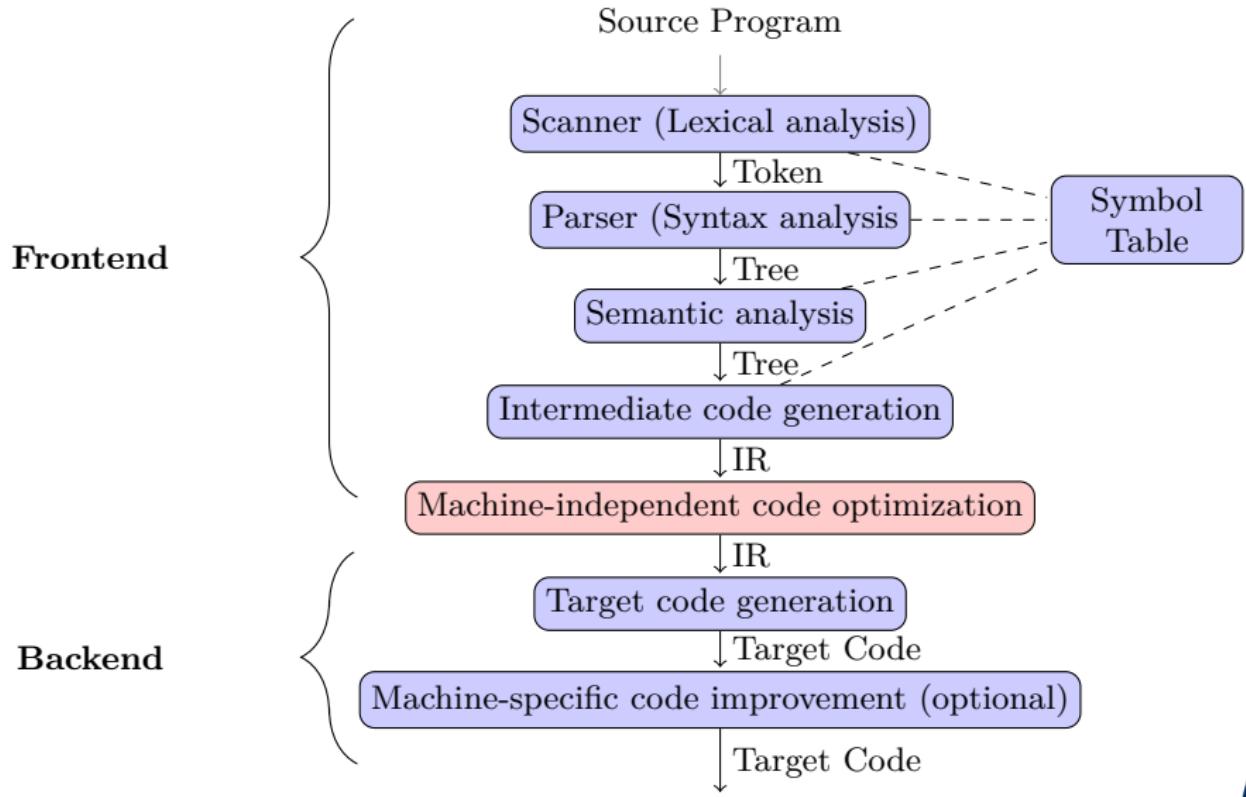


# OPTIMIZATIONS

LECTURE 21  
SECTION 8.5, 9.1

ROKAN UDDIN FARUQUI

Associate Professor  
Dept of Computer Science and Engineering  
University of Chittagong, Bangladesh  
Email: *rokan@cu.ac.bd*



# Optimizations

**local** optimizations – within a basic block,  
**global** optimizations – between basic blocks.



# Outline

1 Local Optimization

2 Global Optimization



# DAG for basic blocks

Three-address code to DAG structure:

- One leaf per initial value.
- One node per statement, with an edge to the node representing the operand value(s).
- Inner node is labelled by operator, and list of variables, which computes the value.
- Output nodes are those labelled with live exit variables.



# DAG for basic blocks

Three-address code to DAG structure:

- One leaf per initial value.
- One node per statement, with an edge to the node representing the operand value(s).
- Inner node is labelled by operator, and list of variables, which computes the value.
- Output nodes are those labelled with live exit variables.



# DAG for basic blocks

Three-address code to DAG structure:

- One leaf per initial value.
- One node per statement, with an edge to the node representing the operand value(s).
- Inner node is labelled by operator, and list of variables, which computes the value.
- Output nodes are those labelled with live exit variables.



# DAG for basic blocks

Three-address code to DAG structure:

- One leaf per initial value.
- One node per statement, with an edge to the node representing the operand value(s).
- Inner node is labelled by operator, and list of variables, which computes the value.
- Output nodes are those labelled with live exit variables.



# DAG optimization uses

- Local common subexpressions.
- Dead code elimination.
- Apply algebraic simplifications.
- Reorder statements that do not depend on one other.



# Local common subexpressions

- Eliminate instructions that has already been computed.

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



# Local common subexpressions

- Eliminate instructions that has already been computed.

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



# Local common subexpressions

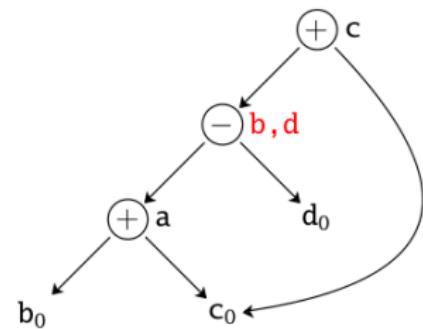
- Eliminate instructions that has already been computed.

