BLUE PRINT : SA-I (IX) : MATHEMATICS

| Unit/Topic | 1 | 2 | 3 | 4 | Total |
|--|------|-------|--------|--------|--------|
| Number System | 1(1) | 2(1) | 6(2)* | 8(2)* | 17(6) |
| Algebra Polynomials | 3(3) | 4(2) | 6(2) | 12(3) | 25(10) |
| Geometry Euclids Geom, Lines and Angles, Triangles | 2(2) | 4(2)* | 15(5)* | 16(4) | 37(13) |
| Coordinate Geometry | - | 2(1) | - | 4(1) | 6(2) |
| Mensuration | 2(2) | = | 3(1) | = | 5(3) |
| Total | 8(8) | 12(6) | 30(10) | 40(10) | 90(34) |

SAMPLE QUESTION PAPER, SA-I

CLASS: IX

Time: 3hrs. MM: 90

SECTION - A

Question numbers 1 to 8 carry 1 mark each. For each question, four alternative choices have been provided of which only one is correct. You have to select the correct choice.

1. Which of the following is a rational number?

(A) $\frac{-2}{3}$ (B) $\frac{-1}{\sqrt{5}}$ (C) $\frac{13}{\sqrt{5}}$ (D) $\frac{\sqrt{2}}{3}$

2. The value of k, for which the polynomial x^3-3x^2+3x+k has 3 as its zero, is

(A) -3

(B) 9

(C) -9

(D) 12

3. Which of the following is a zero of the polynomial x^3+3x^2-3x-1 ?

(A) -1

(B) -2

(C) 1

(D) 2

4. The factorisation of $-x^2+5x-6$ yields:

(A) (x-2)(x-3) (B) (2+x)(3-x) (C) -(x-2)(3-x) (D) -(2-x)(3-x)

In fig.1, ∠DBC equals

(A) 40°

(B) 60°

(C) 80°

(D) 100°

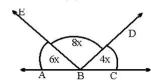


Fig.1

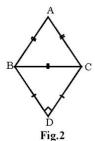
In fig.2, ABC is an equilateral triangle and BDC is an isosceles right triangle, right angled at D. \(ABD \) equals

(A) 45°

(B) 60°

(C) 105°

(D) 120°



7. The sides of a triangle are 12cm, 16cm and 20cm. Its area is

(A) 48cm²

(B) 96cm²

(C) 120cm²

160cm²

8. The side of an isosceles right triangle of hypotenuse $4\sqrt{2}cm$ is

(A) 8cm

(B) 6cm

(C) 4cm

(D) $4\sqrt{3}$ cm

SECTION - B

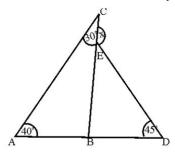
Question numbers 9 to 14 carry 2 marks each :

9. If
$$x = 7 + \sqrt{40}$$
, find the value of $\sqrt{x} + \frac{1}{\sqrt{x}}$

10. Factorise the polynomial: $8x^3 - (2x-y)^3$

11. Find the value of 'a' for which (x-1) is a factor of the polynominal $a^2x^3-4ax+4a-1$

12. In Fig. 3, if AC=BD, show that AB=CD. State the Euclid's postulate/axiom used for the same.



13. In Fig. 4 find the value of x.

Fig. 4

OR

In Fig.5, ABCDE is a regular pentagon. Find the relation between 'a', 'b' and 'c'

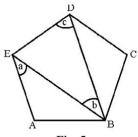


Fig. 5

14. In Fig. 6, ABC is an equilateral triangle. The coordinates of vertices B and C are (3,0) and (-3,0)

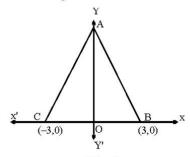


Fig. 6

respectively. Find the coordinates of its vertex A.

