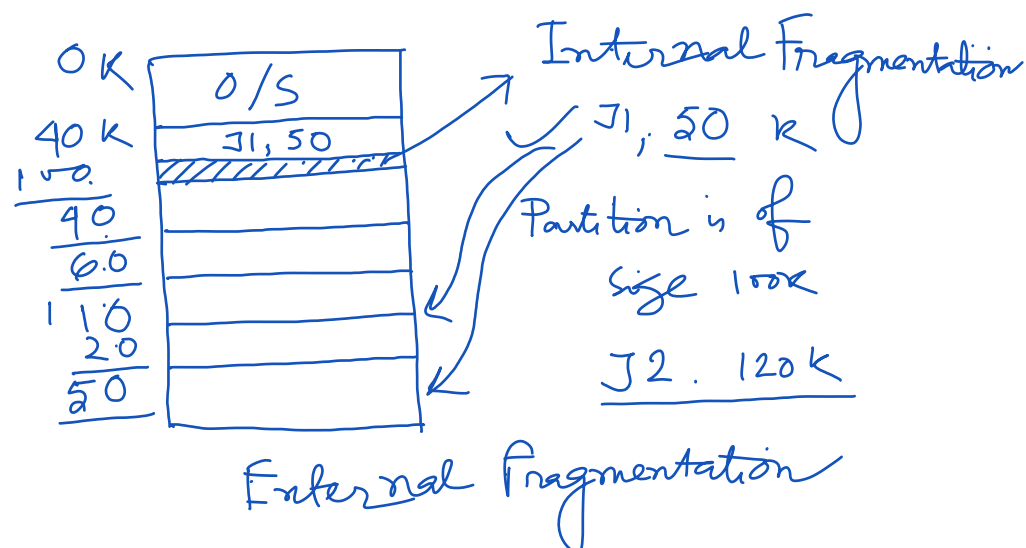


Memory Management

MFT - Multiprogramming with Fixed no. of tasks



- 1) First Fit ✓
- 2) Best Fit ✓
- 3) Worst fit ✓ X

MFT suffers from Internal as well as external fragmentation

MVT

Multiprogramming with Variable no. of tasks

Memory holes will be created
Suffers from external fragmentation

Compaction

logical address

Physical " RAM Address
2 GB

Three problems of memory

- Not enough RAM
- Holes in our address space
- Program writing over each other

Prog 1
0x 1234
value = 3

Prog 2
0x 1234
value = 7

* 0x 1234 = _____ ?

Virtual Memory

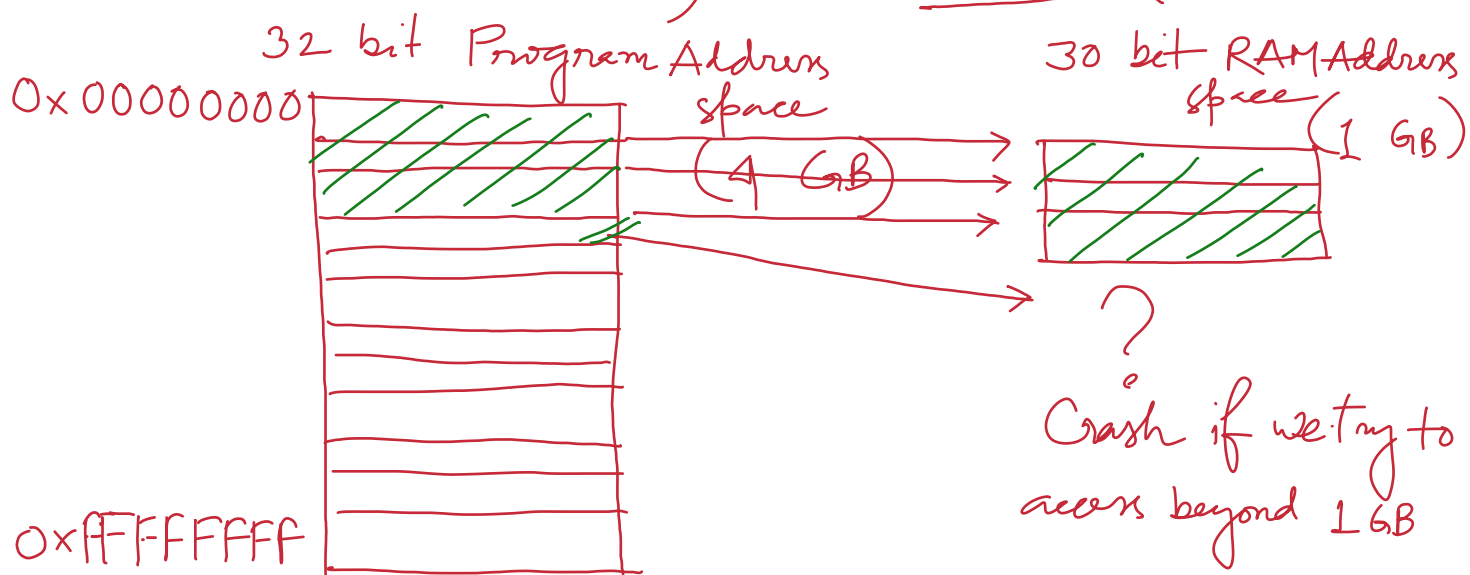
- level of indirection
- How does it solve problem?
- Translation / Page Table

Where does these page table reside?

