

OPTIMIZATIONS

LECTURE 21

SECTION 8.5, 9.1

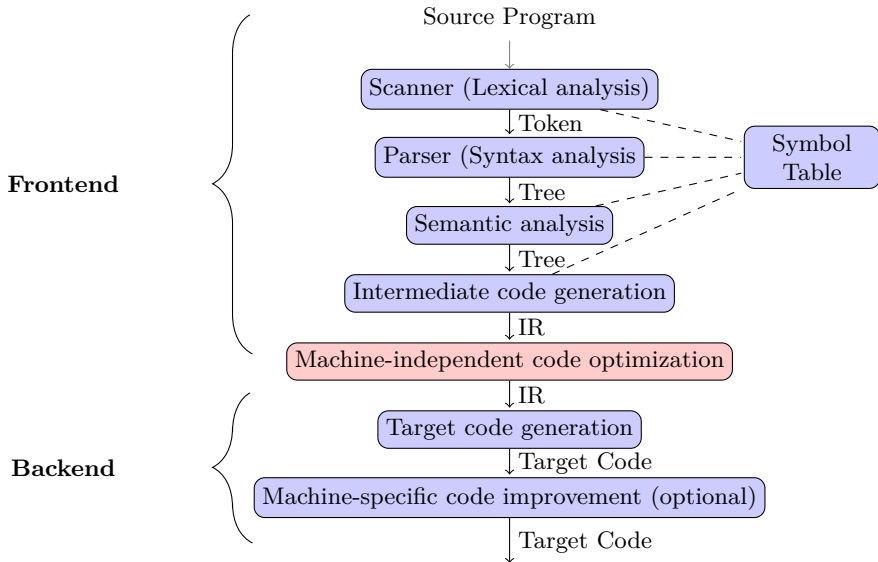
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Optimizations

local optimizations – within a basic block,
global optimizations – between basic blocks.



Outline

1 Local Optimization

2 Global Optimization



DAG for basic blocks

Three-address code to DAG structure:

- One leaf per initial value.
- One node per statement, with an edge to the node representing the operand value(s).
- Inner node is labelled by operator, and list of variables, which computes the value.
- Output nodes are those labelled with live exit variables.



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DAG optimization uses

- Local common subexpressions.
- Dead code elimination.
- Apply algebraic simplifications.
- Reorder statements that do not depend on one other.



Local common subexpressions

- Eliminate instructions that has already been computed.

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



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Local common subexpressions

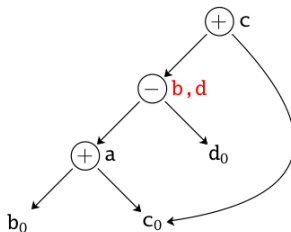
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Local common subexpressions

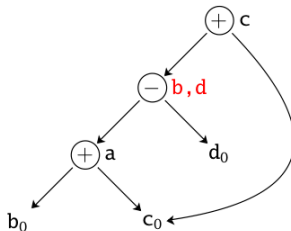
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Dead code elimination

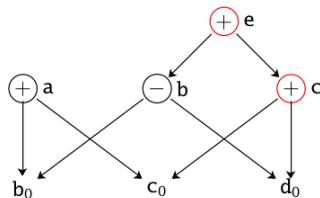
- Eliminate instructions that compute values that are never used

$$a = b + c$$

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Dead code elimination

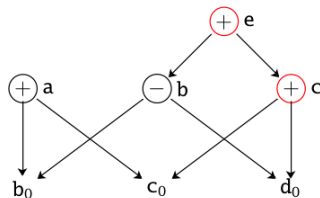
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Algebraic Identities

- Apply algebraic simplification rules.

$$x + 0 = 0 + x = x$$

$$x - 0 = x$$

$$x \times 1 = 1 \times x = x$$

$$x/1 = x$$

$$2 + 2 = 4(\text{constant folding})$$

ExpensiveCheaper

$$x^2 = x \times x(\text{lib function})$$

$$2 \times x = x + x$$

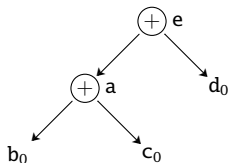
$$x/2 = x \times 0.5$$



Algebraic Identities

- **Commutativity** with local common subexpressions.
- **Associativity** with composite expressions....

