Introduction to Data Structure

* Data is basically a fact or entity.

Data are now facts whereas information is processed data.

* Data refers to value or set of values e.g: - Marks Obtained by the students

* Data can be classified into two types numerical data and alphanumerical data. These two data types sperify the nature of the data items and it is used certain operations. The numerical data type can be any numers with decimal or without decimal poent, for example, integens (10,20,30) and floating point numbers (10.25, 16.5 etc) The alphanumerical data can be single character or group of characters, for example chalacter constants ('A', B', c', etc) and streng constants ("Semon", "Aren", "Arjun" etc)

when a programmer reads any one such type of data for processing, first we need to store into computer memory. The process of storing data elements ento computer memory is called data representation. To process this data, date must be organized in a particular fashion. An Organization means structuring of data.

Data structure - Definiteos

Data Structure deals with the study of how data is organized in the Computer's memory and how it maintains logical relationship between individual elements of data and also, how efficiently the data can be refoleved and manipulated

A date structure is a Systamatic way of storing data in a computer memory and the associated method for retrieving the

Data Blucture - classification Data structure is broadly classified into two categories.

- Strectures 1. primitive data data structures 2. Non-primitive [ADT]
- * Primitère data structures.

There dates Structerres are basec Spectures and are manipulated/operated directly by machine instructions.

The integers, floating-point numbers, characte Constants, String constants etc are some of Constants, String constants etc are some of the primitive data structures. In a language, the primitive data structures are defined these primitive data types such as int, float, their using data types such as int, float, their and double. Representations of these primitive and double. Representations of these primitive data types are already specified in the data types are already specified in the

Abeteart Data types [ADT] or Non-primitive

Data types

Data types

An abetrail data type (ADT) is a

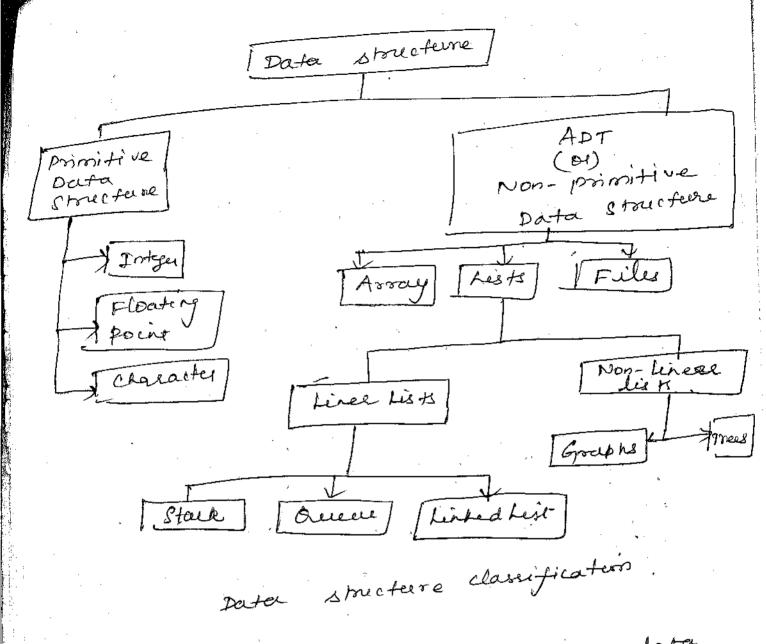
Specification of a data type in a formal

specification of a data type in a formal

way without regard to any particular

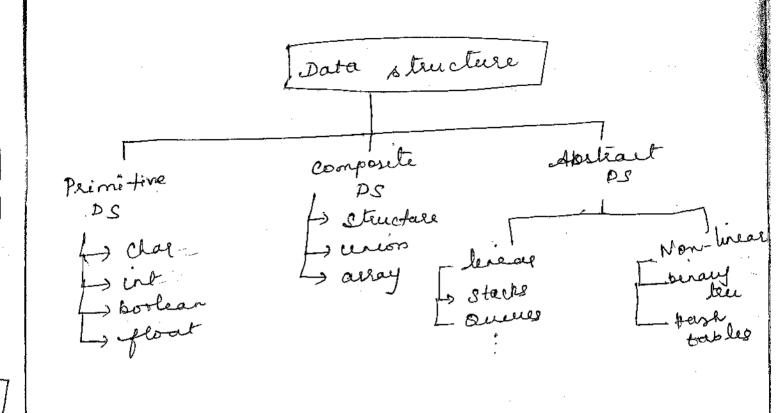
complementation or programming language.