SECTION - C

Question numbers 15 to 24 carry 3 marks each:

15. **Evaluate**:
$$\left\{ \sqrt{5 + 2\sqrt{6}} \right\} + \left\{ \sqrt{8 - 2\sqrt{15}} \right\}$$

OR

If a=9 - $4\sqrt{5}$, Find the value of $a^2 + \frac{1}{a^2}$

16. Simplify the following:

$$\frac{7+3\sqrt{5}}{3+\sqrt{5}} - \frac{7-3\sqrt{5}}{3-\sqrt{5}}$$

OR

If
$$\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}} = a+\sqrt{15}$$
 b, find the values of a and b

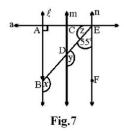
17. Factorise the following:

$$12(x^2+7x)^2-8(x^2+7x)(2x-1)-15(2x-1)^2$$

18. Show that 2 and $-\frac{1}{3}$ are the zeroes of the polynomial $3x^3-2x^2-7x-2$.

Also, find the third zero of the polynomial

19. In Fig. 7, $\ell \parallel m \parallel n$ and $a \perp \ell$. If $\angle BEF = 55^{\circ}$, Find the values of x, y and z



OR

4

In Fig. 8, $\ell \parallel m \parallel n$. From the figure find the value of (y+x): (y-x)

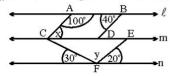
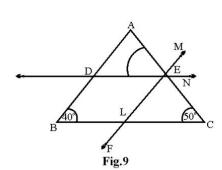


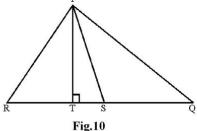
Fig.8

20. In Fig.9, DE||BC and MF||AB.

Find (i) ∠ADE+∠MEN (ii) ∠BDE (iii) ∠BLE



21..., QPR and PT \perp RQ. Show that \angle TPS = $\frac{1}{2}(\angle R - \angle Q)$



22. In Fig. 11, \triangle ABC and \triangle ABD are such that AD=BC, \angle 1 = \angle 2 and \angle 3 = \angle 4. Prove that BD = AC

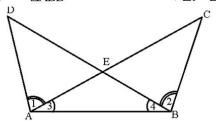
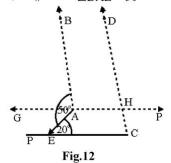


Fig.11

23. In Fig. 12, AB||CD. If $\angle BAE = 50^{\circ}$ and $\angle AEC = 20^{\circ}$, find $\angle DCE$



24. Find the area of a triangle whose perimeter is 180cm and two of its sides are 80cm and 18cm. Also calculate the altitude of the triangle corresponding to the shortest side.

SECTION-D

Question numbers 25 to 34 carry 4 marks each:

25. If
$$x = \frac{1}{2 - \sqrt{3}}$$
, find the value of $x^3 - 2x^2 - 7x + 5$

Simplify:
$$\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} + \dots + \frac{1}{\sqrt{8}+\sqrt{9}}$$

26. If
$$x = \frac{\sqrt{p+2q} + \sqrt{p-2q}}{\sqrt{p+2q} - \sqrt{p-2q}}$$
, then show that $qx^2-px+q=0$

If
$$x = \frac{\sqrt{2} + 1}{\sqrt{2} - 1}$$
 and $y = \frac{\sqrt{2} - 1}{\sqrt{2} + 1}$, find the value of $x^2 + y^2 + xy$

- 27. If x³+mx²-x+6 has (x-2) as a factor, and leaves a remainder n when divided by (x-3), find the values of m and n.
- 28. Prove that $(x+y)^3 + (y+z)^3 + (z+x)^3 3(x+y)(y+z)(z+x) = 2(x^3+y^3+z^3-3xyz)$
- 29. If A and B be the remainders when the polynomials $x^3+2x^2-5ax-7$ and $x^3+ax^2-12x+6$ are divided by (x+1) and (x-2) respectively and 2A+B=6, find the value of 'a'
- 30. From Fig. 13, find the coordinates of the points A,B,C,D,E and F. Which of the points are mirror images in (i) x-axis (ii) y-axis

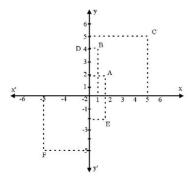


Fig.13

31. In Fig. 14, QT \perp PR, \angle TQR = 40° and \angle SPR = 30°. Find the values of x,y and z

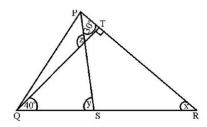


Fig.14

(i) DF=BE

(ii) AM bisects ∠BAD

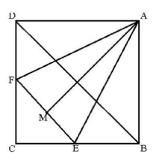
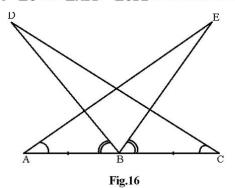


