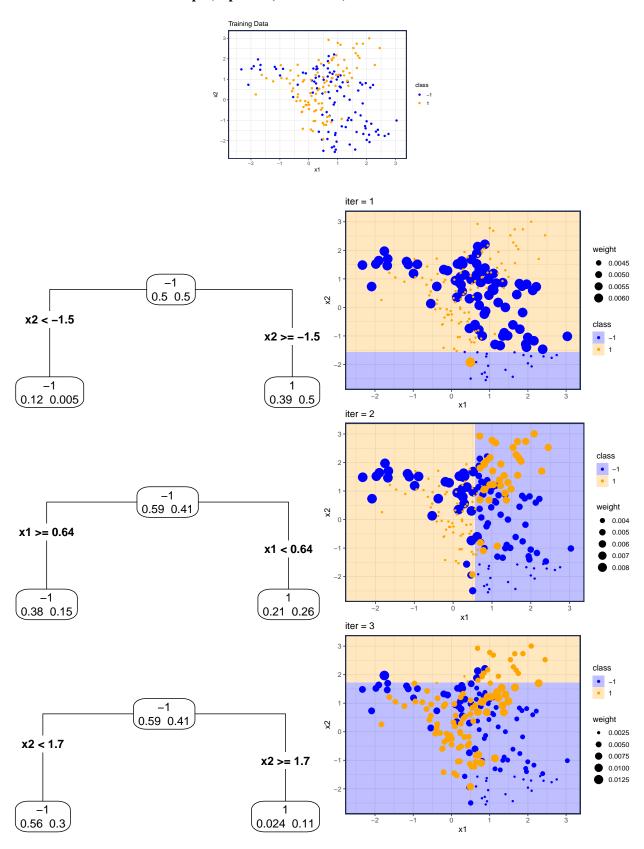
$$\begin{split} \tilde{w}_i &= w_i \cdot \exp\left(\hat{a}_k \cdot \mathbb{1}(y_i \neq \hat{g}_k(x_i))\right) \\ &= \begin{cases} w_i \frac{1 - e_k}{e_k} & \text{if obs } i \text{ is misclassified} \\ w_i & \text{if obs } i \text{ is correctly classified} \end{cases} \\ w_i &= \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j} & \textit{(re-normalize weights)} \end{split}$$

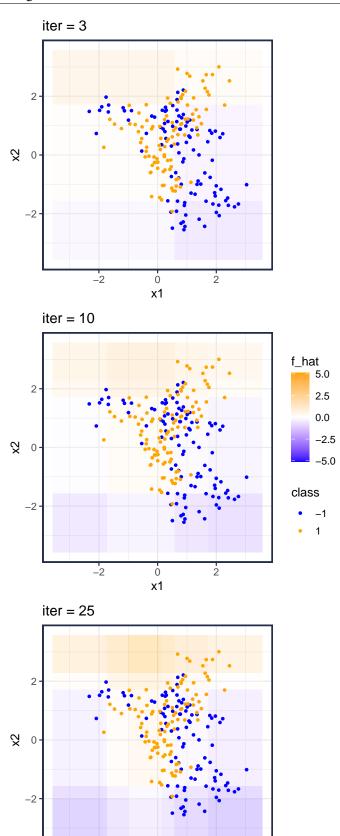
3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \, \hat{g}_k(x)$$

- Where $\hat{f}_k(x)=\hat{a}_k\,\hat{g}_k(x)$ Hard classification: $\hat{f}_M(x)>0$ Or remap to a probability $\hat{p}(x)=\frac{e^{2\hat{f}(x)}}{1+e^{2\hat{f}(x)}}$ for thresholding

