

# Association Analysis

Frequent Itemsets, Market Basket Analysis, and Association Rule Mining

SYS 6018 | Spring 2022

association.pdf

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## 1 Reading

- MMDS 6.1 and 6.2
- ITDM 5.1-5.3; 5.7-5.8
- ESL 14.2
- R package `arules`
- R package `arulesViz`

## 2 Case: Instacart

[Instacart Case](#)

## 3 Association Analysis Motivation

### 3.1 Market-Basket Analysis

- A grocery store records the items purchased in a set of transactions. For example,

TID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
5	{Bread, Milk, Diapers, Cola}

- If they can discover items **frequently** purchased together, they may be able to increase business.
  - If {Diapers, Beer} are frequently purchased together, the store could put diapers on sale and increase the price of beer.
  - If {Bread, Peanut Butter} are frequently purchased together, they may put some Peanut Butter on the shelf next to bread.
  - In on-line retail, you will often see “People who buy {X,Y} also tend to buy {Z}”.
- **Association Rules** are rules that describe potential relationships *of interest* between itemsets.
  - E.g., Given a set of transactions, find *rules that will predict* the occurrence of an item based on the occurrences of other items in the transaction
  - For example, the rule {Diapers}  $\rightarrow$  {Beer} suggests that customers who buy Diapers tend to purchase Beer more than *expected*.
  - Of course, we need to discuss metrics that will permit us to quantitatively evaluate the discovered rules.
  - **Co-occurrence doesn’t necessitate causality!**

### 3.2 Other Applications

- Market Basket
  - Items: Products for sale
  - Baskets: Sets of products purchased in single trip
  - Needs rule to occur frequently to make worthwhile

TID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
5	{Bread, Milk, Diapers, Cola}

- Text Mining (1)
  - Items: Words
  - Baskets: Books/Articles/Webpages/News
  - Frequent itemsets indicate words that are connected

News Article	Words
1: NY Times	{Trump, Tweet, Fake}
2: Wash Post	{Collusion, Russian, Trump}

- Text Mining (2)
  - Items: Documents
  - Baskets: Sentences/Code
  - Frequent itemsets could indicate plagiarism

Sentences/Code	Items
1: Logistic Regression is ...	{Doc 1, Doc 4, Doc 5}
2: ggplot(aes(x=size, y =weight))+ geom_...	{Doc 1, Doc 5}

- Health Mining
  - Items: Drugs and Side-Effects
  - Baskets: Patients
  - Discover combinations of drugs that result in particular side-effects
    - \* {Drug 1, Drug 4, Drug 6} → {Psychosis}
  - Note that absence of drug/side-effect could also be important
    - \* {Drug 1, Drug 4, Not Drug 7} → {Psychosis}

Patient	Items
1	{Drug 1, Drug 3, Rash, Weight-Loss}
2	{Drug 2, Drug 3, Headaches}

- Transportation
  - Items: Features collected after vehicle crash
  - Baskets: The set of vehicle crashes
  - Discover dangerous/safe combinations

---

CrashID	Items
1	{Wet, Night, Rural}
2	{Alcohol, Night, Lights-off}
3	{Day, Flat tire, Elderly}

---

- Survey Data

- Items: Potential Responses to questionnaire
- Baskets: Set of responses by respondent
- {Married, Own house}  $\rightarrow$  {income  $\in$  [60K, 100K]}

---

ID	Items
1	{Sex = <i>Male</i> , Age = [20,25], Type of home = <i>House</i> , ... }
2	{Sex = <i>Female</i> , Age = [30,35], Type of home = <i>Apt</i> , ... }
3	{Sex = <i>Male</i> , Age = [65+], Type of home = <i>House</i> , ... }

---

## 4 Market Basket Model

### 4.1 Data

There are two equivalent data formats:

- **Transaction Lists**

TID	Items
1	{Bread, Milk}
2	{Bread, Diapers, Beer, Eggs}
3	{Milk, Diapers, Beer, Cola}
4	{Bread, Milk, Diapers, Beer}
5	{Bread, Milk, Diapers, Cola}