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



# Local common subexpressions

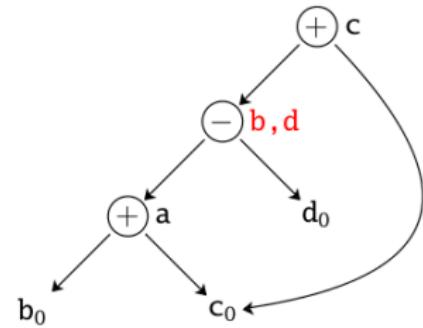
- Eliminate instructions that has already been computed.

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



# Dead code elimination

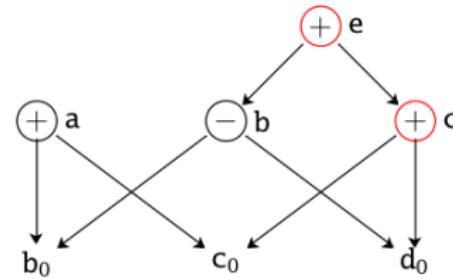
- Eliminate instructions that compute values that are never used

$$a = b + c$$

$$b = b - d$$

$$c = c + d$$

$$e = b + c$$



# Dead code elimination

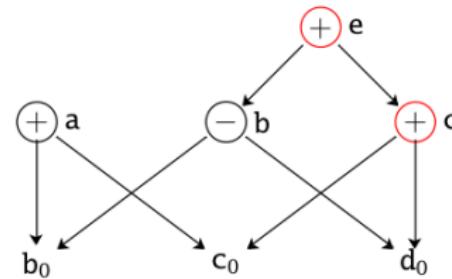
- Eliminate instructions that compute values that are never used

$$a = b + c$$

$$b = b - d$$

$$c = c + d$$

$$e = b + c$$



# Algebraic Identities

- Apply algebraic simplification rules.

$$x + 0 = 0 + x = x$$

$$x - 0 = x$$

$$x \times 1 = 1 \times x = x$$

$$x/1 = x$$

$$2 + 2 = 4 \text{(constant folding)}$$

ExpensiveCheaper

$$x^2 = x \times x \text{(lib function)}$$

$$2 \times x = x + x$$

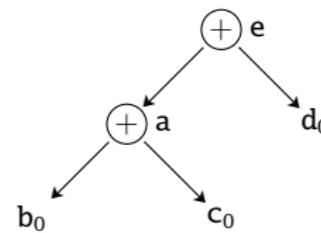
$$x/2 = x \times 0.5$$



# Algebraic Identities

- **Commutativity** with local common subexpressions.
- **Associativity** with composite expressions....

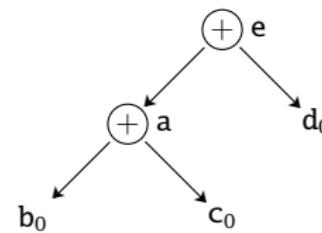
$$\begin{aligned}a &= c + b \\e &= c + d + b\end{aligned}$$



# Algebraic Identities

- **Commutativity** with local common subexpressions.
- **Associativity** with composite expressions....

$$\begin{aligned}a &= c + b \\e &= c + d + b\end{aligned}$$

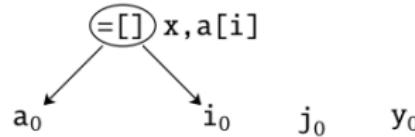


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$

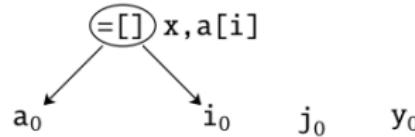


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$

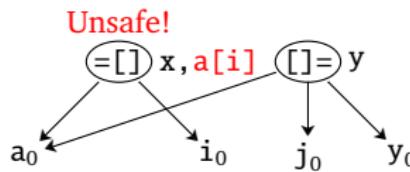


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$

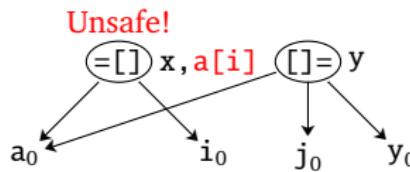


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$

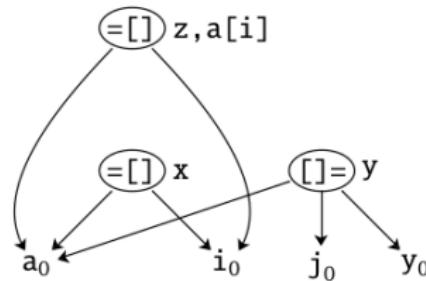


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$

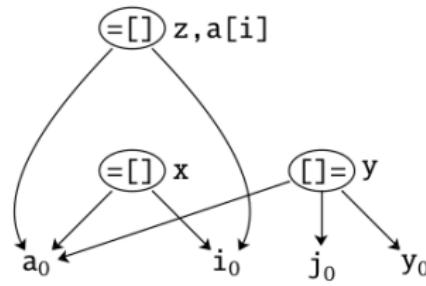


# Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$



# Remarks

- The entire memory is a single array!
- In C: no check of bounds of arrays, so memory can be arbitrarily updated.