date types where a data type is defined by its behavior (semantics) from the point of view of a user of the data, specifically in terms of possible values, possible in terms of possible values, possible operations on data of this type, and the operations of these operations.



Our ain is study the ADT data structures and its operations. Each data structure categorized into different chapters. Each chapter contains data structure 's description, operatione, display of data Structures contents with examples using

c larguage.

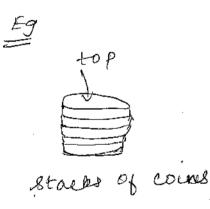


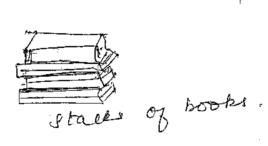
A Stack is an ordered list in which insertions (also called props (also called pushes & adds) and deleterine (also called props and removes) are made at one end called the top.

Stacks

A stack is a linear list in which all additions and deletions are restricted to one end, called the top. If you insert a data series into a stack and then remove it, the order of the data is revensed.

Data input as \$5,10,15,20% is removed as \$20,15,10,5%. This reversing attribute is why stacks are known as the last in-first self-[LIFO] data steachers.





Definition

A stack is a last in-first out (LIFO)

A stack is a last in-first out (LIFO)

data structure in which all insertions

and deletions are restricted to one and,

called the top.

as when you visit a website and browse through the links, a stack of visited pages through the links, a stack of visited page is stored by the browser when you press the backbutton test most recently visited page the backbutton test most recently visited page.

Basic Stack Operations

The three basic stack operations are

* push

* POP

* Stack top

* push operation

The stack. It adds an item at the top of the stack. After the push, the new item becomes the top.

Simple operation is that we must ensure simple operation is that we must ensure that there is room for the new item. If there is not enough room, the stack is in as overflow state and the item cannot be added.

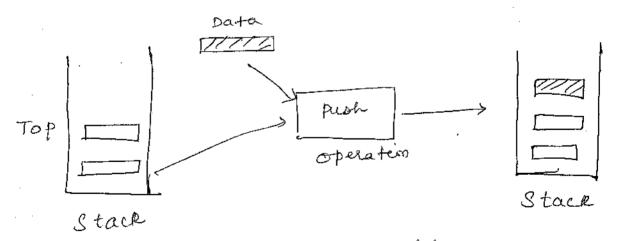


Fig: Push operation

Pop Operation /

when we pop a stack, we remove the item at the top of the stack and return the item at the ver. Because we have removed the it to the user. Because we have removed the top item, the next older item in the stack top item, the next older item in the becomes the top. when the last item in the stack is alleke, the stack must be set to stack is empty state. It pop is called when the stack is empty, it is in an underflow stack is empty, it is in an underflow stack is

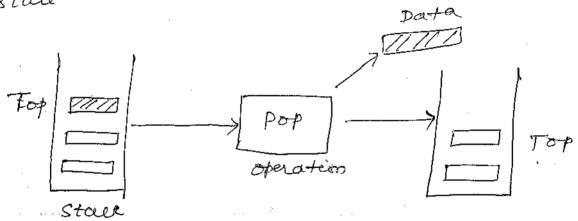


Fig: Pop Stack operation

Stack TOP

The third stack operation is stack top.

