

Boosting

AdaBoost, Gradient Boosting, XGboost

SYS 6018 | Spring 2025

boosting.pdf

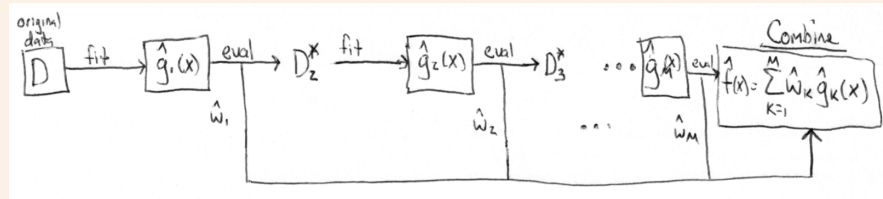
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1 Boosting

Boosting is a *sequential* ensemble method.

Boosting Sketch



- A boosting model can be written as a generic ensemble
 - M is the number of base learners
 - \hat{a}_k is the weight for the k th base learner ($\hat{a}_k \geq 0$).
 - $\hat{g}_k(x)$ is the prediction from the k th base learner

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \hat{g}_k(x)$$

- The key distinction of boosting models is that the base learners are **fitted sequentially**, and the best model at stage $m + 1$ is dependent on all models fit up to stage m .

$$\hat{f}_{m+1}(x) = \arg \min_{a, g(x)} \sum_{i=1}^n w_{mi} L(y_i, \hat{f}_m(x_i) + a g(x_i))$$

- Boosting is primarily a *bias* reducer
 - The base models are often simple/weak (low variance, but high bias) learners (like shallow trees)
- The complexity of the final model is based on i) the complexity of the base learners, ii) the number of iterations M , and iii) the magnitude of the ensemble weights a_k
 - Boosting models will overfit as the number of iterations increases
 - * Early stopping is necessary
 - * Less of a problem for hard classification problems with balanced data
 - Can apply *shrinkage* (making a_k smaller), to reduce complexity
- There are two main versions of boosting:
 - *Gradient Boosting*: fits the next model in the sequence $\hat{g}_k(x)$ to the (pseudo) residuals calculated from the predictions on the previous models
 - *AdaBoost*: fits the next model to sequentially *weighted* observations. The weights are proportional to the how poorly the current models predict the observation.

2 AdaBoost

AdaBoost was motivated by the idea that many *weak* learners can be combined to produce a *strong* aggregate model.

- AdaBoost is for binary classification problems
- Trees are a popular base learner
 - *Weak* learners are usually used. For trees, this means shallow depth.
- At each iteration, the current model is evaluated.
 - The *ensemble weight* of model k is based on its performance (on all the training data)
 - The *observation weight* of observation i is increased if it is mis-classified and decreased if it is correctly classified.
 - Thus, at each iteration, those observations that are mis-classified are weighted higher and get extra attention in the next iteration.
- Because Adaboost uses hard-classifiers, it is sensitive to unbalanced data and unequal misclassification costs.
 - Because the thresholds are set at $p > .50$
 - There are, of course, ways to account for unbalance and unequal costs in the algorithm
 - An improvement to AdaBoost, *LogitBoost* explicitly attempts to estimate the class probability during each iteration which will allow easier post-fitting adjustments for unequal costs

Weighted Loss Functions (with observations weights)

Let $w_i \geq 0$ be a *weight* associated with observation i . The weighted loss for predictions $\hat{\mathbf{y}} = \hat{y}_1, \hat{y}_2, \dots, \hat{y}_n$ is

$$L_{\mathbf{w}}(\mathbf{y}, \hat{\mathbf{y}}) = \sum_{i=1}^n w_i L(y_i, \hat{y}_i)$$

2.1 Adaboost Algorithm**Algorithm: AdaBoost (Discrete)****Inputs:**

- $D = \{(x_i, y_i)\}_{i=1}^n$, where $y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M or other stopping criteria

Algorithm:

1. Initialize *observation weights* $w_i = 1/n$ for all i
2. For $k = 1$ to M :
 - a. Fit a *classifier* $\hat{g}_k(x)$ that maps (x_i, w_i) to $\{-1, 1\}$. In other words, the classifier must make a hard classification using weighted observations.
 - b. Compute the weighted mis-classification rate

$$e_k = \frac{\sum_{i=1}^n w_i \mathbb{1}(y_i \neq \hat{g}_k(x_i))}{\sum_{i=1}^n w_i}$$

Note: $0 \leq e_k \leq .5$ since model fit and evaluated on same training data.

- c. Calculate the *coefficient* for model k (*ensemble weight*)

$$\hat{a}_k = \log \left(\frac{1 - e_k}{e_k} \right)$$

Note: $0 \leq a_k < \infty$.

- d. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

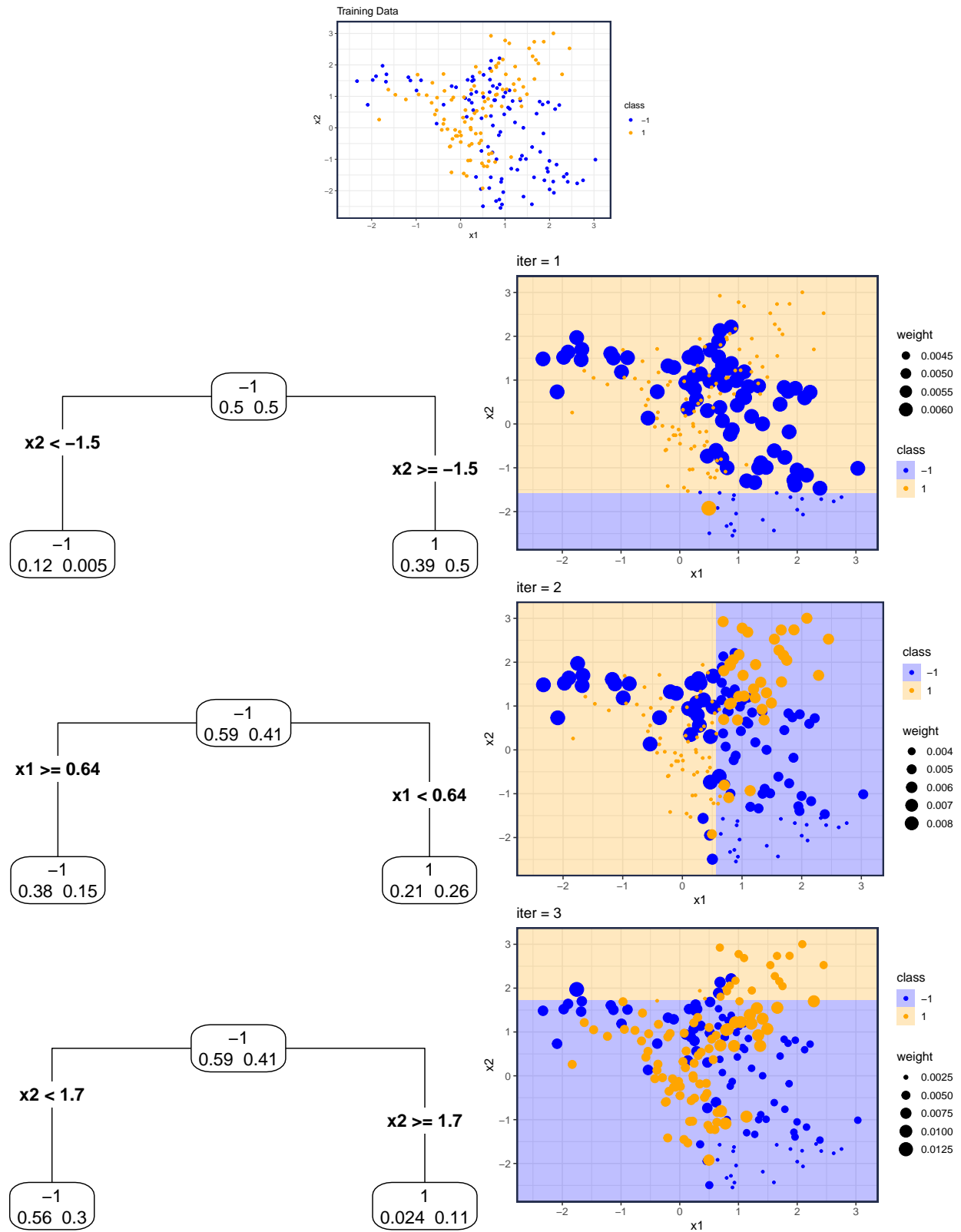
$$\begin{aligned} \tilde{w}_i &= w_i \cdot \exp(\hat{a}_k \cdot \mathbb{1}(y_i \neq \hat{g}_k(x_i))) \\ &= \begin{cases} w_i \frac{1-e_k}{e_k} & \text{if obs } i \text{ is misclassified} \\ w_i & \text{if obs } i \text{ is correctly classified} \end{cases} \\ w_i &= \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j} \quad (\text{re-normalize weights}) \end{aligned}$$