32 bit address

How much memory we can access

- 2^{30} B
- 2^{32} B ✓
- 2^{32} words X



Key to problem

same memory space

Every program has same memory space
and actual RAM has same memory space

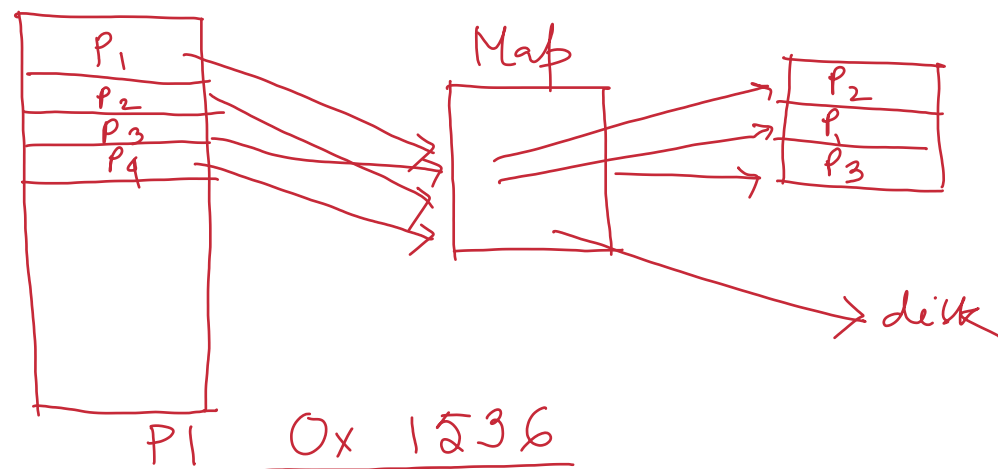
RAM → disk
←

Virtual Memory

RAM — Memory
Disk — Storage

Without Virtual Memory

Program Address = RAM address



- i) RAM address 0
- ii) RAM " 1536
- iii) Need more information

If a program uses more data than can fit into RAM, where does the data go?

Disk

$$32 \text{ bit} \quad 2^{32} \text{ B} = 4 \text{ GB}$$

MAP

VA	PA
!	

MIPS — Word

$$1 \text{ Word} = 4 \text{ B}$$

$$\text{Word} = \frac{2^{32}}{4} = 2^{30} \approx 1 \text{ billion}$$

Page Table

Fine grain: Maps each word address to the map

0 — 4095 words

4096 Words

4096 — 8191 words

Coarse grain Fewer mappings

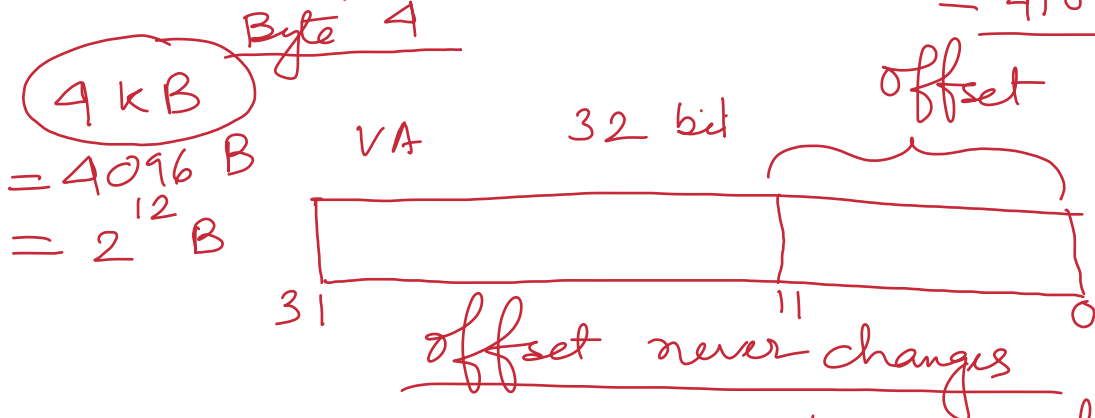
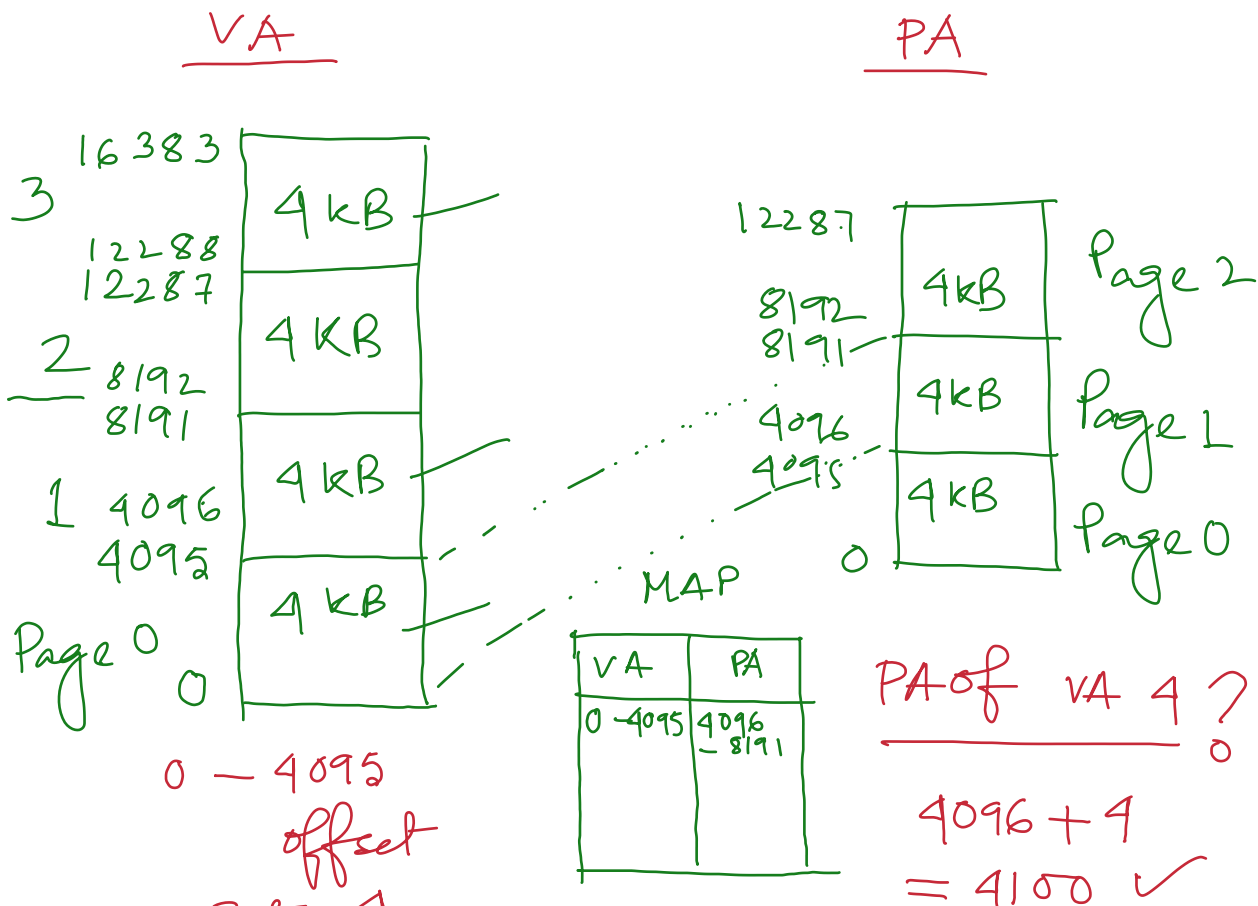
1024 Words