Fig.15

33. In Fig.16, AB=BC, \angle A = \angle C and \angle ABD = \angle CBE . Prove that CD=AE



34.In Fig.17, AB=AC, D is a point in the interior of $\triangle ABC$ such that $\angle DBC = \angle DCB$. Prove that AD bisects $\angle BAC$ of $\triangle ABC$

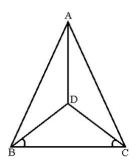


Fig.17

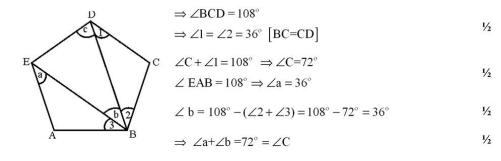
SAMPLE QUESTION PAPER, SA-I

MARKING SCHEME

CLASS: IX

Time: 3hrs. MM: 90 **SECTION - A** 1. (A) 2. (C) 3. (C) 4. (D) 6. (C) 7. (B) 5. (A) 8. (C) 1x8 = 8**SECTION - B** 9. $x = 7 + \sqrt{40} = 7 + 2\sqrt{10} = (\sqrt{5})^2 + (\sqrt{2})^2 + 2(\sqrt{5})(\sqrt{2}) = (\sqrt{5} + \sqrt{2})^2$ 1/2 $\Rightarrow \sqrt{x} = \sqrt{5} + \sqrt{2} , \frac{1}{\sqrt{x}} = \frac{1}{\sqrt{5} + \sqrt{2}} = \frac{\sqrt{5} - \sqrt{2}}{3}$ 1/2 $\therefore \sqrt{x} + \frac{1}{\sqrt{x}} = \frac{3(\sqrt{5} + \sqrt{2}) + (\sqrt{5} - \sqrt{2})}{3} = \frac{1}{3} \left[4\sqrt{5} + 2\sqrt{2} \right]$ 1/2 $=\frac{2}{3}\left[2\sqrt{5}+\sqrt{2}\right]$ 1/2 10. $8x^3 - (2x-y)^3 = (2x)^3 - (2x-y)^3$ 1/2 = $[2x-(2x-y)][(2x)^2+(2x-y)^2+2x(2x-y)]$ 1/2 $= v [4x^2+4x^2+v^2-4xv+4x^2-2xv]$ 1/2 $= v [12x^2 + v^2 - 6xv]$ 1/2 11. $P(x) = a^2 x^3 - 4ax + 4a - 1$ $P(1) = 0 \Rightarrow a^2 - 4a + 4a - 1 = 0 \Rightarrow a = +1$ 1+1 12. $AC=BD \Rightarrow AC - BC = BD - BC$ \Rightarrow AB = CD 1+1/2 Euclid's Axiom: If equals are subtracted from equals, the remainders are equal 1/2 13. $\angle ABC = 180^{\circ} - (40^{\circ} + 30^{\circ}) = 110^{\circ} \Rightarrow \angle CBD = 70^{\circ}$ 1 1 $x = \angle CBD + \angle BDE = 70^{\circ} + 45^{\circ} = 115^{\circ}$

ABCD is a regular pentagon



14. AB = 6 unit $\Rightarrow AC = BC = 6$ units

OA = 3 units and
$$\angle AOC = 90^{\circ}$$

$$\Rightarrow OC^{2} = AC^{2} - OA^{2} = 36 - 9 = 27$$

$$\Rightarrow OC = 3\sqrt{3} \text{ units}$$

 \therefore Coordinates of C are $(0, 3\sqrt{3})$ 1/2

SECTION - C

15.
$$\sqrt{5+2\sqrt{6}} = \sqrt{3+2+2\sqrt{6}}$$

$$= \sqrt{(\sqrt{3})^2 + (\sqrt{2})^2 + 2\sqrt{3}\sqrt{2}} = \sqrt{(\sqrt{3}+\sqrt{2})^2} = \sqrt{3} + \sqrt{2}$$

$$= \sqrt{3} + \sqrt{2}$$

$$= \sqrt{3} + \sqrt{2}$$

Also,
$$\sqrt{8-2\sqrt{15}} = \sqrt{(\sqrt{5})^2 + (\sqrt{3})^2 - 2\sqrt{5}\sqrt{3}} = \sqrt{(\sqrt{5}-\sqrt{3})^2} = \sqrt{5} - \sqrt{3}$$
 \quad \frac{1}{2} + \frac{1}{2}