# Outline

1 Local Optimization

2 Global Optimization



# Example: quicksort

```
void quicksort(int a[], int m, int n) {  
    int i, j, v, x; if (n <= m) return;  
    /*fragment starts here*/  
    i = m-1; j = n; v = a[n];  
    while (1) {  
        do i = i+1; while (a[i] < v);  
        do j = j-1; while (a[j] > v);  
        if (i >= j) break;  
        x = a[i]; a[i] = a[j]; a[j] = x;  
    }  
    x = a[i]; a[i] = a[n]; a[n] = x;  
    /*fragment end here*/  
    quicksort(a,m,j); quicksort(a,i+1,n);  
}
```

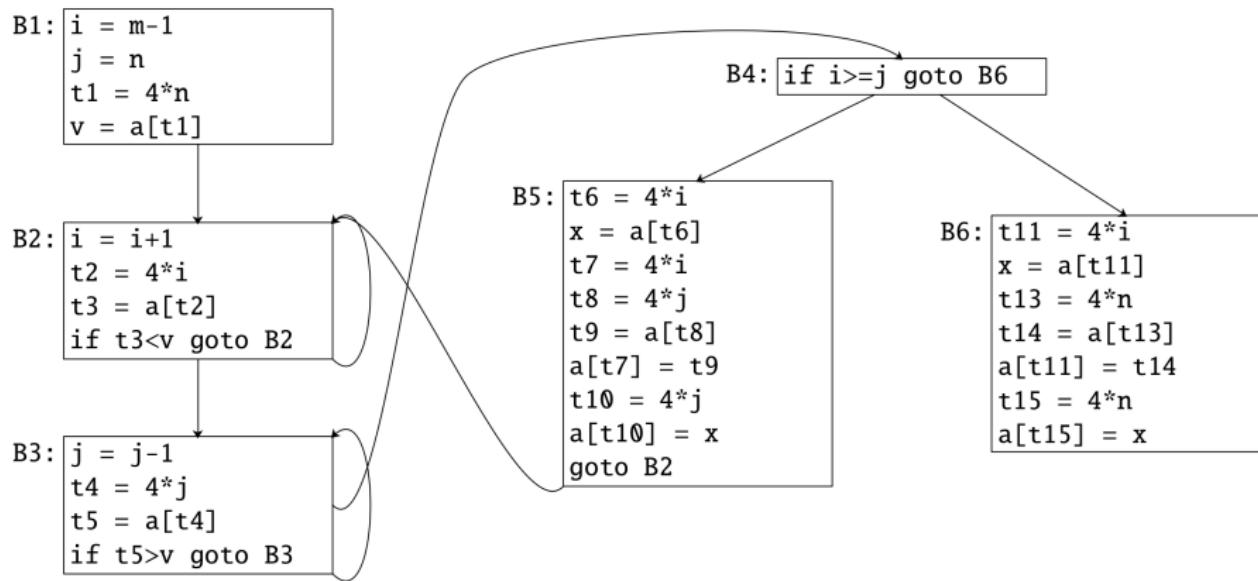


# Three-address code for fragments of qsort

(1)	$i = m-1$	(16)	$t7 = 4*i$
(2)	$j = n$	(17)	$t8 = 4*j$
(3)	$t1 = 4*n$	(18)	$t9 = a[t8]$
(4)	$v = a[t1]$	(19)	$a[t7] = t9$
(5)	$i = i+1$	(20)	$t10 = 4*j$
(6)	$t2 = 4*i$	(21)	$a[t10] = x$
(7)	$t3 = a[t2]$	(22)	goto (5)
(8)	if $t3 < v$ goto (5)	(23)	$t11 = 4*i$
(9)	$j = j-1$	(24)	$x = a[t11]$
(10)	$t4 = 4*j$	(25)	$t12 = 4*i$
(11)	$t5 = a[t4]$	(26)	$t13 = 4*n$
(12)	if $t5 > v$ goto (9)	(27)	$t14 = a[t13]$
(13)	if $i >= j$ goto (23)	(28)	$a[t12] = t14$
(14)	$t6 = 4*i$	(29)	$t15 = 4*n$
(15)	$x = a[t6]$	(30)	$a[t15] = x$



# Basic blocks for quick sort: first try



# Local Common Subexpression Elimination

```
B5: t6 = 4*i  
    x = a[t6]  
    t7 = 4*i  
    t8 = 4*j  
    t9 = a[t8]  
    a[t7] = t9  
    t10 = 4*j  
    a[t10] = x  
    goto B2
```

⇒

```
B5: t6 = 4*i  
    x = a[t6]  
    t8 = 4*j  
    t9 = a[t8]  
    a[t6] = t9  
    a[t8] = x  
    goto B2
```



# Local Common Subexpression Elimination

B5: **t6 = 4\*i**  
x = a[t6]  
**t7 = 4\*i**  
**t8 = 4\*j**  
t9 = a[t8]  
a[t7] = t9  
**t10 = 4\*j**  
a[t10] = x  
goto B2

B5: t6 = 4\*i  
x = a[t6]  
t8 = 4\*j  
t9 = a[t8]  
a[t6] = t9  
a[t8] = x  
goto B2