2.1.1 Illustration with Stumps (depth = 1, n.nodes=2)

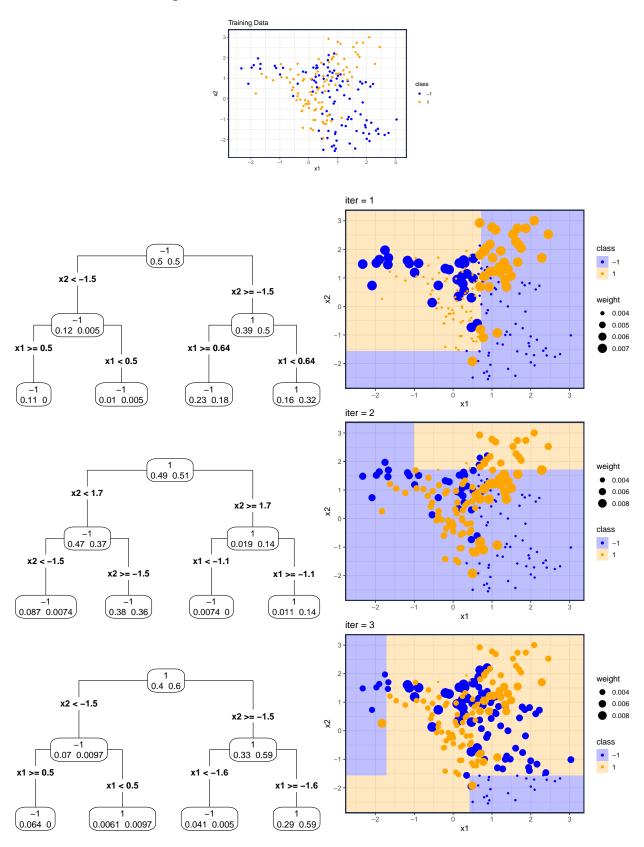




-2

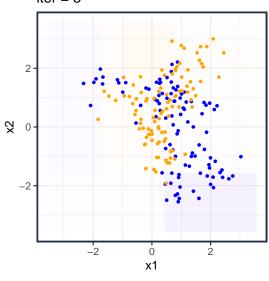
0 x1 2

2.1.2 Illustration with depth = 2, n.nodes=4

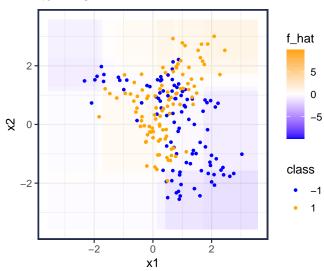




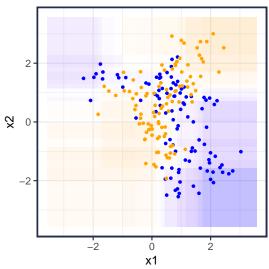
AdaBoost, Gradient Boosting, XGboost

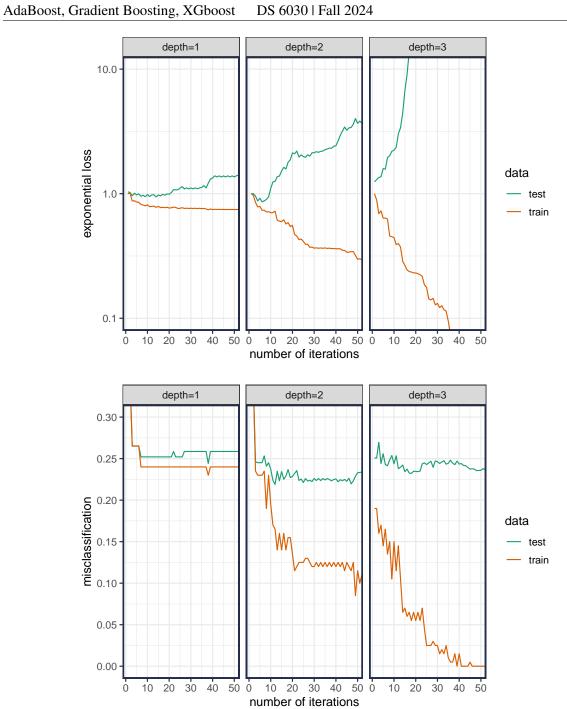


iter = 10



iter = 25





2.2 AdaBoost Details

- Adaboost uses an outcome variable of $y \in \{-1, 1\}$
- AdaBoost implicitly uses the loss function:

$$L(y, f) = e^{-yf}$$

$$= \begin{cases} e^{-f} & y = +1 \\ e^{f} & y = -1 \end{cases}$$

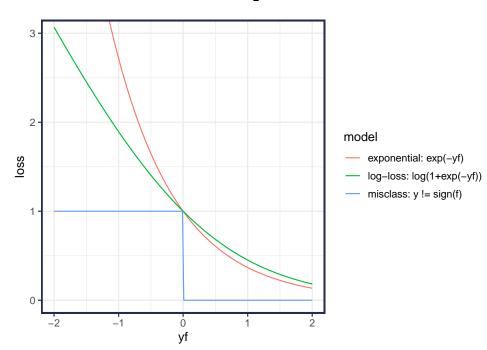
• Adaboost estimates the probability that Y = +1 as

$$\hat{p}(x) = \frac{e^{\hat{f}_M(x)}}{e^{-\hat{f}_M(x)} + e^{\hat{f}_M(x)}}$$
$$= \frac{e^{2\hat{f}_M(x)}}{1 + e^{2\hat{f}_M(x)}}$$

where $p(x) = \Pr(Y = +1 \mid X = x)$

• And $\hat{f}(x)$ is an estimate of

$$\hat{f}_M(x) = \frac{1}{2} \log \frac{\hat{p}(x)}{1 - \hat{p}(x)}$$
$$= \frac{1}{2} \operatorname{logit} \hat{p}(x)$$