1 Word = 4 B

$$1024 \times 4 = 4096 \text{ B}$$

$$1 \text{ Page} = 4096 \text{ B} = 4 \text{ KB}$$

2^{30} entries ≈ 1 word
 $\frac{2^{30}}{1024} \approx 2^{20} \approx 1024$ words
1 million



Can we have a page size of 12 KB?

Page size is power of 2

Page size \rightarrow 256 KB

32 bit VA

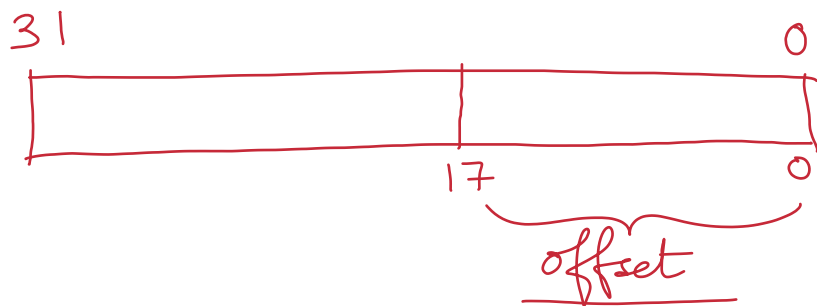
31 bit ? PA

33 bit

RAM 2 GB = 2^{31} B

RAM 8 GB = 2^{33} B

$256 \text{ KB} = 2^8 \times 2^{10} \text{ B}$
 $= 2^{18} \text{ B}$
 18 bit offset



