

## \* Recursion -

## public class Main

{

```
psvm(String [] args)  
{
```

Stack v2

प्रत्यक्ष

function

call

## तीव्र विषय

Dg

## मैक्ट

Direct

Div recursion {

Here  $i=10$  X (Removed from stack)

∴ Recursion stop

then it goes upward  $i = g$  then

$i=8 \dots i=2$  all removed

from stack  $i=1$  also removed from stack

In FILO all are removed (9 to 1) & main removed program stop.

## Recursion

~~imp  
points~~

 1) Function मध्ये कमीत कमी 1 var पाहिजे. (Local var)  
2) Fun ने fun ला call केल पाहिजे. (स्वतःला)  
3) Recursion मधून बोहेर यायला condition पाहिजे.  
(exit)

public class Main

5

```
psvm(String [] args)
```

```
for(int i=0; i<10; i++)  
    fun(i);
```

Here fun is not taking different place in stack  
so it is not recursion

एक function से stack पर 1 पेक्षा जारी रखा  
जाएगा भिन्नते तेवहा Recursion occur होता

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```
public static void mainfun(int i)
{
    SOP(i + ", ");
}
```

```
public class Main {
    psvm(String [] args)
    {
        fun(0);
    }

    public static void fun(int i)
    {
        show();
    }

    private void show()
    {
        main();
    }
}
```

main  
fun  
show  
main  
fun  
show  
;

(Indirect recursion)

Direct recursion - function calls to itself is direct recursion.

```
public class Main {
    psvm(String [] args)
    {
        fun(0);
    }

    public static void fun(int i)
    {
        S.O.P (i+ ", ");
        if(i<10)
            fun(i+1);
    }
}
```

Here every fun call printing only 1 value

// 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10

public static void fun(int i)

```

    {
        (forward)   S.OP(i, " ", ""); // 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10
        FR          if (i < 10)
                    - fun(i+1);

        (जातना)   else
        RR          SOP();
        (रोतना); SOP(i, " ", ""); // 10, 9, 8, 7, 6, 5, 4, 3, 2, 1, 0
    }

```

public class Main{

```

    {
        public static void main(String [] args)
    }

```

printStar(~~i~~);

private static void printStar(int i)

```

    {
        for (int j=0; j < i; j++)
    }

```

SOP("\*");

```

    {
        SOP();
        printStar(i+1);
    }

```

infinite  
\*\*\*\*\*

```

    {
        for (int j=0; j < i; j++)
    }

```

SOP("\*");

```

    {
        SOP();
        if (i < 3)
    }

```

printStar(i+1);

\*  
\*\*  
\*\*\* \*

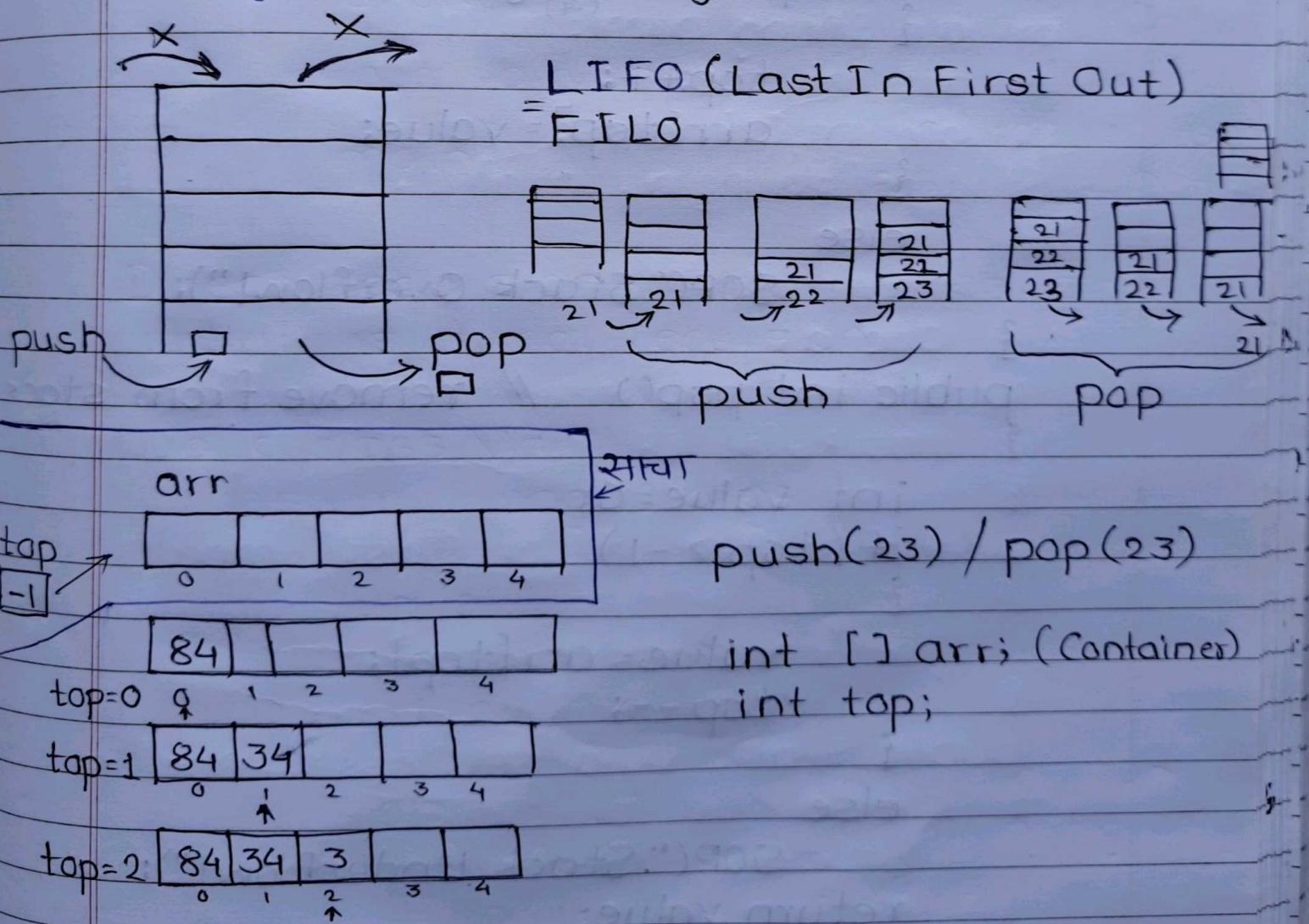
```

