

DATA STRUCTURES

classmate

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1. Data Structure refers to the process of placing data in an organized manner on primary memory.
2. Data Base means the process of storing the data in an organized manner on Secondary memory.

⇒ Data Structures:

1. Hold the data
2. Imposes certain restriction.
3. Users Benefits from restrictions

⇒ Types:

1. Foundational Datastructures:

- * Arrays
- * Linked Lists

2. Derived Datastructures:

- * Stack
- * Queue
- * Tree
- * Graph
- * Set
- * Dictionary
- * Map.

→ STACK:

1. Restrictions imposed by the stack:
 - * Last-In First Out [LIFO]
 - * First-In Last Out [FILO]
- * PUSH: process of putting the data into the stack
- * POP: process of removing the data from the stack

→ QUEUE:

1. Restrictions imposed by the Queue:
 - * Last-In Last Out [LIFO]
 - * First-In First Out [FIFO]
- int p; // p is an integer.
- int p[5]; // p is an Array of 5 integers
- int *p; // p is a pointer to an integer.
- int **p; // p is a pointer to pointer to an integer.
- int *p[5]; // p is an Array of 5 pointers to integer
- int (*p)[5]; // p is a pointer to an Array of 5 integers
- int *(*p)[5]; // p is a pointer to an Array of 5 pointers to integer.

→ Pointer: mechanism gives us an alternative way to access the contents of memory location.

* Data can be accessed in two ways :

- 1 Direct method (Using the variable Name).
- 2 Indirect method (Using pointers).

→ '*' in C language is used for 3 purposes:

1. Used to declare a pointer variable
2. Used for multiplication purpose
3. Used to penetrate or Dereference a pointer

→ Unstructured style:

```
#include <stdio.h>
void main()
{
    int a,b,c;
    clrscr();
    printf("Hey there!");
    getch();
}
```

→ Structured style:

```
#include <stdio.h>

void getch(); // Function prototype
void main()
{
```

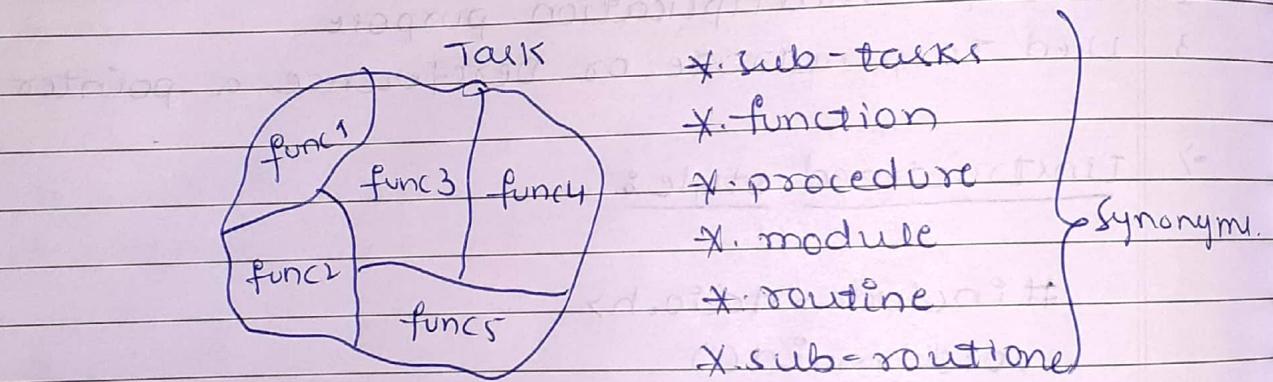
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desc();
greet(); // Function call or function signature
getch();
}
```

```
void greet()
{
    printf("Hey there!");
}
```

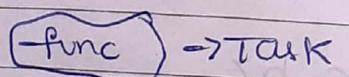
} Function Body.

→ when to use structured programming style:



- * complex & huge task.
- * Division of labour. also called as dividing the task among different teams or members.
- * Structured programming is also called as Procedure Oriented programming language.

→ when to use Unstructured style:



- * Simple & small task.
- * No division of labour is involved, a single fellow can write a function & complete the task.
- * Also called as Unstructured programming style.

→ STACK: is a linear datastructure, in which insertion and deletion of elements is performed from only one end called top of the stack. It works on the principle of LIFO or FILO.

* Applications / uses of STACK:

1. To convert infix expression to postfix or prefix form.
2. To evaluate a postfix or infix expression.
3. Balancing of parenthesis.
4. palindrome
5. Reverse a string
6. sort
7. Recursion.
8. convert decimal to Binary.

→ Arrays Vs STACK:

Arrays

stacks

- | | |
|---------------------|--------------------------|
| 1. can hold data | 1. can holds data. |
| 2. Random insertion | 2. orderly insertion. |
| 3. Random deletion. | 3. LIFO / FILO deletion. |

→ STACK creation:

* push method : [Pseudocode] :