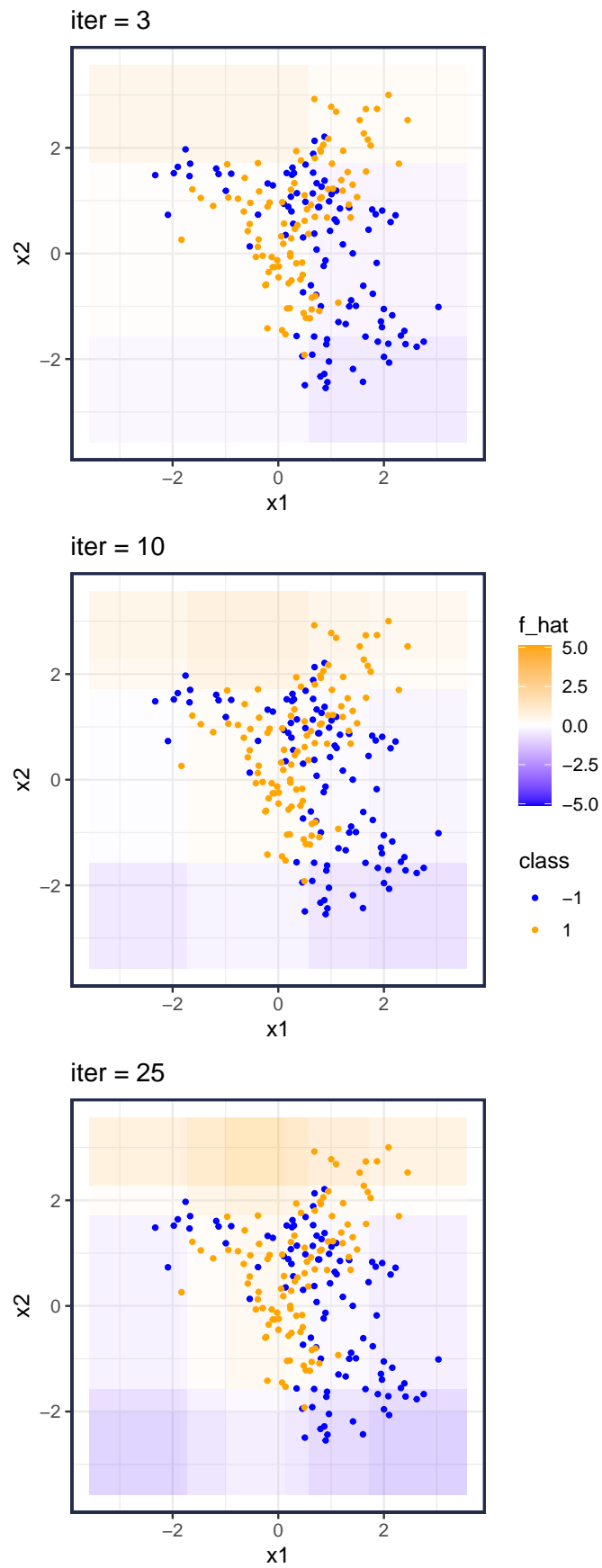
3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \hat{g}_k(x)$$

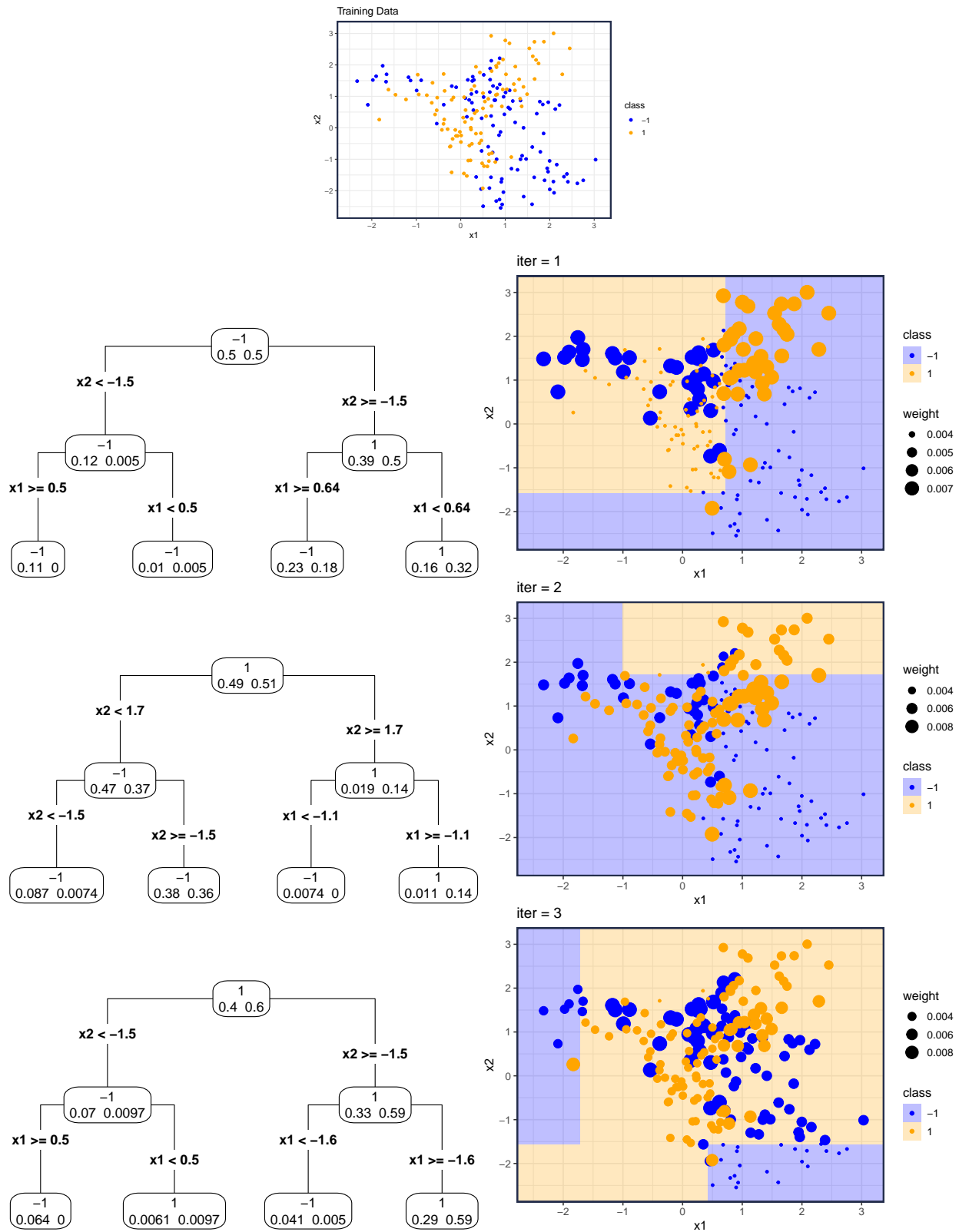
- Where $\hat{f}_k(x) = \hat{a}_k \hat{g}_k(x)$
- Hard classification: $\hat{f}_M(x) > \text{threshold}$
- Or remap to a probability $\hat{p}(x) = \frac{e^{2\hat{f}(x)}}{1+e^{2\hat{f}(x)}}$ for thresholding