* *
* *
* ***
* ***
* *
* 
for(int j=0; j<i; j++)
{
    SOP("*");
}
SOPIn();
if(i<3)
    printStar(i+1);
for(int j=0; j<i; j++)
{
    SOP("*");
}
SOPIn();
    }
```

Forward      Reverse

(Stack)

\* Array - (Classes & Logic)



# \* Data Structure \*

Day-1

\* Stack - What is stack?

public class Stack

{ int [] arr;

int top;

public Stack()

{

top=-1;

arr=new int[5];

}

public void push(int value) // insert on  
{ stack

if(<sup>index</sup> top < arr.length-1)  
{<sup>length</sup> (4)

top++;

arr[top]=value;

}

else

SOP("Stack Overflow!");

}

public int pop() // remove from stack

{

int value=0;

if (top > -1)

{

value=arr[top];

top--;

}

else

SOP("Stack Underflow!");

return value;

}

Debug -  
Breakpoint - stop on specific condition

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public String toString() // printing

{  
String str = "";

if (top == -1)  
{

) str = "Stack is Empty!";

{

else  
{

for (int j = top; j >= 0; j--)  
{

str = str + arr[j];

{

str = str + "\n";

{

return str;

}

}

public class Main

{

psvm (String [] args)  
{

Stack s1 = new Stack();

s1.push(34);

s1.push(84);

s1.push(15); *5X*

s1.pop(); *—*

s1.push(16); *5X*

s1.pop(); *—*

s1.push(10);

SOP(s1);

}

}

// 10, 84, 34,

public Stack (int size)  
{

    top = -1;  
    arr = new int (size);  
}

Int main -

    Stack s2 = new Stack(25);

} User dependent  
size

\* Student Stack -

// Student

public class Student {

    private static int classNumber;

    private String name;

    private int age;

    private int [] marks;

    Student (String n, int a)

{

        name = n;

        age = a;

        marks = new int [1];

        marks [0] = 0;

}

    public static int getClassNumber()  
{

        return classNumber;

}

    public static void setClassNumber(int classNur)  
{

        Student.classNumber = classNumber;

}

    public static void printClassNumber()  
{

```

SOP ("ClassNumber: "+classNumber);
}

Student (String n, int a, int [] m)
{
    name=n;
    age=a;
    marks=m;
}

public void setMarks (int [] m)
{
    marks=m;
}

public int [] getMarks()
{
    return marks;
}

public String toString()
{
    String str="Name: "+name+", age: "+age+", Marks: "+getMarksInString()
              +"\n";
    return str;
}

private String getMarksInString()
{
    String str="{";
    for (int i=0; i<marks.length; i++)
    {
        str=str+marks[i]+", ";
    }
    str=str+"}";
    return str;
}

```

// Stack

public class Stack()

{

    Student [] arr;

    int top;

    public Stack()

{

        top = -1;

        arr = new Student[5];

}

    public void push(Student value)

{

        if (top < arr.length - 1)

{

            top++;

            arr[top] = value;

}

        else

{

            SOP("Stack Overflow!");

}

    public Student pop()

{

        Student value = null;

        if (top > -1)

{

            value = arr[top];

            top--;

}

        else

{

            SOP("Stack Underflow!");

}

    return value;

public String toString()

```

    {
        String str = "";
        if (top == -1)
    }
        str = "Stack is Empty!";
    }
```

```

else
{
```

```

for (int j = top; j >= 0; j--)
{
```

```

    str = str + arr[j];
}
```

```

    str = str + "\n";
}
```

```

return str;
}
```

```

}
```

```
//Main
```

```

public class Main
{
```

public static void main(String[] args)