```
void push()
```

```
{
```

```
if (stack is full)
```

```
P/f "push not possible";
```

4	
3	
2	
1	
0	

-top = -1

S

```
else  
{
```

Ask for the item to be pushed.

collect the item

increment top

$s[\text{top}] = \text{item};$

```
}
```

```
}
```

* conditions:

1. stack empty : if ($\text{top} == -1$)

2. stack full : if ($\text{top} == \text{SIZE} - 1$).

* push - method : [c code snippet]

```
void push()
```

```
{
```

```
int item;
```

```
if ( $\text{top} == \text{SIZE} - 1$ )
```

```
printf (" PUSH operation NOT possible.");
```

```
else
```

```
{
```

```
printf ("In Enter the item to be pushed : ");
```

```
scanf ("%d", &item);
```

```
++top;
```

```
 $s[\text{top}] = \text{item};$ 
```

```
}
```

```
}
```

* push() insures orderly insertion.

* Pop method : [pseudocode]

```
void pop()
{
    if (stack is empty)
        printf "POP Not possible";
    else
    {
        pop the element at top of stack;
        decrement top
    }
}
```

* conditions :

1. stack empty : if ($\text{top} \leq -1$)

* pop method : [c code snippet]:

```
void pop()
{
    if ( $\text{top} \leq -1$ )
        printf ("POP Not possible");
    else
    {
        printf ("Element popped is %d", s[top]);
        --top;
    }
}
```

* Display method : [pseudocode]