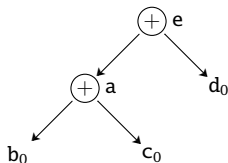
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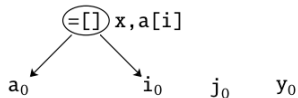
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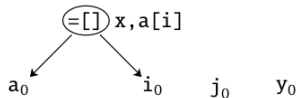
Array References

$$x = a[i]$$

$$a[j] = y$$

$$z = a[i]$$


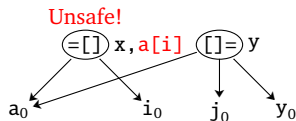
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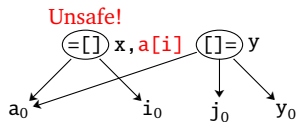
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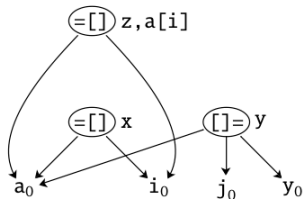
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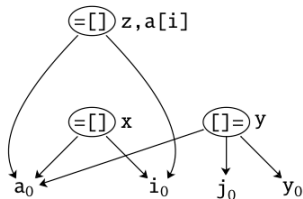
$$a[j] = y$$

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Remarks

- The entire memory is a single array!
- In C: no check of bounds of arrays, so memory can be arbitrarily updated.



Outline

1 Local Optimization

2 Global Optimization



Example: quicksort

```
void quicksort(int a[], int m, int n) {  
    int i, j, v, x; if (n <= m) return;  
    /*fragment starts here*/  
    i = m-1; j = n; v = a[n];  
    while (1) {  
        do i = i+1; while (a[i] < v);  
        do j = j-1; while (a[j] > v);  
        if (i >= j) break;  
        x = a[i]; a[i] = a[j]; a[j] = x;  
    }  
    x = a[i]; a[i] = a[n]; a[n] = x;  
    /*fragment end here*/  
    quicksort(a,m,j); quicksort(a,i+1,n);  
}
```

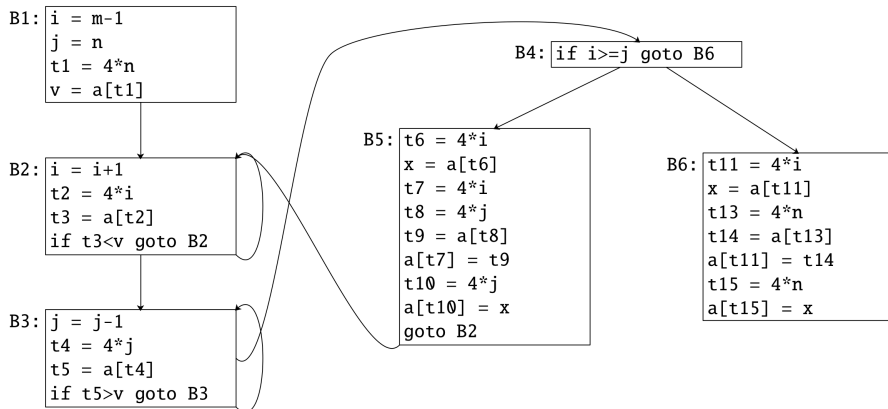


Three-address code for fragments of qsort

(1)	$i = m-1$	(16)	$t7 = 4*i$
(2)	$j = n$	(17)	$t8 = 4*j$
(3)	$t1 = 4*n$	(18)	$t9 = a[t8]$
(4)	$v = a[t1]$	(19)	$a[t7] = t9$
(5)	$i = i+1$	(20)	$t10 = 4*j$
(6)	$t2 = 4*i$	(21)	$a[t10] = x$
(7)	$t3 = a[t2]$	(22)	goto (5)
(8)	if $t3 < v$ goto (5)	(23)	$t11 = 4*i$
(9)	$j = j-1$	(24)	$x = a[t11]$
(10)	$t4 = 4*j$	(25)	$t12 = 4*i$
(11)	$t5 = a[t4]$	(26)	$t13 = 4*n$
(12)	if $t5 > v$ goto (9)	(27)	$t14 = a[t13]$
(13)	if $i \geq j$ goto (23)	(28)	$a[t12] = t14$
(14)	$t6 = 4*i$	(29)	$t15 = 4*n$
(15)	$x = a[t6]$	(30)	$a[t15] = x$



Basic blocks for quick sort: first try



Local Common Subexpression Elimination

```
B5: t6 = 4*i  
    x = a[t6]  
    t7 = 4*i  
    t8 = 4*j  
    t9 = a[t8]  
    a[t7] = t9  
    t10 = 4*j  
    a[t10] = x  
    goto B2
```