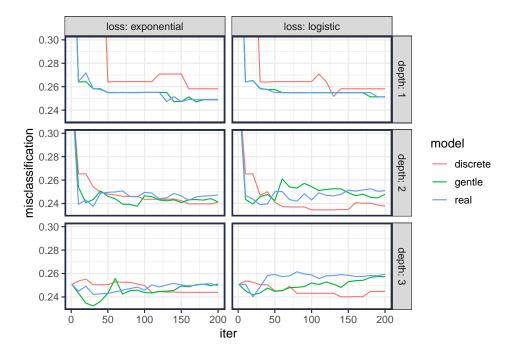
• Comparison with logistic regression (using log-loss / negative binomial log-likelihood)

$$\begin{split} &- \ \hat{f}(x) = \text{logit} \ \hat{p}(x) \\ &- \ \hat{p}(x) = \frac{e^{\hat{f}_M(x)}}{1 + e^{\hat{f}_M(x)}} \\ &- \ \text{Log-loss:} \ \log(1 + e^{-yf}) \ (\text{using} \ y \in \{-1, +1\}) \end{split}$$

2.3 R package ada

The R package ada provides an implementation of AdaBoost (and related methods).

- See Friedman, J., Hastie, T., and Tibshirani, R. (2000). Additive Logistic Regression: A statistical view of boosting. Annals of Statistics, 28(2), 337-374. for the details of model variations
 - {Discrete, Real, Gentle} AdaBoost
 - Logitboost



Algorithm: Real AdaBoost

Inputs:

- $D = \{(x_i, y_i)_{i=1}^n, \text{ where } y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{q}
- Maximum number of iterations, M

Algorithm:

- 1. Initialize observation weights $w_i = 1/n$ for all i
- 2. For k = 1 to M:
 - a. Fit a model $\hat{g}_k(x)$ that uses weighted inputs (x_i,w_i) to estimate a probability $\hat{p}_k(x) = \widehat{\Pr}(Y=1 \mid X=x)$. In other words, the classifier must make a soft classification using weighted observations.

b. Set
$$f_m(x) = \frac{1}{2} \operatorname{logit} \hat{p}_k(x)$$

c. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

$$ilde{w}_i = w_i \cdot \exp\left(-y_i \hat{f}_m(x_i)\right)$$
 $w_i = \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j}$ (re-normalize weights)

3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{f}_k(x)$$

- Hard classification: $\hat{f}_M(x) > 0$
- Or remap to a probability $\hat{p}(x) = \frac{e^{2f}}{1 + e^{2f}}$ for thresholding

Algorithm: Gentle AdaBoost

Inputs:

- $D = \{(x_i, y_i)_{i=1}^n, \text{ where } y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{q}
- Maximum number of iterations, M

Algorithm:

- 1. Initialize observation weights $w_i = 1/n$ for all i and $f_0(x) = 0$
- 2. For k = 1 to M:
 - a. Fit a model $\hat{g}_k(x)$ with weighted least squares that estimates y_i using features x_i and weights w_i .
 - b. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

$$\tilde{w}_i = w_i \cdot \exp\left(-y_i \hat{g}_m(x_i)\right)$$

$$w_i = \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j} \qquad (re\text{-normalize weights})$$

3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^{M} \hat{g}_k(x)$$

• Hard classification: $\hat{f}_M(x) > 0$

Algorithm: LogitBoost

Inputs:

- $D = \{(x_i, y_i)_{i=1}^n, \text{ where } y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M
- Let $y_i^* = (y+1)/2 \in \{0,1\}$

Algorithm:

- 1. Initialize observation weights $w_i = 1/n$ for all i and $f_0(x) = 0$
- 2. For k = 1 to M:
 - a. Like in newton-raphson for logistic regression, calculate the working response and weights for all observations

$$z_i = \frac{y_i^* - p_i}{p_i(1 - p_i)}$$
$$w_i = p_i(1 - p_i)$$

- b. Fit a model $\hat{g}_k(x)$ with weighted least squares that estimates z_i using features x_i and weights w_i .
- c. Update $\hat{f}_k(x) = \hat{f}_{k-1}(x) + \hat{g}_k(x)/2$ and $p_i = e^{\hat{f}_k(x)}/(e^{\hat{f}_k(x)} + e^{-\hat{f}_k(x)})$
- 3. Output final ensemble $\hat{f}_M(x) \in \mathbb{R}$

$$\hat{f}_M(x) = \sum_{k=1}^{M} \frac{1}{2} \, \hat{g}_k(x)$$

- Where $\hat{f}_k(x) = \frac{1}{2} \hat{g}_k(x)$.
- Hard classification: $\hat{f}_M(x) > 0$
- Or remap to a probability $\hat{p}(x) = \frac{e^{2f}}{1+e^{2f}}$ for thresholding

3 Gradient Boosting

The boosting model:

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \, \hat{g}_k(x)$$

Sequential Fitting:

$$\hat{f}_{k+1}(x) = \underset{a, g(x)}{\operatorname{arg\,min}} \sum_{i=1}^{n} L(y_i, \hat{f}_k(x_i) + a g(x_i))$$

The concept of gradient boosting is to sequentially re-fit to the negative (functional) gradients of the loss function (think of the negative gradients as a type of residual; *pseudo residual*).