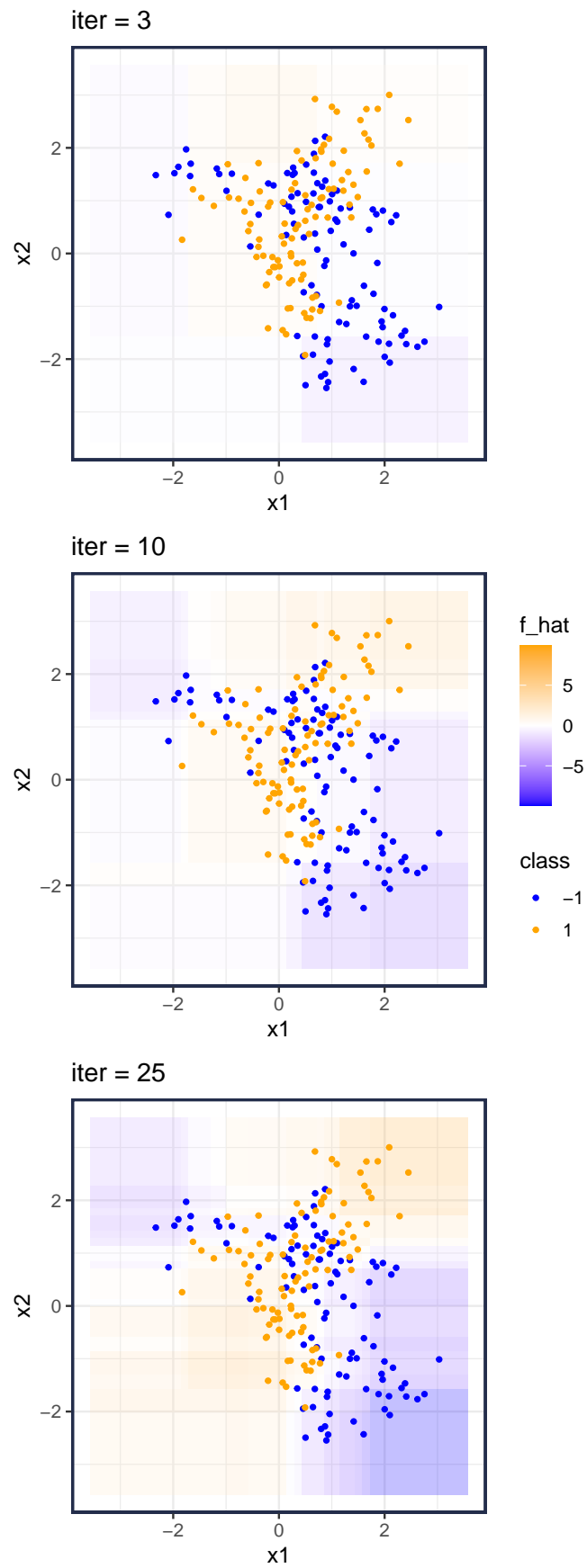
2.1.1 Illustration with Stumps (depth = 1, n.nodes=2)

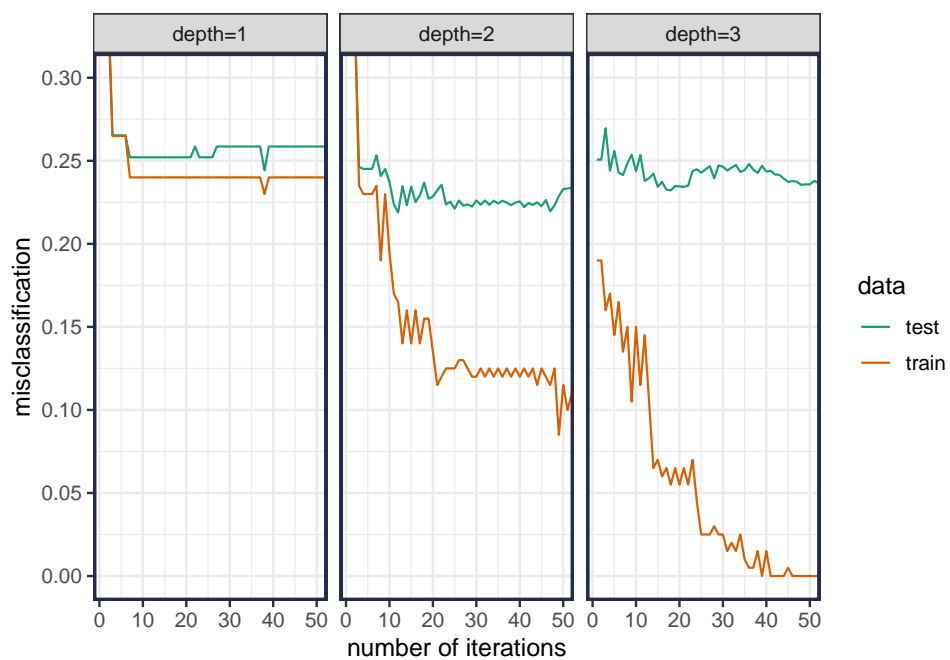
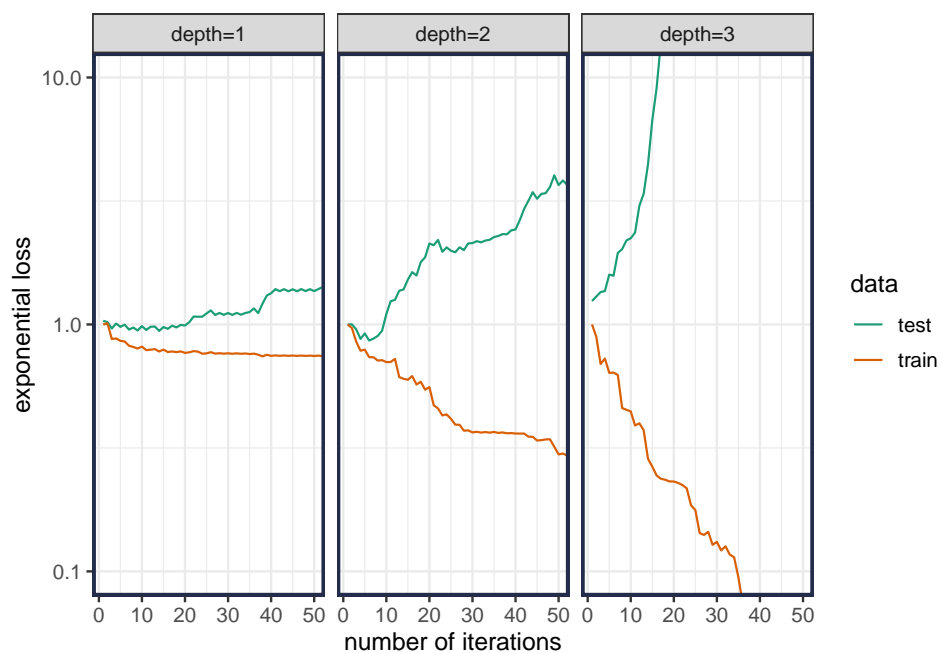




2.1.2 Illustration with depth = 2, n.nodes=4







2.2 AdaBoost Details

- Adaboost uses an outcome variable of $y \in \{-1, 1\}$
- AdaBoost implicitly uses the loss function:

$$L(y, f) = e^{-yf}$$

$$= \begin{cases} e^{-f} & y = +1 \\ e^f & y = -1 \end{cases}$$

- Adaboost estimates the probability that $Y = +1$ as

$$\hat{p}(x) = \frac{e^{\hat{f}_M(x)}}{e^{-\hat{f}_M(x)} + e^{\hat{f}_M(x)}}$$

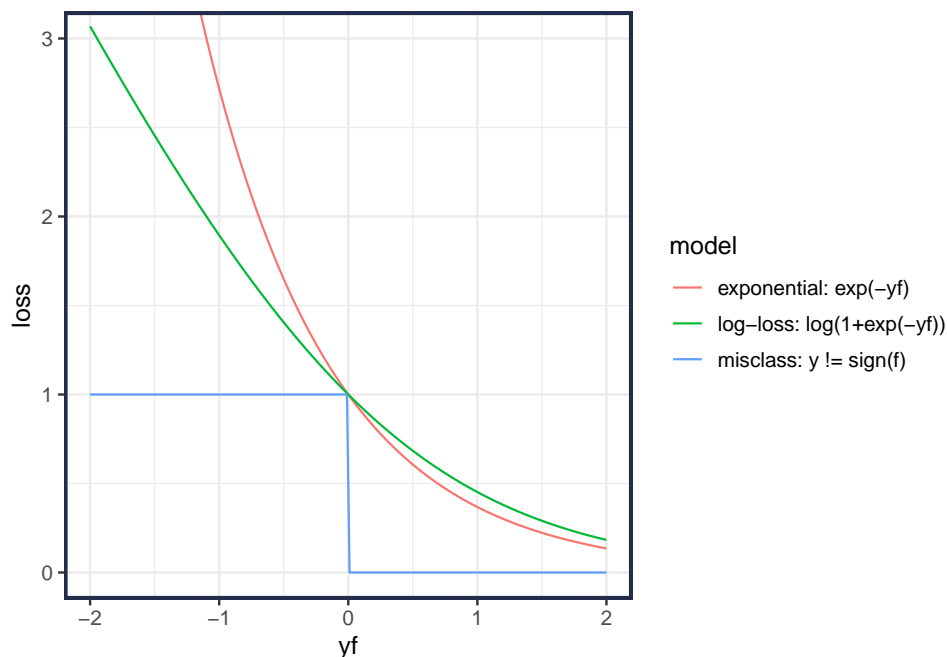
$$= \frac{e^{2\hat{f}_M(x)}}{1 + e^{2\hat{f}_M(x)}}$$