Address Translation

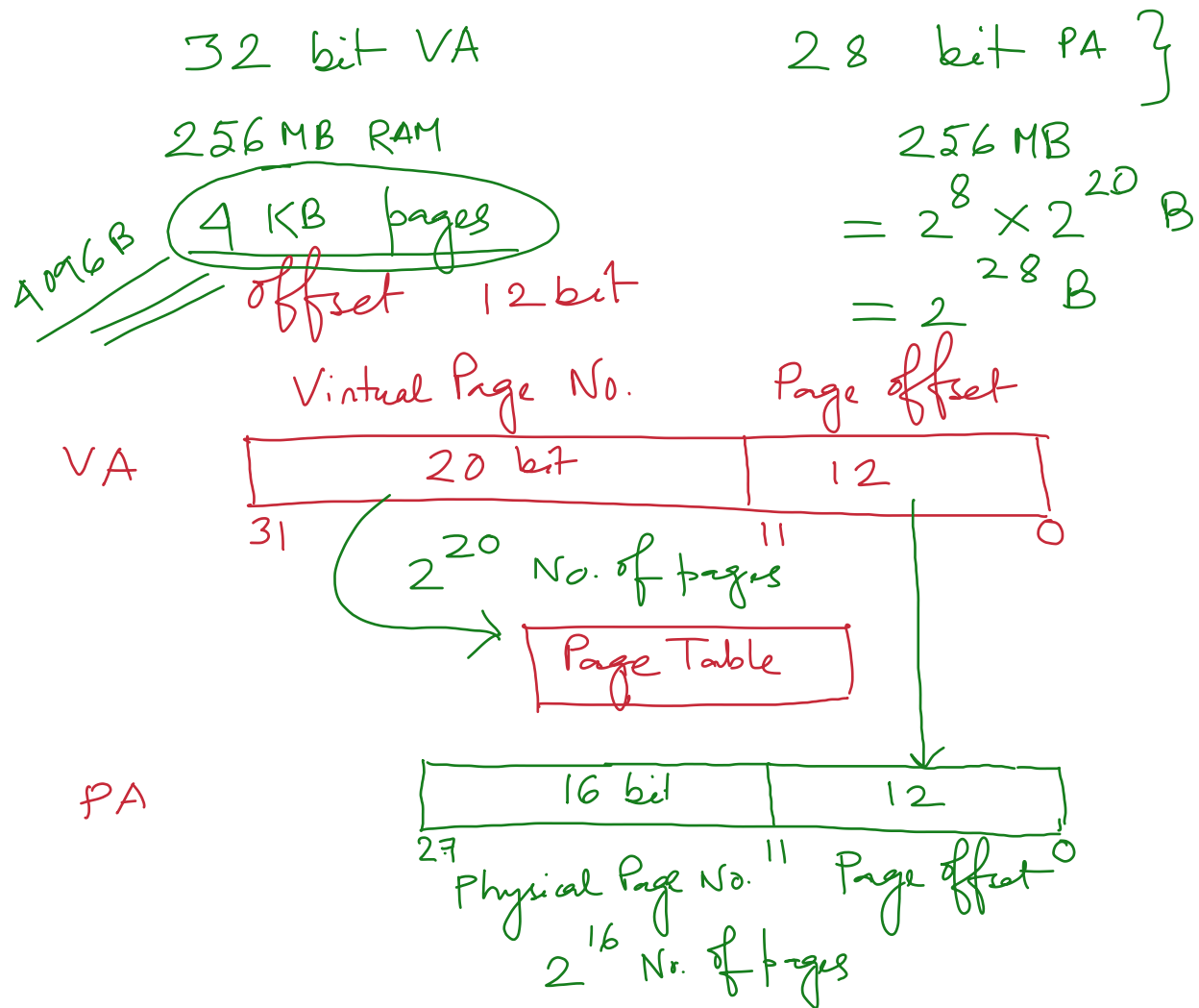
$$2^{30} B = \frac{1 \text{ GB}}{\text{per process}}$$

Program Address Space
4 GB VA space

$$\frac{1024 \text{ words}}{4096 B}$$

$$1 \text{ Page Size} = \frac{4096 B}{4 \text{ KB}}$$

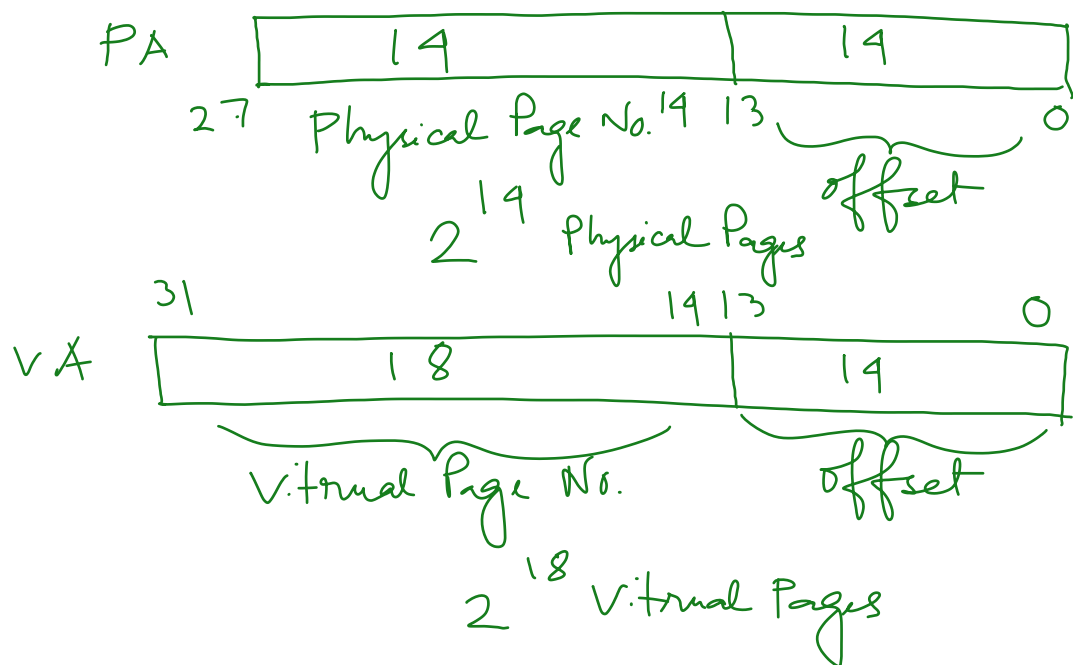
$$\text{Table size } 2^{20} B \Rightarrow \frac{1 \text{ MB}}{1 \text{ MB}}$$