- **Binary Incident Table/Matrix**

TID	Bread	Milk	Diapers	Beer	Eggs	Cola
1	1	1	-	-	-	-
2	1	-	1	1	1	-
3	-	1	1	1	-	1
4	1	1	1	1	-	-
5	1	1	1	-	-	1

### 4.2 Definitions

- $K$  possible items
- $N$  total transactions
- Let  $I$  be an itemset
  - E.g.,  $I = \{\text{Cola, Bread, Fruit}\}$ ,  $I = \{\text{Bread}\}$
  - There are  $2^K - 1$  possible itemsets
- The **support** of  $I$  is the proportion of transactions that contain  $I$ 
  - $S(I) = (\# \text{ of transactions containing } I) / N$
- The support is an estimate of the probability of getting  $I$  in a future basket.
  - $S(I) \triangleq \Pr(I \subseteq T)$ , where  $T$  is a future basket
- A **Frequent Itemset** is one that has support greater than or equal to the **support threshold (minsup)**,  $s$ .
- **Association Rule** is an if-then expression about the content of the baskets
  - The expression  $I \rightarrow J$  means that if a basket contains  $I$ , then it is *more likely* to also contain  $J$ .
  - $I$  and  $J$  should be *disjoint*, e.g.,  $I \cap J = \emptyset$
- The **support** of an association rule is the frequency in which both itemsets are in the same basket

- $S(I \rightarrow J) = (\# \text{ of transactions containing } I \text{ and } J)/N$
- $S(I \rightarrow J) = S(I, J) \triangleq \Pr(I \subseteq T, J \subseteq T)$ , where  $T$  is a future basket.

- The **confidence** of a rule is an estimate of the conditional probability of  $J$  being in a basket given the basket already contains  $I$

$$- C(I \rightarrow J) = \frac{S(I, J)}{S(I)} \triangleq \frac{\Pr(I \subseteq T, J \subseteq T)}{\Pr(I \subseteq T)} = P(J \subseteq T | I \subseteq T)$$

- A **High Confidence** rule is one that has confidence greater than or equal to the **confidence threshold (minconf)**,  $c$ .
- The classic **Association Rule Discovery** task is to find all rules that have *support*  $\geq s$  and *confidence*  $\geq c$

1. Find all *frequent* itemsets,  $I$  2. For every subset  $A \subset I$ , generate the rule  $A \rightarrow I \setminus A$  3. It is easy to find the *largest* confidence set derived from  $I$ . Do you see how?

### 4.3 Practice

#### Your Turn #1

TID	Items
0001	{a, d, e}
0024	{a, b, c, e}
0012	{a, b, d, e}
0031	{a, c, d, e}
0015	{b, c, e}
0022	{b, d, e}
0029	{c, d}
0040	{a, b, c}
0033	{a, d, e}
0038	{a, b, e}

1. What are the value of  $K$  and  $N$ ?
2. What is the *support* of  $\{e\}$ ,  $\{b, d\}$ , and  $\{b, d, e\}$ ?
3. What is the *confidence* of  $\{b, d\} \rightarrow \{e\}$  and  $\{e\} \rightarrow \{b, d\}$ ? Is confidence symmetric?
4. Think of an approach/algorithm to find *all Association Rules* with  $s = 0.4$  and  $c \geq .70$ .