```
void display()
{
    if (stack is empty)
        printf ("Display not possible");
    else
        print all the elements present in the stack.
```

* C code Snippet:

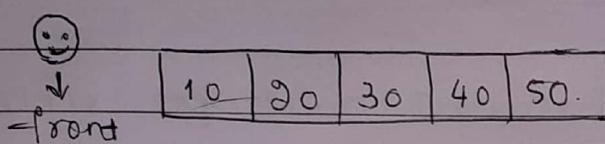
```
void display()
{
    int i;
    if (top == -1)
        printf ("Display not possible");
    else
    {
        for (i = 0; i <= top; i++)
            printf ("%d\n", s[i]);
    }
}
```

→ Implementing stack Using Local variables :

1. Make the global variables as local to main().
2. Pass the parameters from main to the other functions.
3. The other functions must collect the incoming data.
4. If any changes are made to the incoming data then the return statement must be used.
5. Main has to collect the info back from the function.

→ Implementing STACK in OOP:

→ Queue: First-In First-out. or
Last-In Last-out



→ Application / Uses of Queues:

→ Arrays

Queues

- * can holds data
- * Random Insertion
- * Random Deletion
- * Insertion : at rear end { rear = -1 }
- * Deletion : at front end { front = 0 }

→ Insert() : [pseudocode]

void insert()

{

if (queue is full)

print "Inseriton not possible";

else {

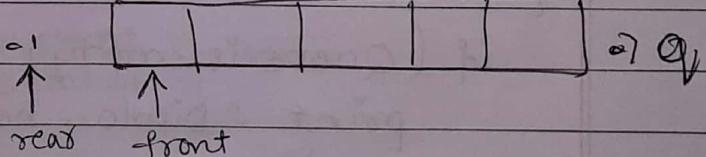
Ask for the item to be inserted.

Collect the item

Increment rear

place item at q [rear]

}



⇒ conditions:

1. Queue full: $\text{rear} == \text{size} - 1$,
2. Queue Empty: $\text{front} > \text{rear}$.

⇒ delete(): [pseudocode]

void delete()

{

if (Queue is Empty)

print "Deletion not possible";

else

{

 Delete the element at the front of queue
 make the next element as the new front
 (By incrementing front).

}

};

⇒ display(): [pseudocode]

void display()

{

if (Queue is empty)

print "Display not possible";

else

 print all elements from front to rear;

};

→ Applications of STACK:

* prefix expression: Invented in 1924 by a poland, initially this notation is called as polish notation.

ex: +ab .

* postfix expression: invented in 1954, also called as Reverse polish notation.

ex: ab+ .

→ steps for evaluating an prefix expression:

1. Reverse the prefix expression.
2. If you encounter, an operand → push
3. If you encounter, an operator → pop the top of stack & make it operand1.
 → pop the next top of stack & make it operand2
 → perform the operation
 → push the result .

<u>ex:</u>	+ 4 * 2 3 .	current symbol	stack
<u>pop:1</u>	3 2 * 4 + .	3	3
		2	2
	*		3
		x	2
		2 * 3 = 6	6
			6
	4		4
			6
	+		4 + 6 = 10 ↴

→ Steps for Evaluating a postfix Expression:

1. No reversal required.
2. If operand → push
3. If operator → pop the top of stack & make it operand
 → pop the next top of stack & make it operand
 → perform operators push the result.

ex: 4 2 3 * +

current symbol

stack

4

[4]

2

[2
4]

3

[3
2
4]

*

$$2 * 3 = 6$$

[6
4]

+

$$4 + 6 = 10$$

[10]

No symbol

10 11.

Q1. convert & evaluate the infix expression : $(8+5)*(6/3)$.

soln: prefix : * + 8 5 / 6 3

1. 3 6 | 5 8 + *

2. current symbol stack



3

3

6

6

3

1

 $6/3 = 2$

2

5

5

2

8

8

5

2.

+

 $8+5 = 13$

13

2

*

 $13 * 2 = 26 //$

Q2. convert & evaluate the infix expression to postfix.
 $(8+5)*(6/3)$

Soln: postfix : 8 5 + 6 3 / *

current symbol	Stack
8	[8]
5	[5] [8]
+	$8+5 = 13$ [13]
6	[6] [13]
3	[3] [6] [13]
/	$6/3 = 2$ [2] [13]
*	$13 * 2 = 26$ [26]
NO symbol.	26 //

$\$ \Rightarrow$ power of symbol.

ex: $4 \$ 2 = 4^2 = 16$.

⇒ Pseudocode of prefix in JAVA:

Create a new stack of Integers.

Reverse the prefix exp & traverse the entire length of prefix

exp

{

Consider the character at i^{th} position as the current symbol
if (the current symbol is a digit)

{

Obtain numerical value of the symbol & place it in num
push num onto the stack.

},

else

{

pop top of stack & place it in opnd1

pop top of stack & place it in opnd2.

verify (if symbol is)

{

case '+': then compute opnd1 + opnd2 and push
it onto the stack.

case '-': then compute opnd1 - opnd2 and push
it onto the stack.

case '*':

case '/':

}

}

}

pop the top of stack & place it in ans

-7 JAVA program to evaluate a prefix expression.

```
class prefix  
{
```

```
    String exp;  
    int ans;
```

```
    public void getInput()  
{
```

```
        System.out.println("Enter a prefix Expression");  
        Scanner sc = new Scanner(System.in);  
        exp = sc.next();  
    }
```

```
    public void evalPoc()  
{
```

```
        Stack<Integer> stK = new Stack<Integer>();
```

```
        for (int i = exp.length() - 1; i >= 0; --i)  
    {
```

```
        char symbol = exp.charAt(i);
```

```
        if (Character.isDigit(symbol))
```

```
    {
```

```
        int num = Character.getNumericValue(symbol);  
        stK.push(num);
```

```
    }
```

```
    else
```

```
    { int opnd1 = stK.pop();
```

```
        int opnd2 = stK.pop();
```

```
        switch (symbol)  
{
```

```
case '+': stck.push (opnd1 + opnd2);  
break;
```

```
case '-': stck.push (opnd1 - opnd2);  
break;
```

```
case '*': stck.push (opnd1 * opnd2);  
break;
```

```
case '/': if (opnd2 == 0)  
{
```

```
    System.out.println ("Division by zero not  
possible");  
    System.exit(0);
```