where $p(x) = \Pr(Y = +1 \mid X = x)$

- And $\hat{f}(x)$ is an estimate of

$$\hat{f}_M(x) = \frac{1}{2} \log \frac{\hat{p}(x)}{1 - \hat{p}(x)}$$

$$= \frac{1}{2} \text{logit } \hat{p}(x)$$

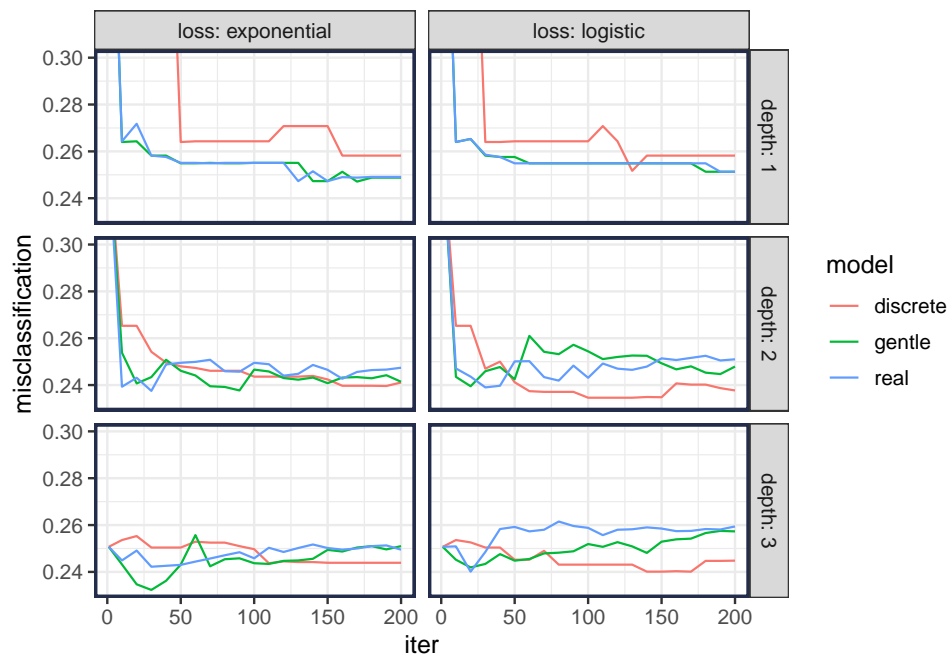


- Comparison with logistic regression (using log-loss / negative binomial log-likelihood)
 - $\hat{f}(x) = \text{logit } \hat{p}(x)$
 - $\hat{p}(x) = \frac{e^{\hat{f}_M(x)}}{1 + e^{\hat{f}_M(x)}}$
 - Log-loss: $\log(1 + e^{-yf})$ (using $y \in \{-1, +1\}$)

2.3 R package ada

The R package `ada` provides an implementation of AdaBoost (and related methods).

- See [Friedman, J., Hastie, T., and Tibshirani, R. \(2000\). Additive Logistic Regression: A statistical view of boosting. *Annals of Statistics*, 28\(2\), 337-374.](#) for the details of model variations
 - {Discrete, Real, Gentle} AdaBoost
 - Logitboost



Algorithm: Real AdaBoost

Inputs:

- $D = \{(x_i, y_i)\}_{i=1}^n$, where $y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M

Algorithm:

1. Initialize *observation weights* $w_i = 1/n$ for all i
2. For $k = 1$ to M :
 - a. Fit a model $\hat{g}_k(x)$ that uses weighted inputs (x_i, w_i) to estimate a probability $\hat{p}_k(x) = \widehat{\Pr}(Y = 1 \mid X = x)$. In other words, the classifier must make a soft classification using weighted observations.
 - b. Set $f_m(x) = \frac{1}{2} \text{logit } \hat{p}_k(x)$
 - c. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

$$\tilde{w}_i = w_i \cdot \exp(-y_i \hat{f}_m(x_i))$$

$$w_i = \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j} \quad (\text{re-normalize weights})$$

3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{f}_k(x)$$

- Hard classification: $\hat{f}_M(x) > 0$
- Or remap to a probability $\hat{p}(x) = \frac{e^{\hat{f}_M(x)}}{1 + e^{\hat{f}_M(x)}}$ for thresholding

Algorithm: Gentle AdaBoost

Inputs:

- $D = \{(x_i, y_i)\}_{i=1}^n$, where $y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M

Algorithm:

1. Initialize *observation weights* $w_i = 1/n$ for all i and $f_0(x) = 0$
2. For $k = 1$ to M :
 - a. Fit a model $\hat{g}_k(x)$ with weighted least squares that estimates y_i using features x_i and weights w_i .
 - b. Update the *observations weights*. Increase weights for observations that are mis-classified by model \hat{g}_k and decrease weights for the correctly classified observations.

$$\tilde{w}_i = w_i \cdot \exp(-y_i \hat{g}_m(x_i))$$

$$w_i = \frac{\tilde{w}_i}{\sum_{j=1}^n \tilde{w}_j} \quad (\text{re-normalize weights})$$

3. Output final ensemble $\hat{f}_M(x)$

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{g}_k(x)$$

- Hard classification: $\hat{f}_M(x) > 0$

Algorithm: LogitBoost

Inputs:

- $D = \{(x_i, y_i)\}_{i=1}^n$, where $y_i \in \{-1, 1\}$
- Tuning parameters for base model \hat{g}
- Maximum number of iterations, M
- Let $y_i^* = (y_i + 1)/2 \in \{0, 1\}$

Algorithm:

1. Initialize *observation weights* $w_i = 1/n$ for all i and $f_0(x) = 0$
2. For $k = 1$ to M :
 - a. Like in newton-raphson for logistic regression, calculate the working response and weights for all observations

$$z_i = \frac{y_i^* - p_i}{p_i(1 - p_i)}$$

$$w_i = p_i(1 - p_i)$$

- b. Fit a model $\hat{g}_k(x)$ with weighted least squares that estimates z_i using features x_i and weights w_i .
 - c. Update $\hat{f}_k(x) = \hat{f}_{k-1}(x) + \hat{g}_k(x)/2$ and $p_i = e^{\hat{f}_k(x)} / (e^{\hat{f}_k(x)} + e^{-\hat{f}_k(x)})$
3. Output final ensemble $\hat{f}_M(x) \in \mathbb{R}$

$$\hat{f}_M(x) = \sum_{k=1}^M \frac{1}{2} \hat{g}_k(x)$$

- Where $\hat{f}_k(x) = \frac{1}{2} \hat{g}_k(x)$.
- Hard classification: $\hat{f}_M(x) > 0$
- Or remap to a probability $\hat{p}(x) = \frac{e^{2\hat{f}}}{1+e^{2\hat{f}}}$ for thresholding

3 Gradient Boosting

The boosting model:

$$\hat{f}_M(x) = \sum_{k=1}^M \hat{a}_k \hat{g}_k(x)$$

Sequential Fitting:

$$\hat{f}_{k+1}(x) = \arg \min_{a, g(x)} \sum_{i=1}^n L(y_i, \hat{f}_k(x_i) + a g(x_i))$$

The concept of gradient boosting is to sequentially re-fit to the negative (functional) gradients of the loss function (think of the negative gradients as a type of residual; *pseudo residual*).

- The same structure can be used for many different loss functions
 - it works the same for regression and classification
 - survival analysis, ranking, etc.