:. Required sum =
$$(\sqrt{3} + \sqrt{2}) + (\sqrt{5} - \sqrt{3}) = \sqrt{2} + \sqrt{5}$$

OR

$$a = 9 - 4\sqrt{5}$$
 , $\frac{1}{a} = \frac{1}{9 - 4\sqrt{5}} = \frac{9 + 4\sqrt{5}}{9^2 - (4\sqrt{5})^2} = 9 + 4\sqrt{5}$

$$\therefore a + \frac{1}{a} = (9-4\sqrt{5}) + (9+4\sqrt{5}) = 18$$

$$a^{2} + \frac{1}{a^{2}} = (a + \frac{1}{a})^{2} - 2 = (18)^{2} - 2$$

$$= 324 - 2 = 322$$

1/2

16.
$$\frac{7+3\sqrt{5}}{3+\sqrt{5}} - \frac{7-3\sqrt{5}}{3-\sqrt{5}} = \frac{(7+3\sqrt{5})(3-\sqrt{5})-(7-3\sqrt{5})(3+\sqrt{5})}{9-5}$$

$$= \frac{1}{4} \left[21 + 2\sqrt{5} - 15 - (21 - 2\sqrt{5} - 15) \right] = \frac{1}{4} \left[6 + 2\sqrt{5} - 6 + 2\sqrt{5} \right] = \sqrt{5}$$
1+1

LHS =
$$\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} = \frac{(\sqrt{5} + \sqrt{3})^2}{5 - 3} = \frac{1}{2} \left[5 + 3 + 2\sqrt{15} \right]$$

$$= 4 + \sqrt{15} = a + \sqrt{15} b$$

$$\Rightarrow$$
 a = 4, b = 1

17. Let $x^2 + 7x = p$, 2x - 1 = q

$$\therefore \text{ Given expression} = 12p^2 - 8pq - 15q^2$$

$$= 12 p^2 - 18pq + 10pq - 15q^2$$

$$= 6p (2p - 3q) + 5q (2p - 3q)$$

$$= (6p + 5q) (2p - 3q)$$
 1+\(\frac{1}{2}\)

:. Factors are :
$$[6(x^2 + 7x) + 5(2x-1)][2(x^2 + 7x) - 3(2x-1)]$$

= $(6x^2 + 52x - 5)(2x^2 + 8x + 3)$

18. $p(x) = 3x^3 - 2x^2 - 7x - 2$

$$p(2) = 3(2)^3 - 2(2)^2 - 14 - 2 = 24 - 8 - 16 = 0 \implies 2 \text{ is a zero of } p(x)$$

$$p\left(\frac{-1}{3}\right) = 3\left(\frac{-1}{3}\right)^3 - 2\left(\frac{-1}{3}\right)^2 - 7\left(\frac{-1}{3}\right) - 2 = \frac{-1}{9} - \frac{2}{9} + \frac{7}{3} - 2 = 0 \implies \frac{-1}{3} \text{ is a zero of p(x)}$$

$$(x-2)(x+\frac{1}{3})$$
 or $(x-2)(3x+1)$ is a factor of p(x)

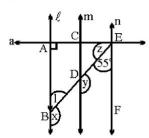
or $3x^2 - 5x - 2$ is a factor of p(x)

$$(3x^3 - 2x^2 - 7x - 2) \div (3x^2 - 5x - 2) = x + 1$$

$$\therefore$$
 x = -1 is the third zero of p(x)

19.

$$\ell \parallel n \Rightarrow \angle CEF = 90^{\circ}$$



$$\Rightarrow Z = (90^{\circ} - 55^{\circ}) = 35^{\circ}$$

$$\Rightarrow \angle x = 90^{\circ} + z = 90^{\circ} + 35^{\circ} = 125^{\circ}$$