```

    Stack s1 = new Stack();

```

```

    Student p = new Student("Ram", 14);

```

```

    Student q = new Student("Sham", 23);

```

```

    s1.push(p);

```

```

    s1.push(q);

```

```

    s1.push(p);

```

```

    s1.push(p);

```

```

    SOP(s1);

```

```

}
```

```

}
```

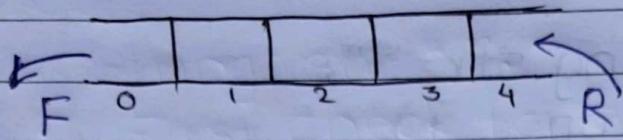
## Queue -

FIFO (First In First Out)

$$F = -1$$

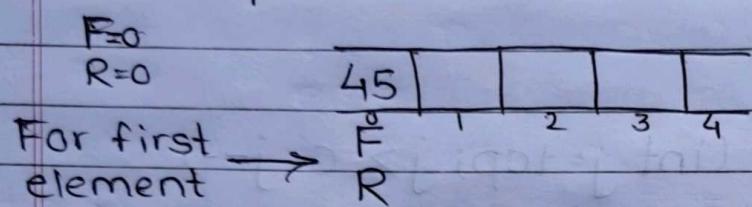
$$R = -1$$

(empty)



Front points to the first -1 at initial state

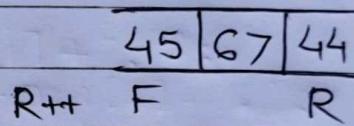
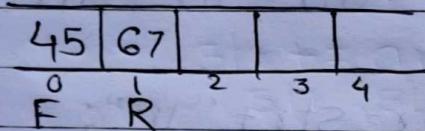
- Front points to the element who will pop first
- Rear points to the last element in queue



Insert

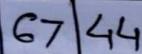
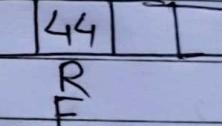
$F=0$

$R++$



Remove 45

$F++$

Remove  
67

Front never cross Rear

// Queue

public class Queue

{

int [] arr;

int F;

int R;

Queue() // Constructor

{

arr = new int [5];

F = -1; // F=R=-1;

R = -1;

{

Queue(int size) // Constructor

{

arr = new int [size];

F = -1;

R = -1;

}

public void insert(int value)

{

if (R < arr.length - 1)

{

R++;

arr[R] = value;

// Check for 1<sup>st</sup> value insertion

if (F == -1)

F = 0;

}

else

SOP("Queue is FULL!");

}

public int remove()

{

// First check for empty condition

if (F == -1)

{

SOP("Queue is Empty!");

return 0;

}

int value = arr[F];

// Check if this was the last value..

if (F == R)

F = R = -1;

else

F++;

return value;

}

public String toString()

{

String str = " ";

//First check for empty condition

if (F == -1)

{

str = "Queue is Empty!";

}

else

{

F to R

for (int i = F; i <= R; i++)

{

str += arr[i] + ", ";

} //str = str + arr[i] + ", ";

}

return str;

}

public void sameAs(Queue x)

{

//q2 → this

//q1 → x

this.F = x.F;

this.R = x.R; //array starts from 0

F to R

for (int i = x.F; (i != -1 && i <= x.R); i++)

{ F starts from -1 (when array is empty)

this.arr[i] = x.arr[i];

}

}

// Main

public class Main

{



```
public static void main(String [] args)
{
```

```
    Queue q1 = new Queue();
```

```
    Queue q2 = new Queue();
```

```
    q2.insert(33);
```

```
    q2.remove();
```

```
    q2.insert(24);
```

```
    q2.insert(36);
```

```
    q2.insert(48);
```

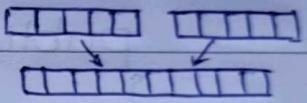
```
    q2.remove();
```

```
    q2.sameAs(q1);
```

```
SOP(q2); // Queue is Empty!
```

```
}
```

```
// Queue q3 = q2.concat(q1);
```



## Employee Queue

// Employee

public class Employee

```
private String name;
private int id;
private int sal;
public Employee(int id)
```

```
{  
    this.id = id;  
    this.sal = 0;  
    this.name = "";  
}
```

public Employee(int id, String name, int sal)

```
{  
    this.id = id;  
    this.sal = sal;  
    this.name = name;  
}
```

public String toString() // call back function