## 5 Apriori Algorithm

### 5.1 Introduction

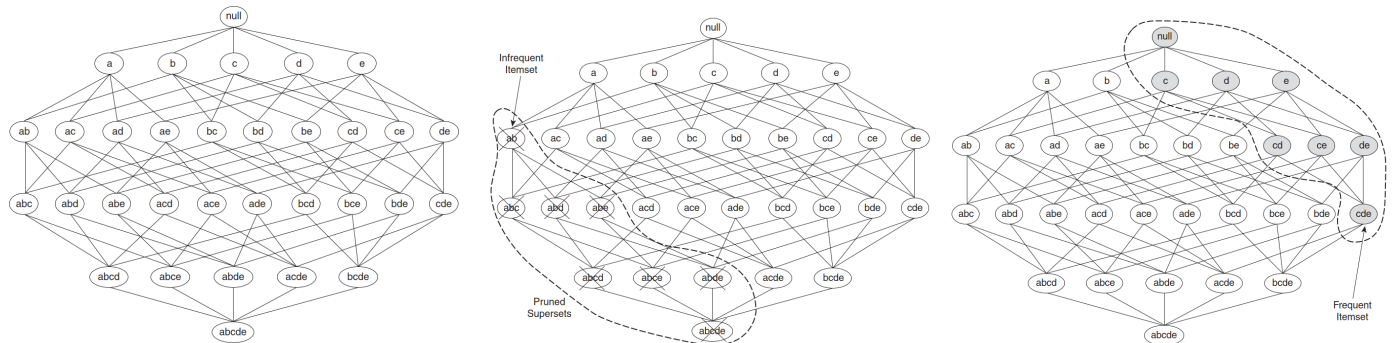
- **Goal:** Discover associations between itemsets.
  - Interested in discovering *frequent itemsets* - those that appear in  $\geq s$  baskets.
  - Interested in discovering *high confidence rules* - those with confidence  $\geq c$  scores.
- **Problem:** There are  $2^K - 1$  possible itemsets and  $3^K - 2^{K+1} + 1$  possible rules.
  - Wal-mart has 100K items
  - 10B webpages
  - Memory and computing time issues
- **Solution:** The **Apriori** principle
  - *If an itemset is frequent, then all of its subsets must also be frequent.*
  - Equivalently, *If an itemset is not frequent, then none of its unions will be frequent.*
- Thus, if item  $i$  does not appear in at least  $s$  baskets (i.e., not frequent), then no itemsets that include item  $i$  will appear in at least  $s$  baskets.

### 5.2 Apriori Approach

- Because of the size of association data, traditional approaches have focused on finding the rules that have support  $\geq s$  and confidence  $\geq c$ .
- This can be efficiently approached in a two step process
  1. Find all frequent itemsets
  2. Find rules, using the frequent itemsets, with high confidence



### 5.2.1 Finding Frequent Itemsets

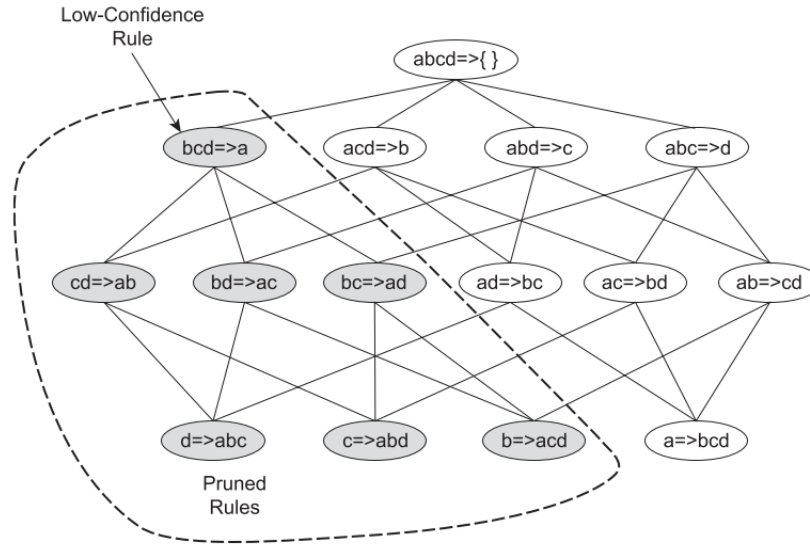


### 5.2.2 Finding High Confidence Rules

#### Your Turn #2

A frequent itemset consists of found items {a,b,c,d}.

1. How many association rules (of any size) can be formed from data with four items?
2. How many association rules can be formed from *this itemset* (exactly four items)?
3. Suppose the *confidence* for rule  $\{b,c,d\} \rightarrow \{a\}$  is low (i.e.,  $C(\{b,c,d\} \rightarrow \{a\}) < c$ ).
  - a. Do we need to calculate  $C(\{d\} \rightarrow \{a,b,c\})$ ?
  - b. Do we need to calculate  $C(\{a,b\} \rightarrow \{c,d\})$ ?



