EE24BTECH11053 - S A Aravind Eswar

Question: Verify if the points A(4, 3), B(6, 4), C(5, -6) and D(-3, 5) are the vertices of a parallelogram.

Solution:

Symbol	Value	Description
A	$\begin{pmatrix} 4 \\ 3 \end{pmatrix}$	Point A
В	$\begin{pmatrix} 6 \\ 4 \end{pmatrix}$	Point B
С	$\begin{pmatrix} 5 \\ -6 \end{pmatrix}$	Point C
D	$\begin{pmatrix} -3 \\ 5 \end{pmatrix}$	Point D

TABLE 0: Given Values

It requires two vectors formed by two unique points to be equivalent for points A,B,C and D to form a parallelogram, .

$$\mathbf{AB} = \mathbf{B} - \mathbf{A} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \tag{0.1}$$

$$\mathbf{BC} = \mathbf{C} - \mathbf{B} = \begin{pmatrix} -1 \\ -10 \end{pmatrix} \tag{0.2}$$

$$\mathbf{CD} = \mathbf{D} - \mathbf{C} = \begin{pmatrix} -8\\11 \end{pmatrix} \tag{0.3}$$

$$\mathbf{DA} = \mathbf{A} - \mathbf{D} = \begin{pmatrix} 7 \\ -2 \end{pmatrix} \tag{0.4}$$

$$\mathbf{BD} = \mathbf{D} - \mathbf{B} = \begin{pmatrix} -9\\1 \end{pmatrix} \tag{0.5}$$

$$\mathbf{AC} = \mathbf{C} - \mathbf{A} = \begin{pmatrix} 1 \\ -9 \end{pmatrix} \tag{0.6}$$

Thus, the points A,B,C and D are not forming a parallelogram.

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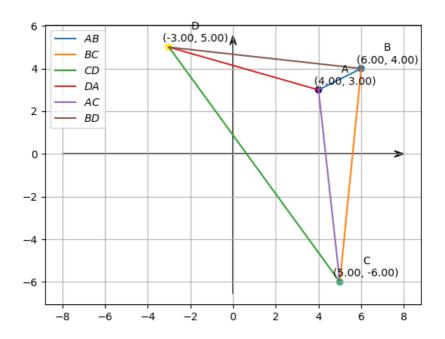


Fig. 0.1: Points A,B,C and D