```
}
```

```
else
```

```
{
```

```
    stck.push (opnd1 / opnd2);  
    break;
```

```
}
```

```
}
```

```
}
```

```
ans = stck.pop();
```

```
}
```

```
public void display()
```

```
{
```

```
    System.out.println ("Evaluation of prefix Exp: " + ans);
```

```
}
```

```
}
```

class Evalprefix {

 public static void main (String args[])

{

 Prefix x = new Prefix();

 x.getInput();

 x.evalPre();

 x.display();

}

}

→ Conversion of Expressions:

* Priorities:

1. Exponential ($\$, ^$)
2. Multiplication, Division ($\times, /$)
3. Addition, subtraction ($+, -$).

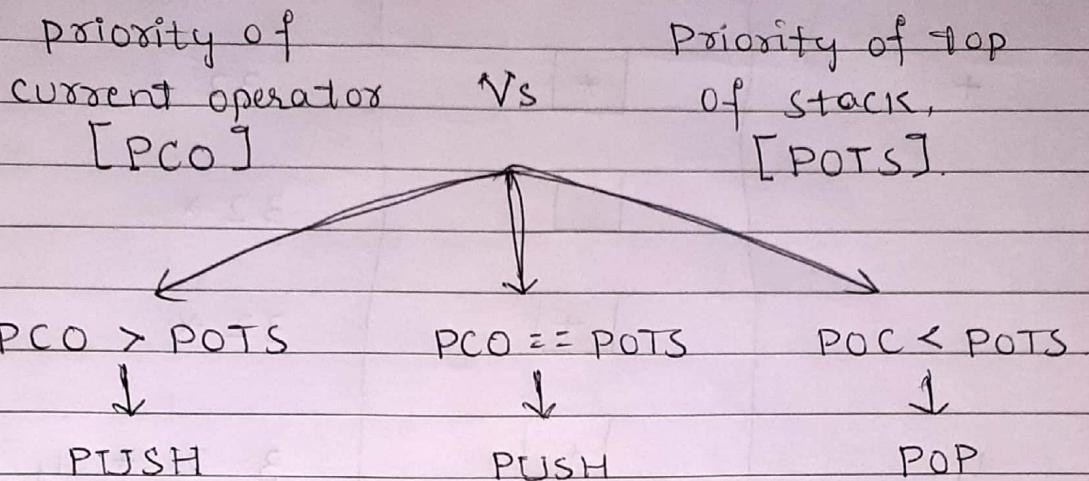
Ex:

$*$	$^$	$*$
$+$	$/$	$-$

$+$	$*$	$-$
$*$	$\$$	$/$

→ Steps for converting an infix Expression to prefix:

1. Reverse the Infix Expression.
2. If operand → send it to prefix expression
3. If operator, then 3 possibilities exists



4. parenthesis

- (push
-) push
- permitted to push any symbol above the brackets
- pop all symbols between (and)

5. Reverse the final expression

Q1 Given, Infix: $4 + 2 * 3$.

Ans: Reverse: $3 * 2 + 4$.

current symbol	STACK	Prefix Expression.
.		
3		3
*	*	3
2	*	3 2

+	*	32
		32 *
	+	32 *
4	+	3 2 * 4
no symbol		3 2 * 4 + .

Prefix Expression: + 4 * 2 3

Q2. $(8+5) * (6/3)$

Soln:) 3 / 6 (*) 5 + 8 (

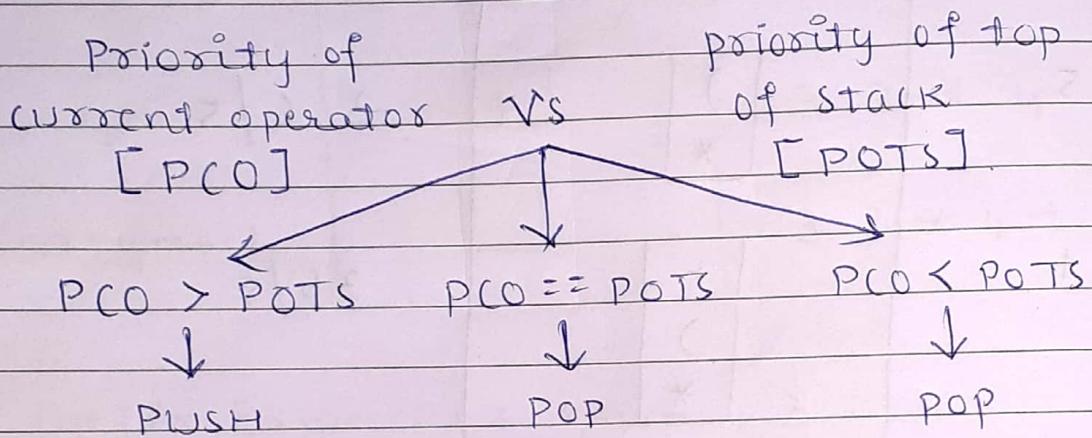
Current symbol	STACK	prefix Expression
))	
3)	3.
/	/)	3
6	/)	3 6
((/)	3 6

	<input type="text"/>	3 6 /
*	<input checked="" type="text"/>	3 6 /
)	<input type="text"/> *	3 6 /
5	<input type="text"/>)	3 6 / 5
+	<input type="text"/> +	3 6 / 5
	<input type="text"/>)	
	<input type="text"/> *	
8	<input type="text"/> (3 6 / 5 8 .
	<input type="text"/> +	
	<input type="text"/>)	3 6 / 5 8)
	<input type="text"/> *	
no symbol.	<input type="text"/> *	3 6 / 5 8 +
		3 6 / 5 8 + *

prefix Expression: * + 8 5 / 6 3 .

→ Steps for converting a infix Expression to postfix:

1. No need to reverse the infix Expression.
2. If operand - send it to postfix Expression.
3. If operators,



4. Parenthesis :