⇒



# Local Common Subexpression Elimination

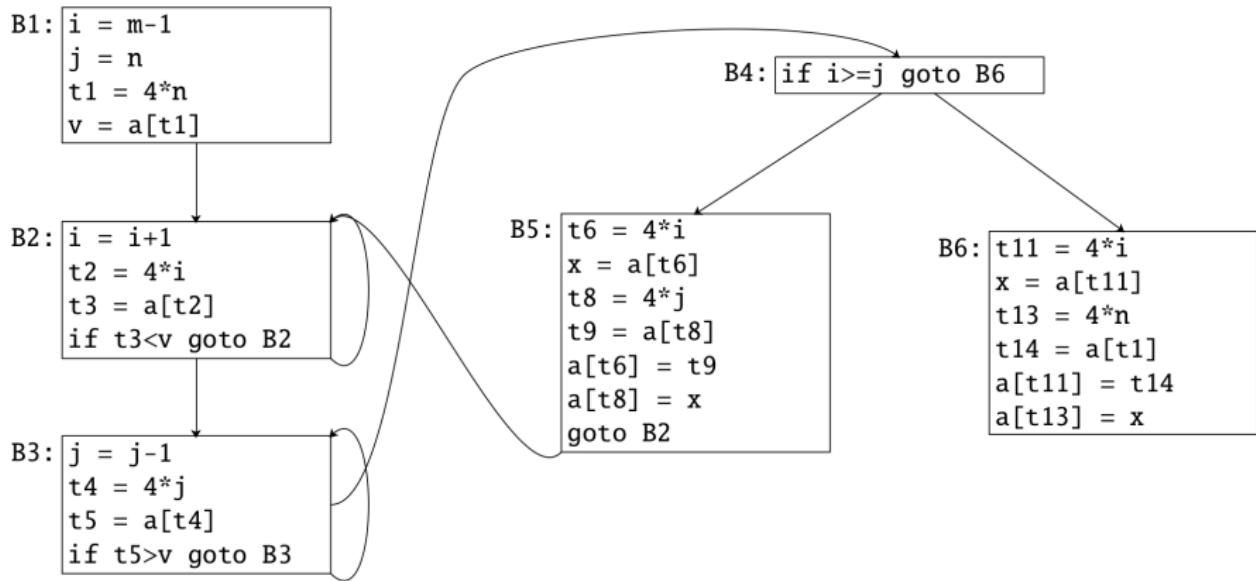
```
B5: t6 = 4*i  
x = a[t6]  
t7 = 4*i  
t8 = 4*j  
t9 = a[t8]  
a[t7] = t9  
t10 = 4*j  
a[t10] = x  
goto B2
```

⇒

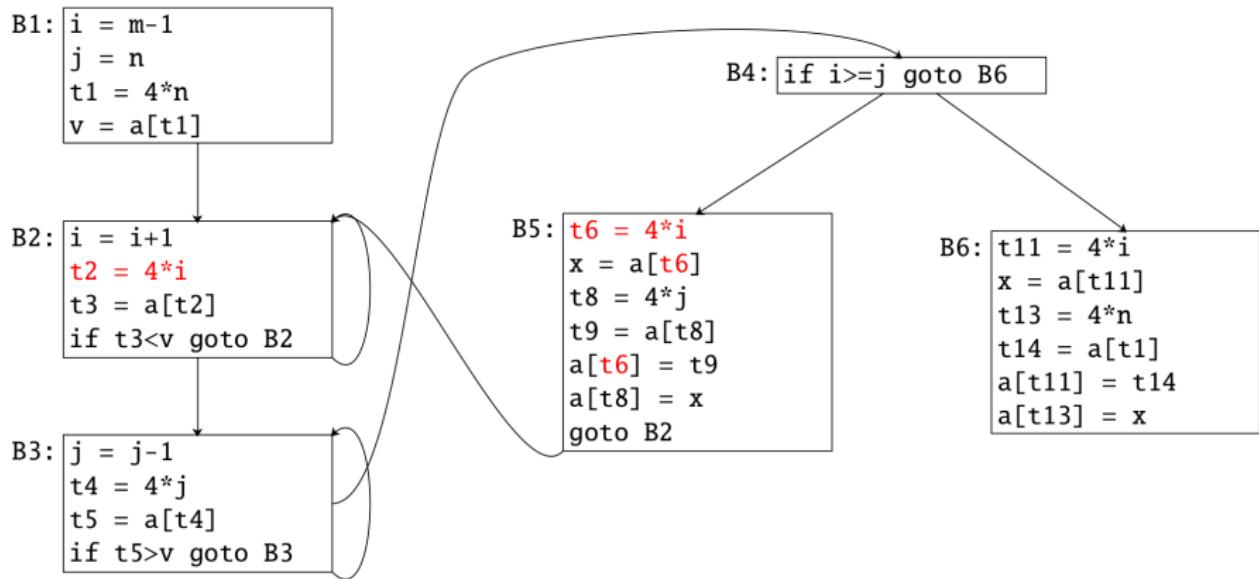
```
B5: t6 = 4*i  
x = a[t6]  
t8 = 4*j  
t9 = a[t8]  
a[t6] = t9  
a[t8] = x  
goto B2
```



