# Regression



Linear Regression is a method used to find similarities between a dependent variable and 1 or more independent variable. The goal of linear regression model is to predict the dependent value by using the independent valeus. Some strengths of linear regression may include that is widely used and it can be used to understand relationships between objects. One weakness may include that it assumes a linear relationship but it may not be the case all the time.

```
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```

```
set.seed(3)
data <- read.csv(file = 'desktop/creditcard.csv')
dim(data)</pre>
```

```
[1] 284807 31
```

Hide

#### head(data)

<b>T</b> <dbl></dbl>		<b>V1</b> <dbl></dbl>	<b>V2</b> <dbl></dbl>	<b>V3</b> <dbl></dbl>	<b>V4</b> <dbl></dbl>	<b>V5</b> <dbl></dbl>	<b>V6</b> <dbl></dbl>	<b>V7</b> <dbl></dbl>
1	0	-1.3598071	-0.07278117	2.5363467	1.3781552	-0.33832077	0.46238778	0.23959855
2	0	1.1918571	0.26615071	0.1664801	0.4481541	0.06001765	-0.08236081	-0.07880298
3	1	-1.3583541	-1.34016307	1.7732093	0.3797796	-0.50319813	1.80049938	0.79146096
4	1	-0.9662717	-0.18522601	1.7929933	-0.8632913	-0.01030888	1.24720317	0.23760894
5	2	-1.1582331	0.87773675	1.5487178	0.4030339	-0.40719338	0.09592146	0.59294075
6	2	-0.4259659	0.96052304	1.1411093	-0.1682521	0.42098688	-0.02972755	0.47620095
6 rc	ws	1-9 of 31 colu	mns					

Add a new chunk by clicking the *Insert Chunk* button on the toolbar or by pressing Cmd+Option+I.

```
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```

```
set.seed(3)
i<-sample(1:nrow(data), nrow(data)*0.8, replace = FALSE)
train<-data[i,]
test<-data[-i,]</pre>
```

When you save the notebook, an HTML file containing the code and output will be saved alongside it (click the *Preview* button or press *Cmd+Shift+K* to preview the HTML file).

```
dim(train)
```

[1] 227845 31

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## head(train)

	Time <dbl></dbl>	<b>V1</b> <dbl></dbl>	<b>V2</b> <dbl></dbl>	<b>V3</b> <dbl></dbl>	<b>V4</b> <dbl></dbl>	<b>V5</b> <dbl></dbl>	<b>V6</b> <dbl></dbl>	
218087 1	41166	1.7933193	0.01984035	-1.9296190	1.34779239	0.5610834	-1.3402134	1.0
236218 1	48714	-0.8220090	0.72748442	-0.8316150	0.98524199	2.2795032	-0.5769322	0.9
229706 1	46020	2.0397723	0.61324571	-2.3616822	0.76673928	0.5995394	-1.7172058	0.3
83869	60061	-0.5231397	0.58988326	3.2996937	3.05804626	-0.4433193	1.5899776	-0.2
197613 1	32097	1.8249885	-0.68401799	-0.7133819	0.09200484	-0.3199603	0.1725305	-0.4
268264 1	63135	-0.2646561	1.00158569	-1.1063368	-1.25530667	1.5773387	-0.5076532	1.6
6 rows   1-	9 of 31 o	columns						

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#### names(train)

[1] "Time"	"V1"	"V2"	"V3"	"V4"	"V5"	"V6"
[8] "V7"	"V8"	"V9"	"V10"	"V11"	"V12"	"V13"
[15] "V14"	"V15"	"V16"	"V17"	"V18"	"V19"	"V20"
[22] "V21"	"V22"	"V23"	"V24"	"V25"	"V26"	"V27"
[29] "V28"	"Amount	" "Class"				

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### colSums(is.na(train))

Time	V1	V2	V3	V4	V5	V6	V7	V8	V9	
0	0	0	0	0	0	0	0	0	0	
V10	V11	V12	V13	V14	V15	V16	V17	V18	V19	
0	0	0	0	0	0	0	0	0	0	
V20	V21	V22	V23	V24	V25	V26	V27	V28	Amount	
0	0	0	0	0	0	0	0	0	0	
Class										
0										

