

Population trend analysis for bull trout in Oregon, Washington, Idaho & Montana

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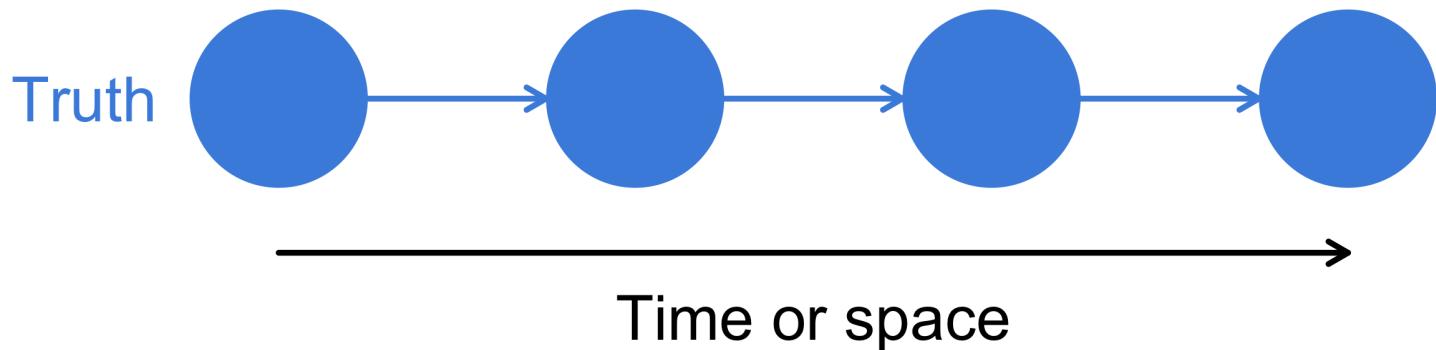
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A model for estimating population trends
with 2 general parts

Part 1: State model

Describes the **true state of nature** over time or space



States of nature might be

Animal location

Species density

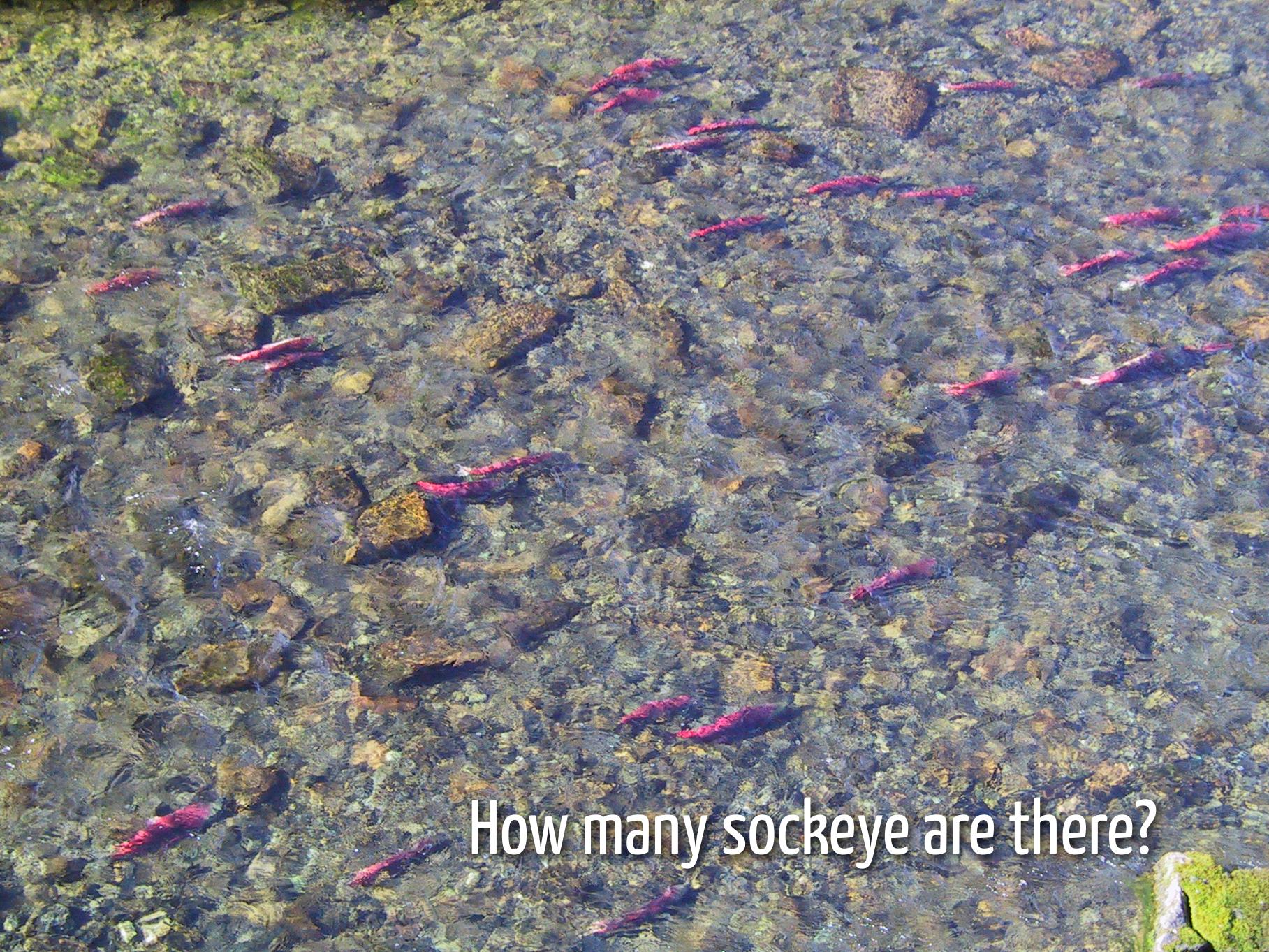
Age structure

Reproductive status

A photograph showing two ornate Venetian masks facing each other. The mask on the left is black with gold embroidery and a large orange feathered plume. The mask on the right is gold with red and black patterns and a green feathered plume. Both masks have decorative elements like beads and sequins.

Revealing the true state requires observations

Observing nature can be easy

A photograph showing a large school of sockeye salmon swimming in a river. The water is clear, revealing a rocky riverbed. The salmon are a vibrant red color, contrasting with the blue and green tones of the water. They are swimming in various directions, creating a sense of movement.

How many sockeye are there?