```
{  
    String str = "";  
    str = "Emp ID:" + id + "In Emp Name:" +  
        name + "In Emp Sal:" + sal;  
    return str;  
}
```

// EmpQueue - using to Employee class

public class EmpQueue

Employee [] arr;

int F;

int R;

array  
 public EmpQueue(int Size) //Constructor  
 {

arr = new Employee[Size];

F = -1;

R = -1;

}

public void insert(Employee value)  
 {

// Check full condition

if (R == arr.length - 1)

{

SOP("Queue is Full");

}

else  
 {

In insert  
all condition  
should be  
with R

// we have some space in queue

// But check if this is first insert

if (R == -1)

{

R++;

F++;

}

else

{

R++;

}

arr[R] = value;

}

if (R == -1)

F++;

R++;

(Fundamentally  
we can write it  
like this way)

}

public Employee remove()

//Check for Empty queue

if ( $F == -1$ )

{

SOP("Queue is Empty!");

return null;

}

In remove  
with F

else

{

Employee e = arr[F];

//check if only one emp in queue?

if ( $F == R$ )

$F = R = -1$ ;

else

$F++$ ;

return e;

{

public String toString() //call back function

String str = "";

//First check for empty condition

if ( $F == -1$ )

{

}

str = "Queue is Empty!";

else

{

for (int i = F; i <= R; i++)

{

str += arr[i] + "\n";

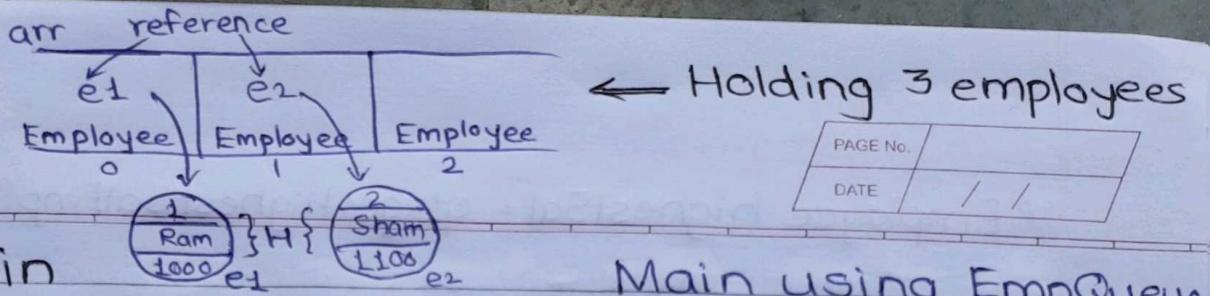
}

at this location java

internally calls toString() method

return str;

of Employee class



// Main

import java.util.Scanner;  
public class Main

{

public static void main(String[] args)

{

Queue obj

Employee obj

EmpQueue q1 = new EmpQueue(3); //Obj  
Employee e1 = getNewEmpWithUserInput();  
q1.insert(e1);  
Employee e2 = getNewEmpWithUserInput();  
q1.insert(e2); Employee e3 = new Employee(1,  
SOP(q1); "Pooja", 11000);  
q1.remove();  
S.O.P();  
SOP(q1);

{

public static Employee getNewEmpWithUserIn-  
put()

{

Scanner sc = new Scanner(System.in);  
int sal, id;  
String name;  
SOP("Enter ID:");  
id = sc.nextInt();  
SOP("Enter Name:");  
name = sc.next();  
SOP("Enter Sal:");  
sal = sc.nextInt();  
Employee e = new Employee(id, name, sal);  
return e;

{

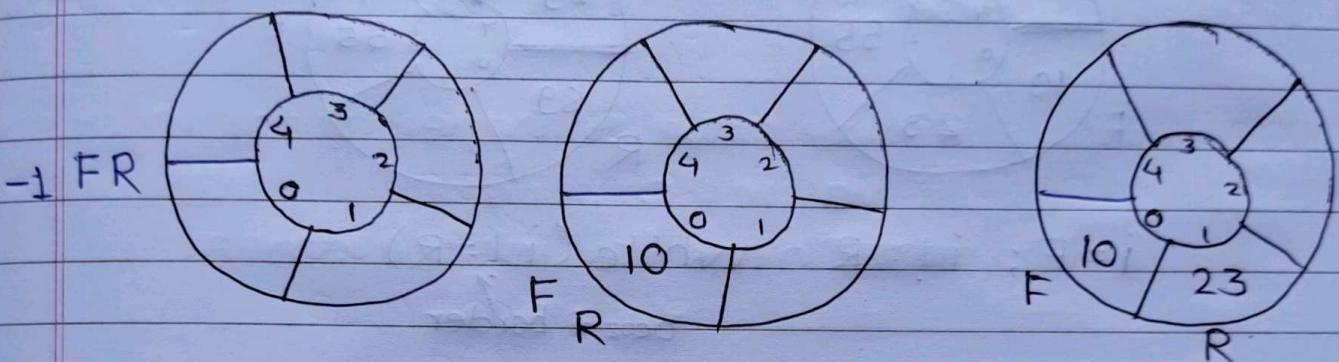