3.1 Gradient Descent

- Our objective is to find the model (or model parameters) that minimize the loss function
- From any starting point, we can move toward the optimum using *gradient descent*:

$$f_{k+1} = f_k - \nu_k L'(f_k)$$

- $\nu_k > 0$ is the step-size
 - $L'(f_k)$ is the functional derivative of the loss with respect to the model f_k
- Boosting fits models sequentially:
$$\hat{f}_{k+1}(x) = \hat{f}_k(x) + \hat{a}_k \hat{g}_k(x)$$
- So we see a parallel; each boosting model $\hat{g}_k(x)$ can be viewed as estimating the *negative derivative* of the loss function.

3.2 L_2 Boosting

L_2 boosting is based on the the squared error loss function

$$L(y_i, \hat{f}(x_i)) = \frac{1}{2}(y_i - \hat{f}(x_i))^2$$

- The *negative gradients* are

$$\begin{aligned} r_i &= \left[-\frac{\partial L(y_i, f_i)}{\partial f_i} \right]_{f_i=\hat{f}(x_i)} \\ &= y_i - \hat{f}(x_i) \end{aligned}$$

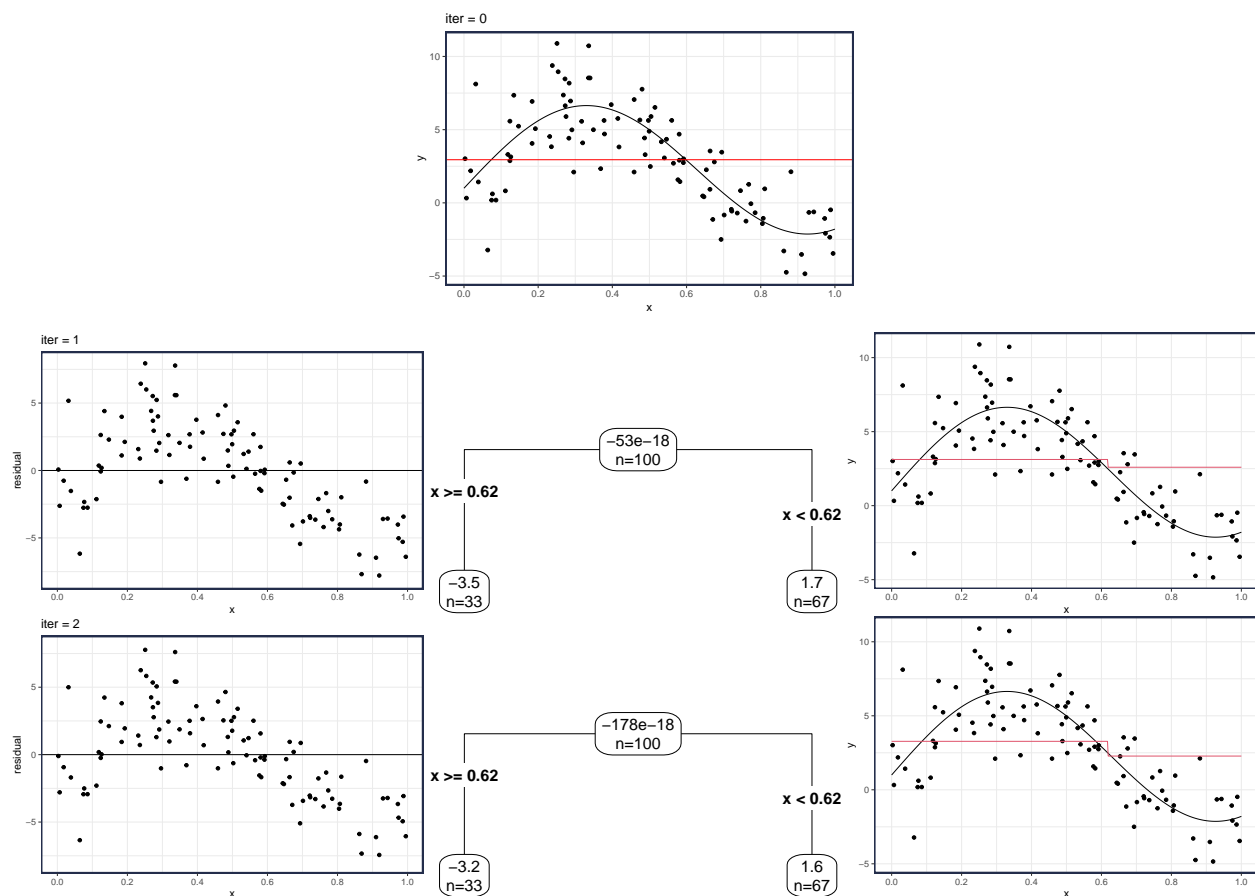
- L_2 Boosting is simply re-fitting to the residuals.

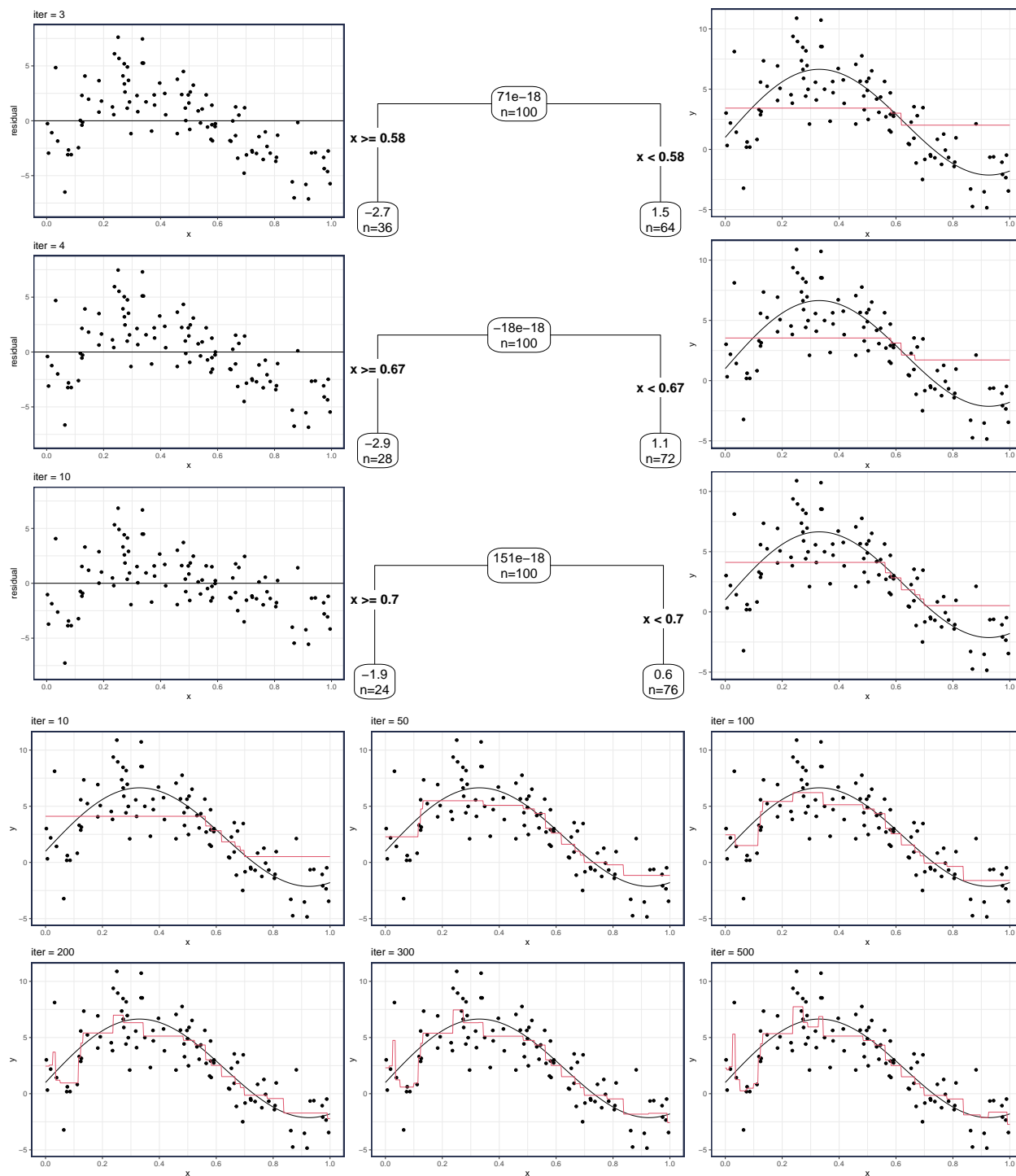
Algorithm: L_2 Boosting

1. Initialize $\hat{f}_0(x) = \bar{y}$
2. For $k = 1$ to M :
 - a. Calculate residuals $r_i = y_i - \hat{f}_{k-1}(x_i)$ for all i
 - b. Fit a base learner (e.g., regression trees) to the residuals $\{(x_i, r_i)\}_{i=1}^n$ to get the model $\hat{g}_k(x)$
 - c. Update the overall model $\hat{f}_k(x) = \hat{f}_{k-1}(x) + \nu \hat{g}_k(x)$
 - $0 \leq \nu \leq 1$ is the step-size (*shrinkage*)
3. Final model is $\hat{f}_M(x) = \bar{y} + \sum_{k=1}^M \nu \hat{g}_k(x)$

- Like AdaBoost, emphasis is given to observations that are predicted poorly (large residuals)

3.2.1 Illustration using stumps (depth=1, n.nodes=2, $\nu = .1$)





3.3 GBM (Gradient Boosting Machine)

- R package `gbm`
- [GBM Documentation](#)
- GBM is a first order approach. It does not consider Hessian.