Page Size 16 KB Page offset

$= 2^4 \times 2^{10} B$ 14 bit

$= 2^{14} B$



Q. How do we know if a page is not in RAM?

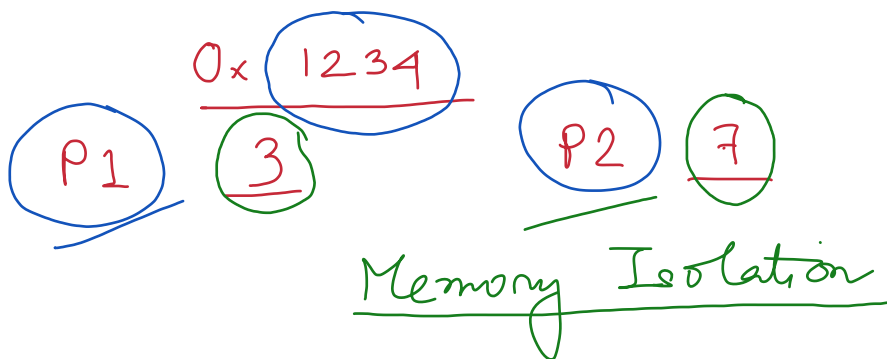
- No entry in the PT
- PT entry points to disk
- Address does not fit in the physical address space

256 MB RAM

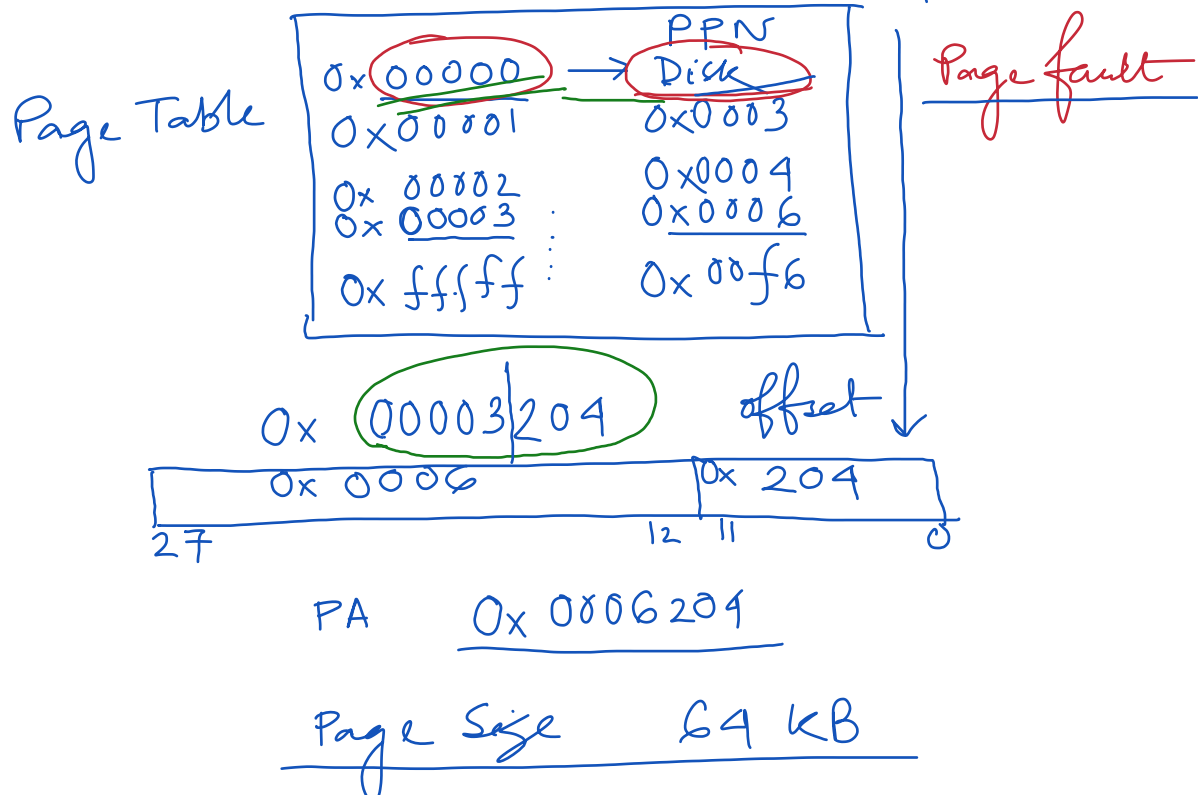
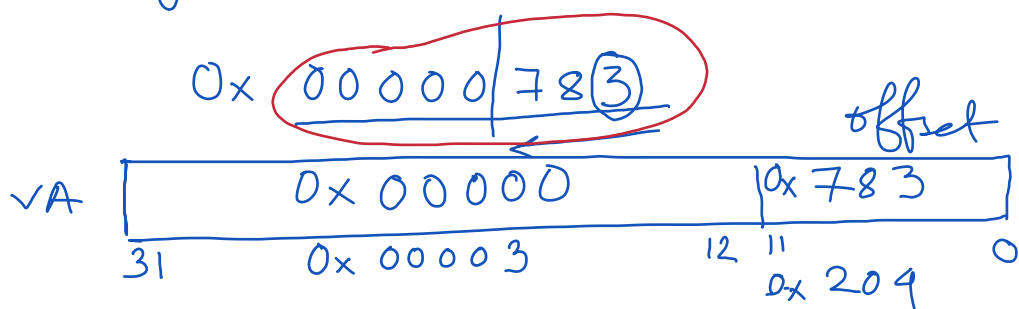
8 GB RAM 32 VA, 4 KB Page Size

- Page offset would be larger
- PA would be the same size as the VA
- You would not need VM
- PA would be larger than VA

8 GB RAM - 33 bit PA
 Page offset 12 bit
 $VPN \Rightarrow 20$
 $PPN \Rightarrow 21$



VA 32 bit
 PA 28 bit
 Page Size 4 KB 0x 3
 0011



- PTE says the page is on disk ~ 1 cycle
 - H/w (CPU) generates a Page Fault Exception ~ 100 cycles
 - The H/w jumps to OS page fault handler ~ 20000 cycles
 - The OS chooses a page to evict from RAM and write to disk $\sim 40,000,000$ cycles
 - If the page is dirty, it needs to be written back to disk first
 - OS reads the page from disk and it puts it in RAM ~ 4000 cycles
 - OS then changes the PT to map the new page ~ 1000 cycles
 - The OS jumps back to the instruction that caused the page fault ~ 10000 cycles
- Next time when this page is required
Will it be Page fault? No

How long does this take?