{



Here only 1 element can be inserted in linear queue

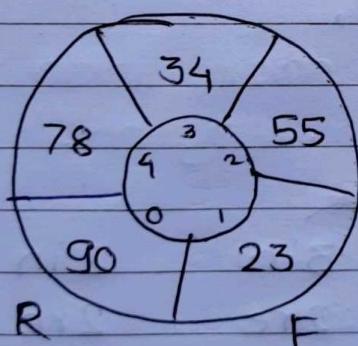
Solution-

### \* Circular Queue -

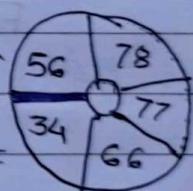


If you are on 4<sup>th</sup> index do not  $R++$   
then index start from 0.  
(Out of bound)

So start from 0<sup>th</sup> index after last index

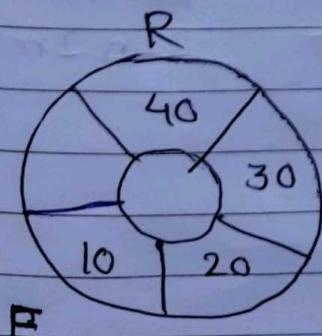


Full  $\rightarrow \underline{R+1 == F}$  \*

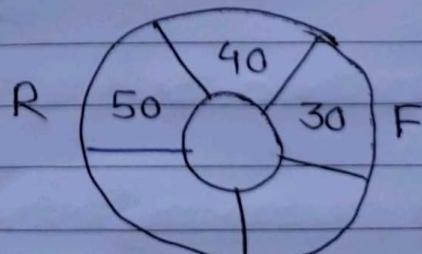


& IF R is at 4<sup>th</sup> & F is at 0<sup>th</sup>  
then full condition is  
Full  $\rightarrow \underline{F == 0 \& R == len-1}$  \*

### \* Insert -



$R++$



check  $R == arr.length-1$

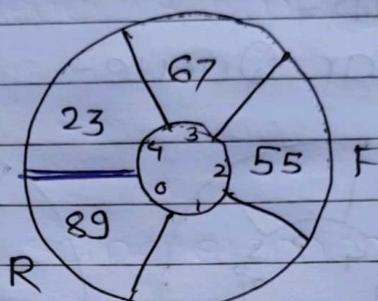
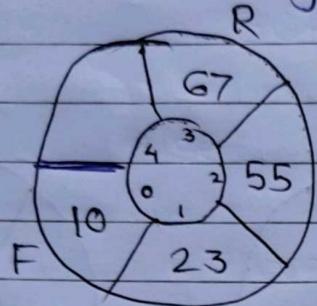
$R == 0$

For 1<sup>st</sup> element - if ( $F == -1$ )

$F++$

now insert value  $\rightarrow \text{arr}[R] = \text{value}$

\* Print(`toString`) -



$F == 1$

Queue empty

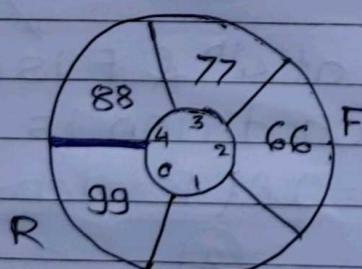
$i = F; i != R \quad \text{while } (i <= R)$   
beoz of border

\* Remove -

$F == -1 \rightarrow \text{Queue empty}$

$F == R \rightarrow \text{value} = \text{arr}[F];$

$F = R = -1;$



→ 6 ins  
 (5 in      3 in      2 in )  
 2 re      2 re      2 re  
 1 in      3 in      4 in  
 Possible to get this case  
 1 element रहती

} empty ...  
 then 4 insert  
 4 in  
 not possible  
 2 in 2 re → -1 ला जाती

//CQueue

public class CQueue {

    int [] arr;

    int F;

    int R;

    public CQueue()

}

        arr = new int[5];

        F = R = -1;

}

    public CQueue(int size)

{

        arr = new int[size];

        F = R = -1;

}

    public void insert(int value)

{

        if ((F == 0 && R == arr.length - 1) || (R + 1 == F))

{

            SOP("Queue is Full");

}

        else

{

            // we have some space in CQueue

            if (R == arr.length - 1)

                R = 0;

            else

                R++;

            // now insert element in queue

            arr[R] = value;

            // Check if this is the first element in Queue

            if (F == -1)

                F++;