3.3.1 Model/Tree Tuning Parameters

- Tree depth (`interaction.depth`)
 - Grows trees to a depth specified by `interaction.depth` (unless there are not enough observations in the terminal nodes)
- Minimum number of observations allowed in the terminal nodes (`n.minobsinnode`)
- Sub-sampling (`bag.fraction`)
 - *Stochastic Gradient Boosting*
 - Sample (without replacement) at each iteration
- Loss Function (`distribution`)
 - The loss function is determined by the `distribution` argument
 - Use `distribution="gaussian"` for squared error
 - Other options are: `bernoulli` (for logistic regression), `poisson` (for Poisson regression), `pairwise` (for ranking/LambdaMart), `adaboost` (for the adaboost exponential loss), etc.

3.3.2 Boosting Tuning Parameters

- Number of iterations/trees (`n.trees`)
 - Need to tune
- Shrinkage parameter (`shrinkage`)
 - Set small, but the smaller the `shrinkage`, the more iterations/trees need to be used
 - “Ranges from 0.001 to 0.100 usually work”
- Cross-validation (`cv.folds`)
 - `gbm` has a built in cross-validation
 - no way to manually set the folds

3.3.3 Computational Settings

- Number of Cores (`n.cores`)
 - Only used when cross-validation is implemented

3.4 xgboost (Extreme Gradient Boosting)

- R package `xgboost`
- [xgboost Documentation](#)
- [xgboost Model](#)
- [xgboost Paper](#)

3.4.1 Model/Tree Tuning Parameters

- Different base learners (`booster`)
 - `gbtree` is a tree
 - `gblinear` creates a (generalized) linear model (forward stagewise linear model)
- Tree building (`tree_method`)
 - To speed up the fitting, only consider making splits at certain quantiles of the input vector (rather than considering every unique value)
- Sub-sampling (`subsample`)
 - *Stochastic Gradient Boosting*
 - Sample (without replacement) at each iteration
- Feature sampling (`colsample_bytree`, `colsample_bylevel`, `colsample_bynode`)
 - Like used in Random Forest, the features/columns are subsampled
 - Can use a subsample of features for each tree, level, or node

Model Complexity Parameters

- Tree depth (`max_depth`)
 - Grows trees to a depth specified by `max_depth` (unless there are not enough observations in the terminal nodes)
 - Trees may not reach `max_depth` if the `gamma` or `min_child_weight` arguments are set.
- Minimum number of observations (or sum of weights) allowed in the terminal nodes (`min_child_weight`)
- Pruning (`gamma` or `min_split_loss`)
 - Minimum loss reduction required to make a further partition on a leaf node of the tree
 - The larger `gamma` is, the more conservative the algorithm will be
- ElasticNet type penalty (`lambda` and `alpha`)
 - `lambda` is an L_2 penalty
 - `alpha` is an L_1 penalty

Note

- Recall that trees model the outcome as a *constant* in each region

$$\hat{f}_T(x) = \sum_{m=1}^M \hat{c}_m \mathbb{1}(x \in \hat{R}_m)$$

- Cost-complexity pruning found the optimal tree as the one that minimized the penalized loss objective

function:

$$C_{\gamma}(T) = \sum_{m=1}^{|T|} \text{Loss}(T) + \gamma|T|$$

- XGBoost selects a tree at each iteration using the following penalized loss:

$$C_{\gamma,\lambda,\alpha}(T) = \sum_{m=1}^{|T|} \text{Loss}(T) + \gamma|T| + \frac{\lambda}{2} \sum_{m=1}^{|T|} \hat{c}_m^2 + \alpha \sum_{m=1}^{|T|} |\hat{c}_m|$$

- Loss Function (objective)
 - The loss function is determined by the objective argument
 - Use `reg:squarederror` for squared error
 - Other options are: `reg:logistic` or `binary:logistic` (for logistic regression), `count:poisson` (for Poisson regression), `rank:pairwise` (for ranking/LambdaMart), etc.

3.4.2 Boosting Tuning Parameters

- Shrinkage parameter (`eta` or `learning_rate`)
 - Set small, but the smaller the `eta`, the more iterations/trees need to be used
- Number of iterations/trees (`num_rounds`)
- Cross-validation (`xgb.cv`)
 - `xgboost` has a built in cross-validation
 - It is possible to manually set the folds

3.4.3 Computational Settings

- Number of Threads (`nthread`)
- GPU Support (<https://xgboost.readthedocs.io/en/latest/gpu/index.html>)
 - Used for finding tree split points and evaluating/calculating the loss function

3.5 CatBoost

- R package: (<https://github.com/catboost/catboost/tree/master/catboost/R-package>)
- [CatBoost Documentation](#)
- Model/Tree Tuning Parameters:

- Boosting Tuning Parameters:

3.6 LightGBM

- R Package: <https://github.com/microsoft/LightGBM/tree/master/R-package>
- [LightGBM Documentation](#)
- Model/Tree Tuning Parameters:

- Boosting Tuning Parameters:

4 Appendix: L2 Tree Boosting R Code

```

# L2 Boost Algorithm
library(rpart)

# L2boost()
#-----#
# L2 boosted trees (boosted regression trees)
# Inputs:
# x,y: training data. x should be data frame or matrix, y a vector
# xtest optional test data (data frame or matrix)
# M: number of iterations
# depth: tree depth. depth = 2 gives 4 leaf nodes.
# nu: shrinkage parameter
# Outputs:
# YHAT: matrix of in-sample predictions (predicting x)
# R: matrix of residuals
# YHAT.test: matrix of predictions for xtest
# TREE: list of rpart trees
#-----#

L2boost <- function(x, y, xtest=NULL, M=100, depth=2, nu=.1){

  #- use training data if test data is not specified
  if(is.null(xtest)) {
    xtest = x
  }

  #- storage
  n = length(y)
  R = YHAT = matrix(NA_real_, n, M)
  YHAT_test = matrix(NA_real_, nrow(xtest), M)
  colnames(YHAT) = colnames(YHAT_test) = colnames(R) = paste0("iter = ", 1:M)
  TREE = vector("list", M)
  names(TREE) = paste0("iter = ", 1:M)

  #-- 1) initialize model with mean
  mu = mean(y)
  yhat = rep(mu, nrow(x))
  yhat_test = rep(mu, nrow(xtest))

  for(m in 1:M){