1

1

1

1

1

1/2

$$\angle y = \angle x = 125^{\circ}$$

OR

$$y = 180^{\circ} - (30^{\circ} + 20^{\circ}) = 130^{\circ}$$
 1/2

$$\ell \parallel m \Rightarrow x + 100^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
 x = 80°

$$x+y = 130^{\circ} + 80^{\circ} = 210^{\circ}$$

$$y-x = 130^{\circ} - 80^{\circ} = 50^{\circ}$$

$$\Rightarrow$$
 $(y + x) : (y - x) = 21:5$

20. DE || BC and AB is a transversal

$$\Rightarrow \angle ADE = 40^{\circ}$$

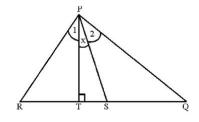
DE \parallel BC and LE \parallel AB \Rightarrow DBLE is a \parallel gm

$$\therefore$$
 DEL = \angle MEN = 40°

$$\therefore (i) \angle ADE + \angle MEN = 2 \times 40^{\circ} = 80^{\circ}$$

(ii)
$$\angle$$
 BDE = $180^{\circ} - 40^{\circ} = 140^{\circ}$

21. $\angle 1 + \angle x = \angle 2 \text{ (Given)} \dots$



$$\triangle 1 + \angle R = \angle 2 + x + \angle Q$$

$$\triangle 1 + \angle R = \angle 1 + 2x + \angle Q + \cdots$$
 1

$$\Rightarrow 2x = \angle R - \angle Q \Rightarrow \angle TPS = \frac{1}{2} (\angle R - \angle Q)$$

22. It is given that $\angle 1 = \angle 2$ and $\angle 3 = \angle 4$

$$\angle 1 + \angle 3 = \angle 2 + \angle 4 \Rightarrow \angle DAB = \angle CBA$$

In Δ 's DAB and CBA

$$AD = BC$$
, $AB = AB$, $\angle DAB = \angle CBA$

$$\therefore \Delta DAB \cong \Delta CBA \Rightarrow BD = AC$$

25.
$$x = \frac{1}{2 - \sqrt{3}} = \frac{2 + \sqrt{3}}{(2)^2 - (\sqrt{3})^2} = 2 + \sqrt{3}$$

$$\Rightarrow (x-2)^2 = 3 \Rightarrow x^2 - 4x + 1 = 0$$

$$(x^3 - 2x^2 - 7x + 5) \div (x^2 - 4x + 1) \Rightarrow \text{Quotient} = x + 2, \text{ Remainder} = 3$$

$$\therefore x^3 - 2x^2 - 7x + 5 = (x + 2)(x^2 - 4x + 1) + 3 = 3$$
1

$$\frac{1}{\sqrt{2}+1} = \frac{\sqrt{2}-1}{(\sqrt{2}+1)(\sqrt{2}-1)} = \sqrt{2}-1, \frac{1}{\sqrt{3}+\sqrt{2}} = \sqrt{3}-\sqrt{2}, \frac{1}{\sqrt{4}+\sqrt{3}} = \sqrt{4}-\sqrt{3}$$

$$\frac{1}{\sqrt{8}+\sqrt{9}} = \sqrt{9}-\sqrt{8}$$

:. Given expression =
$$(\sqrt{2} - 1) + (\sqrt{3} - \sqrt{2}) + (\sqrt{4} - \sqrt{3}) + \dots + (\sqrt{8} - \sqrt{7}) + (\sqrt{9} - \sqrt{8})$$
 1

$$\sqrt{9} - 1 = 3 - 1 = 2$$

26.
$$x = \frac{\left[\sqrt{p+2q} + \sqrt{p-2q}\right]^2}{\sqrt{p+2q-p+2q}} = \frac{1}{4q} \left[p + 2\sqrt{q} + p - 2\sqrt{q} + 2\sqrt{p^2 - 4q^2}\right]$$
 1+1/2

$$= \frac{1}{2q} \left[p + \sqrt{p^2 - 4q^2} \right] \Rightarrow 2qx - p = \sqrt{p^2 - 4q^2}$$
1/2+1/2

$$\Rightarrow Aq^2x^2 + p^2 - Apqx = p^2 - Aq2$$

$$qx^2 - px + q = 0$$

$$x = (\sqrt{2} + 1)^2 = 3 + 2\sqrt{2}$$
, $y = 3 - 2\sqrt{2}$

$$x+y=6$$
, $xy=9-8=1$

$$x^2+y^2+xy = (x+y)^2 - xy = 36-1=35$$
 1+\(\frac{1}{2}\)