```

public int remove()
{
    int value = 0;
    if (F == -1)
    {
        System.out.println("Queue is Empty");
    }
    else
    {
        // we have some element in queue
        value = arr[F];
        // Check for last element
        if (F == R)
        {
            F = R = -1;
        }
        else
        {
            // we have more than 1 element
            if (F == arr.length - 1)
                F = 0;
            else
                F++;
        }
    }
    return value;
}

public String toString()
{
    String str = "";
    if (F == -1)
    {
        str = "Queue is empty!";
    }
}

```

```

for(int j=0; j<50; j++)
{
    SOP(j%5);
}
O/p → 01234012340123401234...
    ↑
    border
}

else
{
    int i=F;
    while(i!=R)
    {
        str = str + arr[i] + ", ";
        if(i == arr.length-1)
            i=0;
        else
            i++;
        // i = (++i) % arr.length;
    }
    // to capture last element
    str = str + arr[i] + ", ";
}

return str;
}

// Main
public class Main{
    public static void main(String [] args)
    {
        CQueue q1 = new CQueue();
        q1.insert(10);
        q1.insert(20);
        q1.insert(30);
        q1.insert(10);
        q1.remove();
        q1.insert(20);
        q1.insert(30);
        q1.remove();
        SOP(q1);
    }
}

```

PAGE No.	
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DS  
arr  
LL  
Tree

DSA  
Stack  
queue  
Queue  
map  
hashmap

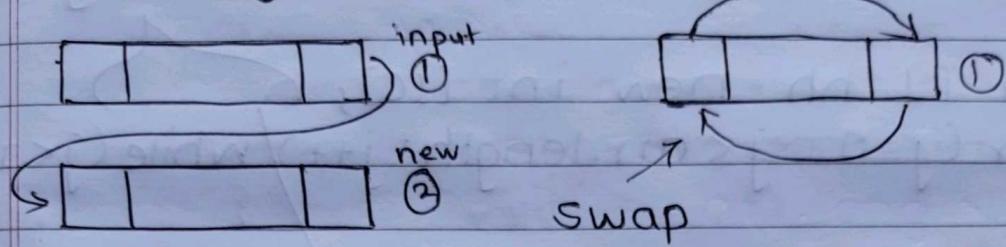
Day-4

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5/10/21

Memory → RAM



Space - Big O (Depends on heap)

fun(int [] arr)

{

    for(int j=0; j<arr.length; j++)

{

        int [] a = new int [10];

}

Time  
 $O(n)$

Space  
 $O(n)$

↓  
no of units

    fun(int [] arr)

{

        // allocation is 1 time

        int [] a = new int [10];

    for(int j=0; j<arr.length; j++)

{

→ Space  
 $O(1)$

Time  
 $O(n)$

}

    fun(int [] arr)

{

        for(int j=0; j<arr.length; j++) // n

{

            for(int k=0; k<arr.length; k++) // n

{

                int [] a = new int [10];

{

Space  
 $O(n^2)$

$n \times n$

If type is not mention then default is Time

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Time - If no loop  $\rightarrow O(1)$

fun(int [] arr){}

Space =  $O(1)$

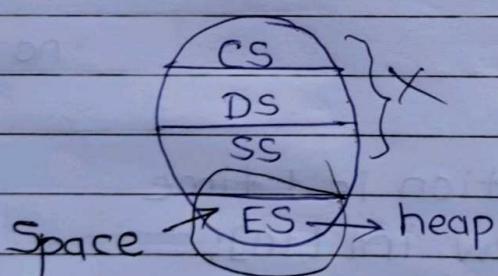
any loop

int [] hh = new int [10];  
 for(j=0; j<arr.length; j++) / while(j<arr.length)  
 { } { }

Time  
 $O(2n)$

2 loops  
 $\therefore 2n$   
 for(k=0; k<arr.length; k++)  
 { }

{ }



time  $\propto$  number of input  
 suppose n

$O(n) \rightarrow 1$  loop

$O(2n) \rightarrow 2$  loop

$O(n^2) \rightarrow 1$  loop inside another loop  
 $\therefore nxn=n^2$

## \* Sorting -

Selection  
 Insertion  
 Bubble

Quick  
 Merge

Heap  