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str(train)

```
'data.frame':
                227845 obs. of 31 variables:
                141166 148714 146020 60061 132097 ...
$ Time
        : num
$ V1
         : num
                1.793 -0.822 2.04 -0.523 1.825 ...
$ V2
                0.0198 \ 0.7275 \ 0.6132 \ 0.5899 \ -0.684 \ \dots
         : num
$ V3
                -1.93 - 0.832 - 2.362 3.3 - 0.713 ...
         : num
                1.348 0.985 0.767 3.058 0.092 ...
$ V4
         : num
                0.561 2.28 0.6 -0.443 -0.32 ...
$ V5
         : num
                -1.34 -0.577 -1.717 1.59 0.173 ...
$ V6
         : num
                1.081 0.938 0.392 -0.201 -0.491 ...
$ V7
         : num
                -0.619 -0.118 -0.411 0.362 0.133 ...
$ V8
         : num
                -0.356 -0.25 0.439 -0.294 0.779 ...
$ V9
         : num
$ V10
                0.267 0.222 -1.221 0.575 0.123 ...
         : num
$ V11
                -0.4948 0.4926 0.3239 0.0458 0.5658 ...
         : num
$ V12
         : num
                0.8447 -0.9152 0.0279 0.3468 0.8999 ...
$ V13
                1.1326 -2.2665 0.4242 -0.3725 0.0711 ...
        : num
$ V14
        : num
                0.604 - 0.742 - 2.618 - 0.885 0.137 ...
                0.1103 -0.487 1.0684 -1.4965 -0.0971 ...
$ V15
         : num
                -0.512 -0.397 0.692 -0.442 0.758 ...
$ V16
         : num
               -0.448 0.94 1.8 0.255 -0.902 ...
$ V17
        : num
$ V18
        : num
                -0.635 1.131 1.126 0.572 0.174 ...
                -0.509 0.996 -0.773 1.813 0.379 ...
$ V19
         : num
                0.0696 0.1527 -0.1313 0.272 0.041 ...
$ V20
        : num
$ V21
                0.2258 -0.0806 0.1085 -0.0874 -0.188 ...
        : num
                0.519 0.237 0.546 0.209 -0.718 ...
$ V22
        : num
               -0.1445 - 0.4062 - 0.0462 - 0.2926 0.3409 \dots
$ V23
        : num
$ V24
                0.0275 0.1415 -0.2154 0.0288 0.3405 ...
        : num
               0.4489 0.0203 0.2581 0.0884 -0.6436 ...
$ V25
        : num
$ V26
        : num
               -0.5 -0.413 -0.099 0.294 0.193 ...
                -0.0471 0.4572 0.0262 -0.0263 -0.066 ...
$ V27
         : num
               -0.03701 0.09948 0.00825 -0.13511 -0.03495 ...
$ V28
         : num
$ Amount: num
               144 21 1 29 98 ...
$ Class : int
               0 0 0 0 0 0 0 0 0 0 ...
```

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```
install.packages("vioplot")
```

```
The downloaded binary packages are in /var/folders/fx/fht6tvb95xldy2488rl0ctj00000gn/T//RtmpNP8aNE/downloaded_packages
```

```
library("vioplot")
```

```
Loading required package: sm
Package 'sm', version 2.2-5.7: type help(sm) for summary information
Loading required package: zoo

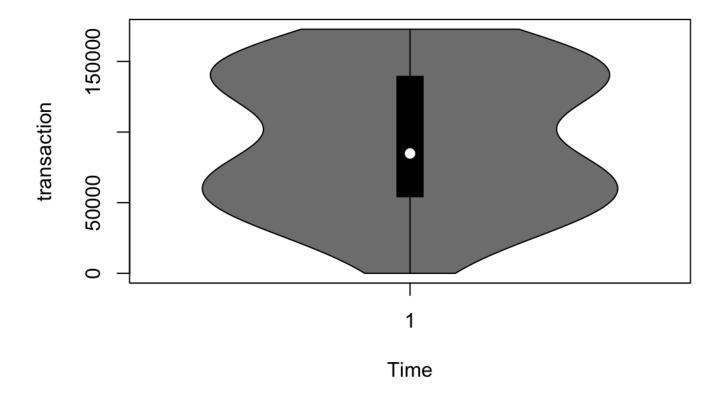
Attaching package: 'zoo'

