1. Stock Prices Are Non-Stationary

- Prices trend upward or downward over time.
- The standard deviation of a trending series (like stock prices) grows over time it's not a stable measure.
- Therefore, the volatility measured from raw prices **includes the trend** (drift), and overstates true risk.

Returns, on the other hand, are (approximately) **stationary** — they fluctuate around a mean (often close to 0) and don't trend like prices.

Statistic	Usefulness for Volatility	Problem
Raw price	X Misleading — not stationary	Includes trend, not comparable
$\mathbf{Price\ Delta}\ P_t - P_{t-1}$	O Better, but still scale-dependent	Can't compare across stocks
Percent change $\frac{P_t - P_{t-1}}{P_{t-1}}$	✓ Okay	Still additive bias over time
Log return $\log \left(\frac{P_t}{P_{t-1}} \right)$	✓ Best choice	Time-additive, scale-invariant

2. Standard Deviation Assumes Mean-Reverting Data

- Volatility is a statistical concept that assumes data fluctuates around a mean.
- Prices **do not** revert to a mean but **returns do**.
- If you apply standard deviation to prices, you're measuring both trend and noise, which confuses the interpretation.

3. Comparability Across Assets

- The price of AAPL at \$180 and AMZN at \$3500 are in different numerical ranges.
- You can't compare standard deviation of prices across these assets.
- **Returns** normalize this. A 1% move is a 1% move, whether the price is \$10 or \$1000.

1 4. Volatility is About Risk — i.e., Price Movement Relative to Price Level

- A \$5 swing means different things for a \$10 stock vs a \$1000 stock.
- Risk should be measured **relative to the price**, which is exactly what returns capture.