 (requires tree)

\* Selection sort - प्रत्येक element ला, <sup>select करून</sup> याच्या proper जागेवर नेवून ठेवायच.

\* Insertion - Specific <sup>विकाऱी</sup> कुठला element बसवो.

Binary search requires sorted array.

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\* 1) Selection Sort - Select 1 ele & put on proper position

arr

34	55	3	13	10
----	----	---	----	----

i 1 2 3 4

tmp → [34]

Increment 'i' till tmp > arr[i]  
then swap temp & arr[i]

34	55	34	13	10
----	----	----	----	----

i

tmp [3]

increment i

compare tmp & arr[i]

i goes outside loop

(put 3 at proper pos)

3	55	34	13	10
---	----	----	----	----

Now,

& i start from 55

tmp [55]

compare ~~arr~~ temp > arr[i]

swap temp & arr[i]

i ++

3	55	55	13	10
---	----	----	----	----

i

34 > 13 ∴ swap

tmp [34]

i ++

3	55	55	34	10
---	----	----	----	----

13 > 10 ∴ swap

tmp [13]

i ++

3	55	55	34	13
---	----	----	----	----

tmp [10]

place 10 at location

j

3	10	55	34	13
---	----	----	----	----

j

Now j++ →

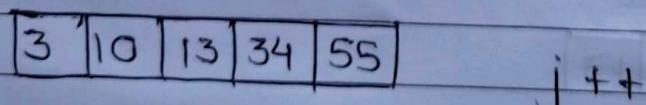
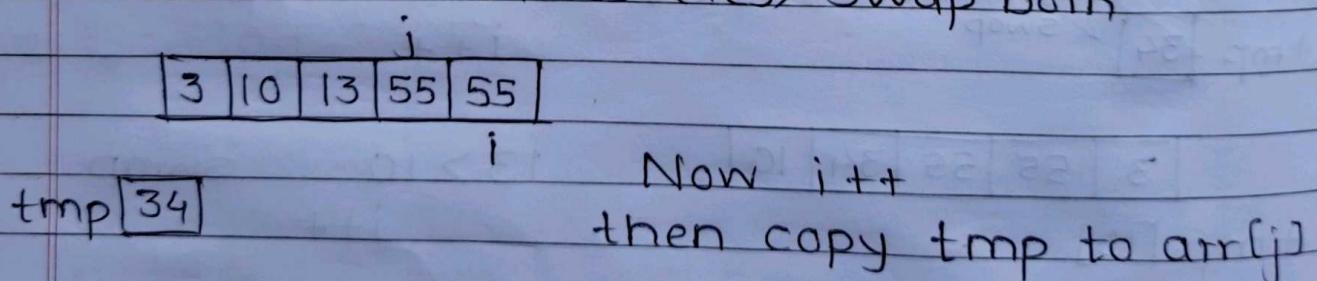
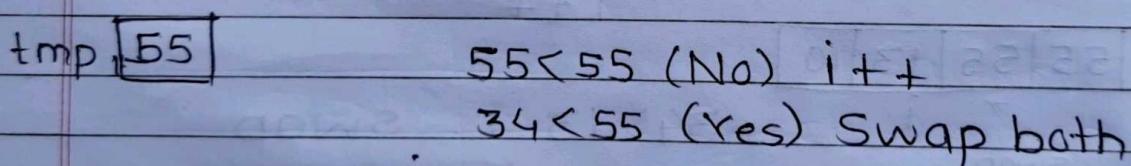
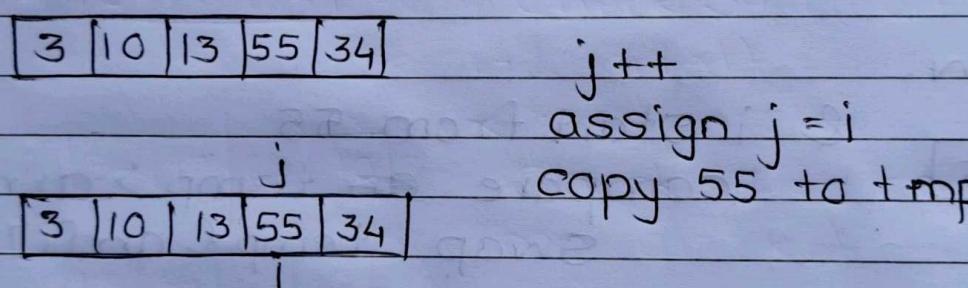
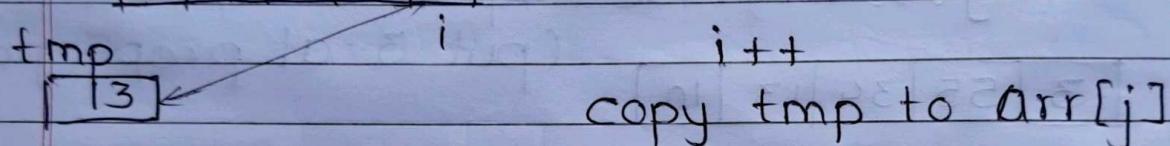
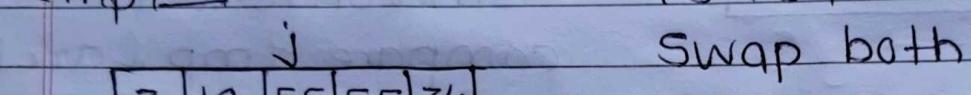
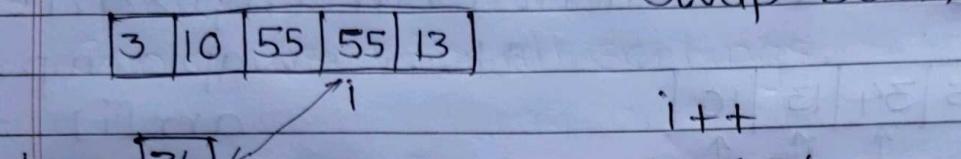
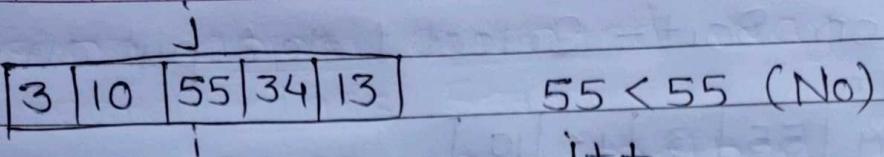
3	10	55	34	13
---	----	----	----	----

Assign i with j

→ i

j - for place (for each j, i will perform iteration)  
 i - for iteration

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1.  $j \rightarrow 0$  to  $\text{len}-1$
2.  $\text{temp} \rightarrow \text{arr}[j]$
3.  $i \rightarrow j+1$  to  $\text{len}$
4. check  $\text{arr}[i] < \text{temp}$
5. Swap  $\text{arr}[i]$  &  $\text{temp}$
6.  $\text{arr}[j] = \text{temp}$

In complexity constant are negligible  
 $O(2n) \rightarrow O(n)$   
 $O(n-1) \rightarrow O(n)$

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```
public class Main {
    public static void main(String[] args) {
        int [] arr = new int [] {2, 45, -3, 67,
                               67, 78, 42, 10, 34, 27};
        printArray(arr);
        selectionSort(arr);
        printArray(arr);
    }

    public static void selectionSort(int [] arr) {
        for(int j=0; j<arr.length-1; j++) {
            int temp = arr[j];
            for(int i=j+1; i<arr.length; i++) {
                if(arr[i]<temp)//As ascending
                {
                    int x = temp;
                    temp = arr[i];
                    arr[i] = x;
                }
                arr[j] = temp;
            }
        }
    }

    public static void printArray(int [] arr) {
        for(int i=0; i<arr.length; i++) {
            System.out.print("arr[" + i + "] = " + arr[i]);
        }
        System.out.println();
    }
}
```