Stack top copies the item at the top of the

Stack, that is, it returns the data in the

Stack, that is, it returns the data in the

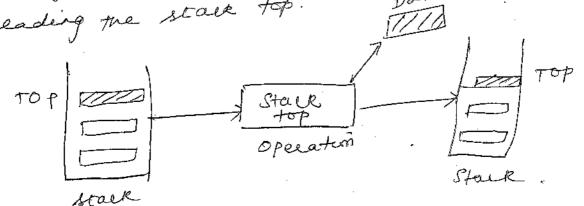
top element to the user but does not allele

top element to the user but does not allele

it. you might thenk of this operation as

it. you might thenk of this operation as

heading the stack top.



Implementation of stack using array # is clude < stdio. h> # include < conio.h> # deferie max 100 int. Stack [max], top 29; top = -1; void main () drscr(); do Printf ("\n Stack"); Printf ("In 1. push In 2. pop In 3. Display h"); Printf ("In A. Exit"); Print ("In Enter Hour choice:"); Scarf (" 7. d", &ch); Switch (ch) case 1: push (); Break; case 2 : Pop (); break,

```
case 3: display()
                     break.
            Case 4: exit();
                     Printf ( "In Enser a Valid chois)
  3 while (1);
     push()
Void
    if Ctop==max+1
      Print ["In overflow"]
   Olse
      int element;
       print ["Enter 2 lement: \n");
       Scanf ("1.d", & element);
       Printf [" \n Slement (1.d) has been pushed
                     at '/.d", element, top);
        Stack [top] = element
```

```
void pop ()
      ·4 (+01 == -1)
       paintf ("underflow (n");
         Prints ("Element has been popped out!")
   void display ()
       if (top = = = 1)
           Paintf ("Stack is Empty!!");
for(i=top; i>20; i-).
         20) ( for (i=0; i =0; i++)
               paints ("1.d", steur [i]);
   Stacks structures are usually implemented
    using arrays or linked list
```

Stack Applications

Stack applications can be classified into four broad categories

- 1) reversing data
- 2) Parsing data -> unmatched parentheses used in compiler.

-> 3) Postponing data Usage infix to

transformation 4) backtracking slips : > computer Gaming and evaluation decision analysis and expect eyelong

The following applications are discussed & is detail

> * Recurren > Sum of n members factorial of given number > Fibonacci Series

- GCD -> Tower of Hanoi

Conversion and evaluation of infix, prefix and postfix

Lecursion

In general, there are two approaches to waiting repetitive algorithme one uses iteration and other user recursion

definition

Recursion is a repetitive product in which an algorithm calls itself.

- * Sometimes, the best way to solve a problem is by solving a smaller version of the exact same problem first.
- * Receives en à a technique that solves a problem problem by solving a smaller problem of the Same type
- * A procedure that is defined in terms of itself.
 - * In secursein approach the function calls elself until the condition is roset. It is elself until the condition is roset. Il slower than elevation, which means it use more menory than iteration.
 - A Reculsion makes Code Smaller and clean.