- The same structure can be used for many different loss functions
 - it works the same for regression and classification
 - survival analysis, ranking, etc.

3.1 Gradient Descent

- Our objective is to find the model (or model parameters) that minimize the loss function
- From any starting point, we can move toward the optimum using gradient descent:

$$f_{k+1} = f_k - \nu_k L'(f_k)$$

- $\nu_k > 0$ is the step-size
- $L'(f_k)$ is the functional derivative of the loss with respect to the model f_k
- Boosting fits models sequentially:

$$\hat{f}_{k+1}(x) = \hat{f}_k(x) + \hat{a}_k \, \hat{g}_k(x)$$

• So we see a parallel; each boosting model $\hat{g}_k(x)$ can be viewed as estimating the *negative derivative* of the loss function.

3.2 L_2 Boosting

 L_2 boosting is based on the squared error loss function

$$L(y_i, \hat{f}(x_i)) = \frac{1}{2}(y_i - \hat{f}(x_i))^2$$

• The negative gradients are

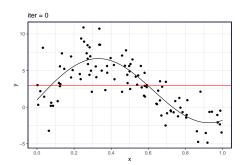
$$r_{i} = \left[-\frac{\partial L(y_{i}, f_{i})}{\partial f_{i}} \right]_{f_{i} = \hat{f}(x_{i})}$$
$$= y_{i} - \hat{f}(x_{i})$$

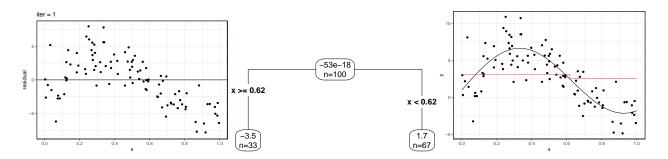
• L2 Boosting is simply re-fitting to the residuals.

Algorithm: L_2 Boosting

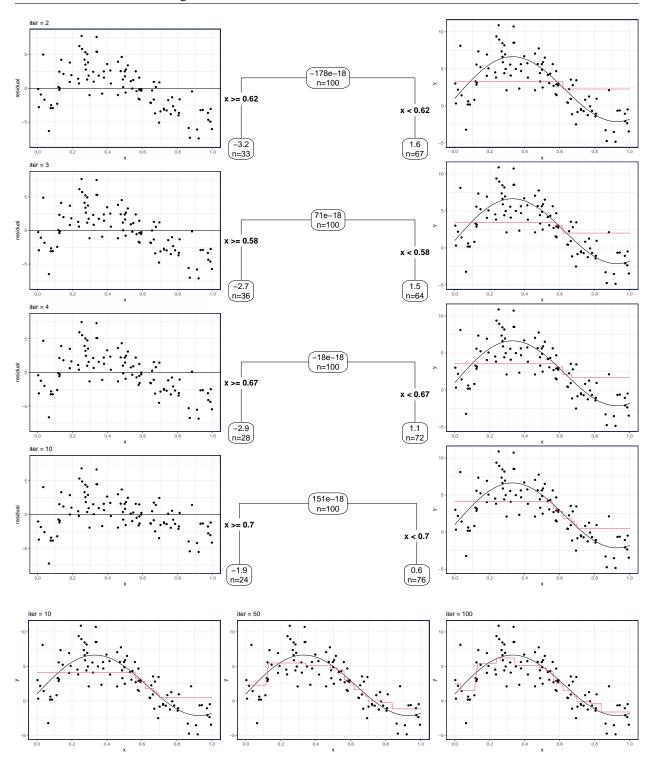
- 1. Initialize $\hat{f}_0(x) = \bar{y}$
- 2. For k = 1 to M:
 - a. Calculate residuals $r_i = y_i \hat{f}_{k-1}(x_i)$ for all i
 - b. Fit a base learner (e.g., regression trees) to the residuals $\{(x_i, r_i)\}_{i=1}^n$ to get the model $\hat{g}_k(x)$
 - c. Update the overall model $\hat{f}_k(x) = f_{k-1}(x) + \nu \hat{g}_k(x)$
 - $0 \le \nu \le 1$ is the step-size (shrinkage)
- 3. Final model is $\hat{f}_M(x) = \bar{y} + \sum_{k=1}^M \nu \hat{g}_k(x)$
- Like AdaBoost, emphasis is given to observations that are predicted poorly (large residuals)

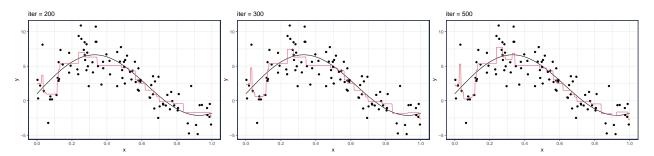
3.2.1 Illustration using stumps (depth=1, n.nodes=2, $\nu=.1$)





AdaBoost, Gradient Boosting, XGboost





3.3 GBM (Gradient Boosting Machine)

- R package gbm
- GBM Documentation
- GBM is a first order approach. It does not consider Hessian.