### 5.3 Targeted Items

- Suppose we are especially interested in one item (e.g., Honey).
- If we want to find an association itemset that *increases the probability* that targeted item is in a basket (i.e., item of interest on the rhs), then it may help to convert the problem into a *supervised learning* classification problem.
  - Same “association is not causation” caveat applies
- If we want to see how the target item associates with other items (i.e., target item on lhs), then we don’t need to run a full search, but only build up the rhs items sequentially.

## 6 Example: Instacart

### 6.1 Instacart Case

See the [Instacart Case](#) for details.

### 6.2 Load Data

#### Note

The R Code *instacart.R* (see course webpage) contains a detailed example.

1. The data have already been downloaded and extracted to the course website. The two relevant datasets can be load into R using `readr::read_csv()`

```
library(readr)
#-- Load the "orders_products__train.csv" (notice two __) and "products.csv"
data.dir = "https://mdporter.github.io/SYS6018/data/"
orders = read_csv(file.path(data.dir, "order_products__train.csv"))
products = read_csv(file.path(data.dir, "products.csv"))

#> # A tibble: 1,384,617 x 4
#>   order_id product_id add_to_cart_order reordered
#>   <dbl>      <dbl>          <dbl>      <dbl>
#> 1         1         49302              1          1
#> 2         1         11109              2          1
#> 3         1         10246              3          0
#> 4         1         49683              4          0
#> 5         1         43633              5          1
#> 6         1         13176              6          0
#> 7         1         47209              7          0
#> 8         1         22035              8          1
#> 9         36         39612              1          0
#> 10        36         19660              2          1
#> # ... with 1,384,607 more rows
#> # A tibble: 49,688 x 4
#>   product_id product_name aisle_id department_id
#>   <dbl>      <chr>      <dbl>      <dbl>
#> 1         1 Chocolate Sandwich Cookies        61         19
#> 2         2 All-Seasons Salt             104         13
#> 3         3 Robust Golden Unsweetened Oolong Tea        94          7
#> 4         4 Smart Ones Classic Favorites Mini Rigatoni~       38          1
#> 5         5 Green Chile Anytime Sauce              5         13
#> 6         6 Dry Nose Oil                   11         11
#> 7         7 Pure Coconut Water With Orange           98          7
#> 8         8 Cut Russet Potatoes Steam N' Mash          116          1
#> 9         9 Light Strawberry Blueberry Yogurt          120         16
#> 10        10 Sparkling Orange Juice & Prickly Pear Beve~      115          7
#> # ... with 49,678 more rows
```

2. Join orders and products to get data frame of *order\_id*, *product\_id*, and *product\_name*.

- Using `dplyr` functions:

```
library(dplyr)
Y = left_join(orders %>% select(order_id, product_id),
              products %>% select(product_id, product_name),
              by = "product_id") %>%
  arrange(order_id)
```

```
#> # A tibble: 1,384,617 x 3
#>   order_id product_id product_name
#>   <dbl>      <dbl> <chr>
#> 1         1         49302 Bulgarian Yogurt
#> 2         1         11109 Organic 4% Milk Fat Whole Milk Cottage Cheese
#> 3         1         10246 Organic Celery Hearts
#> 4         1         49683 Cucumber Kirby
#> 5         1         43633 Lightly Smoked Sardines in Olive Oil
#> 6         1         13176 Bag of Organic Bananas
#> 7         1         47209 Organic Hass Avocado
#> 8         1         22035 Organic Whole String Cheese
#> 9         36         39612 Grated Pecorino Romano Cheese
#> 10        36         19660 Spring Water
#> # ... with 1,384,607 more rows
```

### 6.3 Clean Data

- The data should have a one-to-one mapping between *product\_name* and *product\_id*
- Transactions should not contain duplicate items
- May need to clean item names or ids