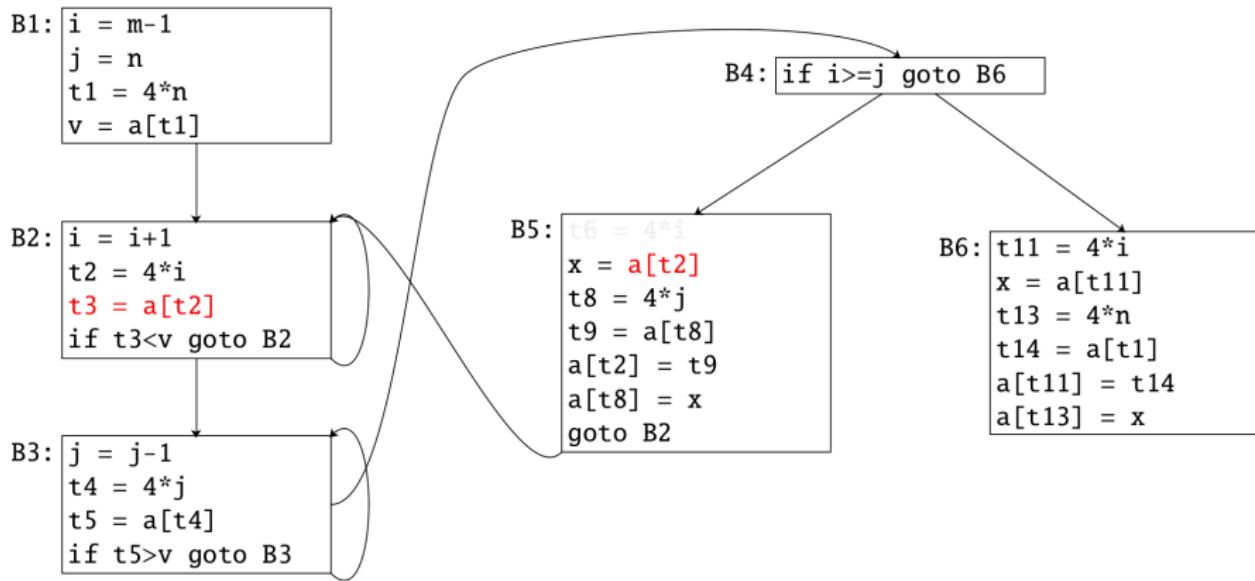
# Global Common Subexpression Elimination



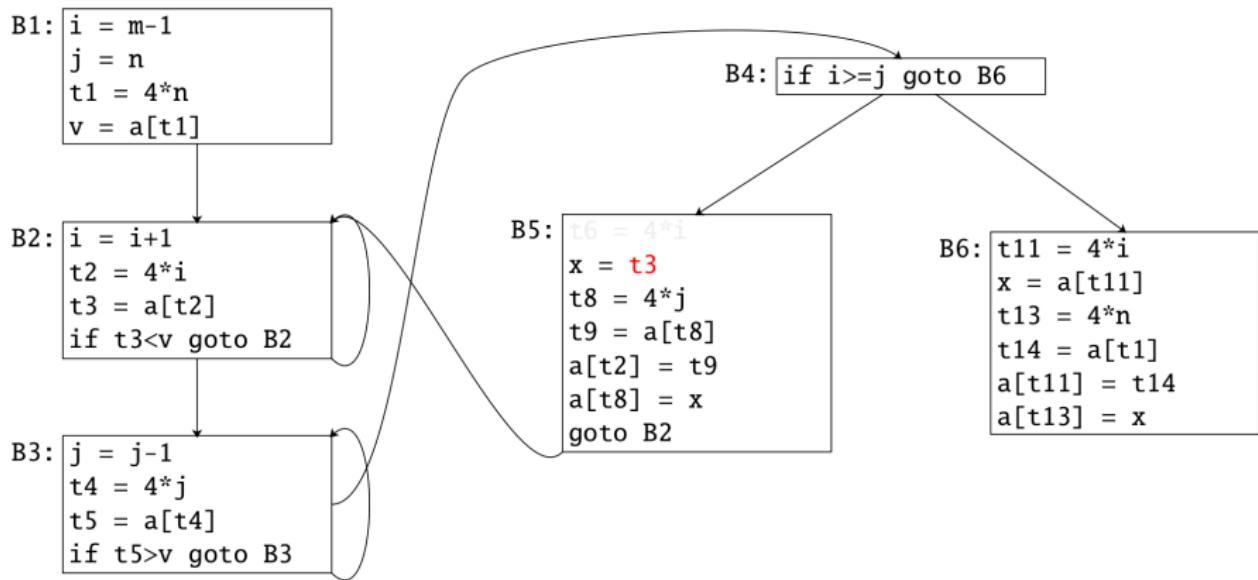
# Global Common Subexpression Elimination