3.3.1 Model/Tree Tuning Parameters

- Tree depth (interaction.depth)
 - Grows trees to a depth specified by interaction.depth (unless there are not enough observations in the terminal nodes)
- Minimum number of observations allowed in the terminal nodes (n.minobsinnode)
- Sub-sampling (bag.fraction)
 - Stochastic Gradient Boosting
 - Sample (without replacement) at each iteration
- Loss Function (distribution)
 - The loss function is determined by the distribution argument
 - Use distribution="gaussian" for squared error
 - Other options are: bernoulli (for logistic regression), poisson (for Poisson regression), pairwise (for ranking/LambdaMart), adaboost (for the adaboost exponential loss), etc.

3.3.2 Boosting Tuning Parameters

- Number of iterations/trees (n.trees)
 - Need to tune
- Shrinkage parameter (shrinkage)
 - Set small, but the smaller the shrinkage, the more iterations/trees need to be used
 - "Ranges from 0.001 to 0.100 usually work"
- Cross-validation (cv.folds)
 - gbm has a built in cross-validation
 - no way to manually set the folds

3.3.3 Computational Settings

- Number of Cores (n.cores)
 - Only used when cross-validation is implemented

3.4 xgboost (Extreme Gradient Boosting)

- R package xqboost
- xgboost Documentation
- · xgboost Model
- xbgoost Paper

3.4.1 Model/Tree Tuning Parameters

- Different base leaners (booster)
 - gbtree is a tree
 - gblinear creates a (generalized) liner model (forward stagewise linear model)
- Tree building (tree method)
 - To speed up the fitting, only consider making splits at certain quantiles of the input vector (rather than considering every unique value)
- Sub-sampling (subsample)
 - Stochastic Gradient Boosting
 - Sample (without replacement) at each iteration
- Feature sampling (colsample_bytree, colsample_bylevel, colsample_bynode)
 - Like used in Random Forest, the features/columns are subsampled
 - Can use a subsample of features for each tree, level, or node

Model Complexity Parameters

- Tree depth (max_depth)
 - Grows trees to a depth specified by max_depth (unless there are not enough observations in the terminal nodes)
 - Trees may not reach max_depth if the gamma or min_child_weight arguments are set.
- Minimum number of observations (or sum of weights) allowed in the terminal nodes (min_child_weight)
- Pruning (gamma or min split loss)
 - Minimum loss reduction required to make a further partition on a leaf node of the tree
 - The larger gamma is, the more conservative the algorithm will be
- ElasticNet type penalty (lambda and alpha)
 - lambda is an L_2 penalty
 - alpha is an L_1 penalty

Note

• Recall that trees model the outcome as a *constant* in each region

$$\hat{f}_T(x) = \sum_{m=1}^M \hat{c}_m \, \mathbb{1}(x \in \hat{R}_m)$$

• Cost-complexity pruning found the optimal tree as the one that minimized the penalized loss objective function:

$$C_{\gamma}(T) = \sum_{m=1}^{|T|} \operatorname{Loss}(T) + \gamma |T|$$

• XGBoost selects a tree at each iteration using the following penalized loss:

$$C_{\gamma,\lambda,\alpha}(T) = \sum_{m=1}^{|T|} \operatorname{Loss}(T) + \gamma |T| + \frac{\lambda}{2} \sum_{m=1}^{|T|} \hat{c}_m^2 + \alpha \sum_{m=1}^{|T|} |\hat{c}_m|$$

- Loss Function (objective)
 - The loss function is determined by the objective argument
 - Use reg: squarederror for squared error
 - Other options are: reg:logistic or binary:logistic (for logistic regression), count:poisson (for Poisson regression), rank:pairwise (for ranking/LambdaMart), etc.

3.4.2 Boosting Tuning Parameters

- Shrinkage parameter (eta or learning_rate)
 - Set small, but the smaller the eta, the more iterations/trees need to be used
- Number of iterations/trees (num_rounds)
- Cross-validation (xgb.cv)
 - xgboost has a built in cross-validation
 - It is possible to manually set the folds

3.4.3 Computational Settings

- Number of Threads (nthread)
- GPU Support (https://xgboost.readthedocs.io/en/latest/gpu/index.html)
 - Used for finding tree split points and evaluating/calculating the loss function

3.5 CatBoost

- R package: (https://github.com/catboost/catboost/tree/master/catboost/R-package)
- CatBoost Documentation
- Model/Tree Tuning Parameters:

• Boosting Tuning Parameters:

3.6 LightGBM

- R Package: https://github.com/microsoft/LightGBM/tree/master/R-package
- LightGBM Documentation
- Model/Tree Tuning Parameters:

• Boosting Tuning Parameters:

4 Appendix: L2 Tree Boosting R Code

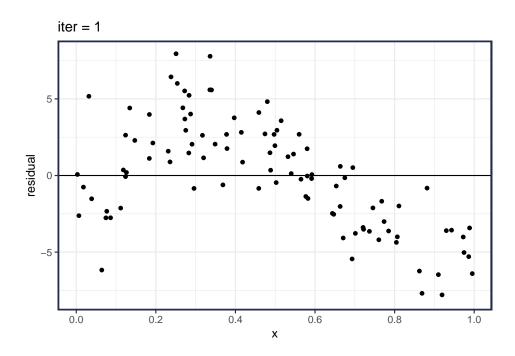
```
#: L2 Boost Algorithm
library(rpart)
# L2boost()
# L2 boosted trees (boosted regression trees)
# Inputs:
# x,y: training data. x should be data frame or matrix, y a vector
# xtest optional test data (data frame or matrix)
# M: number of iterations
# depth: tree depth. depth = 2 gives 4 leaf nodes.
# nu: shrinkage parameter
# Outputs:
# YHAT: matrix of in-sample predictions (predicting x)
# R: matrix of residuals
# YHAT.test: matrix of predictions for xtest
# TREE: list of rpart trees
L2boost <- function(x, y, xtest=NULL, M=100, depth=2, nu=.1){
```

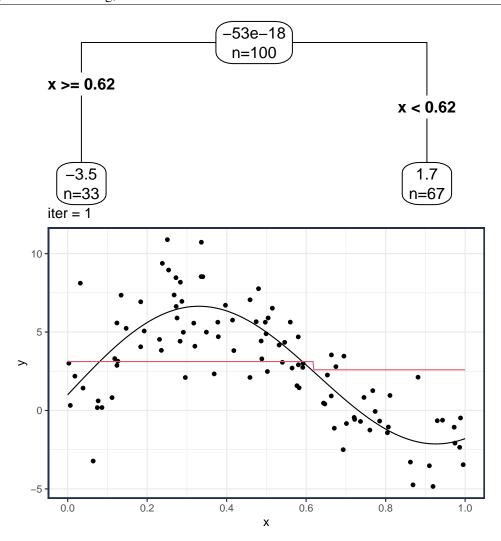
```
#- use training data if test data is not specified
  if(is.null(xtest)) {
    xtest = x
  #- storage
  n = length(y)
  R = YHAT = matrix(NA_real_, n, M)
  YHAT_test = matrix(NA_real_, nrow(xtest), M)
  colnames(YHAT) = colnames(YHAT_test) = colnames(R) = paste0("iter = ", 1:M)
  TREE = vector("list", M)
  names(TREE) = paste0("iter = ", 1:M)
  #-- 1) initialize model with mean
  mu = mean(y)
  yhat = rep(mu, nrow(x))
  yhat_test = rep(mu, nrow(xtest))
  for (m in 1:M) {
    #-- 2a) Calculate Residuals
    r = y - yhat
    R[,m] = r
    #-- 2b) Fit regression tree
    tree = rpart(r ~ ., data = x,
                 maxdepth = depth, # control tree depth
                 cp = -1,  # no pruning
minsplit = 0,  # allow all splits
minbucket = 1,  # no minimum on leaf size
                  method = "anova", # least-squares loss function
                  xval = 0)
                                     # no cross-validation
    TREE[[m]] = tree
    #-- 2c) Update model
    yhat = yhat + nu*predict(tree, x)
    YHAT[, m] = yhat
    yhat_test = yhat_test + nu*predict(tree, xtest)
    YHAT_test[, m] = yhat_test
  #-- 3) Output
  return(list(YHAT=YHAT, R=R, YHAT.test=YHAT_test, TREE=TREE))
#: Data Generation
n = 100
                                          # number of observations
```

```
x_eval = seq(0, 1, length=500)
                                         # evaluation points
```

```
#: Implement L2 boosting
L2 = L2boost(data.frame(x), y, xtest=data.frame(x=x_eval), # data
            depth = 1, M = 100, nu = .1)
                                                      # tuning parameters
```

```
#: Plotting
library(tidyverse)
                   # for ggplot2 package
library(rpart.plot) # for prp()
# set iteration
i = 1
# Residual Plot
ggplot(data_train, aes(x)) +
  geom_point(aes(y = L2$R[,i]), col="black") +
  geom_hline(yintercept=0, col="black") +
  scale_x_continuous(breaks=seq(0, 1, by=.20)) +
  coord_cartesian(ylim=c(-8, 8)) +
  labs(y="residual", title=colnames(L2$R)[i])
# Tree
prp(L2$TREE[[i]], type=4, extra=1, branch=1, clip.right.labs = FALSE, roundint=FALSE)
# Model prediction
ggplot(data_train, aes(x, y)) +
  geom_point() +
  annotate("line", x=x_eval, y=f(x_eval), color = "black") +
  geom_line(data=tibble(x=x_eval, y=L2$YHAT.test[,i]), col=2) +
  scale_x_continuous(breaks=seq(0, 1, by=.20)) +
  labs(title=colnames(L2$R)[i])
```