### 6.4 arules package

- The R package *arules* has functions for performing association analysis
  - More details in the vignette <https://cran.r-project.org/web/packages/arules/vignettes/arules.pdf>
- The main function is `apriori()`
  - the arguments *parameter*, *appearance*, and *control* are used to run certain analyses
- The data needs to be converted to *transaction* class (essentially a sparse binary matrix)
  - This is done by using the function `as(tList, "transactions")`, where *tList* is a **transaction list**
  - This means we need to convert our transaction data frame into a transaction *list*

### 6.5 Find Frequent Itemsets

- Frequent itemsets can be found by running the function

```
apriori(trans, parameter = list(support = .01, target="frequent"))
```

- *trans* is the transactions object
- support threshold is set to .01
- target="frequent" indicates we only want frequency, not rules
- The `parameter=` argument can be used focus on certain classes of itemsets
  - E.g., support, minlen, maxlen

### 6.6 Find Association Rules

- Association rules can be found by running the function

```
apriori(trans, parameter = list(support = .001, confidence=.50,
                                target="rules"))
```

- *trans* is the transactions object

- support threshold is set to  $s = .01$
- confidence threshold is set to  $c = .50$
- target="rules" indicates we only want rules

## 6.7 Plot Association Rules

- the `arulesViz` R package provides some plotting functionality
  - More details in the vignette <https://cran.r-project.org/web/packages/arulesViz/vignettes/arulesViz.pdf>

## 6.8 Target specific itemsets

- Specific itemsets can be targeted by setting the `appearance =` parameter

## 7 More Interesting Rules

### 7.1 Measures of Interestingness

The utility of a particular association rule is based on the needs of the business/research (e.g., sell more products, increase profit). When in a purely exploratory mode, the **interestingness** of a rule determines its value. So far, we have only examined *support* and *confidence*, but there are many other measures of interestingness.

#### 7.1.1 Think About It

##### Your Turn #3

For each of the following questions, provide an example of an association rule from the market basket domain that satisfies the following conditions. Also, describe whether such rules are subjectively interesting.

1. A rule that has high support and high confidence.
2. A rule that has reasonably high support but low confidence.
3. A rule that has low support and low confidence.
4. A rule that has low support and high confidence.

### 7.2 Lift

- Why would the rule Caviar  $\rightarrow$  Vodka be interesting, even if it has low support?
- In general, an interesting rule is one that occurs more (or less) than *expected*.
- Support and Confidence are measured against an expected **uniform** distribution.
- **Lift**, on the other hand is based on statistical independence.
  - Notice that lift is **not** directional

$$L(I, J) = \frac{C(I \rightarrow J)}{S(J)}$$

$$= L(J, I)$$

- If  $I$  and  $J$  are independent, then  $\Pr(I, J) = \Pr(I) \Pr(J)$ .
  - Lift  $> 1$  indicates positive association
  - Lift  $< 1$  indicates negative association ( $I$  and  $J$  *inhibit* each other)
- Because its a ratio, *lift* can be large even when the *support* is low and small when the *confidence* is large.

#### Your Turn #4

Consider the following beverage preferences from 1000 people:

	Coffee	No Coffee
Tea	150	50
No Tea	650	150

1. What is the *support* of  $\{\text{Tea}\} \rightarrow \{\text{Coffee}\}$ ?
2. What is the *confidence* of  $\{\text{Tea}\} \rightarrow \{\text{Coffee}\}$ ?
3. What is the *lift* of  $\{\text{Tea}\} \rightarrow \{\text{Coffee}\}$ ?
4. Interpret.

- What is the lift for more than two items (e.g.,  $L(I, J, L)$ )?