if we write static function, no need to create the sort class object in main class.  
 we can call function used class name itself.  
 If static is not used then create object in main and call functions.

Using object oriented way it can be

1. Create class Sort
  2. Write selection() method in Sort class
  3. Call Sort.selection(arr) in main()
  4. print() in main
- Can be used for all sortings.

## \*2) Insertion Sort -

arr

2	34	17	12	10
Sorted	→ Unsorted			

Check 2 fit on which location  
 (Sorted)

2	34	17	12	10
Sorted	→ Unsorted			

Check 34 fit on which location  
 (Sorted)

2	34	17	12	10
Sorted	→ Unsorted			

Check 17 fit on which location

2	17	34	12	10
Sorted	→ Unsorted			

2	17	34	12	10
Sorted	→ Unsorted			

Check 12 fit on which location

2	12	17	34	10
Sorted	→ Unsorted			

arr	0	1	2	3	4
	2	34	17	12	10
i					

1. Consider arr[0] is sorted  
 i++

2	34	17	12	10	
K	i	→ Unsorted			

$tmp = arr[i];$

$k = i - 1;$

check  $k >= 0$

check  $34 < 2$  (No)

$arr[k+1] = temp$

$break;$   
 $k--$  ( $k = -1$ )

34  
 tmp

i++

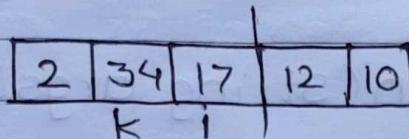
tmp = arr[i]

$k = i - 1$  (2)

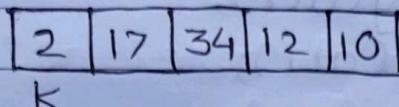
check  $k >= 0$

check  $17 < 34$  (arr[k])

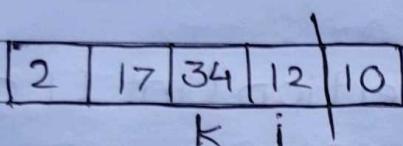
arr[k+1] = arr[k]  
(34)



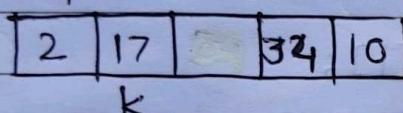
tmp  
17



k--



tmp  
12



i++  
tmp = arr[i]

$k = i - 1$

check  $k >= 0$

check  $12 < 34$

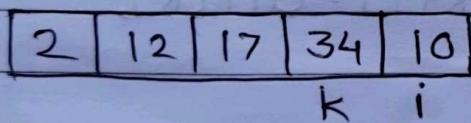
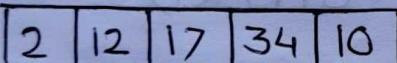
arr[k+1] = arr[k]  
(34)

k--

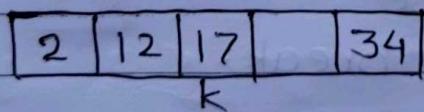
check  $12 < 17$

arr[k+1] = arr[k]  
k--

arr[k+1] = tmp  
(12)



tmp  
10

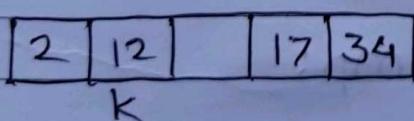


$k >= 0$

check  $10 < 34$

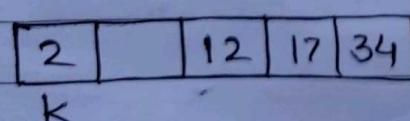
arr[k+1] = arr[k]  
(34)

k--



check  $10 < 17$

arr[k+1] = arr[k]  
k-- (17)



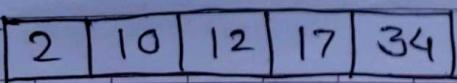
check  $10 < 12$

arr[k+1] (12) = arr[k]

check  $10 < 2 \rightarrow$  break;  
~~while ( $k >= 0$ )~~ → false

arr[k+1] = tmp

✓



```
public class Main{  
    public static void main(String args[])
```

{

```
        int [] arr = new int [] {2, 45, -3, 67, 67, 78, 42, 10,  
                                34, 27};
```

```
        printArray(arr);
```

```
        insertion(arr);
```

```
        printArray(arr);
```

}

```
    public static void insertion(int [] arr)  
    {
```

```
        for (int i=1; i<arr.length; i++)  
        {
```

```
            int tmp = arr[i];
```

```
            int k = i-1;
```

```
            while (k >= 0)  
            {
```

$O(n^2)$

```
                if (tmp < arr[k])  
                {
```

```
                    arr[k+1] = arr[k];
```

```
                    k--;
```

```
                }  
                else  
                    break;
```

```
            }
```

```
            arr[k+1] = tmp;
```

}