5 Appendix: xgboost and lightgbm

```
#: Load required packages
library(tidyverse)
library(palmerpenguins) # data
library(xgboost)
library(lightgbm)
```

We will use the palmer penguins data:

```
palmerpenguins::penguins
#> # A tibble: 344 x 8
#> species island bill_length_mm bill_depth_mm flipper_length_mm body_mass_g
#> <fct> <fct>
                            <db1> <db1>
                                                         <int>
                                                                    <int>
#> 1 Adelie Torgersen
                             39.1
                                          18.7
                                                           181
                                                                      3750
#> 2 Adelie Torgersen
                             39.5
                                          17.4
                                                            186
                                                                      3800
#> 3 Adelie Torgersen
                             40.3
                                          18
                                                            195
                                                                      3250
#> 4 Adelie Torgersen
#> 5 Adelie Torgersen
                              NA
                                           NA
                                                            NA
                                                                       NA
                              36.7
```

```
#> 6 Adelie Torgersen 39.3 20.6 190 3650

#> # i 338 more rows

#> # i 2 more variables: sex <fct>, year <int>
```

with a goal of predicting the species from the other variables. This is a three-class probability estimation problem. Most tree-based models can handle multiple classes naturally.

Note that the sex and island predictors are categorical.

5.1 xgboost

Requires a numeric matrix as input, and suggests using a special xgb formatted matrix for efficiency. The approach here is to create a *recipe* that does some pre-processing to handle missing values and categorical predictors and then create the special matrix.

Notes:

- The recipe removes observations with missing outcomes. It also sets unknown categorical/nominal values to an explicit level. Any missing values in the resulting data are handled internally by xgboost.
- the categorical (or nominal) predictors are dummy encoded.
- the three level outcome variables *species* is recoded to be $\{0, 1, 2\}$. All xgboost data must be numeric, even if it represents a nominal variable.

```
library(recipes) # part of tidymodels
library(xgboost)
#: pre-processing specs
rec_xgb = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
 step_naomit(species) %>% # remove cases with missing outcome label
 step_unknown(all_nominal_predictors()) %>% # add "unknown" level if missing
 # replace categorical/factors with numeric
 step_dummy(all_nominal_predictors(), one_hot = FALSE) %>%
 step_integer(species, zero_based = TRUE) %>%
 # train or prepare the pre-process step using the data provided in recipe()
 prep()
#: xgboost data object
xgb_data =
 xgb.DMatrix(
   data = bake(rec_xqb, new_data = NULL, composition = "matrix",
               all_predictors()),
   label = bake(rec_xgb, new_data = NULL, all_outcomes()) %>% pull()
 )
#: tuning parameters
xgb_tuning = list(
 learning_rate = .1,
 gamma = 1,
 max_depth = 2,
 subsample = .80
# Note, the number of iterations, nrounds, is not part of the params.
```

```
#: fit model
set.seed(1234) # xgboost can use stochastic resampling
xgb = xgboost(data = xgb_data,
             params = xgb_tuning, nrounds = 100, # tuning parameters
             num_class = 3, # this is required for multi-class problems
             objective = "multi:softprob", # multi-class loss function
             verbose = 0) # don't print output during training
#: make predictions
predict(xgb, xgb_data, reshape = TRUE) %>% head()
#> [,1] [,2] [,3]
#> [1,] 0.9941 0.003113 0.002755
#> [2,] 0.9938 0.003303 0.002924
#> [3,] 0.9938 0.003303 0.002924
#> [4,] 0.5404 0.025182 0.434446
#> [5,] 0.9941 0.003113 0.002755
#> [6,] 0.9941 0.003113 0.002755
```

5.2 lightgbm

Following a similar process to what is required for xgboost. LightGBM requires a matrix as input, and suggests using a special formatted matrix. The approach here follows the recipe that is used for xgboost with the exception that lightgbm can internally handle categorical predictors.