Observing nature can also be hard



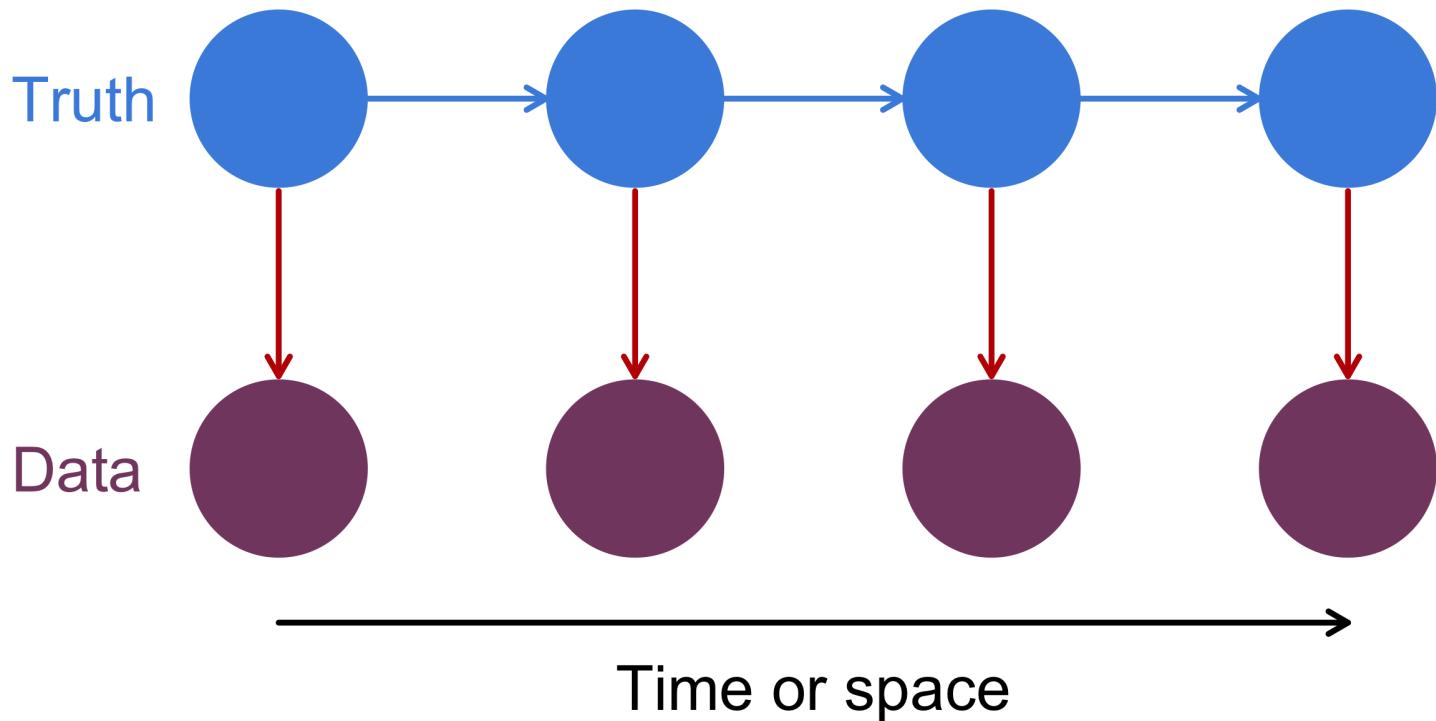
How many mayflies are there?

Part 2: Observation model

Data = Truth \pm Errors

Part 2: Observation model

Data = Truth \pm Errors



OK, but why bother?

Advantages

1. Can combine many different data types

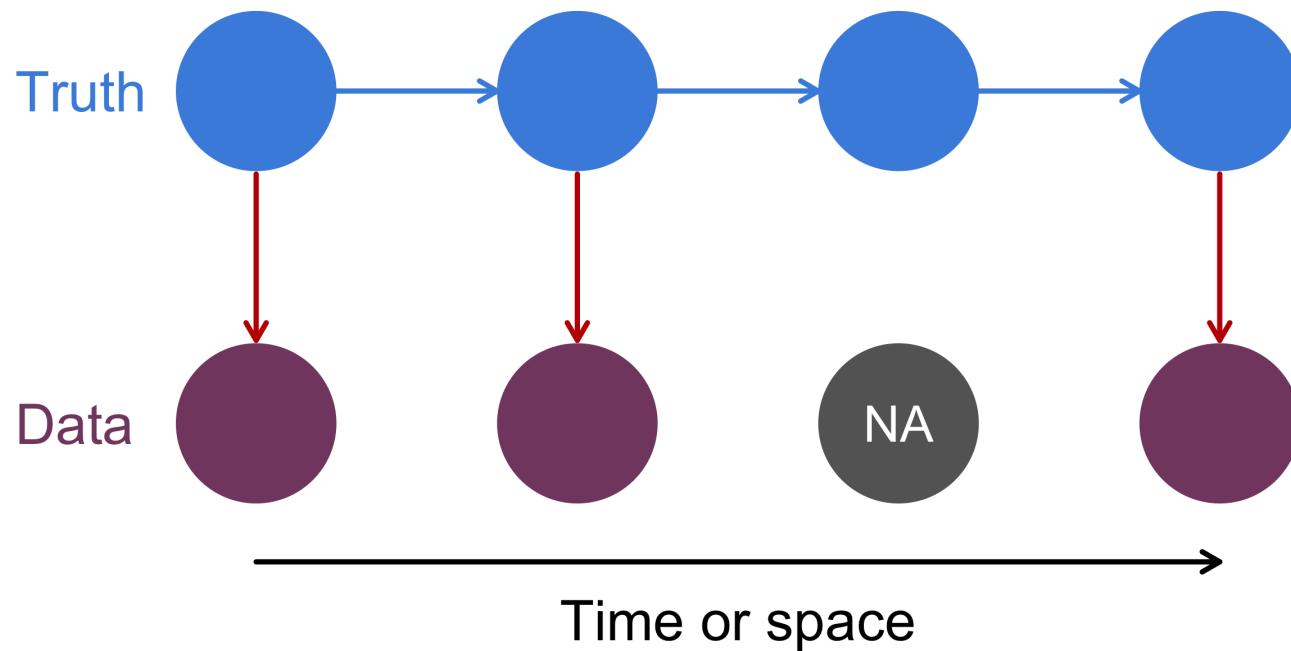
Changes in observers or sensors

Varying survey locations & effort

Direct & remote sampling

Advantages

2. Missing data are easily accommodated



Advantages

3. Improved accuracy & precision

Article | [OPEN](#) | Published: 08 February 2016

Joint estimation over multiple individuals improves behavioural state inference from animal movement data

Ian Jonsen 

Scientific Reports **6**, Article number: 20625 (2016) | [Download Citation](#) 