- (: push
-) : push
- permitted to push any symbol above the brackets
- pop all symbols b/w (and)

5. No need to Reverse the final expression.

Q1. $4 + 2 * 3$

Step:	Current Symbol	Stack	Postfix Expression
1	4		4
2	+	4	4
3	2	42	42

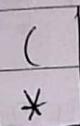
*	<table border="1"><tr><td>*</td><td>+</td></tr></table>	*	+	4 2 .
*	+			
3	<table border="1"><tr><td>*</td></tr><tr><td>+</td></tr></table>	*	+	4 2 3
*				
+				
no symbol	<table border="1"><tr><td></td></tr></table>		4 2 3 * +	

postfix Expression: 4 2 3 * + .

Q2. $(8+5) * (6/3)$

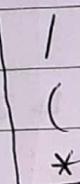
Opn:	current symbol	stack.	postfix Expression
	(((
	8	(8 .
+		+ (8 .
	5	+ (8 5 .
)) + (8 5 .
*) + *	8 5 + .
	((*	8 5 + .

6



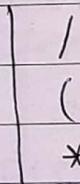
$$85 + 6$$

1



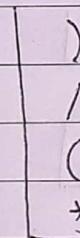
$$85 + 6.$$

3

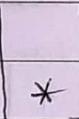


$$85 + 63.$$

)



$$85 + 63$$



$$85 + 63 /$$

no symbol



$$85 + 63 / *$$

postfix : $85 + 63 / *$.

⇒ Rules to convert prefix to infix Expression :

1. push every symbol encountered in the prefix Expression.
2. search for the pattern

operand 2
Operand 1
Operator : } and replace it with

operand1 operator operand2 } pattern

3. Treat the new pattern as operand1 if it is immediately present above the operator. otherwise treat it as operand2.

Q1. $+4 * 2 3$

Ans:

current symbol

STACK.

+

+ |

4

4 |

+ |

*

* |

opnd1 oper

4 |

opnd1

+ |

oper

2

2 |

opnd1

* |

opnd1 oper

4 |

opnd1

+ |

oper

2

2
*
4
f

3

3	opnd2	{}
2	opnd1	
*	oper	
4	opnd1	
+	oper	

2	*	3	opnd2
4			opnd1
+			oper

 $4 + 2 * 3$ Infix Expression : $4 + 2 * 3$ → Rules to prefix-to postfix Expression:

1. push every symbol encountered in the prefix expression
2. Search for the pattern

opnd2 }
opnd1 } pattern & replace it
oper } with

opnd1 opnd2 oper } pattern.

3. Treat the new pattern as opnd1 if it is immediately present above the operator. otherwise treat it as opnd2.

→ Single statement for push operation:

```
void push(int item)
{
    S[++top] = item;
}
```

→ Single Statement for pop operation:

```
int
void pop()
{
    return S[top--];
}
```

I. strrev() → i/p: ABCID
o/p: DICBA.

II. sentrev() → i/p: ABCID is compulsory
yrostlupmoc si DICBA

III. strpal → i/p: ABCID i/p: MADAM
o/p: NOT a palindrome o/p: palindrome.

IV. sentwordrev() → i/p: ABCID is compulsory
o/p: DICBA & i yrostlupmoc.

→ Reversal of a String using STACK :

Ask for the input string
collect the input string.

As long as (not the end of string)

{
 consider the current symbol as item
 push the item
 proceed

As long as (the stack is not empty)

{
 pop & place it in the rev array.
 proceed

}

print the rev array.

→ void store()

{

int i=0, j=0;

char str[200], rev[200];

char item;

p/f ("Enter string :");

s/f ("%s", str); // gets(str); Sentence Reversal

while (str[i] != '\0')

{

item = str[i];

push(item);

++i;

}

```

while (top != -1)
{
    rev[j] = pop();
    ++j;
}
rev[j] = '\0';
p/f ("%s", rev);
}

```

⇒ palindrome:

```

void palin()
{
    int i=0, j=0;
    char str[200], rev[200], item;

    printf ("Enter a string:");
    scanf ("%s", str);

    while (str[i] != '\0')
    {
        item = str[i];
        push(item);
        ++i;
    }

    while (top != -1)
    {
        rev[j] = pop();
        ++j;
    }
    rev[j] = '\0';
}

```

```

if (strcmp(str, rev) == 0)
    printf("palindrome");
else
    printf("Not palindrome");
}

```

→ Reversal of individual words in a Sentence:

```

void sentwordrev()
{
    int i = 0, j = 0;
    char str[200], rev[200], item;

    printf("Enter a sentence: ");
    scanf("%s", gets(str));
    while (str[i] != '\0') // — (I) —
    {
        while (str[i] != ' ' && str[i] != '\0') // (II)
        {
            item = str[i];
            push(item);
            ++i;
        }
        while (top != -1) // — (III) —
        {
            rev[j] = pop();
            ++j;
        }
        rev[j] = '\0';
        printf("%c", rev); ++i; // it reset the loop index
    } // variable i to the beginning
      // of the next word.
}

```

- (I) It works on all the words of a given sentence [1st while loop].
 - (II) pushing every character of the word into the stack. [2nd while loop].
 - (III) popping every character of the stack & finally printing the reversed word.
- Balanced parenthesis: [simple parenthesis] [pseudocode]

As for the string containing simple parenthesis.
collect the string & place it in the array str.

As long as (not the end of string)

{

 consider the current symbol as item

 if (item is '(')

 push the item

 else

 pop the top of stack.

 proceed

}

if (stack is Empty)

 print "Balanced";

else

 print "Not Balanced";

```
void simpleParanthesisBalance()
```

{

```
char str[100], item
```

```
int i
```

```
printf("In Enter a string of simple parenthesis : ");
```

```
scanf("%s", str);
```

```
i = 0;
```

```
while (str[i] != '\0')
```

{

```
if (item == '(')
```

```
push(item);
```

```
else
```

```
pop();
```

```
++i
```

{

```
if (top == -1)
```

```
printf("Balanced");
```

```
else
```

```
printf("Not Balanced");
```

{

→ [Complex Balanced parenthesis]:

```
void complexParanthesisBalance()
```

{

```
char str[100], item;
```

```
int i = 0;
```

```
printf("Enter a string of parenthesis : ");
```

```
scanf("%s", str);
```

```

while (str[i] != '\0')
{
    item = str[i];
    if (item == '(' || item == '[' || item == '{')
        push(item);
    else if (item == ')' || item == ']' || item == '}')
        pop();
    ++i;
}
if (top == -1)
    pf("Balanced");
else
    pf("UnBalanced");
}

```

⇒ Conversion of Decimal Number to Binary form:

```

void decTobin()
{
    int num; int rem;
    pf("Enter the number to be converted : \n");
    pf("%d", &num);

    while (num != 0)
    {
        rem = num % 2;
        num = num / 2;
        push(rem);
    }
    display();
}

```

→ pseudocode : [Decimal to Binary Using stack] :

As long as (the num is not equal to zero)

{

rem = num%2;

num = num/2;

push the rem;

}

display the stack.

→ Search for the given Key element : [pseudocode]

if (no data in the data structure)

print "operation not possible";

else

{

Ask for the key to be searched collect the key.

for (every data present in the data structure)

{

remove the data & place it in temp

if (temp matches with the key)

{

print "key found"

stop

{

{

print "Key not found";

{

* Search for the given key Using STACK :

```
void searchKey()
{
    int key, i, temp;
    if (top == -1)
        printf("In operation not possible");
    else
    {
        printf("Enter key to be searched : ");
        scanf("%d", &key);

        for (i = top; i >= 0; i--)
        {
            temp = pop();
            if (temp == key)
            {
                printf("Key found");
                getch();
                exit(0);
            }
        }
        printf("Key not found");
    }
}
```

*. Search for the given key Using QUEUE.