### 7.3 Other Measures

There are [many other measures](#). Here are a few:

- **Piatetsky-Shapiro (PS)/Leverage**: difference of observed and expected.

$$PS(I, J) = S(I, J) - S(I)S(J)$$

- **Correlation ( $\phi$ )**: normalized version of **PS**.

$$\phi(I, J) = \frac{PS(I, J)}{\sqrt{S(I)(1 - S(I))S(J)(1 - S(J))}}$$

- **Added Value (AV)**: difference between conditional and unconditional.

$$\begin{aligned} AV(I \rightarrow J) &= C(I \rightarrow J) - S(J) \\ &= PS(I, J)/S(I) \\ &\hat{=} \Pr(J|I) - \Pr(J) \end{aligned}$$

- **Conditional Entropy  $H(J|I)$** : amount of info needed to describe distribution of  $J$  given  $I$ .

$$H(J|I) = H(I, J) - H(I)$$

- **Mutual Information (MI)**: type of Kullback-Leibler divergence where independence is used for alternative distribution.

$$MI(I, J) = H(J) - H(J|I)$$

- Michael Hahsler, author of the `arules` package, details [many other interest measures](#)

#### Your Turn #5

Consider the following results from 1000 people:

	Honey	No Honey
Tea	100	100
No Tea	20	780

1. What is the *support* of  $\{\text{Tea}\} \rightarrow \{\text{Honey}\}$ ?
2. What is the *confidence* of  $\{\text{Tea}\} \rightarrow \{\text{Honey}\}$ ?
3. What is the *lift* of  $\{\text{Tea}\} \rightarrow \{\text{Honey}\}$ ?
4. What is the *Added Value (AV)* of  $\{\text{Tea}\} \rightarrow \{\text{Honey}\}$ ?
5. What is the *Piatetsky-Shapiro (PS)* score for  $\{\text{Tea}\} \rightarrow \{\text{Honey}\}$ ?
6. Interpret.



## 7.4 Adding additional interesting measures in **arules** package

The `arules` package provides the function `interestMeasure()` that will calculate a wide range of metrics.

- For example, *lift* can be calculated for all frequent itemsets

## 8 Statistical Issues

### 8.1 Repeatable Patterns

- **Co-occurrence does not mean causality**
- The patterns/associations of interest are those that are *repeatable*, i.e., the patterns will appear in future transactions.
- If future transactions will come from a different distribution than the observed data, proceed with caution!
- Rule metrics are constructed from *counts* e.g.,  $N(I)$ ,  $N(J)$ ,  $N(I, J)$ .
  - If the transactions are *independent*, then  $N(A) \sim \text{Bino}(p_A, N)$ .
    - \* What is a good estimate of  $p_A$ ?
    - \* What is the confidence interval for  $p_A$ ?
  - What if the transactions are **not** independent (same person makes multiple transactions)?

#### Your Turn #6

Suppose we have  $N = 10\,000$  transactions and found two itemsets  $I$  and  $J$  with  $N(I, J) = 500$ ,  $N(I) = 1000$ ,  $N(J) = 4000$ .

1. What is a good point estimate of  $\Pr(I, J)$ ?
2. What is the confidence interval for  $\Pr(I, J)$  (pick the confidence level)?
3. What is a good point estimate of  $P(J|I)$ ?
4. Confidence interval for  $P(J|I)$ ?
5. What should we do if the transactions are *not* independent? E.g., the  $N$  transactions are made by  $M = 100$  customers.

### 8.2 Probability Estimation and Statistical Significance

- **Sampling:** If metrics are based on counts/probability estimates, then sampling can help alleviate the computational burden while still discovering the associations

- Much in the same way as polling is used to estimate the percentage of people who will vote for a particular candidate.
- Note: Should you sample items or transactions, or both?
- **Multiple Testing:** Statistical significance and confidence intervals are approaches to help us avoid *spurious associations*. One challenge with association analysis is that we are searching through a large data set and are likely to find (empirically) strong associations that are due to chance alone.
  - We need to be especially careful about rules/associations that are based on small counts as they will have the most variation (especially metrics based on ratios).
- **Simpson's Paradox:** See ITDM 5.7.3