Notes:

- The recipe removes observations with missing outcomes. It also sets unknown categorical/nominal values to an explicit level. Any missing values in the resulting data are handled internally by lightgbm.
- the categorical (or nominal) predictors are integer encoded $\{0,1,...\}$ so they are numeric, and then handled internally by lightGBM. The categorical_features argument in the lgb.Dataset() function is used to specify which predictors should be treated as categorical.
- the three level outcome variables *species* is recoded to be $\{0, 1, 2\}$. All lightgbm data must be numeric, even if it represents a nominal variable.

```
library(recipes) # part of tidymodels
library(lightgbm)
#: pre-processing specs
rec_lgbm = recipe(species ~ ., data = palmerpenguins::penguins) %>%
 # Handle missing data
 step_naomit(species) %>% # remove cases with missing outcome label
 step_unknown(all_nominal_predictors()) %>% # add "unknown" level if missing
  # replace categorical/factors with numeric
 step_integer(all_nominal_predictors(), zero_based = TRUE) %>%
 step_integer(species, zero_based = TRUE) %>%
 # train or prepare the pre-process step using the data provided in recipe()
 prep()
#: 1gb data object
X = bake(rec_lgbm, new_data = NULL, composition = "matrix", all_predictors())
lgbm_data =
 lgb.Dataset(
 data = X,
```

```
colnames = colnames(X),
    categorical_feature = c("island", "sex"),
    label = bake(rec_lgbm, new_data = NULL, all_outcomes()) %>% pull()
#: tuning parameters
lgbm_tuning = list(
  # settings
 objective = "multiclass",
 num_class = 3,
  # tuning parameters
 nrounds = 100,
 min_gain_to_split = 1,
 learning_rate = 0.1,
 max_depth = 2,
                     # enable subsampling
 bagging_freq = 1,
 bagging_fraction = 0.8, # subsample size
 bagging_seed = 123 # controls the internal sampling
#: fit model
lgbm = lightgbm(data = lgbm_data, params = lgbm_tuning, verbose = -1)
#: make predictions
predict(lgbm, X) %>% head()
#> [,1] [,2]
                          [,3]
#> [1,] 0.9979 0.001190 0.000868
#> [2,] 0.9973 0.001540 0.001123
#> [3,] 0.9972 0.001700 0.001123
#> [4,] 0.8176 0.015829 0.166561
#> [5,] 0.9976 0.001413 0.001031
#> [6,] 0.9979 0.001190 0.000868
```

5.3 **Tidymodels**

The bonsai and xgboost packages are necessary to use lightgbm and xgboost in parsnip.

```
library(tidymodels)
library(bonsai) # for lightgbm
library(xgboost) # for xgboost
```

This defines the parsnip model specification for xgboost, modifies the recipe to leave the outcome as a factor, and adds it to a workflow.

```
#: pre-processing specs
rec_xgb = recipe(species ~ ., data = palmerpenguins::penguins) %>%
 # Handle missing data
 step_naomit(species) %>% # remove cases with missing outcome label
 step unknown(all nominal predictors()) %>% # add "unknown" level if missing
  # replace categorical/factors with numeric
 step_dummy(all_nominal_predictors(), one_hot = FALSE)
# Define the XGBoost model specification
xgb_spec = boost_tree(
 trees = 100,
                                  # nrounds
 tree\_depth = 2,
                                # Max depth of the trees
```

```
learn_rate = 0.1,
                               # Learning rate
 loss_reduction = 1,
                                # Gamma (min_split_loss)
  sample\_size = 0.8,
                                # Subsample ratio
  mode = "classification"
                                # For multi-class classification
  set_engine("xgboost", objective = "multi:softprob", num_class = 3)
#: Create XGBoost workflow (combine recipe with model specification)
xgb_wf = workflow(preprocessor = rec_xgb, spec = xgb_spec)
# Fit the model
set.seed(1234)
xgb_fit = fit(xgb_wf, data = palmerpenguins::penguins)
#> Warning: ! The argument `num_class` is guarded by parsnip and will not be passed to
#> `xgb.train()`.
# Make predictions on the training data
predict(xgb_fit, palmerpenguins::penguins, type = "prob") %>% head()
#> # A tibble: 6 x 3
#> .pred_Adelie .pred_Chinstrap .pred_Gentoo
     <db1> <db1> <db1> <db1> 0.994 0.00311 0.00275
#>
#> 1
0.00330
0.00330
                                    0.00292
                                    0.00292
#: pre-processing specs
rec_lgbm = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
  step_naomit(species) %>% # remove cases with missing outcome label
  step unknown(all nominal predictors()) # add "unknown" level if missing
# Define the lightgbm model specification
lgbm_spec = boost_tree(
 trees = 100,
tree_depth = 2,
learn_rate = 0.1,
                               # nrounds
                               # Max depth of the trees
                               # Learning rate
 loss_reduction = 1,
sample_size = 0.8,
                               # min_gain_to_split
                                # Subsample ratio
  mode = "classification"
                                # For multi-class classification
  set_engine("lightgbm", objective = "multiclass", num_class = 3, num_threads = 6) %>%
  set_args(
   bagging_seed = 123, # controls the internal sampling
  )
#: Create XGBoost workflow (combine recipe with model specification)
lgbm_wf = workflow(preprocessor = rec_lgbm, spec = lgbm_spec)
# Fit the model
lgbm_fit = fit(lgbm_wf, data = palmerpenguins::penguins)
```

Make predictions on the training data

```
predict(lgbm_fit, palmerpenguins::penguins, type = "prob") %>% head()
#> # A tibble: 6 x 3
```