```
void searchkey()
{
    int key, i, -temp;
    if (front > rear)
        printf (" search not possible ");
    else
    {
        printf (" Enter the key to be searched : ");
        scanf ("%d", &key);

        for (i = front; i <= rear; i++)
        {
            -temp = delete();
            if (-temp == key)
            {
                printf (" Key found ");
                getch();
                exit(0);
            }
        }
        printf (" Key not found ");
    }
}
```

⇒ Search for the multiples of a given number : [STACK]

```

void searchmul()
{
    int num, i, temp;
    if (top == -1)
        printf("Operation not possible");
    else
    {
        printf("Enter number whose multiples are to be
               searched : ");
        scanf("%d", &num);

        for (i = top; i >= 0; i--)
        {
            temp = pop();
            if (temp % num == 0)
                printf("%d", temp);
        }
    }
}

```

⇒ Search for the maximum [Largest] Element in the STACK:

```

void searchMax()
{
    int max = -9999, temp;
    if (top == -1)
        printf("Operation not possible.");
    else
    {
}

```

```
-for (i = -top; i >= 0; i--)  
{  
    temp = pop();  
    if (temp > max)  
        max = temp;  
}  
printf ("%d", max);  
};
```

⇒ Pseudocode for Searching maximum Element in a STACK or QUEUE:

```
if (no data in the data structure)  
    print "operation not possible";  
else  
{  
    max = -9999;  
    for (every data present in the data structure)  
    {  
        remove the data & place it in temp  
        if (temp > max)  
            update the max  
    }  
    print max.  
};
```

→ Reversal of a QUEUE: [Pseudocode]

```
if (no data in the Queue)
    print "Reversal not possible";
else
{
    for (every data present in the queue)
    {
        delete the data from queue & place it in temp
        push temp into the stack
        increment count.
    }

    for (every data present in the stack)
    {
        pop from the stack & place it in temp
        insert temp into the queue.
    }

    Display the queue.
}
```

→ C code for Reversal of a Queue:

```
void reverseQ()
{
    int temp, count = 0;
    if (front > rear)
        printf("Reversal not Possible");
    else
    {
        for (int i = front; i <= rear; i++)
        {
            temp = delete();
            insert(temp);
        }
    }
}
```

```

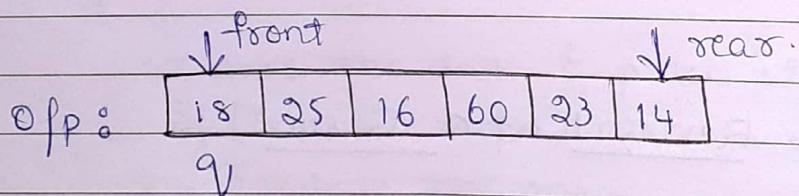
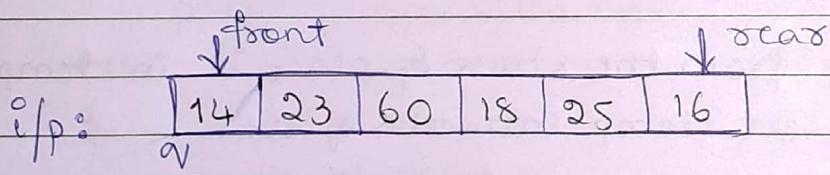
    push(temp)
    ++count;
}

for (int i = 0; i <= count - 1; i++)
{
    temp = pop();
    q[++rear] = temp;
}

display();
}
}.

```

⇒ Partial Reverse of a Queue:



```

void partialReverse()
{
    int i, temp, K, count = 0;
    if (front > rear)
        printf ("Reversal not possible");
    else
    {

```

```
printf("Enter the number of items to be Reversed  
");  
scanf("%d", &i);  
  
for(i=front; i<=K-1; i++)  
{  
    temp = delete();  
    push(temp);  
    ++count;  
}  
  
for(i=0; i<=count-1; i++)  
{  
    temp = pop();  
    q[++rear] = temp;  
}  
display();  
}
```