Advantages

4. Data-poor benefit from **data-rich**



Model for the state of nature

Population dynamics

Exponential growth/decline in continuous time

$$N(t) = N_0 \exp(u) \exp(wt)$$

Population dynamics

Exponential growth/decline in continuous time

$$N(t) = N_0 \underbrace{\exp(u)}_{\text{growth rate}} \exp(wt)$$

Population dynamics

Exponential growth/decline in continuous time

$$N(t) = N_0 \exp(u) \underbrace{\exp(wt)}_{\text{stochastic environment}}$$

Population dynamics

Exponential growth/decline in continuous time

$$N(t) = N_0 \exp(u) \exp(wt)$$

In discrete time, with a time step of 1 year

$$N_t = N_{t-1} \exp(u + w_t)$$

Population dynamics

In discrete time, with a time step of 1 year, the model is

$$N_t = N_{t-1} \exp(u + w_t)$$

Taking the logarithm of both sides yields

$$\log(N_t) = \log(N_{t-1}) + u + w_t$$

Population dynamics

We can define

$$x = \log(N)$$

such that

$$\log(N_t) = \log(N_{t-1}) + u + w_t$$



$$x_t = x_{t-1} + u + w_t$$

Biased random walk

If we assume that the errors are white noise

$$w_t \sim N(0, q)$$

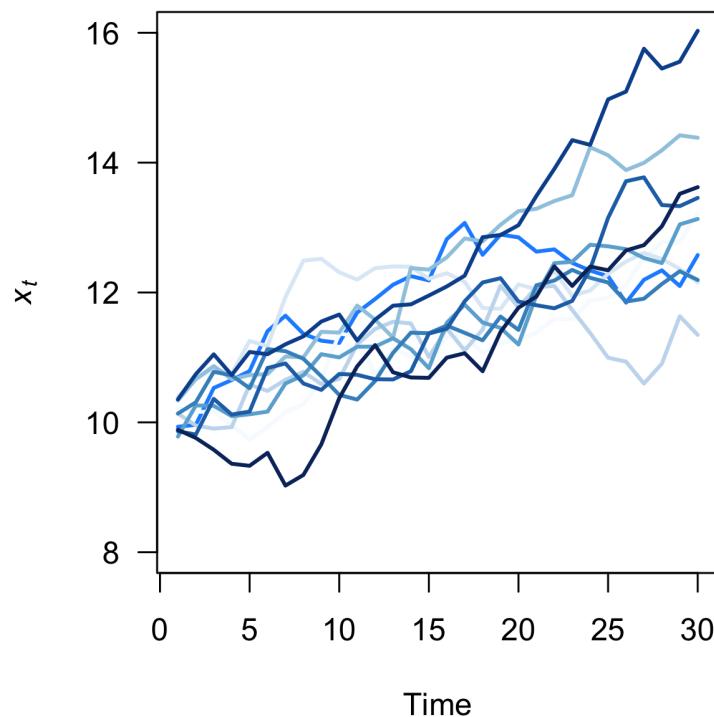
then our model of populations dynamics

$$x_t = x_{t-1} + u + w_t$$

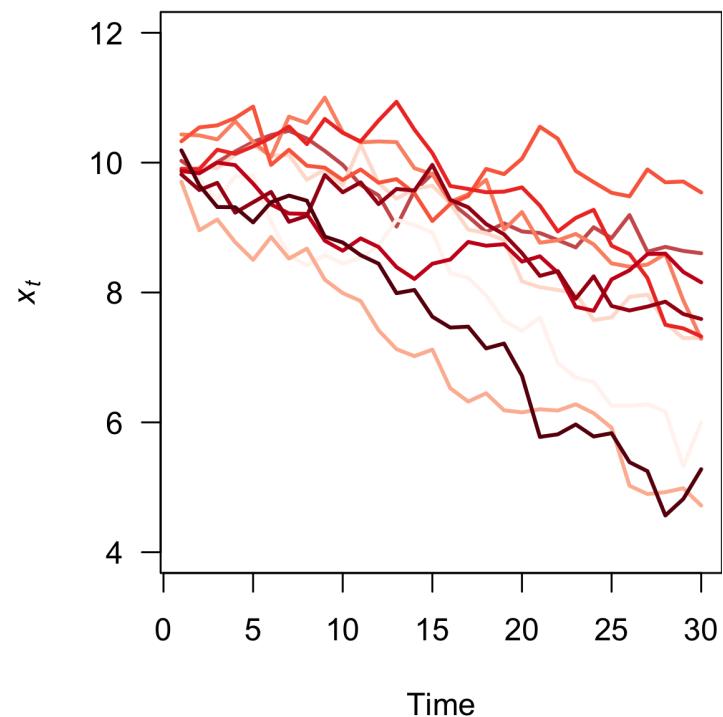
is a so-called *biased random walk*

Examples of biased random walks

Positive bias



Negative bias



Observation (data) model

Observation model

In log-space

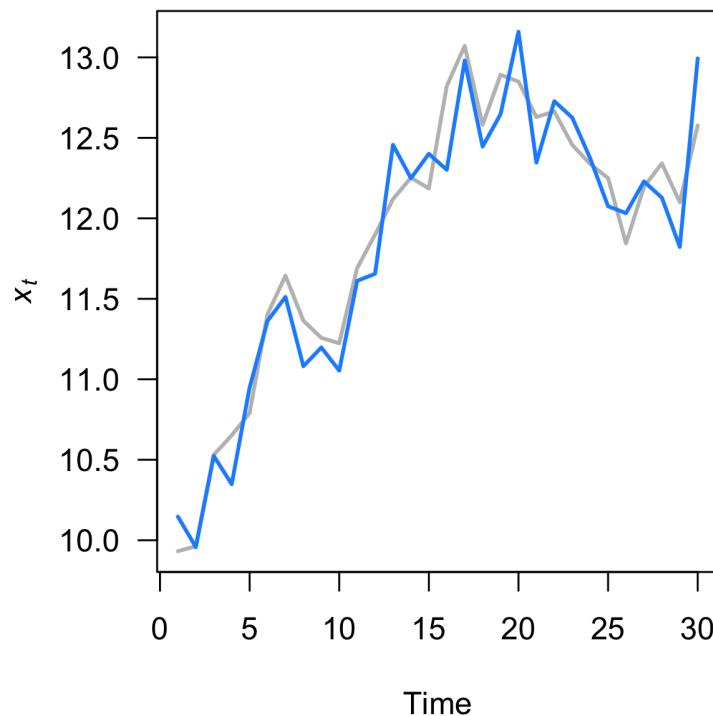
$$\underbrace{y_t}_{\text{observed counts}} = \underbrace{x_t}_{\text{true counts}} + \underbrace{v_t}_{\text{observer error}}$$

