

Learning L^AT_EX

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I. SECTION B

6. If $f(1) = 1, f'(1) = 2$, then $\lim_{x \rightarrow 1} \frac{\sqrt{f(x)} - 1}{\sqrt{x} - 1}$ is [2002]
- 1) 2
 - 2) 4
 - 3) 1
 - 4) $\frac{1}{2}$
7. f is defined in $[-5, 5]$ as [2002]
 $f(x) = x$ if x is rational
 $= -x$ if x is irrational. Then
- 1) $f(x)$ is continuous at every x , except $x = 0$
 - 2) $f(x)$ is discontinuous at every x , except $x = 0$
 - 3) $f(x)$ is continuous everywhere
 - 4) $f(x)$ is discontinuous everywhere
8. $f(x)$ and $g(x)$ are two differentiable functions on $[0, 2]$ such that $f''(x) - g''(x) = 0, f'(1) = 2g'(1) = 4, f(2) = 3g(2) = 9$ then $f(x) - g(x)$ at $x = \frac{3}{2}$ is [2002]
- 1) 0
 - 2) 2
 - 3) 10
 - 4) 5
9. If $f(x + y) = f(x) \cdot f(y) \forall x, y$ and $f(5) = 2, f'(0) = 3$, then $f'(5)$ is [2002]
- 3
 - 1) 0
 - 2) 1
 - 3) 6
 - 4) 2
10. $\lim_{x \rightarrow \infty} \frac{1 + 2^4 + 3^4 + \dots + n^4}{n^5} - \lim_{x \rightarrow \infty} \frac{1 + 2^3 + 3^3 + \dots + n^3}{n^5}$ [2003]
- 1) $\frac{1}{5}$
 - 2) $\frac{1}{30}$
 - 3) Zero
 - 4) $\frac{1}{4}$
11. If $\lim_{x \rightarrow 0} \frac{\log(3+x) - \log(3-x)}{x} = k$, then the value of k is [2003]
- 1) $-\frac{2}{3}$
 - 2) 0
 - 3) $-\frac{1}{3}$
 - 4) $\frac{2}{3}$
12. The value of $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \sec^2 t dt}{x \sin x}$ is [2003]
- 1) 0
 - 2) 3
 - 3) 2
 - 4) 1
13. Let $f(a) = g(a) = k$ and their n th derivatives $f^n(a), g^n(a)$ exist and are not equal for some n . Further if $\lim_{x \rightarrow a} \frac{f(a)g(x) - f(a) - g(a)f(x) + f(a)}{g(x) - f(x)} = 4$ then the value of k is [2003]
- 1) 0
 - 2) 4
 - 3) 2
 - 4) 1
14. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\left[1 - \tan\left(\frac{x}{2}\right)\right] [1 - \sin x]}{\left[1 + \tan\left(\frac{x}{2}\right)\right] [\pi - 2x]^3}$ is [2003]
- 1) ∞
 - 2) $\frac{1}{8}$
 - 3) 0
 - 4) $\frac{1}{32}$
15. If $f(x) = \begin{cases} xe^{-(\frac{1}{|x|} + \frac{1}{x})}, & x \neq 0 \\ 0, & x = 0 \end{cases}$ then $f(x)$ is
- 1) discontinuous every where
 - 2) continuous as well as differentiable for all x
 - 3) continuous for all x but not differentiable at $x = 0$
 - 4) neither differentiable not continuous at $x = 0$

16. if $\lim_{x \rightarrow \infty} \left(1 + \frac{a}{x} + \frac{b}{x^2}\right)^{2x} = e^2$, then the values of a and b , are [2004]

- 1) $a = 1$ and $b = 2$
- 2) $a = 1$ and $b \in \mathbf{R}$
- 3) $a \in \mathbf{R}, b = 2$
- 4) $a \in \mathbf{R}, b \in \mathbf{R}$

17. $f(x) = \frac{1 - \tan x}{4x - \pi}$, $x \neq \frac{\pi}{4}$, $x \in \left[0, \frac{\pi}{4}\right]$. If $f(x)$ is continuous in $\left[0, \frac{\pi}{4}\right]$, then $f\left(\frac{\pi}{4}\right)$ is

- 1) -1
- 2) $\frac{1}{2}$
- 3) $-\frac{1}{2}$
- 4) 1

18. $\lim_{n \rightarrow \infty} \left[\frac{1}{n^2} \sec^2 \frac{1}{n^2} + \frac{2}{n^2} \sec^2 \frac{4}{n^2} + \dots + \frac{1}{n} \sec^2 1 \right]$
equals [2005]

- 1) $\frac{1}{2} \sec 1$
- 2) $\frac{1}{2} \operatorname{cosec} 1$
- 3) $\tan 1$
- 4) $\frac{1}{2} \tan 1$

19. Let α and β be the distinct roots of $ax^2 + bx + c = 0$, then, $\lim_{x \rightarrow \alpha} \frac{1 - \cos(ax^2 + bx + c)}{(x - \alpha)^2}$ is equal to [2005]

- 1) $\frac{a^2}{2}(\alpha - \beta)^2$
- 2) 0
- 3) $\frac{-a^2}{2}(\alpha - \beta)^2$
- 4) $\frac{1}{2}(\alpha - \beta)^2$

20. Suppose $f(x)$ is a differentiable at $x = 1$ and $\lim_{h \rightarrow 0} \frac{1}{h} f(1 + h) = 5$, then $f'(1)$ equals [2005]

- 1) 3
- 2) 4
- 3) 5
- 4) 6