The following objects are masked from 'package:base':

as.Date, as.Date.numeric
```

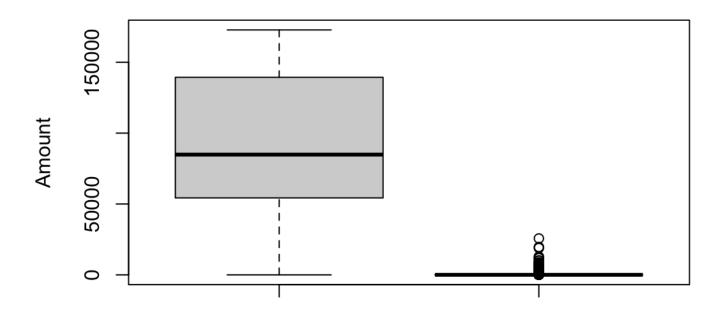
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vioplot(train\$Time, xlab = "Time", ylab = "transaction")



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boxplot(train\$Time, train\$Amount, xlab="Time", ylab = "Amount")



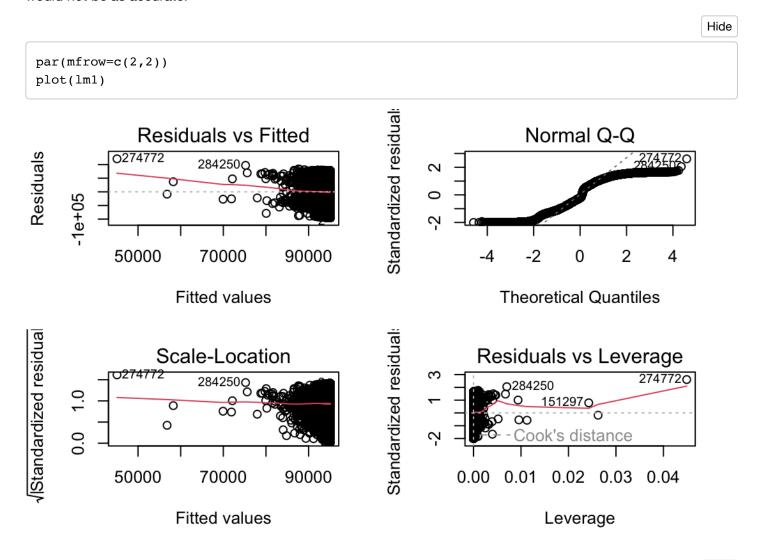
## Time

```
lm1<-lm(Time~Amount, data = train)
summary(lm1)</pre>
```

```
Call:
lm(formula = Time ~ Amount, data = train)
Residuals:
           1Q Median
                         3Q
-95058 -40574 -10074 44482 121125
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 95062.9008
                         105.3560 902.302 < 2e-16 ***
Amount
               -1.9458
                           0.3929
                                  -4.952 7.35e-07 ***
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 47480 on 227843 degrees of freedom
Multiple R-squared: 0.0001076, Adjusted R-squared: 0.0001032
F-statistic: 24.52 on 1 and 227843 DF, p-value: 7.352e-07
```

From this summary we can learn that the p value is extremely small which represents that there is a trong relationship between time and amount. the multiple R squared value is very low which suggests that the model explains very little of the variance of time. the residual standard error is high which indicates that the prediction

would not be as accurate.

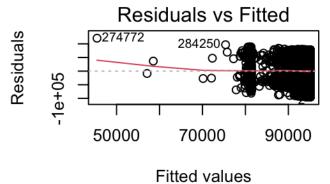


Hide

lm2<-lm(Time~Amount+Class, data = train)
summary(lm2)</pre>

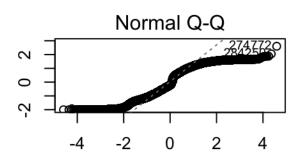
```
Call:
lm(formula = Time ~ Amount + Class, data = train)
Residuals:
  Min
           10 Median
                         3Q
                               Max
-95081 -40570 -10082
                      44481 120752
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                        1.054e+02 901.939
             9.509e+04
                                   -4.918 8.77e-07 ***
Amount
            -1.932e+00
                        3.929e-01
Class
            -1.374e+04
                        2.355e+03
                                   -5.835 5.39e-09 ***
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Residual standard error: 47470 on 227842 degrees of freedom
Multiple R-squared: 0.000257, Adjusted R-squared:
F-statistic: 29.29 on 2 and 227842 DF, p-value: 1.918e-13
```

par(mfrow=c(2,2))
plot(lm2)

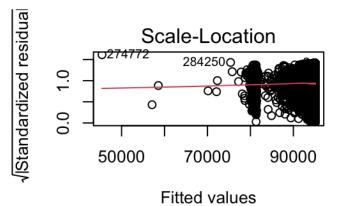


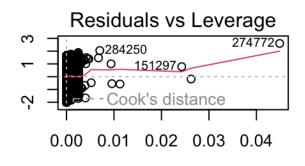


Standardized residual:



Theoretical Quantiles





Leverage

Hide