```

```

    ##-- 2a) Calculate Residuals
    r = y - yhat
    R[,m] = r

    ##-- 2b) Fit regression tree
    tree = rpart(r ~ ., data = x,
                  maxdepth = depth, # control tree depth
                  cp = -1,          # no pruning
                  minsplit = 0,     # allow all splits
                  minbucket = 1,    # no minimum on leaf size
                  method = "anova", # least-squares loss function
                  xval = 0)         # no cross-validation

    TREE[[m]] = tree

    ##-- 2c) Update model
    yhat = yhat + nu*predict(tree, x)
    YHAT[, m] = yhat

    yhat_test = yhat_test + nu*predict(tree, xtest)
    YHAT_test[, m] = yhat_test

  }

  ##-- 3) Output
  return(list(YHAT=YHAT, R=R, YHAT.test=YHAT_test, TREE=TREE))
}

##: Data Generation
n = 100 # number of observations
generate_x <- function(n) runif(n) # U[0,1]
f <- function(x) 1 + 2*x + 5*sin(5*x) # true mean function
sd = 2 # stdev for error

set.seed(825) # set seed for reproducibility
x = generate_x(n) # get x values
y = f(x) + rnorm(n, sd=sd) # get y values
data_train = data.frame(x, y) # training data
x_eval = seq(0, 1, length=500) # evaluation points

##: Implement L2 boosting
L2 = L2boost(data.frame(x), y, xtest=data.frame(x=x_eval), # data
             depth = 1, M = 100, nu = .1) # tuning parameters

##: Plotting
library(tidyverse) # for ggplot2 package
library(rpart.plot) # for prp()

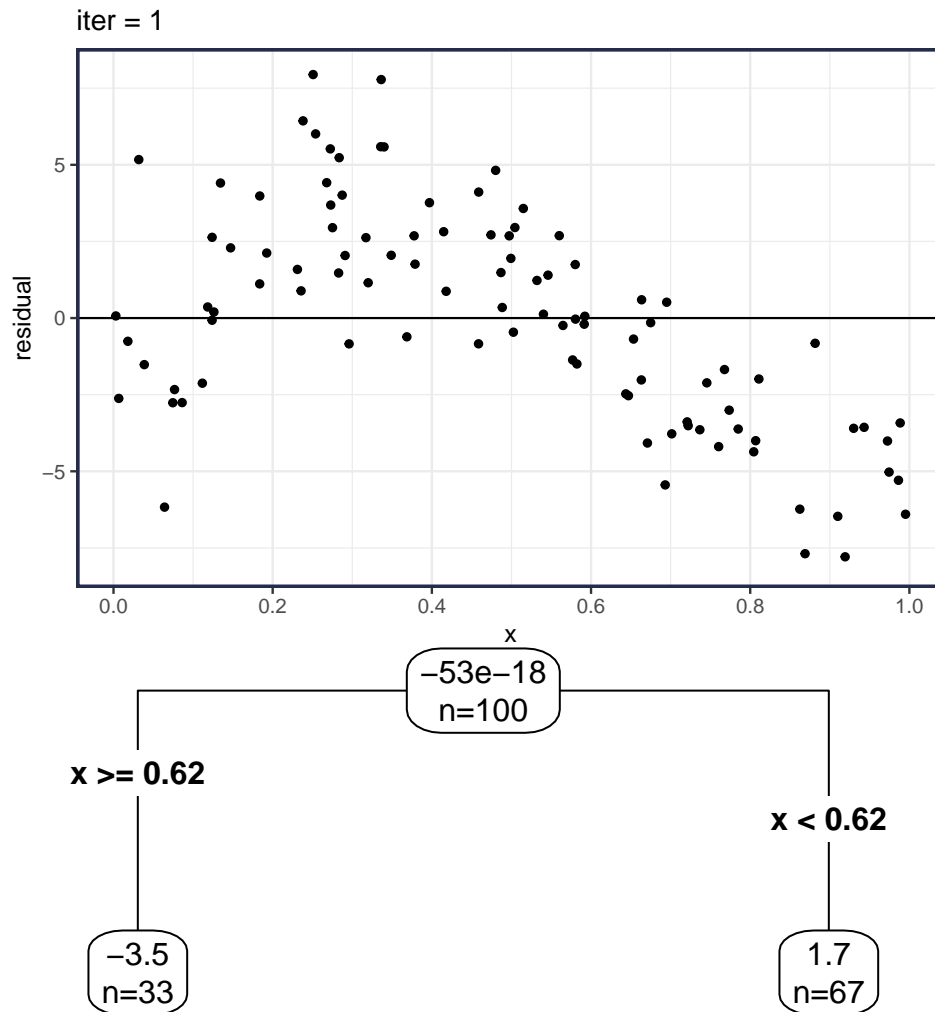
# set iteration
i = 1

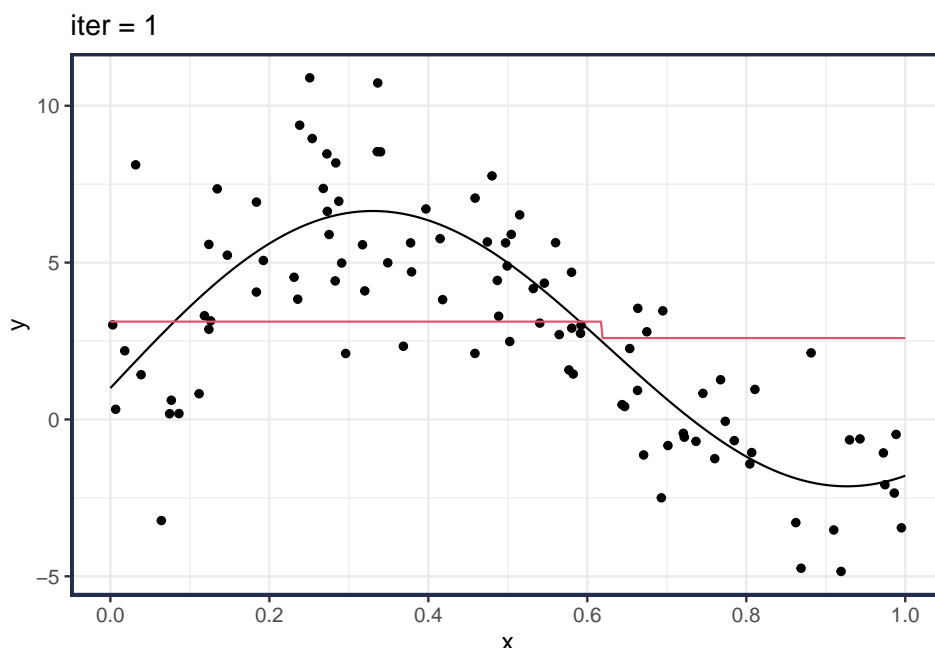
# Residual Plot
ggplot(data_train, aes(x)) +
  geom_point(aes(y = L2$R[,i]), col="black") +
  geom_hline(yintercept=0, col="black") +
  scale_x_continuous(breaks=seq(0, 1, by=.20)) +
  coord_cartesian(ylim=c(-8, 8)) +
  labs(y="residual", title=colnames(L2$R)[i])

```

```
# Tree
prp(L2$TREE[[i]], type=4, extra=1, branch=1, clip.right.labs = FALSE, roundint=FALSE)

# Model prediction
ggplot(data_train, aes(x, y)) +
  geom_point() +
  annotate("line", x=x_eval, y=f(x_eval), color = "black") +
  geom_line(data=tibble(x=x_eval, y=L2$YHAT.test[,i]), col=2) +
  scale_x_continuous(breaks=seq(0, 1, by=.20)) +
  labs(title=colnames(L2$R)[i])
```





5 Appendix: xgboost and lightgbm

```
# Load required packages
library(tidyverse)
library(palmerpenguins) # data
library(xgboost)
library(lightgbm)
```

We will use the [palmer penguins data](#):

```
palmerpenguins::penguins
#> # A tibble: 344 x 8
#>   species island bill_length_mm bill_depth_mm flipper_length_mm body_mass_g
#>   <fct>   <fct>         <dbl>         <dbl>         <int>         <int>
#> 1 Adelie  Torgersen         39.1          18.7          181          3750
#> 2 Adelie  Torgersen         39.5          17.4          186          3800
#> 3 Adelie  Torgersen         40.3           18          195          3250
#> 4 Adelie  Torgersen          NA           NA           NA           NA
#> 5 Adelie  Torgersen         36.7          19.3          193          3450
#> 6 Adelie  Torgersen         39.3          20.6          190          3650
#> # i 338 more rows
#> # i 2 more variables: sex <fct>, year <int>
```

with a goal of predicting the species from the other variables. This is a three-class probability estimation problem. Most tree-based models can handle multiple classes naturally.

Note that the sex and island predictors are categorical.

5.1 xgboost

Requires a numeric matrix as input, and suggests using a special xgb formatted matrix for efficiency. The approach here is to create a *recipe* that does some pre-processing to handle missing values and categorical predictors and then create the special matrix.

