

## CprE 419 Lab 3: Graph Processing using MapReduce

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### Experiment 1 (40 points):

#### output the top ten patents and their significance

In this task I used three map-reduce rounds:

Round 1: for each A, get all the patents A cites and all the patents A is cited by.

Input: V1 V2

After map: <V1, V2 cite>, <V2, V1 citedby>

After reduce: <V1, cite V2 V3 ...|citedby V4 V5 ...>

```
4116485 cite 2912137 1259138 3418005|citedby 4214788
4116487 cite 360959 3334945 3350889 3830545|citedby 4165129
```

Round 2: find all the 1-hop and 2-hop citations for A

Input: V1, cite V2 V3 ...|citedby V4 V5 ...

After map: <V2, V1 citedby V4 V5 ...>

<V3, V1 citedby V4 V5 ...>

....

<A, B citedby C D...>

// B is the 1-hop citation of A and C D ... are the 2-hop citations of A

After reduce: <A, number of 1-hop and 2-hop citations>

// put all the 1-hop and 2-hop citations of A together

// remove the duplicates

// count the number

```
2954023 21
2954025 2
2954027 28
2954029 25
2954030 48
2954032 17
2954034 7
2954036 42
2954038 27
2954043 3
2954047 20
```

Round 3: find the top 10 patents with most citations

Input: A, number of 1-hop and 2-hop citations

After map: <uniform key, A number of 1-hop and 2-hop citations >

// push everything to a single reducer

After reduce: top ten patents

// while scanning all the patents,

// use a TreeMap to keep tracking the top 10 largest frequencies

```
[shuowang@n0 ~]$ hcat /scr/shuowang/lab3/exp1/output/part-r-00000
4463359 2130
4656603 2150
4063220 2200
3976982 2201
4277837 2207
3747120 2220
3702886 2280
4445892 2574
4558413 2854
4228496 3046
[shuowang@n0 ~]$
```

So the most frequent cited patent is ID 4228496: Multiprocessor system, invented by Katzman; James A. in 1976.

## Experiment 2 (40 points):

### compute the global clustering coefficient

In this task I used three map-reduce rounds:

Round 1: get all the neighbors of A and the number of triplets with A in the middle

Input: A B

After map:  $\langle A, B \rangle, \langle B, A \rangle$

After reduce:  $\langle A, \text{neighbor } 2 \text{ triplet } 1 \text{ B C} \rangle$

// A has 2 neighbors: B C, and there is one triplet with A in the middle: BAC

// The number of triplets =  $\text{neighbor \#} * (\text{neighbor \#} - 1) / 2$ ;

// for example: B,C,D are the 3 neighbors of A,

// then there are  $3 * (3 - 1) / 2 = 3$  triplets with A in the middle are BAC,BAD,CAD

```
2319459 neighbor 2 triplet 1 4941806 4176793
2319462 neighbor 2 triplet 1 4567968 4114829
2319464 neighbor 4 triplet 6 4506464 4712320 4612715 4611459
2319468 neighbor 1 triplet 0 4102102
2319471 neighbor 1 triplet 0 5733082
```

Round 2: finds all the triangles having A for each A

Input: A, neighbor 2 triplet 1 B C

After map:  $\langle B, A \text{ neighbor } 2 \text{ triplet } 1 \text{ B C} \rangle$

$\langle C, A \text{ neighbor } 2 \text{ triplet } 1 \text{ B C} \rangle$

....

$\langle A, B \text{ neighbor } n \text{ triplet } m \text{ C D} \dots \rangle$

// B is the neighbor of A and C D ... are the neighbors of B

After reduce:  $\langle A, \text{the triangles having A} \rangle$

```
// for each <A, B neighbor n triplet m C D...>
// check whether the other neighbors of A (except B),
// are the also the neighbors of B
// remove the duplicates
```

```
3525617 [352561751328785438166, 352561747646445438166]
3525620 [352562042847094518354, 352562042847094510233]
3525622 [352562240750194243737]
3525624 []
3525626 []
3525628 [352562839223565651795]
3525631 []
3525633 []
```

Round 3: counts all the triangles in the network

Input: A, [ABC, ACD]

After map: <uniform key, [ABC, ACD]>

```
// push all the triangles to a single reducer
```

After reduce: number of triangles

```
// put all the triangles together
```

```
// remove the duplicates
```

```
[shuowang@n0 ~]$ hcat /scr/shuowang/lab3/exp2/output1/part-r-00000
Number of Triangles: 2111096
```

Round 4: counts all the triplets in the network

Input: A, neighbor 2 triplet 1 B C

```
// the output of round 1 is the input of round 4
```

After map: <uniform key, number of triplets>

```
// push all the numbers to a single reducer
```

```
// there is no duplicates
```

After reduce: number of triplets

```
// sum them all
```

```
[shuowang@n0 ~]$ hcat /scr/shuowang/lab3/exp2/output2/part-r-00000
Number of Triplets: 335781273
```

The final answer:

the global clustering coefficient =  $3 * 2111096 / 335781273 = \mathbf{0.018861}$

Communication complexity:

Exp#	Round	Total map cost	Per reducer cost	Total reducer cost	Total M-R communication
Exp1	1	$\Theta(\#edges)$	$\Theta(\#edges / \#patents)$	$\Theta(\#edges)$	$\Theta(\#edges)$
	2	$\Theta(\#patents)$	$\Theta(1)$	$\Theta(\#patents)$	$\Theta(\#patents)$
	3	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$
Exp2	1	$\Theta(\#edges)$	$\Theta(\#edges / \#patents)$	$\Theta(\#edges)$	$\Theta(\#edges)$
	2	$\Theta(\#patents)$	$\Theta(1)$	$\Theta(\#patents)$	$\Theta(\#patents)$
	3	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$
	4	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$	$\Theta(\#patents)$

Exp1:

Round 1: The number of input atoms =  $\#edges$ , and the in map-reduce process no information is missed. So the total maps cost, total reduce cost and total M-R communication are all linear functions of  $\#edges$ . Each patent goes to a different reducer, so there are  $\#patents$  reducers and the per reducer cost = Total reducer cost / number of reducers =  $\Theta(\#edges / \#patents)$ .

Round 2: The number of input atoms =  $\#patents$ , and the in map-reduce process no information is missed. So the total maps cost, total reduce cost and total M-R communication are all linear functions of  $\#patents$ . Each patent goes to a different reducer, so there are  $\#patents$  reducers and the per reducer cost = Total reducer cost / number of reducers =  $\Theta(\#patents / \#patents) = \Theta(1)$ .

Round 3: The number of input atoms =  $\#patents$ , and the in map-reduce process no information is missed. So the total maps cost, total reduce cost and total M-R communication are all linear functions of  $\#patents$ . There is only one reducer, so the per reducer cost = Total reducer cost / number of reducers =  $\Theta(\#patents / 1) = \Theta(\#patents)$ .

Exp2:

Round 1: similar to Exp1.round 1

Round 2: similar to Exp1.round 2

Round 3: similar to Exp1.round 3

Round 4: similar to Exp1.round 3