Recursion and Stacks

- + Most compilers implement recursion using stacks
 - * when a method is called the compiler pushes the arguments to the method and the Return address on the stack and the Return address on the beather and then transfers the control to the method and then transfers the control to the method
- * when the method returns, it pops these Values Off the stack.
- * The arguments disappear and the control geturns to the return address.

```
Main Memony

Void main ()

furt a, b, c;

float x;

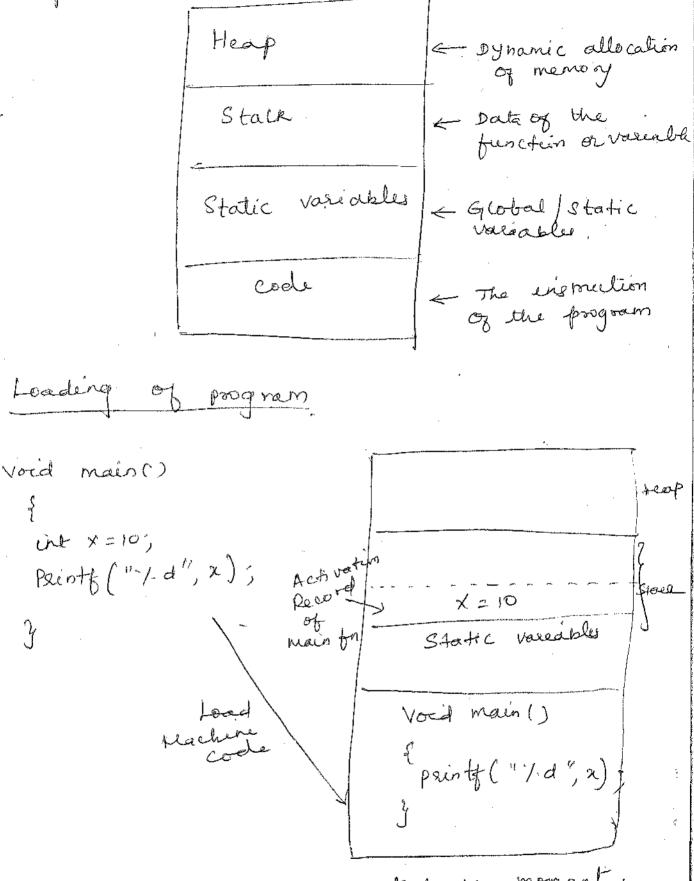
Data

Chae c;

Printf ("Enter 3 numbers");

Scanf ("1-d 1-d 1/d", 2a, 2b, 4c);

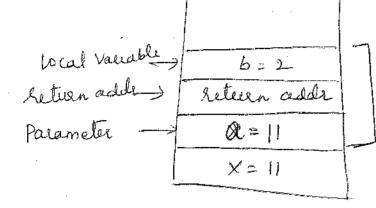
Instruction
```



Activation Record is created the moment. The function is called For every function activation record is created.

Function call [Stack Usage in function call] void main () int x = 10; X++; A(x); Functioncall Void A (int a) f int b = 2; g Prints ("/d",a); -> when main function is called, the local Variable X is pushed into a stack. $\times = 1$ -> when main function calls function A, the following operations will be performed. * Push Palameters required by function * return address of main function

* local variables of function A



Stack frame of function A.

Once function A completes its task, task, it returns the control back to the it returns the control back to the called function. This is a complised by called function the obtain return address pop the items tell to obtain return address done by function A. Once the control is done by function A. Once the control is returned, the main function will clean returned, the main function (A).

```
Factorial of given number
          The factorial of a positive number
is the product of the integral values from
1 to . The number :
         Factorial algorithm can be defined
recursively as
  Factorial (n) =
                 nx(Factorial(n-1)) 4 n>0
                The factorial algorithm call itself seach time with different set of
  Algorithm
                                       -parameters *
     Factorial (n)
     1 if (n==0)
       2 Seturn 1;
      3 else
       return (nx Factorial (n-1))
      z
                                   Factorial(3) = 3 x 2 = 6
  Factorial(3) = 3 * Factorial(2)
                                   Factorial(2)=2×1=
  Factorial(2) = 2 * Factorial(1)
                                   Factorial (1) = 1 *1 =
  Factorial (1) = 1 * Factorial (0)
```

Factorial(0) = 1

Recursive solution for a problem involves a two way journey, first we decompose the problem from the top to the bottom, then we solve it from the bottom to the top

Stack Usage in Lecursive function

** Factorial(s) -> factorial(s

Parante value will be.

GICD -> Greatest Common Divesor Detween two non negative integers. The recursive definition of GCD is $gcd(a,b) = \begin{cases} a & \text{if } b = 0 \\ b & \text{if } a = 0 \end{cases}$ $gcd(b, a \mod b) \text{ otherwise}$ Alapoeithm int gcd (int a, int b) { | if (b == 0) 2 return a, 34 (a==0) 4 return b; 5 seturn gcd (b, a%b); 9(4/10,25)

24(5,0)-4

Fibonacei Numbers

In Fibonacii series, each number is, the sum of the previous 2 numbers.

0,1,1,2,3,5,8,13,21,2*

To start a fibonacei series, we need to know the first 2 numbers.