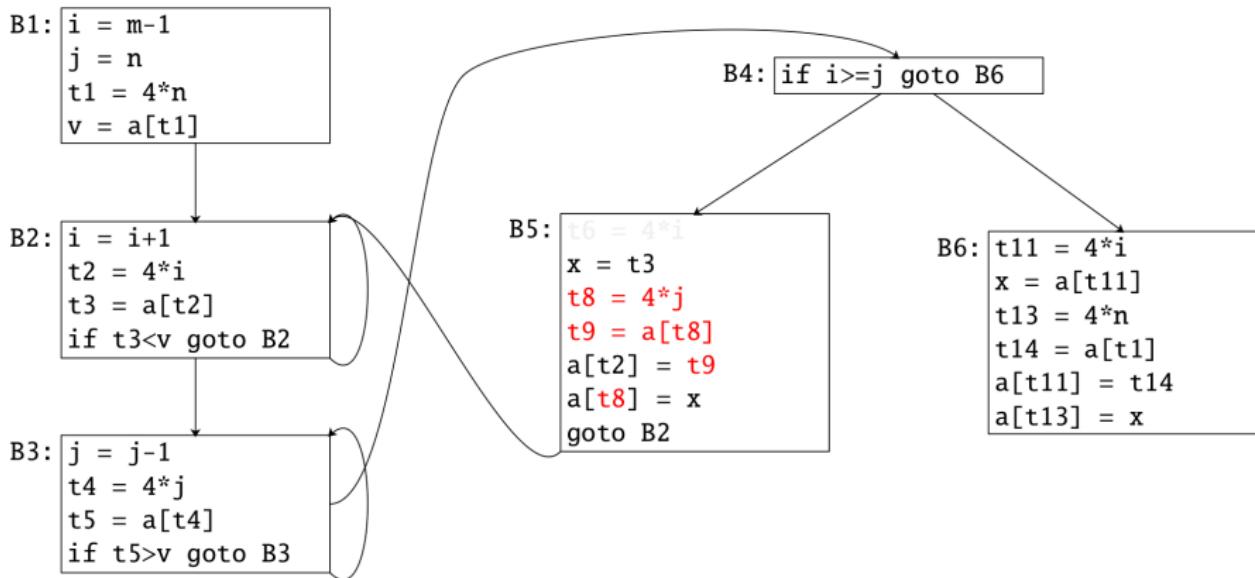
# Global Common Subexpression Elimination



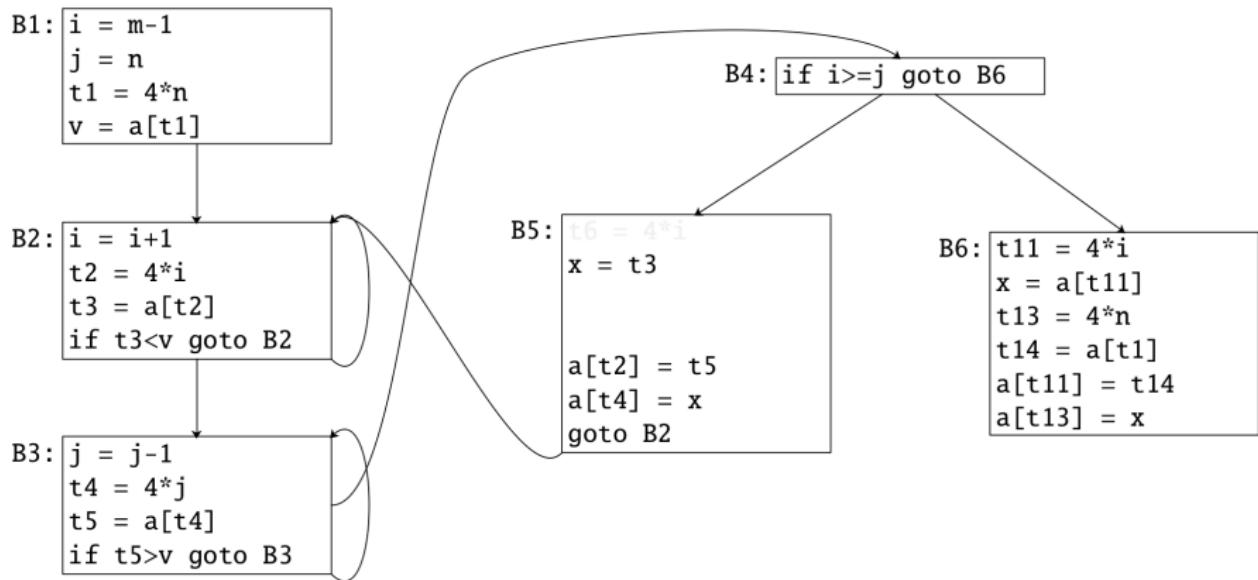
# Global Common Subexpression Elimination



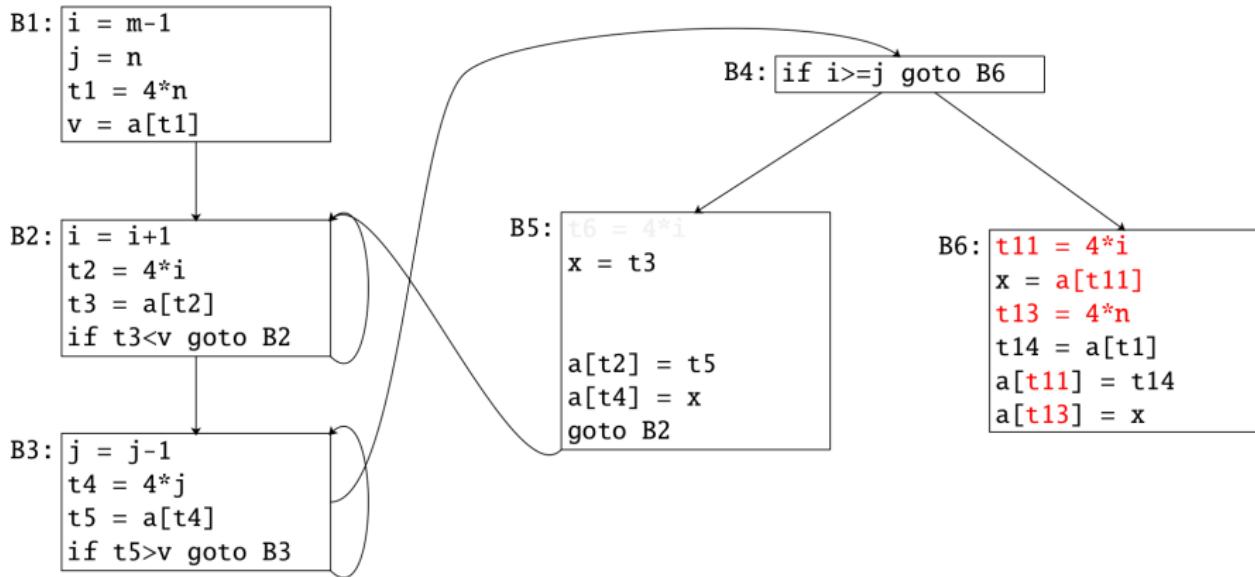
# Global Common Subexpression Elimination