Short time

Long time

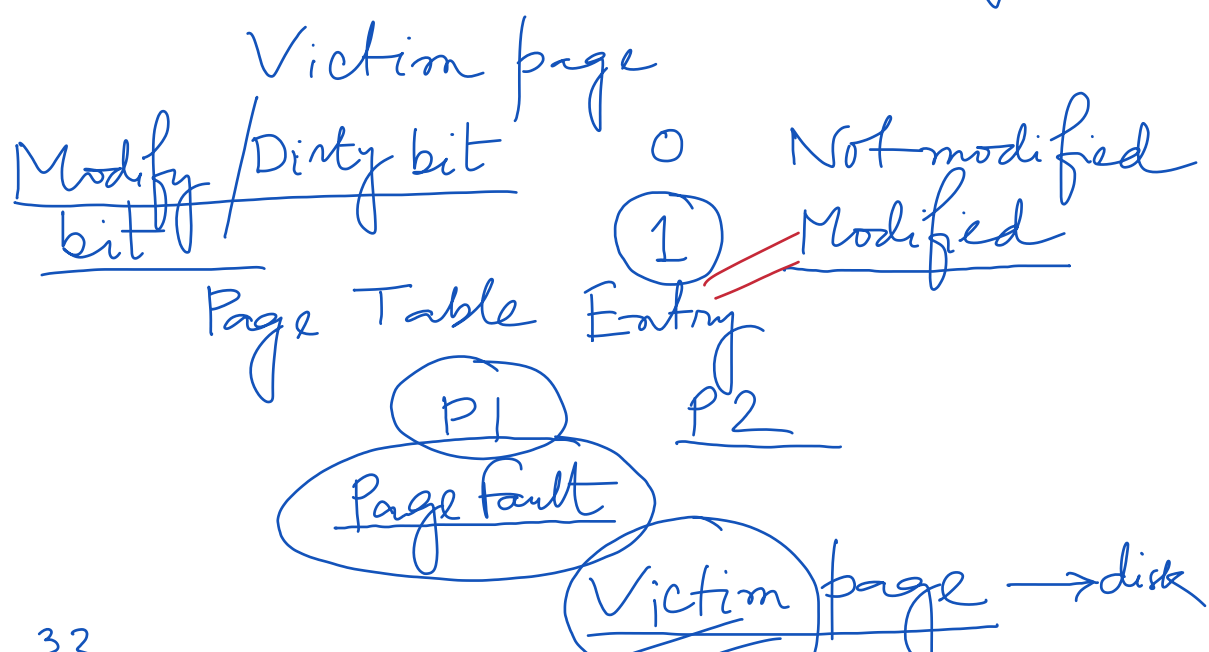
incredibly long time 80 million cycles

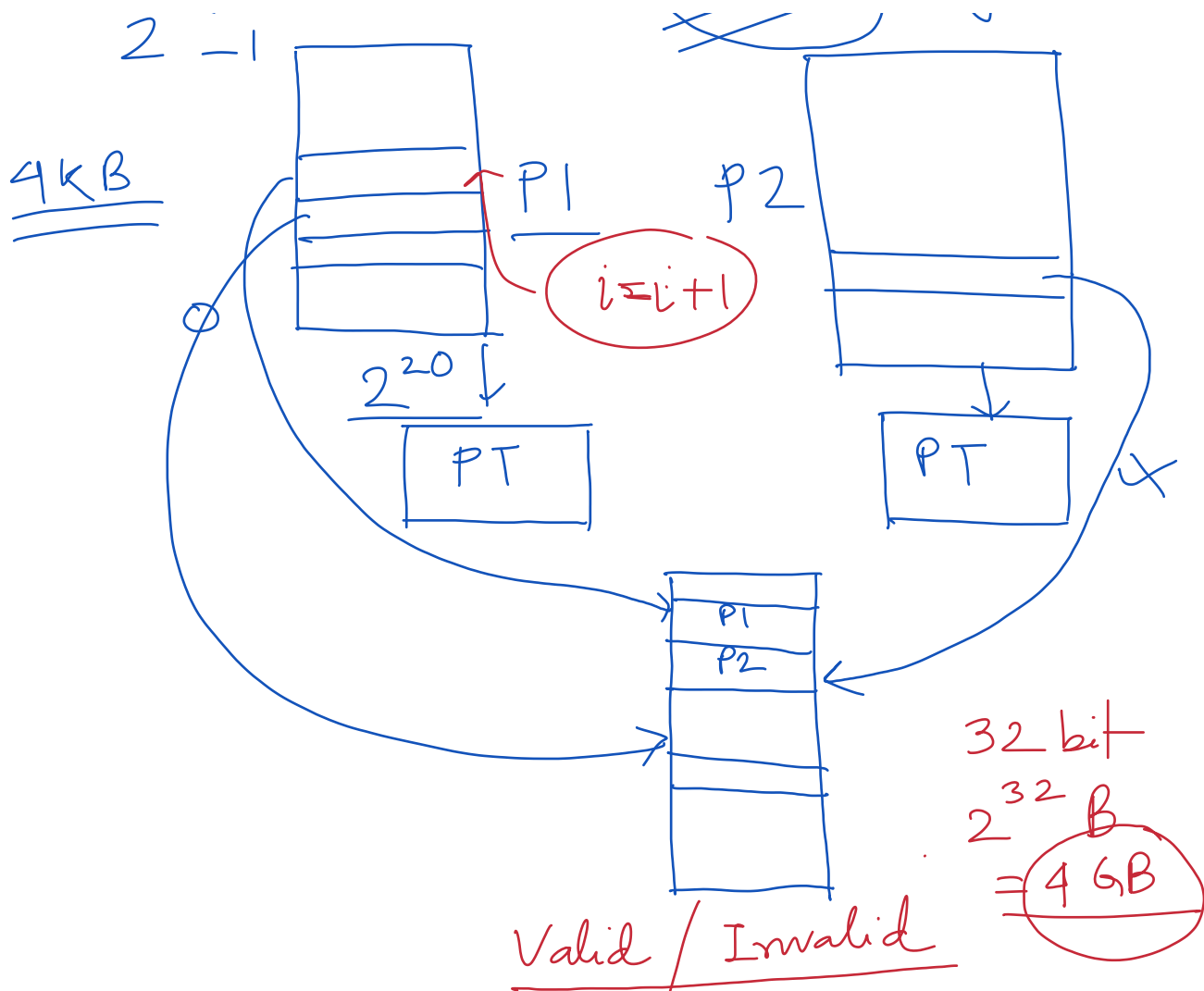
OSX 10.9 the OS compresses page first.