where

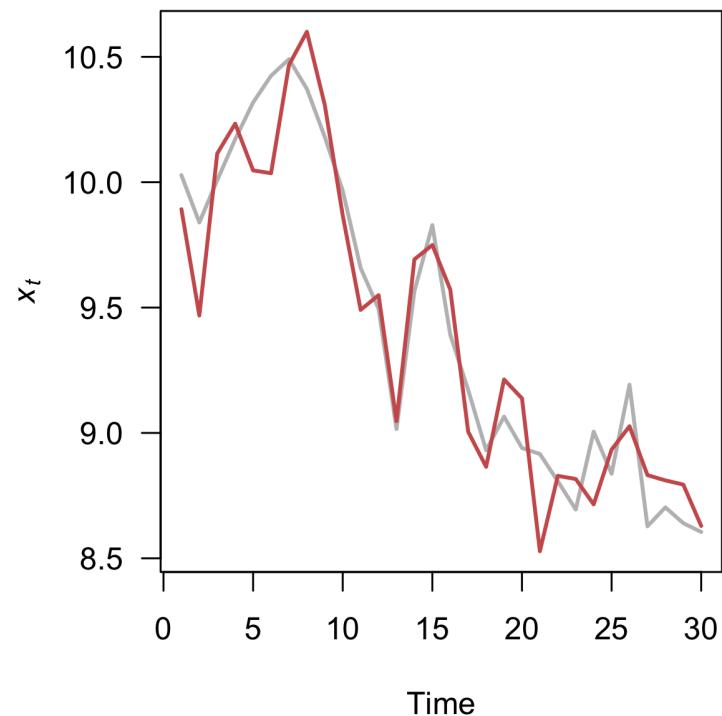
$$v_t \sim N(0, r)$$

Examples with observation error

Positive bias



Negative bias



Multiple time series of abundance

Many populations within many core areas

4 states

8 recovery units

61 core areas

242 populations

Expanding our model for multiple core areas

We're estimating population trends at the level of *core areas*

$$x_{1,t} = x_{1,t-1} + u_1 + w_{1,t}$$

$$x_{2,t} = x_{2,t-1} + u_2 + w_{2,t}$$

⋮

$$x_{n,t} = x_{n,t-1} + u_n + w_{n,t}$$

Expanding our model for multiple core areas

In matrix notation we have

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}_t = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}_{t-1} + \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_n \end{bmatrix} + \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}_t$$

Observation model for multiple time series

Core areas have from 1-22 populations within them

We need a way to map populations to their respective core area

Observation model for multiple time series

Example with 5 popns (1-5) and 2 core areas (A & B)

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{bmatrix}_t = \begin{bmatrix} x_A \\ x_A \\ x_B \\ x_B \\ x_B \end{bmatrix}_t + \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \\ a_5 \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \end{bmatrix}_t$$

Full state-space form

Mapping populations onto core areas

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{bmatrix}_t = \underbrace{\begin{bmatrix} 1 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 1 \\ 0 & 1 \end{bmatrix}}_{\substack{\text{rows are popns} \\ \text{cols are cores}}} \begin{bmatrix} x_A \\ x_B \end{bmatrix}_t + \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \\ a_5 \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \end{bmatrix}_t$$

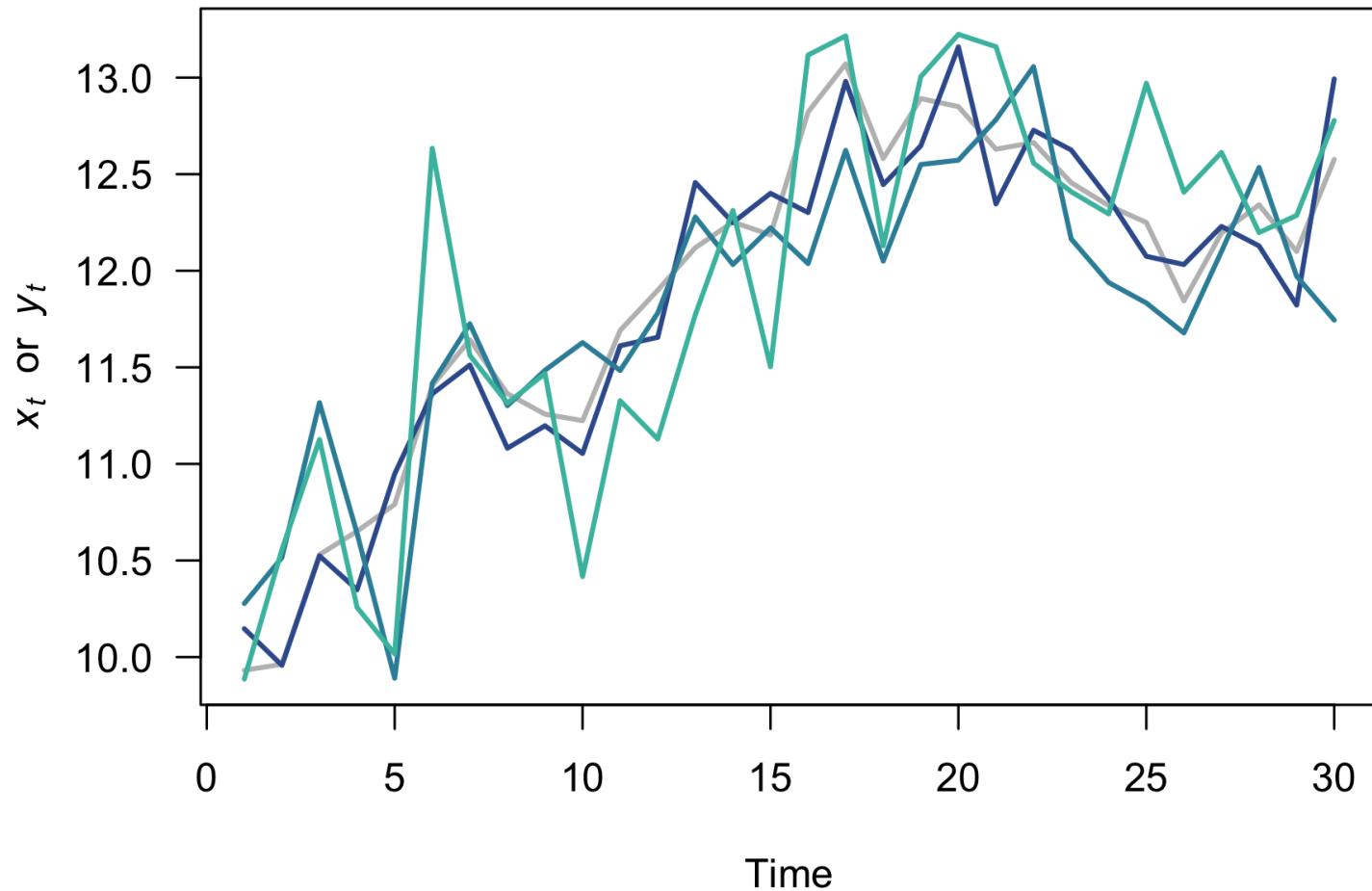
Full state-space form

Combining the observation & state models

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{bmatrix}_t = \begin{bmatrix} 1 & 0 \\ 1 & 0 \\ 0 & 1 \\ 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_A \\ x_B \end{bmatrix}_t + \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \\ a_5 \end{bmatrix} + \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \end{bmatrix}_t$$

$$\begin{bmatrix} x_A \\ x_B \end{bmatrix}_t = \begin{bmatrix} x_A \\ x_B \end{bmatrix}_{t-1} + \begin{bmatrix} u_A \\ u_B \end{bmatrix} + \begin{bmatrix} w_A \\ w_B \end{bmatrix}_t$$