Notes:

- The recipe removes observations with missing outcomes. It also sets unknown categorical/nominal values to an explicit level. Any missing values in the resulting data are handled internally by xgboost.
- the categorical (or nominal) predictors are dummy encoded.
- the three level outcome variables *species* is recoded to be $\{0, 1, 2\}$. All xgboost data must be numeric, even if it represents a nominal variable.

```
library(recipes) # part of tidymodels
library(xgboost)

# pre-processing specs
rec_xgb = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
  step_naomit(species) %>% # remove cases with missing outcome label
  step_unknown(all_nominal_predictors()) %>% # add "unknown" level if missing
  # replace categorical/factors with numeric
  step_dummy(all_nominal_predictors(), one_hot = FALSE) %>%
  step_integer(species, zero_based = TRUE) %>%
  # train or prepare the pre-process step using the data provided in recipe()
  prep()

# xgboost data object
xgb_data =
  xgb.DMatrix(
    data = bake(rec_xgb, new_data = NULL, composition = "matrix",
                 all_predictors()),
    label = bake(rec_xgb, new_data = NULL, all_outcomes()) %>% pull()
  )

# tuning parameters
xgb_tuning = list(
  learning_rate = .1,
  gamma = 1,
  max_depth = 2,
  subsample = .80
)

# Note, the number of iterations, nrounds, is not part of the params.

# fit model
set.seed(1234) # xgboost can use stochastic resampling
xgb = xgboost(data = xgb_data,
              params = xgb_tuning, nrounds = 100, # tuning parameters
              num_class = 3, # this is required for multi-class problems
              objective = "multi:softprob", # multi-class loss function
              verbose = 0) # don't print output during training

# make predictions
predict(xgb, xgb_data, reshape = TRUE) %>% head()
#>      [,1]      [,2]      [,3]
#> [1,] 0.9941 0.003113 0.002755
#> [2,] 0.9938 0.003303 0.002924
#> [3,] 0.9938 0.003303 0.002924
#> [4,] 0.5404 0.025182 0.434446
#> [5,] 0.9941 0.003113 0.002755
#> [6,] 0.9941 0.003113 0.002755
```

5.2 lightgbm

Following a similar process to what is required for xgboost. LightGBM requires a matrix as input, and suggests using a special formatted matrix. The approach here follows the recipe that is used for xgboost with the exception that lightgbm can internally handle categorical predictors.

Notes:

- The recipe removes observations with missing outcomes. It also sets unknown categorical/nominal values to an explicit level. Any missing values in the resulting data are handled internally by lightgbm.
- the categorical (or nominal) predictors are integer encoded $\{0, 1, \dots\}$ so they are numeric, and then handled internally by lightGBM. The `categorical_features` argument in the `lgb.Dataset()` function is used to specify which predictors should be treated as categorical.
- the three level outcome variables `species` is recoded to be $\{0, 1, 2\}$. All lightgbm data must be numeric, even if it represents a nominal variable.

```
library(recipes) # part of tidymodels
library(lightgbm)

# pre-processing specs
rec_lgbm = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
  step_naomit(species) %>% # remove cases with missing outcome label
  step_unknown(all_nominal_predictors()) %>% # add "unknown" level if missing
  # replace categorical/factors with numeric
  step_integer(all_nominal_predictors(), zero_based = TRUE) %>%
  step_integer(species, zero_based = TRUE) %>%
  # train or prepare the pre-process step using the data provided in recipe()
  prep()

# lgb data object
X = bake(rec_lgbm, new_data = NULL, composition = "matrix", all_predictors())
lgbm_data =
  lgb.Dataset(
    data = X,
    colnames = colnames(X),
    categorical_feature = c("island", "sex"),
    label = bake(rec_lgbm, new_data = NULL, all_outcomes()) %>% pull()
  )

# tuning parameters
lgbm_tuning = list(
  # settings
  objective = "multiclass",
  num_class = 3,
  # tuning parameters
  nrounds = 100,
  min_gain_to_split = 1,
  learning_rate = 0.1,
  max_depth = 2,
  bagging_freq = 1, # enable subsampling
  bagging_fraction = 0.8, # subsample size
  bagging_seed = 123, # controls the internal sampling
  seed = 987 # controls feature sampling
)

# fit model
lgbm = lightgbm(data = lgbm_data, params = lgbm_tuning, verbose = -1)
```

```
#> Warning in .get_default_num_threads(): Optional package 'RhpcBLASctl' not
#> found. Will use default number of OpenMP threads.

# : make predictions
predict(lgbm, X) %>% head()
#>      [,1]      [,2]      [,3]
#> [1,] 0.9979 0.001190 0.000868
#> [2,] 0.9973 0.001540 0.001123
#> [3,] 0.9972 0.001700 0.001123
#> [4,] 0.8176 0.015829 0.166561
#> [5,] 0.9976 0.001413 0.001031
#> [6,] 0.9979 0.001190 0.000868
```

5.3 Tidymodels

The `bonsai` and `xgboost` packages are necessary to use `lightgbm` and `xgboost` in `parsnip`.

```
library(tidymodels)
library(bonsai) # for lightgbm
library(xgboost) # for xgboost
```

This defines the `parsnip` model specification for `xgboost`, modifies the recipe to leave the outcome as a factor, and adds it to a *workflow*.

```
# : pre-processing specs
rec_xgb = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
  step_naomit(species) %>% # remove cases with missing outcome label
  step_unknown(all_nominal_predictors()) %>% # add "unknown" level if missing
  # replace categorical/factors with numeric
  step_dummy(all_nominal_predictors(), one_hot = FALSE)

# Define the XGBoost model specification
xgb_spec = boost_tree(
  trees = 100,                # nrounds
  tree_depth = 2,             # Max depth of the trees
  learn_rate = 0.1,           # Learning rate
  loss_reduction = 1,         # Gamma (min_split_loss)
  sample_size = 0.8,          # Subsample ratio
  mode = "classification"     # For multi-class classification
) %>%
  set_engine("xgboost", objective = "multi:softprob", num_class = 3)

# : Create XGBoost workflow (combine recipe with model specification)
xgb_wf = workflow(preprocessor = rec_xgb, spec = xgb_spec)

# Fit the model
set.seed(1234)
xgb_fit = fit(xgb_wf, data = palmerpenguins::penguins)
#> Warning: ! The argument `num_class` is guarded by parsnip and will not be passed to
#> `xgb.train()`.

# Make predictions on the training data
predict(xgb_fit, palmerpenguins::penguins, type = "prob") %>% head()
#> # A tibble: 6 x 3
#>   .pred_Adelie .pred_Chinstrap .pred_Gentoo
#>   <dbl>        <dbl>        <dbl>
#> 1      0.994      0.00311      0.00275
```

```
#> 2      0.994      0.00330      0.00292
#> 3      0.994      0.00330      0.00292
#> 4      0.540      0.0252      0.434
#> 5      0.994      0.00311      0.00275
#> 6      0.994      0.00311      0.00275
```

```
#: pre-processing specs
rec_lgbm = recipe(species ~ ., data = palmerpenguins::penguins) %>%
  # Handle missing data
  step_naomit(species) %>% # remove cases with missing outcome label
  step_unknown(all_nominal_predictors()) # add "unknown" level if missing

# Define the lightgbm model specification
lgbm_spec = boost_tree(
  trees = 100,                # nrounds
  tree_depth = 2,             # Max depth of the trees
  learn_rate = 0.1,           # Learning rate
  loss_reduction = 1,         # min_gain_to_split
  sample_size = 0.8,          # Subsample ratio
  mode = "classification"     # For multi-class classification
) %>%
  set_engine("lightgbm", objective = "multiclass", num_class = 3, num_threads = 6) %>%
  set_args(
    bagging_seed = 123 # controls the internal sampling
  )

#: Create XGBoost workflow (combine recipe with model specification)
lgbm_wf = workflow(preprocessor = rec_lgbm, spec = lgbm_spec)

# Fit the model
lgbm_fit = fit(lgbm_wf, data = palmerpenguins::penguins)

# Make predictions on the training data
predict(lgbm_fit, palmerpenguins::penguins, type = "prob") %>% head()
#> # A tibble: 6 x 3
#>   .pred_Adelie .pred_Chinstrap .pred_Gentoo
#>   <dbl>        <dbl>        <dbl>
#> 1     0.998      0.00119      0.000868
#> 2     0.997      0.00154      0.00112
#> 3     0.997      0.00170      0.00112
#> 4     0.818      0.0158       0.167
#> 5     0.998      0.00141      0.00103
#> 6     0.998      0.00119      0.000868
```