Recursève definétion of Fiboracci numbers is

Fibonacci
$$(n) = \begin{cases} 0 & \text{if } n = 0 \\ \text{if } n = 1 \end{cases}$$

Fibonacci $(n-1)$ + Fibonacci $(n-2)$ o therwise

Algorithm

long fib (log long num)

if (m===0 |) num===1)

return (fib(n-1) + fib(n-2));

9

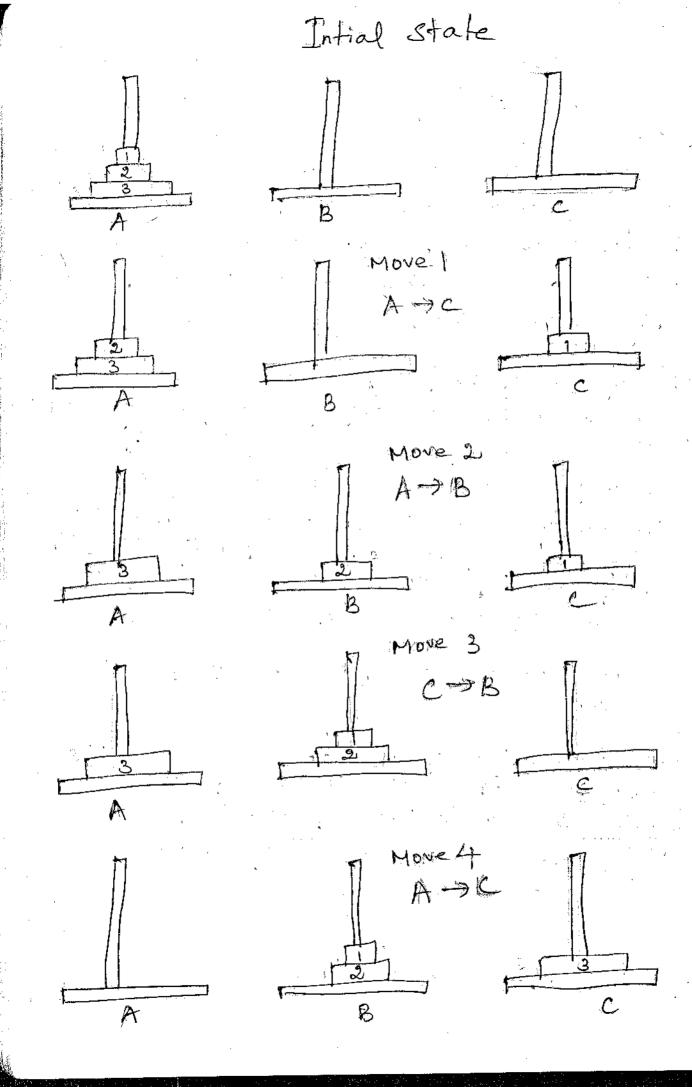
Tower of Hanoi

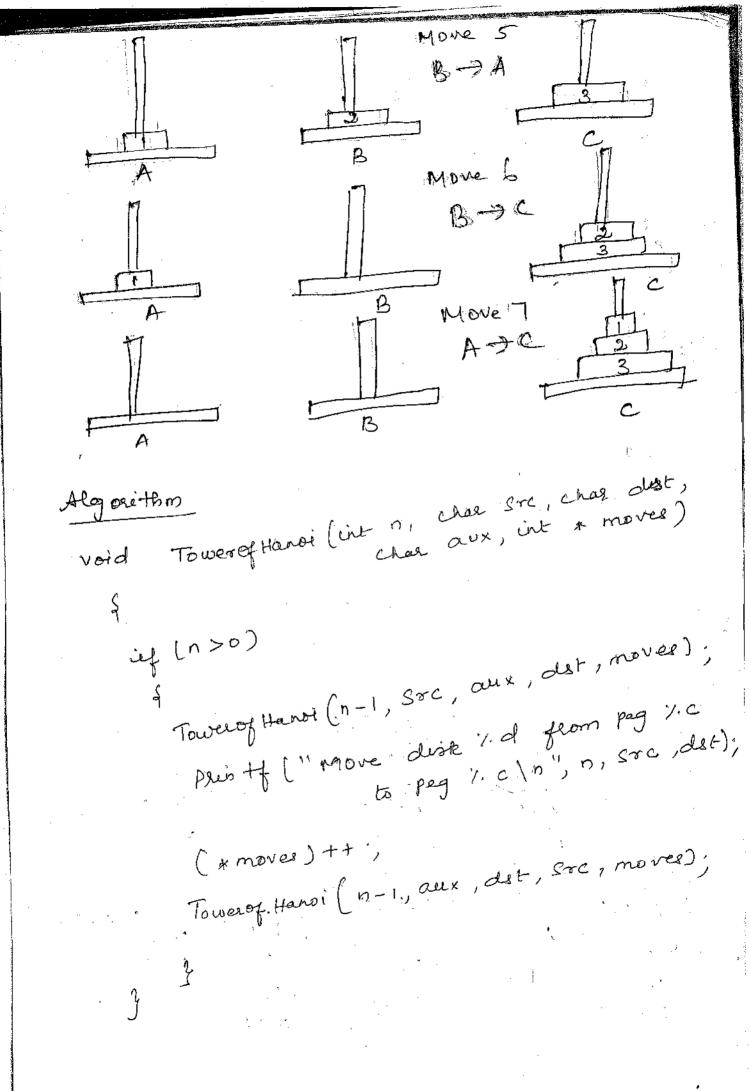