Example of 3 observations of a state



Different survey methods have different observation variances

For example, weir counts are more accurate than snorkel surveys

Multiple surveys of each type help inform the variance estimates

Fitting the models

We used the time period from 1991-2020

Time series needed at least 10 years of non-missing data

Fitting the models

We used the time period from 1991-2020

Time series needed at least 10 years of non-missing data

All models were fit in R using the {MARSS} package

I estimated 90% confidence intervals on bias terms

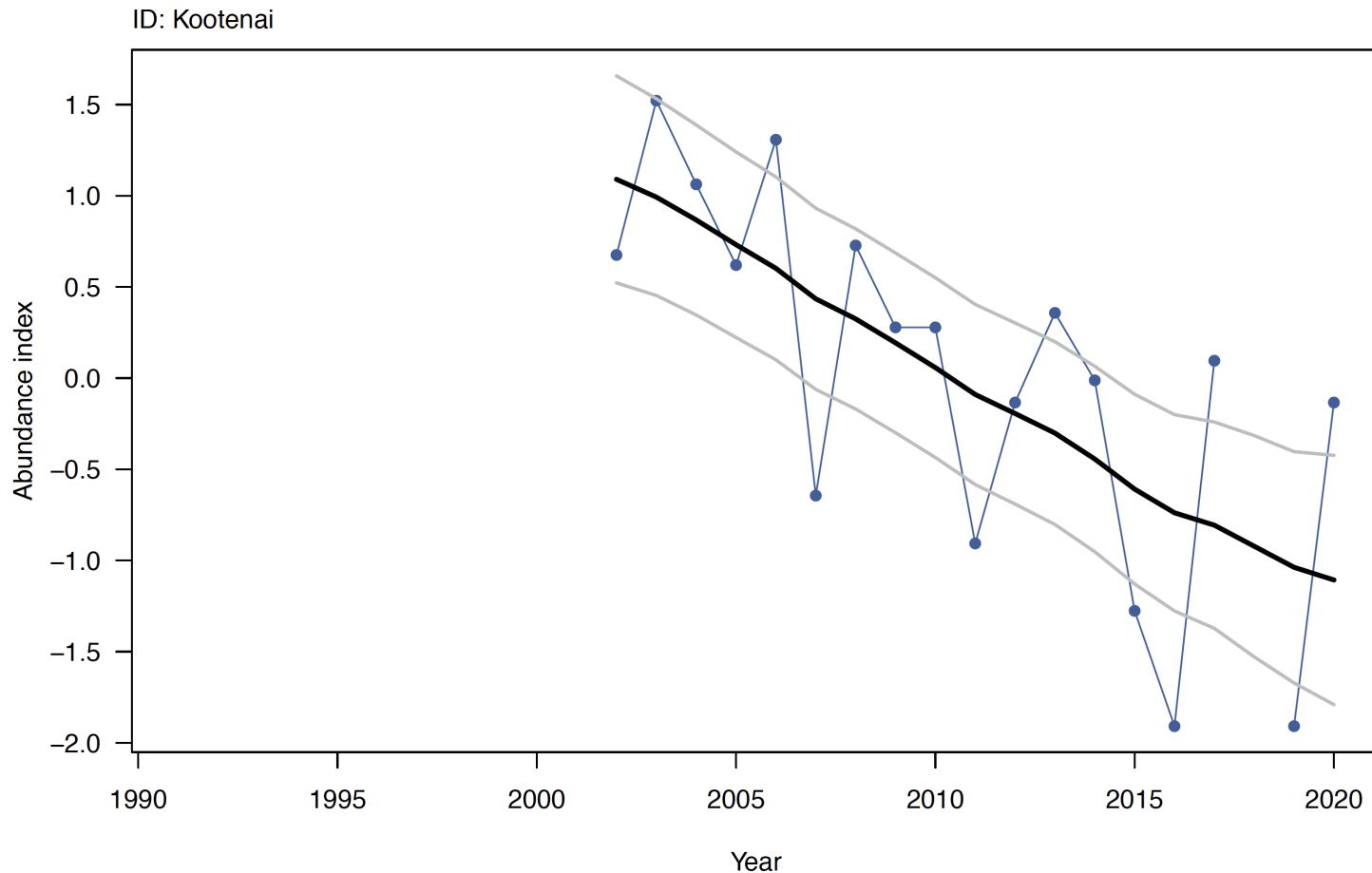
RESULTS

Bias in trends

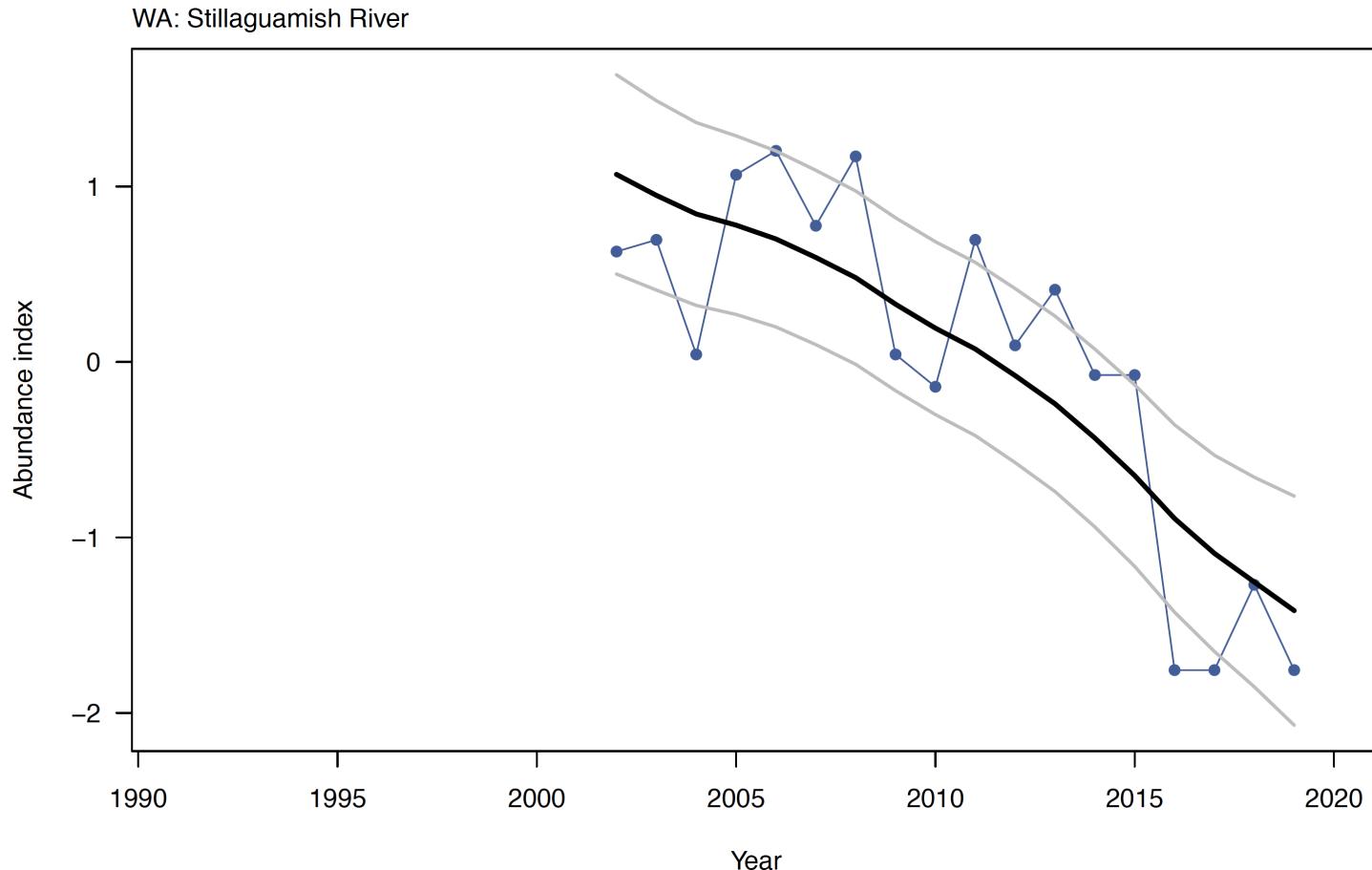
35/61 core areas had a negative trend

But only 3/61 were "significantly" negative

Example of a significant decline



Example of a significant decline



Bias in trends

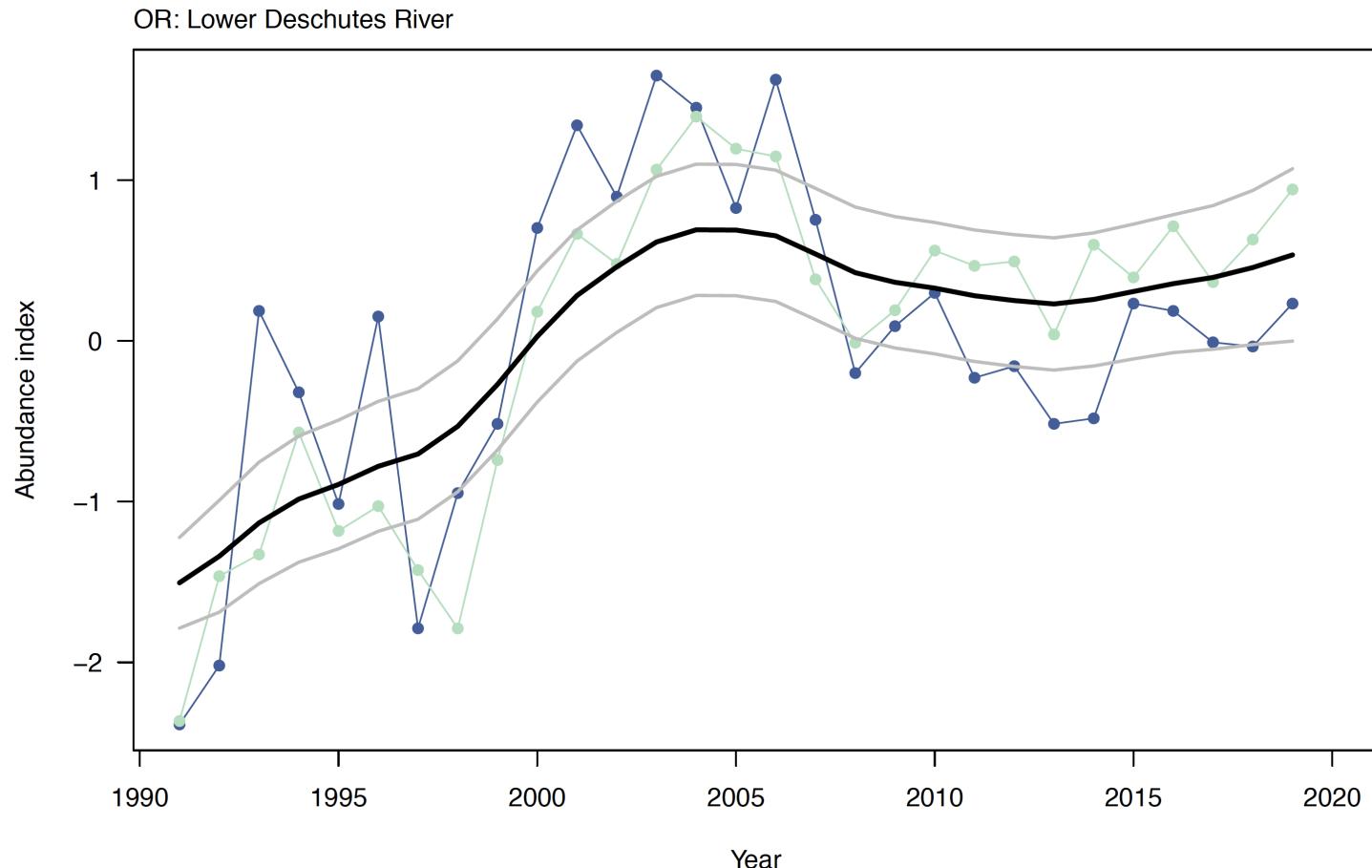
35/61 core areas had a negative trend

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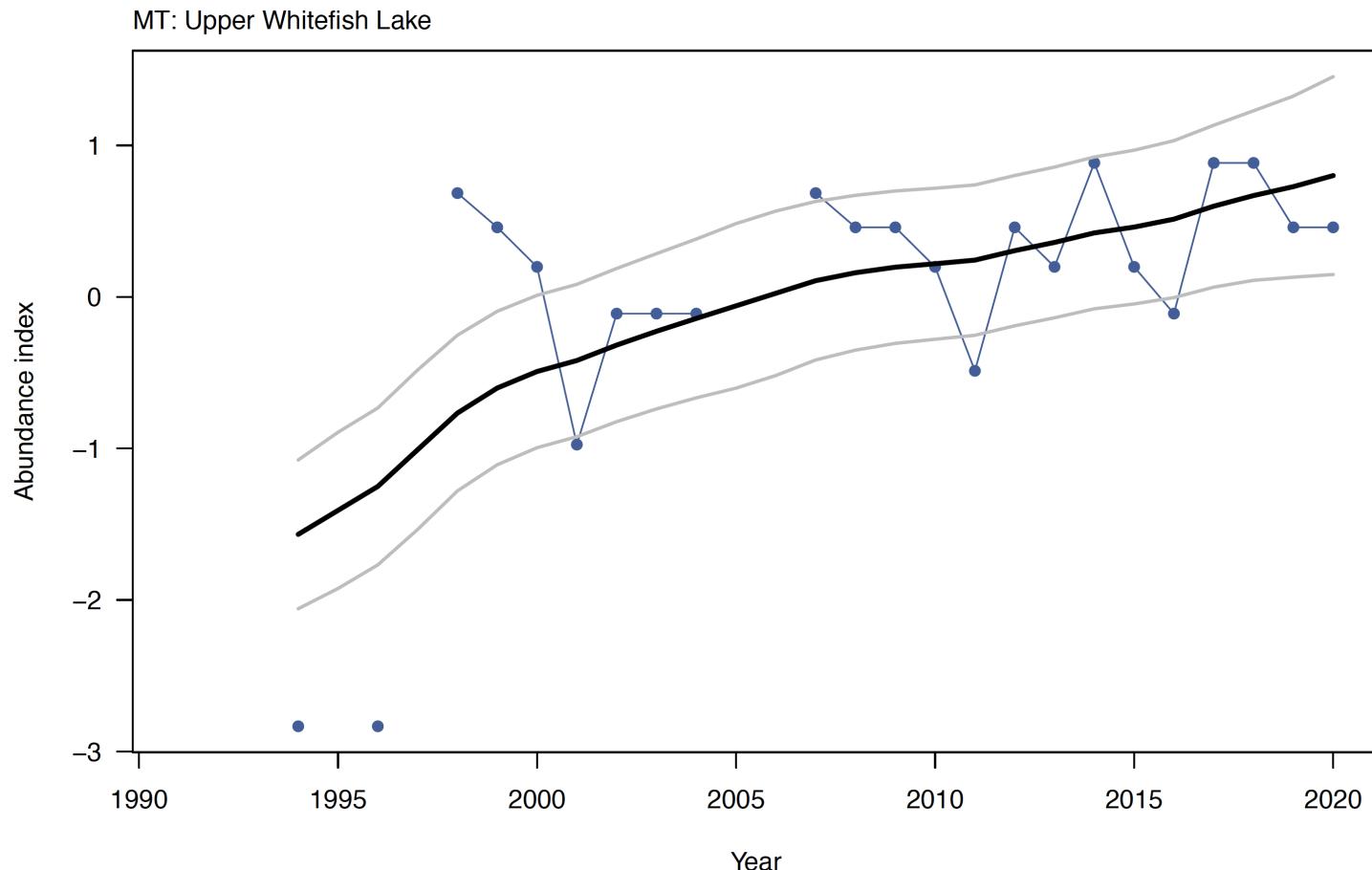
26/61 core areas had a positive trend