```
lm3<-lm(Time ~ Time+Amount+Class, data = train)</pre>
```

Warning: the response appeared on the right-hand side and was droppedWarning: problem with term 1 in model.matrix: no columns are assigned

Hide

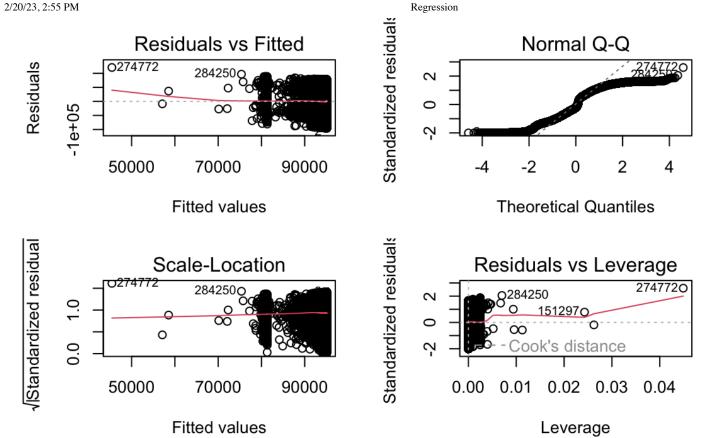
```
summary(1m3)
```

```
Call:
lm(formula = Time ~ Time + Amount + Class, data = train)
Residuals:
  Min
          1Q Median
                         3Q
                              Max
-95081 -40570 -10082 44481 120752
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 9.509e+04 1.054e+02 901.939 < 2e-16 ***
Amount
           -1.932e+00 3.929e-01 -4.918 8.77e-07 ***
Class
           -1.374e+04 2.355e+03 -5.835 5.39e-09 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 47470 on 227842 degrees of freedom
Multiple R-squared: 0.000257, Adjusted R-squared: 0.0002482
F-statistic: 29.29 on 2 and 227842 DF, p-value: 1.918e-13
```

Hide

```
par(mfrow=c(2,2))
plot(lm3)
```

Warning: the response appeared on the right-hand side and was droppedWarning: problem with term 1 in model.matrix: no columns are assigned



```
pred1<-predict(lm1, newdata = test)</pre>
cor1 <- cor(pred1, test$Time)</pre>
mse1 <- mean ((pred1-test$Time)^1)</pre>
rmse1 <-sqrt(mse1)</pre>
print(paste('correlation: ',cor1))
[1] "correlation: 0.0115679423668671"
                                                                                               Hide
print(paste('mse: ',mse1))
[1] "mse: 385.643485196248"
                                                                                               Hide
print(paste('rmse: ',rmse1))
[1] "rmse: 19.6378075455548"
                                                                                               Hide
pred2<-predict(lm2, newdata = test)</pre>
cor2 <- cor(pred2, test$Time)</pre>
mse2 <- mean ((pred2-test$Time)^2)</pre>
rmse2 <-sqrt(mse2)</pre>
print(paste('correlation: ',cor2))
[1] "correlation: 0.0170486625902318"
                                                                                               Hide
print(paste('mse: ',mse2))
[1] "mse:
           2257396538.92481"
                                                                                               Hide
print(paste('rmse: ',rmse2))
[1] "rmse: 47512.0672979488"
                                                                                               Hide
pred3<-predict(lm3, newdata = test)</pre>
```

```
Warning: prediction from a rank-deficient fit may be misleading

Hide

cor3 <- cor(pred3, test$Time)
mse3 <- mean ((pred3-test$Time)^2)
rmse3 <-sqrt(mse3)
print(paste('correlation: ',cor3))

[1] "correlation: 0.0170486625902318"

Hide

print(paste('mse: ',mse3))

[1] "mse: 2257396538.92481"

Hide

print(paste('rmse: ',rmse3))

[1] "rmse: 47512.0672979488"
```

Output: Fromt the correlation, mse and rmse we notice that the first linear regression model is the best one. We see that because of the low mse and rmse of the the first one compared to the other two. this may happen because the variables in the second and third models may not connect with the prediction. They divert the data in some other way.