The Tower of Hanoi is a mathematical game or puzzle. It consists of three rods, and a number of disks of different sizes where can slide ends onto any rod. The puzzle starts with the disks in a neat stack in ascending order of size on one rod, the smallest at the top, thus making a conical shape.

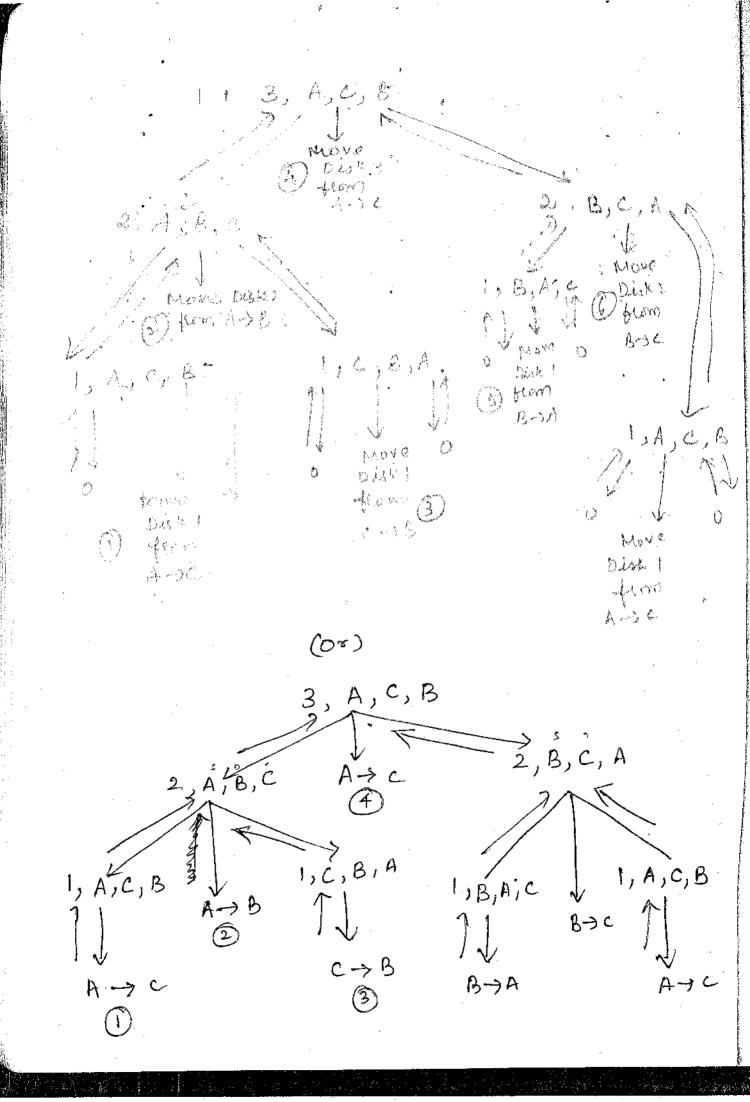
the objective of the puzzle is to move the entire Stack to another rad, obeying the following simple rules.