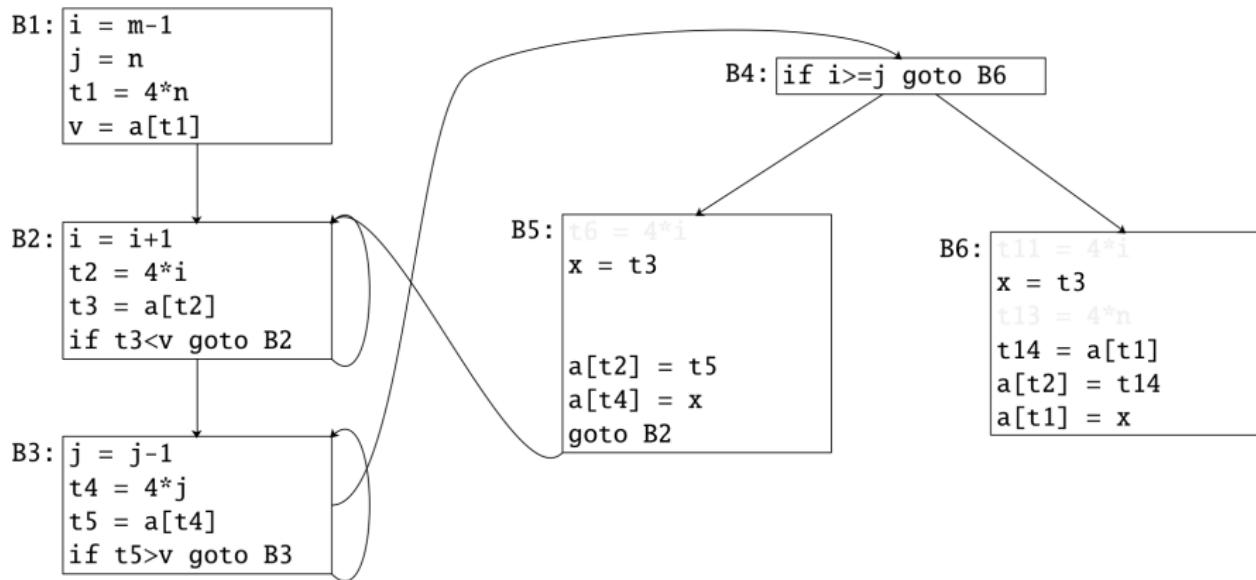
# Global Common Subexpression Elimination



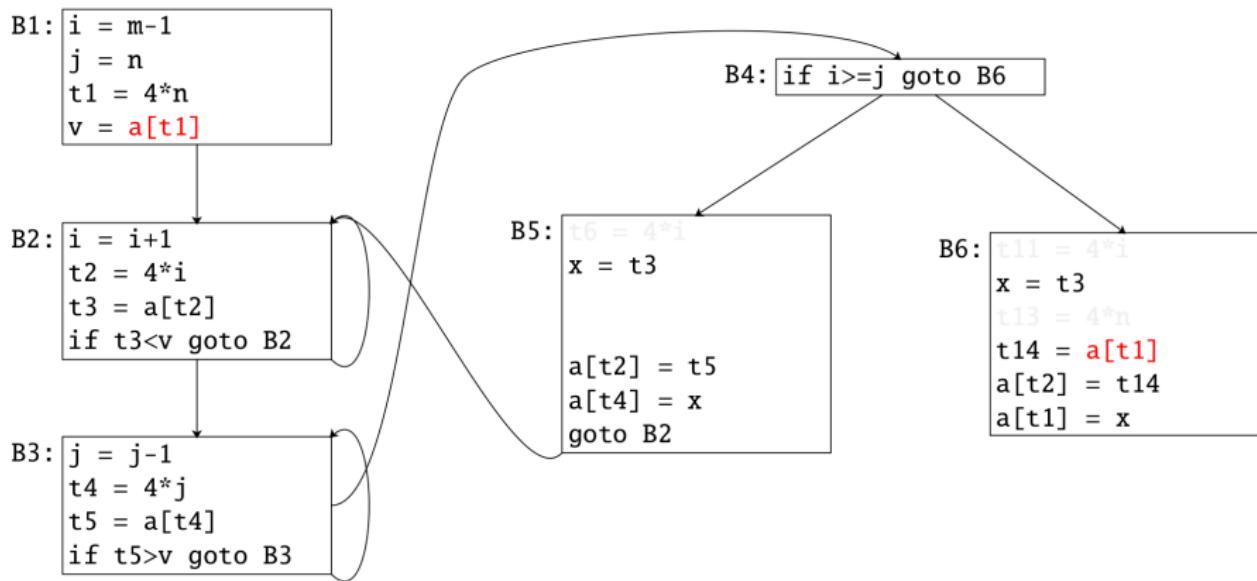
# Global Common Subexpression Elimination