### 8.2.1 Simulation

Here is some simulated transaction data. All items are generated independently and all transactions are independent. This means that there are no “real” associations; anything we discover is spurious. Ten items (1-10) have probability of .25 of being included in any transaction, ten items (11-20) have probability of .10 of being included in any transaction, and the remaining items have probability of .01.

```

#-- Settings
K = 2000 # total number of items
N = 50000 # number of transactions
p = c(rep(.25, 10), rep(.10, 10), rep(.01, K-20)) # probabilities

#-- function to generate transactions
get_transaction <- function(p) {
  K = length(p)
  (1:K)[runif(K) <= p]
}

#-- Simulate N transactions
X = replicate(N, get_transaction(p))

#-- Run apriori
library(arules)
trans = as(X, "transactions")

apriori(trans, parameter=list(support=100/N, confidence=.20, minlen=2),
        control=list(verbose=FALSE)) %>%
  sort(by="lift") %>% head(n=5) %>% R6018::tidy()
#> # A tibble: 5 x 7
#>   lhs      rhs support confidence coverage lift count
#>   <chr>    <chr>   <dbl>      <dbl>    <dbl> <dbl> <int>
#> 1 {5,10,15} {1}    0.00208    0.355  0.00586  1.41  104
#> 2 {2,3,16} {8}    0.00204    0.329  0.0062   1.32  102
#> 3 {1643}   {2}    0.00322    0.329  0.0098   1.32  161
#> 4 {3,7,16} {9}    0.00222    0.326  0.0068   1.31  111
#> 5 {1,10,15} {5}    0.00208    0.322  0.00646  1.30  104

```

- There are no “real” patterns in these data, but we can find many apparent patterns
- Notice the relatively large values of *lift* (expected lift is 1)
- Notice from which groups the items come from (high, medium, low probabilities). Why do we get these patterns?
- **Statistical Testing Approaches:**

- Due to multiple comparisons, the exact distribution of a test statistic is often elusive.
- However, it may not be too difficult estimate the distribution of a test statistic using simulation.
- **Independence:** randomly permute each column (in the transaction matrix) independently. However, this may change the distribution of the transaction length (number of items in a transaction). A method called *swap randomization* can help.
- Bootstrap the transactions
- Cross-Validation / Hold-out analysis

## 9 Extensions

### 9.1 Non-Market Basket Format

- Association analysis can be performed on non-market basket data.
- It only requires a data set of *binary* features
  - Categorical Data is dummy coded
  - Numerical data is binned

#### 9.1.1 Categorical Data

- A *categorical variable* is one that can one of  $k$  possible values
  - *nomial* is unordered (e.g., *blue*, *green*, *brown*)
  - *ordinal* is ordered (e.g., *Great*, *Good*, *Average*, *Below*, *Poor*)
- Dummy coding (*one-hot-encoding*) is the way to convert a categorical variable to a set of *binary* variables
  - A  $k$  level variable will create  $k$  binary variables
  - This is different than the usual dummy coding for regression, where  $k - 1$  levels are generated
  - This full  $k$  level coding is referred to as *one-hot-encoding* in the machine learning literature

```
#-- categorical vector with k=3 levels
x.cat = c('a', 'b', 'a', 'c', 'b')

#-- Convert to matrix with 3 columns
model.matrix(~x.cat-1)
#>   x.cata x.catb x.catc
#> 1      1      0      0
#> 2      0      1      0
#> 3      1      0      0
#> 4      0      0      1
#> 5      0      1      0
#> attr(,"assign")
#> [1] 1 1 1
#> attr(,"contrasts")
#> attr(,"contrasts")$x.cat
#> [1] "contr.treatment"
```

- May need to be creative in making interesting levels.
  - *Eyes = blue* vs. *Eyes  $\neq$  blue*

#### 9.1.2 Numeric Data

- Numeric data must be converted into binary format
- For example,  $age \leq 25 = TRUE$
- Numeric data could also be discretized or binned. This converts it into categorical data which is then dummy encoded.
  - E.g., *age 14-17*, *age 18-24*, ..., *age 65+*