- 1. Only one disk can be moved at a time
- of another stacks and placing it on top of another stacks. (i.e) a disk can only be moved if it is the uppermost disk on a stack.
- 3. No disk may be placed on Top of a smaller disk

with three disks, the puzzle, can be solved in seven moves. The minimum number of moves hequired to solve a Tower of Hanoi puzzle is hequired to solve a Tower of Hanoi puzzle is 2^n-1 , where n is the number of disks.







numbers Sum of n Algorithm int gersum (n) Static int sum=0; if (n>0) Sum = sum +n; get-Sum (n-1); getuen seem; 5-6 g. H. 3 + 2 + 1

Postponment

Often the logic of an application

often the logic of an application

hequires that the Usage of data be deferred

until some later point. A stack can be

until some later point hequires that

useful when the capplication requires that

useful when the posponed for a while

the use of clata be posponed for a while

Consider the Sum of A and B.

we think of applying the operation" + " to

be operands A and B and write the

Sum as A+B. This particular representation

is called infix.

There are two alternate notations for expressing the Sum of A and B using the Symbols A, B and t. These are the Symbols A, B and t. These are

+ AB prefix
AB + post fix

The prefixes "pre-", "post-," and "in-"
refer to the relative possition of the
operator with respect to the two operands.

To prefix notation the operator precedes

The two operands, in post-fix notation the
operator the teoo operands and
operator the teoo operands and
operator the operator is between
in frintix notation the operator is between
the two operands.

Conversion of infine to postfix

one of the disadvantages of the infox notation is that we need to use parentheses to control the evaluation of the parentheses to control the evaluation of the operators we thus have an evaluation operators we thus have an evaluation method that includes parentheses and two operator priority classes.

In the postfix and prefix notatione, we do not need parentheses, each provides only one evaluation rule.

Although Some high-level languages carnot use infix notation, such expressions carnot be directly evaluated. Rather, they must be be directly evaluated. Rather, they must be analyzed to defermine the order in which analyzed to defermine the evaluated. A common the expression are to be evaluated. A common evaluateon technique is to convert the expression evaluateon technique is to convert the expression to post fix notation before generating the code to evaluate them.

Rules for Converting infix to Postfix expression

- 1. Fully parenthesix the expression using any explicit parentheses and the acithmetic precedence multiply and divide before add and subtract.
- 2. change all infix notations in each parenthesis to postfix notation, starting from the innermose-expression. Conversion to postfix notation is done by moving the operator to the location of the by moving the operator to the location of the expression's closing parenthesis.
- 3. Remove all Parentheses.

وم ا

A+R+C

Step 1

(A+(B*c))

Step 2

(A+ (Bc*))

(A(BC*)+)

S-lep3

ABC*+

Step 1

Step2

Step 3

AB+C*D+CF*+G-

493

Step

Sly2

Step3

[AVERGED] ((A+4) - (c+5)) Cally) ((AB+) A (+D+)) ((AR) ((1))+) ABHCDYA 25 [(A+B) * C - D * F + C) ale i ((((A+B) *c) - (B*F))+c) 240 ((((AB+)C+)-(DF+))+c) (((((AB+)C+),(Dr+)-)C+) About the second M.

Algorithms Steps to convert infix to Postfix

- 1. Print operands as they arrive.
- If the stack is empty or contains a left parenthesis on top, push the incoming left parenthesis on top. operator onto the stack
- It the incoming symbol is left parenthesis, push it on the stack.
- 4. If the incoming symbol is right parentsesis, pop the stack and print the operators until you see a left parentsesie.