How will you evict the victim page?

Page Replacement Algorithm

Paged Translation — Coarse grain





Valid / Invalid

Notepad.exe user level

Kernel mode 2 GB user space
 User mode 2 GB system space

Address Sequence:

0100, 0432, 0101, 0612, 0102, 0103, 0104, 0101, 0611, 0102, 0103, 0104, 0101, 0610, 0102, 0103, 0104, 0101, 0609, 0102,

100 Bytes Per Page

Page size = 100 B

1, 4, 1, 6, 1, 1, 1, 1, 6, 1

FIFO — FIRST IN FIRST OUT

Demand Paging

Page Fault = 15

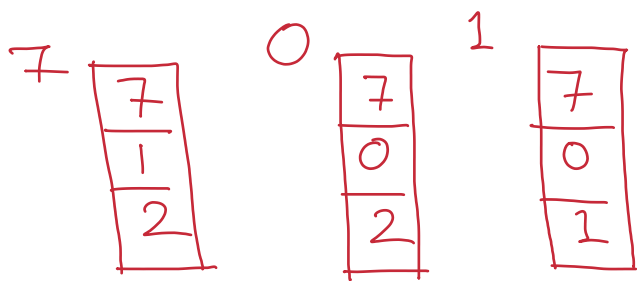
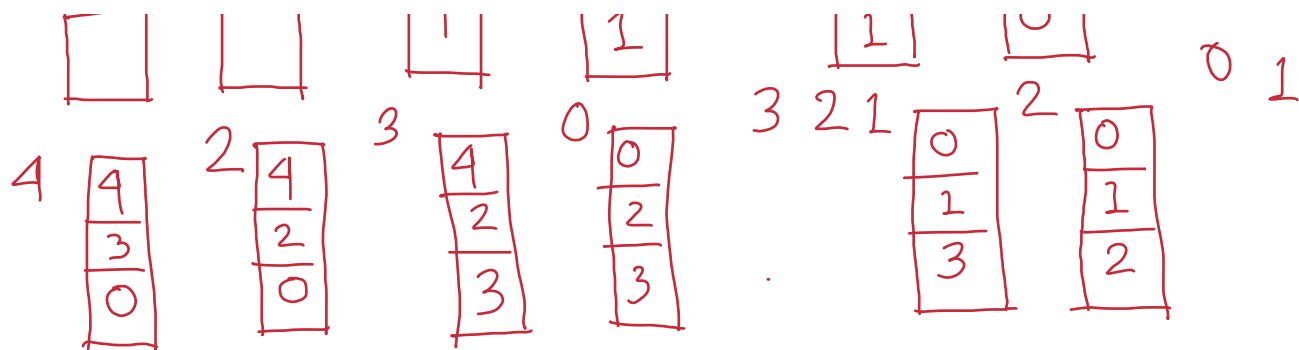
Reference string