#### 9.1.3 Categorical and Numeric Data in **arules** package

- The **arules** package has functionality to automatically handle categorical and numeric data

```

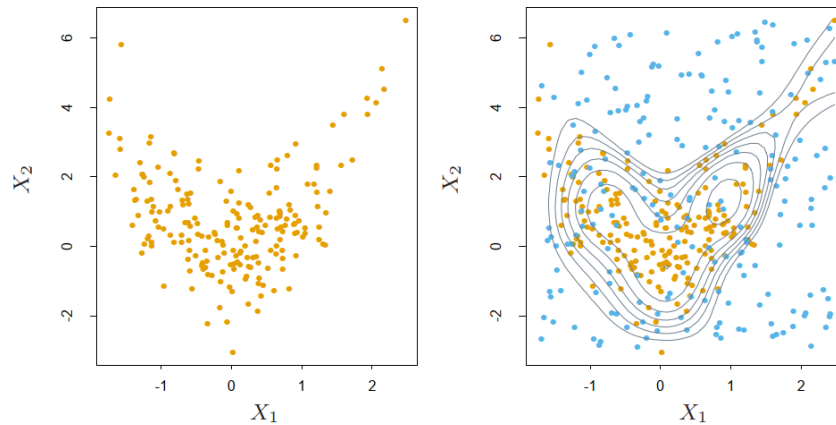
library(arules)

#-- Load data
data("IncomeESL") # load income data from arules package
summary(IncomeESL) # summary of data
#>      income      sex      marital status      age
#> [0,10) :1745  male :4075  married      :3334  14-17: 878
#> [50,75):1308  female:4918  cohabitation: 668  18-24:2129
#> [30,40):1110      divorced      : 875  25-34:2249
#> [40,50): 969      widowed      : 302  35-44:1615
#> 75+      : 884      single      :3654  45-54: 922
#> [20,25): 813      NA's      : 160  55-64: 640
#> (Other):2164      65+      : 560
#>      education      occupation      years in bay area
#> grade <9      : 264  professional/managerial:2820  <1 : 270
#> grades 9-11      :1046  student      :1489  1-3 :1042
#> high school graduate:2041  clerical/service      :1062  4-6 : 686
#> college (1-3 years) :3066  sales      : 770  7-10: 900
#> college graduate      :1524  laborer      : 767  >10 :5182
#> graduate study      : 966  (Other)      :1949  NA's: 913
#> NA's      : 86  NA's      : 136
#>      dual incomes  number in household  number of children
#> not married:5438  2      :2664      0      :5724
#> yes      :2211  3      :1670      1      :1506
#> no      :1344  1      :1620      2      :1148
#>      4      :1526      3      : 412
#>      5      : 686      4      : 117
#>      (Other): 452      5      : 46
#>      NA's      : 375      (Other): 40
#>      householder status      type of home      ethnic classification
#> own      :3256  house      :5073  white      :5811
#> rent      :3670  condominium: 655  hispanic:1231
#> live with parents/family:1827  apartment  :2373  black      : 910
#> NA's      : 240  mobile Home: 151  asian      : 477
#>      other      : 384  other      : 225
#>      NA's      : 357  (Other) : 271
#>      NA's      : 68
#>      language in home
#> english:7794
#> spanish: 579
#> other : 261
#> NA's : 359
#>
#>
#>
#-- convert to transactions object
trans = as(IncomeESL, "transactions")

```

## 9.2 Supervised Learning Problem

- The ESL text (ESL 14.2.4 - 14.2.7) outlines an interesting approach for finding frequent itemsets
- The idea is to simulate additional data under an appropriate null distribution (e.g., independence, uniform), combine the simulated data with the observed data, and assign a *label* indicating if the observation comes from the observed or simulated data



- Now any supervised learning procedure can be used to find regions of deviation from the null
  - That is, regions where there are more actual observations than simulated observations
- This concept can be incorporated into other tasks, like density estimation and clustering

### 9.3 Research Opportunities

- How can “repeatable patterns” be confirmed? E.g., statistical significance.
- How to incorporate resampling (bootstrap, cross-validation)?
- How to handle structure in items?
  - e.g., *small oranges*, *large oranges*, *bag of oranges* are all oranges
- Detect temporal changes in transaction data
- Find outliers and anomalies in transaction data
- Transaction clustering
- Weighted transactions