⇒

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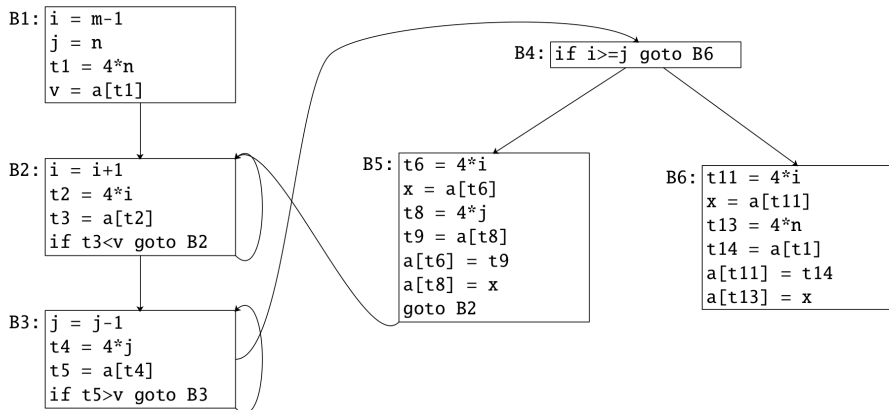
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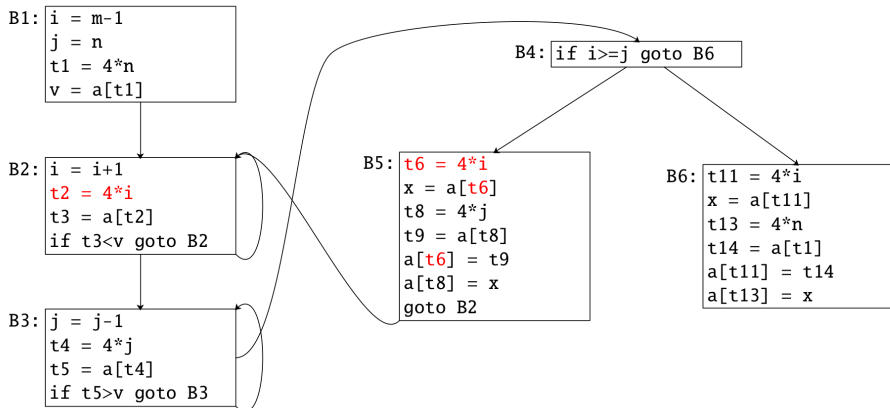
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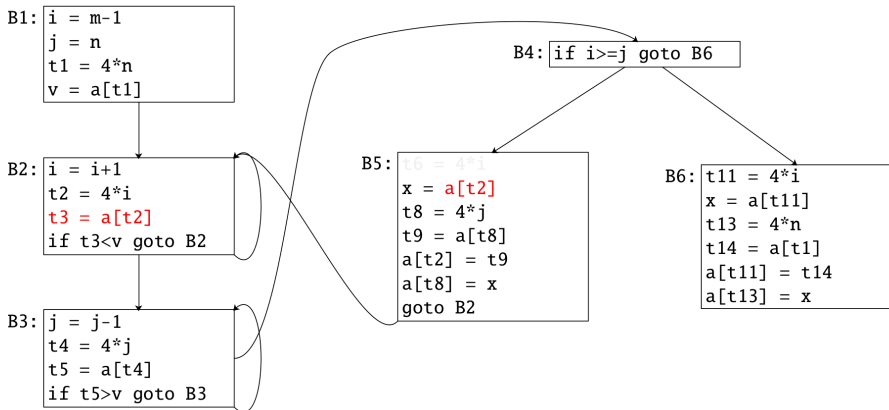
Global Common Subexpression Elimination