7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1

Frame

7	7	7	2	2	2
	0	0	0	3	3

size 1
and 5



Hit rate

$$= \frac{5}{20} \times 100$$

Page Hit = 5

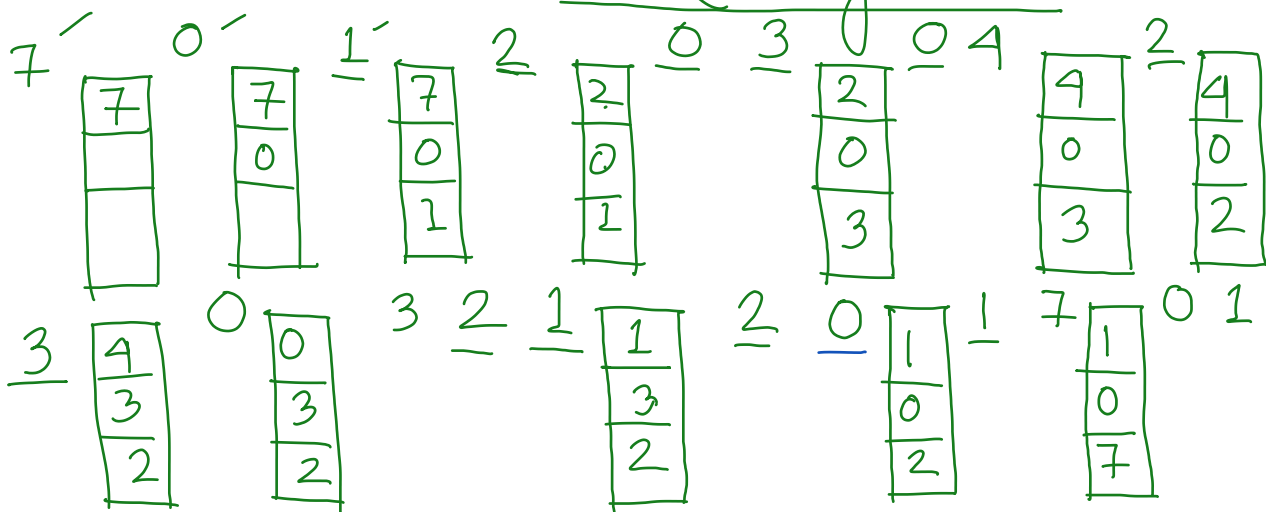
= 25%

Miss Rate = 75%

By increasing frame no. for certain reference string, it has been observed that the no. of page fault increases

Belady's Anomaly

LRU — Least Recently Used



Page Fault = 12

Hit = 8

$$\text{Hit Ratio} = \frac{8}{20} \times 100 = 40\%$$

$$\text{Miss Ratio} = \frac{12}{20} \times 100 = 60\%$$

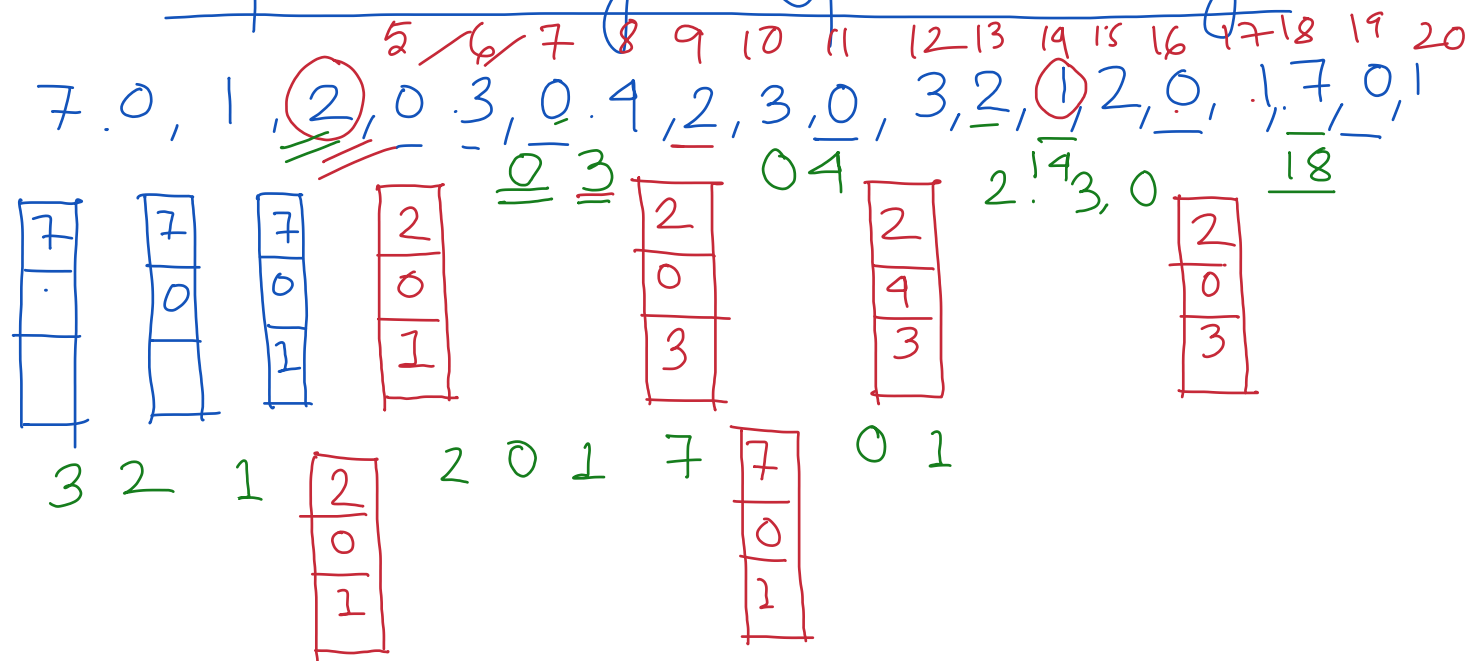
$$\frac{0-7}{8} = 2^3 \text{ binary bit } 3$$

$$\frac{0-2}{0, 1, 2} \text{ 2 bit } (3) \text{ NRU}$$

8 frames

u - + Pseudo LRU

Optional Page Replacement Algorithm



Page Fault = 9

Hit Rate = $\frac{11}{20} \times 100$

= 55%

Miss Rate = $\frac{9}{20} \times 100 = 45\%$