[Discard the pair of parentherses]

- If the incoming Symbol has higher proceedence than the top of the start, push it on the
 - If the incoming symbol has aqual procedures.

 With the top of the stace, Use association. It the association is left to right, pop and print the top of the stack and then push the incoming operator. It the association is sight to left, fush the
- If the incoming symbol has Lower precedence than the symbol on the top of the stack, pop the stack and print the top operator. Then test the incoming operators against the new top of stack.

8. At the end of the expression, pop and paint all operators on the Stack (No parentheses Should remain)

Algorithm inTo Post Fix (formula)

CreateStair (Stack)

Loop (for each character in formula)

if (Character is open parenthesis)

Push Stair (Stack, character)

elseif (character is close parenthesis)

popStack (Stack, character)

Loop (character not open parenthesis)

concatenate character to post-Fix Expr

popStair (Stair, character)

end Loop

elseif (character is operator)

StackTop (Stack, topToken)

Loop (not emplyStack (Stack)

AND Priority (character) (= priority (topToken))

PopStack (Stack, tokenout)

Concatenate tokenOut to PostFixExpr

StackTop (Stack, topToken)

endloop

PushStack (Stack, token)

else

Concatenate token to Post Fix Expr end loop end loop loop (not emptyStace (Stace)) popStace (Stace) popStace (Stace) concatenate token to post Fix Expr

end loop
return postfix
end in To Post-Fix

	Stack	-postfix
inji x	Comments of the Comments of th	
A+B+C-D/E		A
+ B * C = D/E		A-
B * c - p/E		
* C - D/E		A B
C - D/C		A 2
- 2/6	and the second	ABC
D/E	The state of the s	ABCX+
f(x)		Abothila

the reasonable and the reasonable are a second	
292	
(A+B)+C-D+F+C	
MARINE DATHE	
A+B)*C-D*F1C	· ·
10)+0-10+0-1	A
b) & c _ D & f _ C	A B
) x c - D x F + < []	ABT
* C - D*F1C (*)	ABH
C-Dyrac / #	AB+C

PX F+C AB+C+ D* F+C L- ABAC*D * FIC (*) ARHOND Pic la Abarrabe ACHORDER Con file to the contract

Evaluation Postfix expression

A.C.

In the postfix expression, the operands come before the operators. This means that we will have to postpone the Use of the we will this time, not the operators. We operands this time, not the steek when we therefore put them into the steek when we find the operator, we pop the two operands find the operator, we pop the two operands at the top of the steek and perform the at the top of the steek and perform the operation. We then push the value back operation. We then push the value back of the stack to be used between into the stack of the stack to be used between the stack of the st

when the empression has been completely who should be in the

Algorithm

post Fix Evaluate (expr) Algeri thm create Stack (stack) loop (for each character) if (character is operand) push Stack (Stack, Character) elee PopStack (Stack, oper 2) PopStack (Stack, open) operator = character Set value to calculate (oper 1, operator, oper2) pushSteek (stack, value) endif end loop popStack (Stack, result) return (result) pose Fix Evaluate

Recursión

- I Recursive function is a cfunction that is partially defined by itself
- 2) Recursión uses Selection Structure
- 3) Infinite recursion occurs if the recursion occurs if the recursion step does not reduce step does not reduce the publish in a manner the publisher in a manner that converges on some that converges on some condition) Condition (base condition)
- 4) Recursion terminates when abase case is openized
- 5) Recurring le Usually Slower than Eteration due to overhead of maintaing stack

i toeration

Iterative instructions of Loop based repetitions of a process.

Iteration uses repetition Structure.

An infinite loop occurs with l'teration if the with loop-condition test never becomes false.

Iteration terminates when the loop undition fails.

Iteration close not use Hack so it is faster than recursion.

- b) Recursion Uses more memory than iltration
- 7) Infinite recursion can crash the Eystern
 - 8) Recursión makes code Smaller

I teration concurre less

infinite looping uses cov cycles nepeatedly.

Ilaration makers code Longer.