1

Learning LATEX

EE24BTECH11053 - S A Aravind Eswar*

I. SECTION B

11. If $\lim_{x \to 0} \frac{\log(3+x) - \log(3-x)}{x} = k$, then the value of k is [2003]

12. Value of k is [2003] [2002]

- 1) 2
- 2) 4
- 3) 1
- 4) $\frac{1}{2}$

7. f is defined in [-5,5] as [2002] f(x) = x if x is rational = -x if x is irrational. Then

- 1) f(x) is continuous at every x, except x = 0
- 2) f(x) is discontinuous at every x, except x = 0
- 3) f(x) is continuous everywhere
- 4) f(x) is discontinuous everywhere

8. f(x) and g(x) are two differentiable functions on [0,2] such that f''(x)-g''(x)=0, f'(1)=2g'(1)= $4, f(2) = 3g(2) = 9 \text{ then } f(x) - g(x) \text{ at } x = \frac{3}{2} \text{ is}[2002]$

- 1) 0
- 2) 2
- 3) 10
- 4) 5

9. If $f(x + y) = f(x).f(y) \forall x, y \text{ and } f(5) =$ 2, f'(0) = 3, then f'(5) is [2002]

- 1) 0
- 2) 1
- 3) 6
- 4) 2

 $[2003]^{x}$

- 1) $\frac{1}{5}$ 2) $\frac{1}{30}$ 3) Zero
- 4) $\frac{1}{4}$

12. The value of $\lim_{x\to 0} \frac{\int_0^{x^2} \sec^2 t dt}{x \sin x}$ is [2003]

- 1) 0
- 2) 3
- 3) 2
- 4) 1

13. Let f(a) = g(a) = k and their nth derivatives $f^{n}(a), g^{n}(a)$ exist and are not equal for some n. Further if $\lim_{x \to a} \frac{f(a)g(x) - f(a) - g(a)f(x) + f(a)}{g(x) - f(x)} = 4$ then the value of k is [2003]

- 1) 0
- 2) 4
- 3) 2
- 4) 1

14.
$$\lim_{x \to \frac{\pi}{2}} \frac{\left[1 - \tan\left(\frac{x}{2}\right)\right] [1 - \sin x]}{\left[1 + \tan\left(\frac{x}{2}\right)\right] [\pi - 2x]^3}$$
 is [2003]

- 1) ∞
- 2) $\frac{1}{8}$ 3) 0

 $\frac{10. \lim_{x \to \infty} \frac{1 + 2^4 + 3^4 + \dots n^4}{n^5} - \lim_{x \to \infty} \frac{1 + 2^3 + 3^3 + \dots n^3}{n^5} \quad 15. \text{ If } f(x) = \begin{cases} xe^{-\left(\frac{1}{|x|} + \frac{1}{x}\right)}, & x \neq 0 \\ 0, & x = 0 \end{cases} \text{ then } f(x) \text{ is } f(x) = \begin{cases} xe^{-\left(\frac{1}{|x|} + \frac{1}{x}\right)}, & x \neq 0 \\ 0, & x = 0 \end{cases}$

- 1) discontinuous every where
- 2) continuous as well as differentiable for all x
- 3) continuous for all x but not differentiable at
- 4) neither differentiable not continuous at x = 0

16. if $\lim_{x \to \infty} \left(1 + \frac{a}{x} + \frac{b}{x^2} \right)^{2x} = e^2$, then the values of a and b, are [2004]

- 1) a = 1 and b = 2
- 2) a = 1 and $b \in \mathbf{R}$
- 3) $a \in \mathbf{R}, b = 2$
- 4) $a \in \mathbf{R}, b \in \mathbf{R}$

17. $f(x) = \frac{1 - \tan x}{4x - \pi}, x \neq \frac{\pi}{4}, x \in \left[0, \frac{\pi}{4}\right]$. If f(x) is continuous in $\left[0, \frac{\pi}{2}\right]$, then $f\left(\frac{\pi}{4}\right)$ is

- 1) -12) $\frac{1}{2}$ 3) $-\frac{1}{2}$ 4) 1

18.
$$\lim_{n \to \infty} \left[\frac{1}{n^2} \sec^2 \frac{1}{n^2} + \frac{2}{n^2} \sec^2 \frac{4}{n^2} \dots \frac{1}{n} \sec^2 1 \right]$$
 equals [2005]

- 1) $\frac{1}{2} \sec 1$ 2) $\frac{1}{2} \csc 1$
- 3) tan 1
- 4) $\frac{1}{2} \tan 1$

19. Let α and β be the distinct roots of $ax^2 + bx + c = 0$, then, $\lim_{x \to \alpha} \frac{1 - \cos(ax^2 + bx + c)}{(x - a)^2}$ is equal to [2005]

- 1) $\frac{a^2}{2}(\alpha \beta)^2$ 2) 0 3) $\frac{-a^2}{2}(\alpha \beta)^2$ 4) $\frac{1}{2}(\alpha \beta)^2$

20. Suppose f(x) is a differentiable at x = 1 and $\lim_{h\to 0} \frac{1}{h} f(1+h) = 5, \text{ then } f'(1) \text{ equals}$ [2005]

- 1) 3
- 2) 4
- 3) 5
- 4) 6