But only 6/61 were "significantly" positive

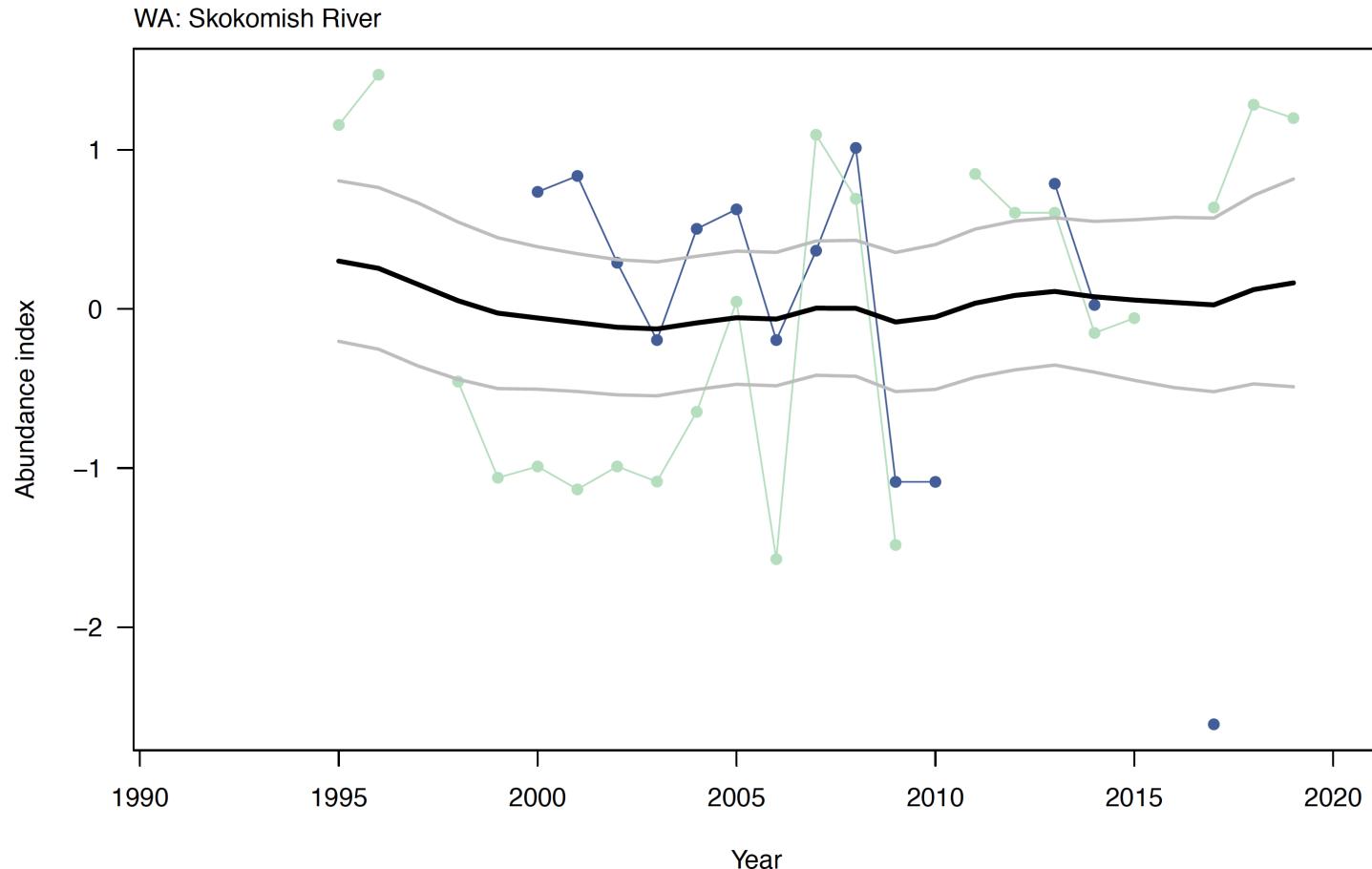
Example of a significant increase



Example of a significant increase

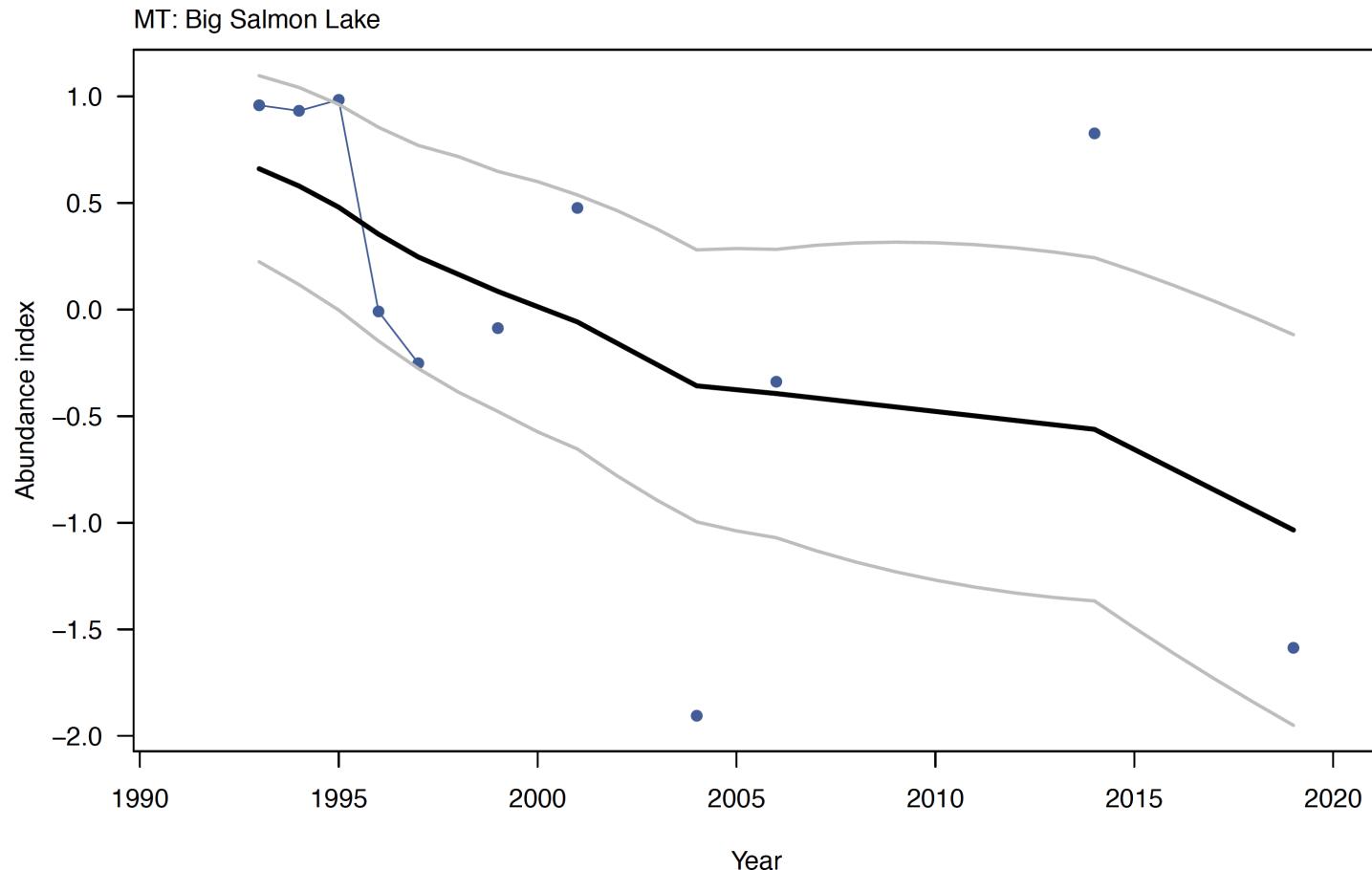


Example of no systematic trend

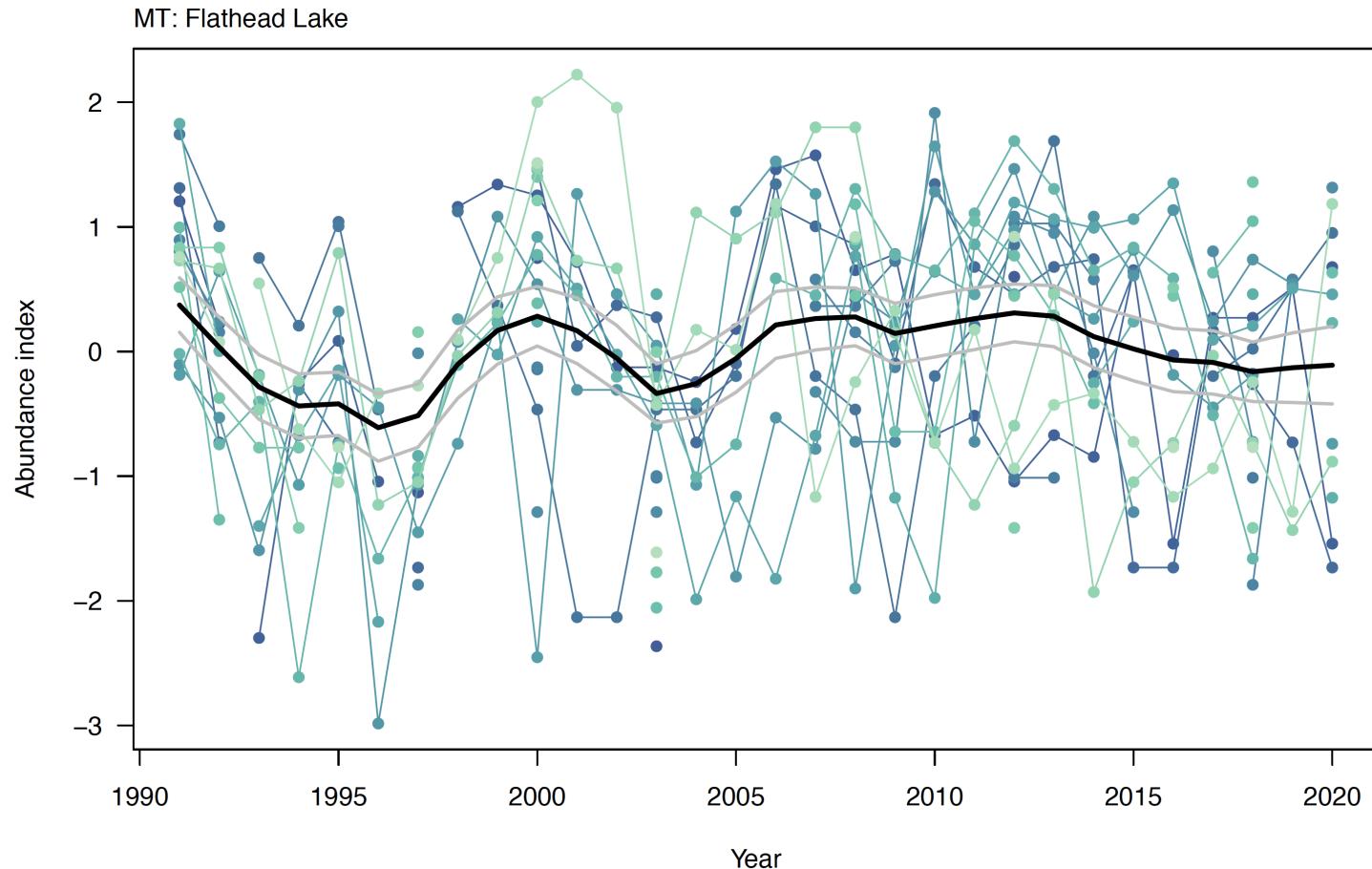


Data quality influences our ability to
estimate biases

Example of a data-poor core area



Example of a data-rich core area



In summary

We found minimal evidence of systematic biases in estimated trends

~5% of core areas were declining significantly

~10% of core areas were increasing significantly

Next steps

Complete a similar analysis with juvenile data

Use fitted models to project trends into the future

Open science

<https://github.com/mdscheuerell/bulltrout>

Image sources

Carnival: *Frank Kovalchek (2010)*

Robin Hood: *John Escott*

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