27.
$$p(x) = x^3 + mx^2 - x + 6$$
, $p(2) = 0 \implies 8 + 4m - 2 + 6 = 0$

$$\Rightarrow 4m = -12 \Rightarrow m = -3$$
 1+\frac{1}{2}

$$p(3) = n$$
, $\therefore n = (3)^3 + (-3)(3)^2 - 3 + 6$

28. We know that
$$a^3+b^3+c^3-3abc = (a+b+c)(a^2+b^2+c^2-ab-bc-ca)$$
 1/2

Let a = x+y, b=y+z, c=z+x

LHS =
$$2(x+y+z)[(x+y)^2+(y+z)^2+(z+x)^2-(x+y)(y+z)-(y+z)(z+x)-(z+x)(x+y)]$$

$$= 2(x+y+z) [x^2+y^2+2xy+x^2+y^2+z^2+2yz+z^2-xy-y^2-xz-yz-z^2+2zx-yz-xy-xz-2x-x^2-yz-xy-1/2]$$

$$= 2 (x+y+z) [x^2+y^2+z^2-xy-yz-zx]$$

$$= 2 (x^3+y^3+z^3+-3xyz)$$

29.
$$p(x) = x^3 + 2x^2 - 5ax - 7$$
, $q(x) = x^3 + ax^2 - 12x + 6$

It is given that
$$p(-1) = A$$
 and $q(2) = B$

$$A = -1 + 2 + 5a - 7 \implies A = 5a - 6$$

$$B = 8 + 4a - 24 + 6 \implies B = 4a - 10$$
1

Also
$$2A+B=6 \Rightarrow 10a-12+4a-10=6$$

$$\Rightarrow 14a = 28 \Rightarrow a=2$$

1

D is the mirror image of B in y-axis

31. In \triangle RPS, \angle P + \angle S + x = 180°

$$\Rightarrow x = 180^{\circ} - 100^{\circ} - 30^{\circ} = 50^{\circ}$$

$$y = 180^{\circ} - \angle PSR = 180^{\circ} - 100^{\circ} = 80^{\circ}$$

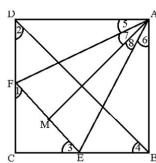
$$z = y + 40^{\circ}$$
 = 120° 1½

32.

 $EF \parallel BD \Rightarrow \angle 1 = \angle 2$ and $\angle 3 = \angle 4$

$$\angle 2 = \angle 4 \Rightarrow \angle 1 = \angle 3$$

$$\therefore DF = BE [\because BC - CE = CD - CF]$$



 \triangle ADF \cong \triangle ABE [AD = AB, FD = BE, \angle D = \angle B = 90°] \Rightarrow AF = AE and $\angle 5 = \angle 6$

$$\triangle$$
 AMF \cong \triangle AME [AF = AE, FM = EM, AM = AM] $\frac{1}{2}$

$$\therefore \angle 7 = \angle 8 \Rightarrow \angle 7 + \angle 5 = \angle 8 + \angle 6 \Rightarrow \angle MAD = \angle MAB$$

33.

$$\angle 1 = \angle 2$$
 (Given)

$$\therefore \angle 1 + \angle x = \angle 2 + \angle x$$

$$\Rightarrow \angle ADE = \angle CBD$$

1+1/2

1

1



(i)
$$\angle 3 = \angle 4$$
 (Given) (ii) $\angle ADE = \angle CBD$

$$(iii)$$
 AB = BC

2+1/2

$$\Rightarrow \Delta$$
's are $\cong \Rightarrow CD=AE$

$$AB = AC \implies \angle ABC = \angle ACB \dots (i)$$

34.

It
$$\frac{23}{A}$$

1/2

$$\angle ABD = \angle ACD$$

$$\Delta$$
's ABD and ACD are \cong by (sss)

is given that $\angle DBC = \angle DCB \dots (ii) \Rightarrow DB = DC1$ from [(i)-(ii))], weget

1/2

1

1