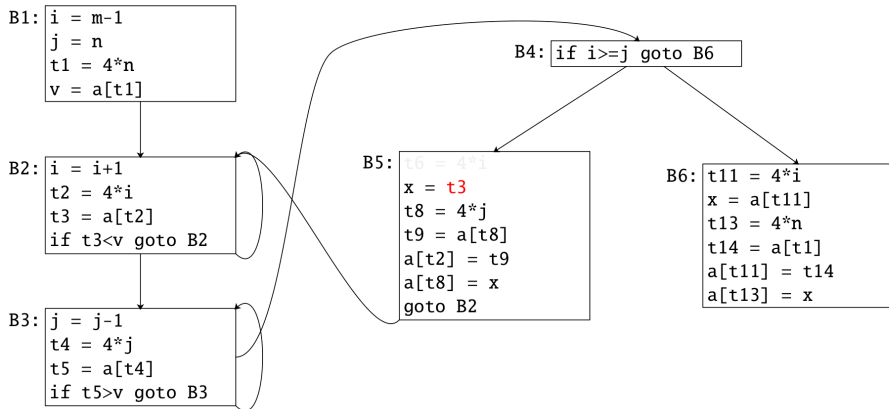
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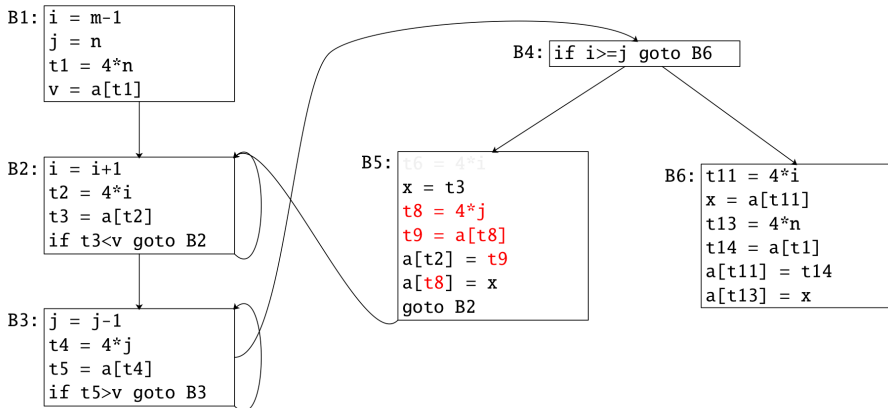
Global Common Subexpression Elimination