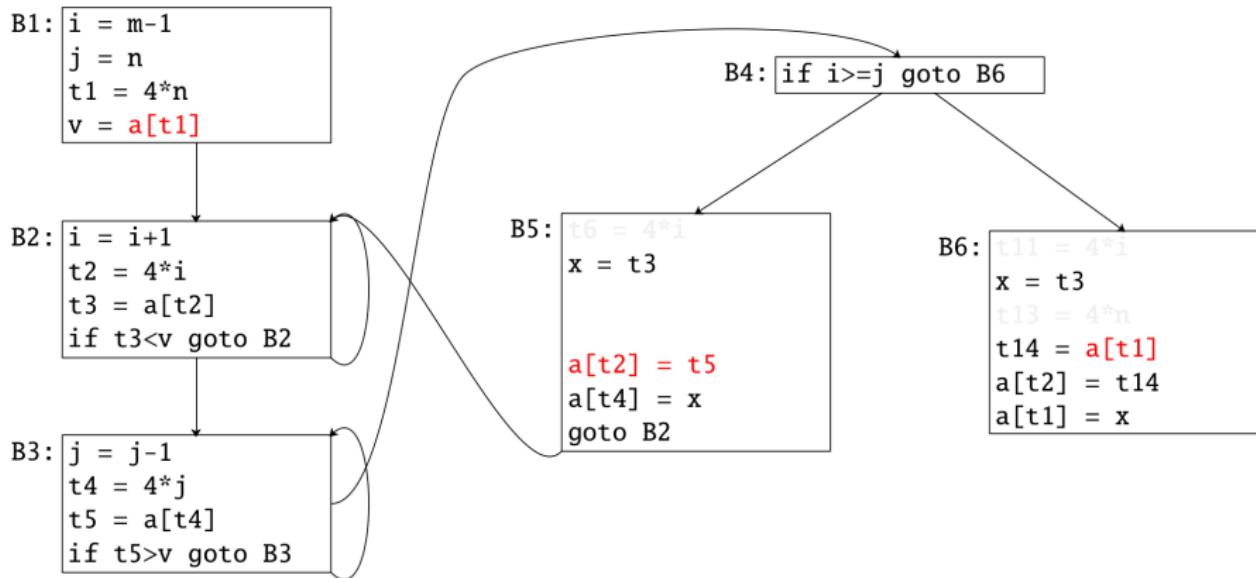
# Global Common Subexpression Elimination



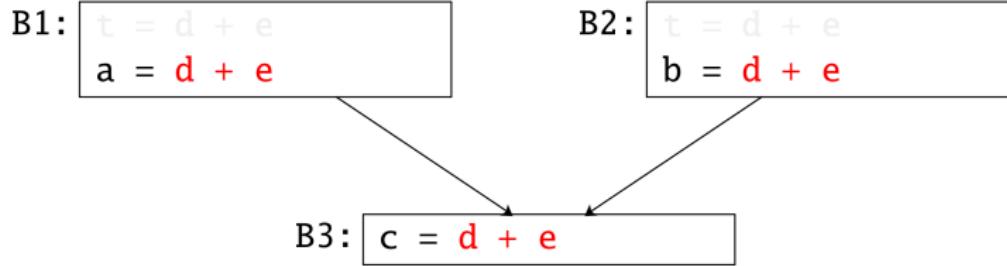
# Global Common Subexpression Elimination



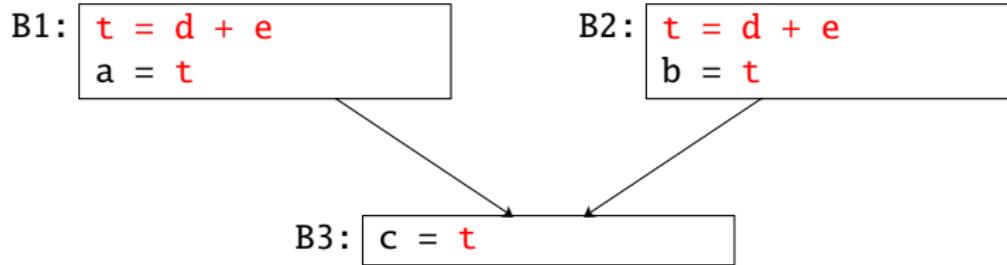
# Global Common Subexpression Elimination



# Copy Propagation



# Copy Propagation



# Dead-code Elimination

```
if (debug) print  
debug = FALSE
```



# Code Motion

**while** (i <= limit-2) /\*not changing limit\*/  
becomes

t = limit-2;

**while** (i <= t) /\*not changing limit or t\*/



# Summary

Reduce redundancy but preserve semantics!

- Global Common Subexpressions.
- Copy Propagation.
- Dead-code Elimination.
- Code Motion.