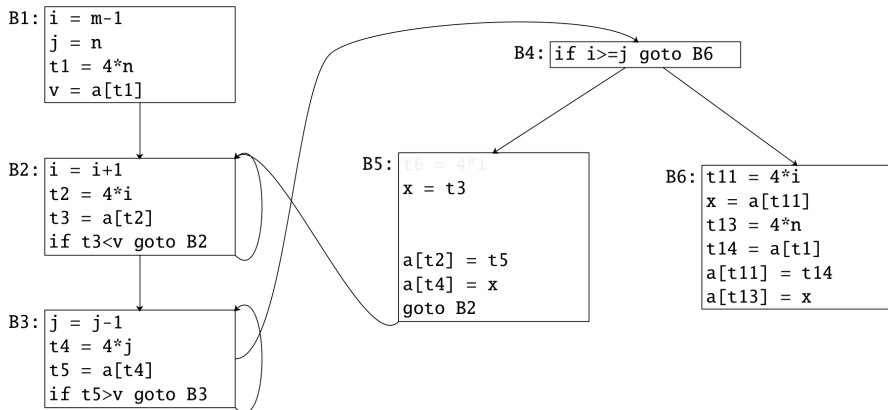
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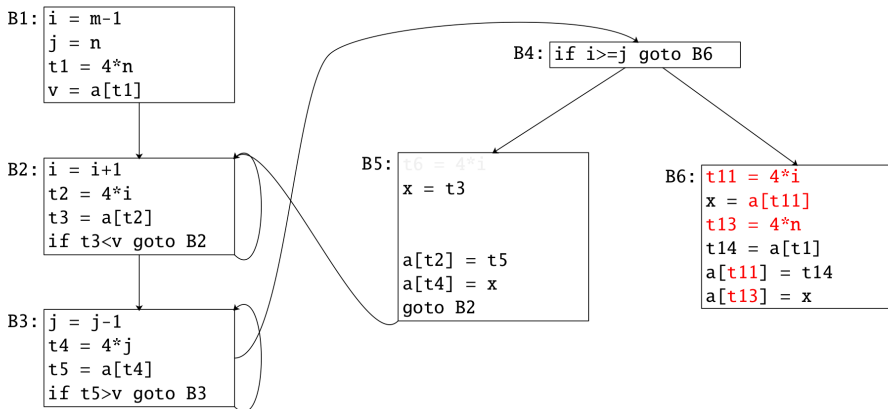
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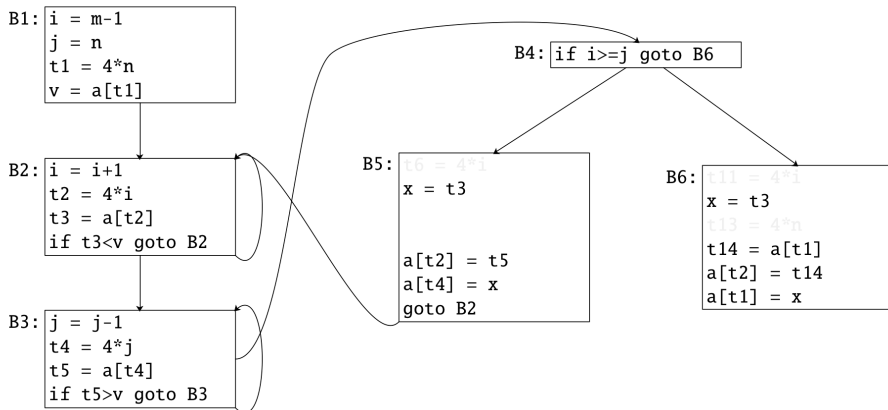
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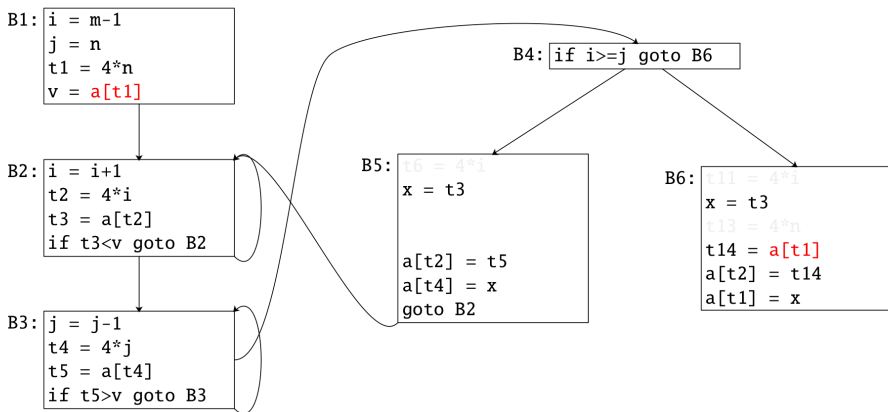
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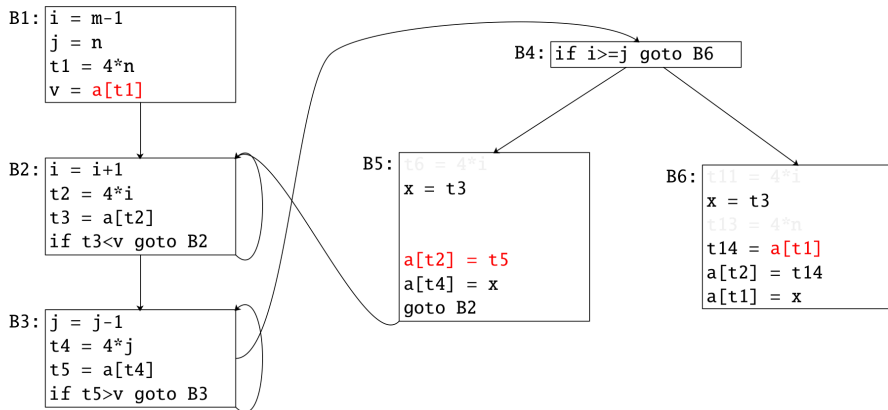
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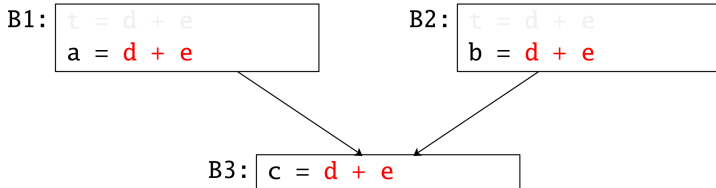
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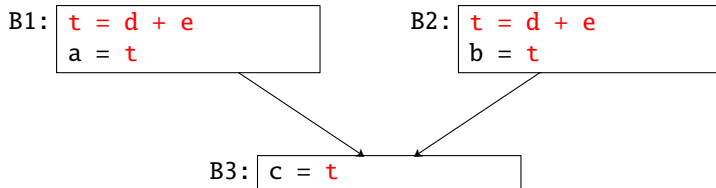
Global Common Subexpression Elimination



Copy Propagation



Copy Propagation



Dead-code Elimination

```
if (debug) print  
debug = FALSE
```



Code Motion

```
while (i <= limit-2) /*not changing limit*/
```

becomes

```
t = limit-2;
```

```
while (i <= t) /*not changing limit or t*/
```



Summary

Reduce redundancy but preserve semantics!

- Global Common Subexpressions.
- Copy Propagation.
- Dead-code Elimination.
- Code Motion.

