# 06- File Organization and Indexing

School of Computer Science University of Windsor

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#### **Announcements**

Reading Week: Jun 19 - 23 - No Classes

**P2:** Milestone report submission

Sec. 1 & 4: Jun 25; Sec. 2: Jun 26; Sec. 3: Jun 27

P2: Milestone presentation: Next week (Jun 26 - 28)



#### Test 1

- Date: Sat, July 8th
- Time: 9:00AM 10:00AM. The total time length of the test is 1 hour.
- Location: ER1120 (Please note that location has changed. It is not the same as given in syllabus)
- Maximum credits/points: 100 points (this accounts for 20% of your overall grade).
- Portion: First six weeks lectures. All lectures covered before reading week. Labs and assignment related material will not be included in the test.
- Format: This is an **in-person**, paper-based, closed-book and closed-notes test. You are not allowed to use textbooks, your notes, a computer, or any other materials during the exam. Cell phones, laptops, and all other devices must be turned off. MCQs, essay and implementation questions.
- Make sure your name and student ID is written on the test and scantron sheets.
- The Scantron software and hardware is used for computerized test scoring of MCQs. Don't forget to **bring No. 2 pencil** to fill the scantron sheet.
- Fill in circles on the scantron sheet completely. If you want to change an answer when completing a test, you must erase the answer you provided completely and not simply put an X through it.
- Please make sure that as soon as you have handed in the test paper, you sign-out on the sheet and leave the room quietly.



## Agenda

#### **Lecture**

- Organizing the data on the disk
- Introduction to Indexing
- Single-Level Ordered Indexes
  - Primary Indexes
  - Clustering Indexes
  - Secondary Indexes
- Multilevel Indexes
  - Two-Level Primary Indexing
- Dynamic Multilevel Indexes
  - B Trees
  - B+ Trees
- CREATE INDEX Command in SQL
- **➤**Workshop on Indexing
- **≻**Assignment-1 Quiz

## **Introductory Questions**

Why is indexing important?

What is the aim of having an index?

What are the downsides of indexes?

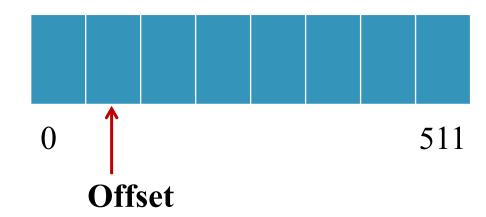
What are the different types of indexes used for query optimizations?

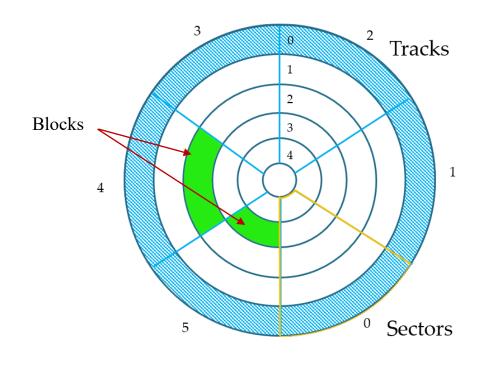
What to choose for creating indexes?

#### **Disk Structure**

 $Block\ Address$ =  $\langle Track\ Num, Sector\ Num \rangle$ 

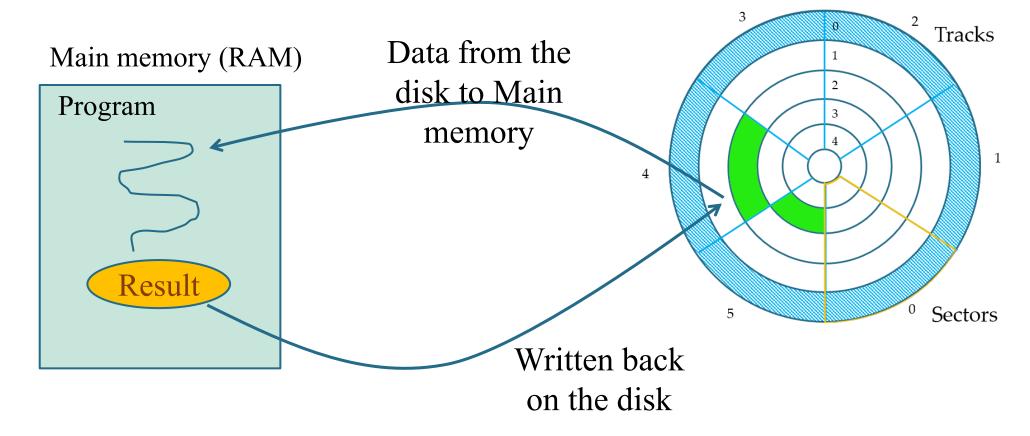
Let's assume a block size is 512 bytes







#### Disk Structure

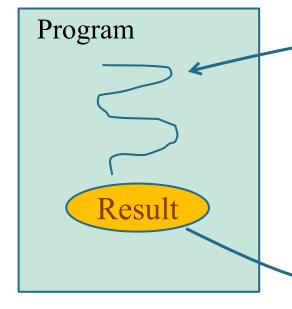


So, the data cannot be directly processed upon the disk it has to be brought into the main memory and then access .

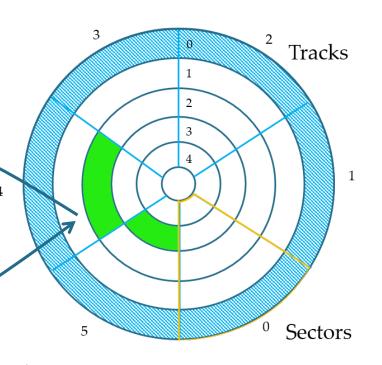
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#### Disk Structure

Main memory (RAM)



Data from the disk to Main memory



Written back on the disk

Organizing the data inside the main memory that is directly used by the program is **Data Structures**.

Organizing the data on the disk efficiently so that it can be easily utilized that is **DBMS**.

8



#### How is data stored on Disk?

#### **Employees**

Fields	Size
Eid	10
Name	50
Depart	30
Gender	8
Salary	30
Total size	128 bytes

128 bytes

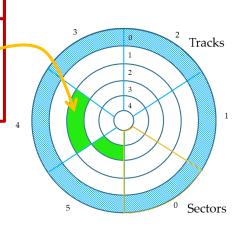
In each block how many rows can be stored?

Number of Records/ Block = 512/128 = 4

#### **Employees**

Eid	Name	Depart
1	Jenkins	Manager
2	Williams	Sales Rep
3	Smith	Sales Rep
4	Crosby	Manager
5	Albright	Secretary
6	Sawyer	Sales Rep
7	Thomas	Secretary
8	Albright	Worker
9	Crawford	Manager

What is the size of a record?



Block Size = 512 bytes

100 records



#### How is data stored on Disk?

#### **Employees**

Fields	Size
Eid	10
Name	50
Depart	30
Gender	8
Salary	30
Total size	128 bytes

**SELECT** Eid=7 **FROM** Employees

Number of Records/ Block = 512/128 How many blocks are required for 100 records?

100 Records can be stored in = 100/4 or 12800/512

= 25 blocks

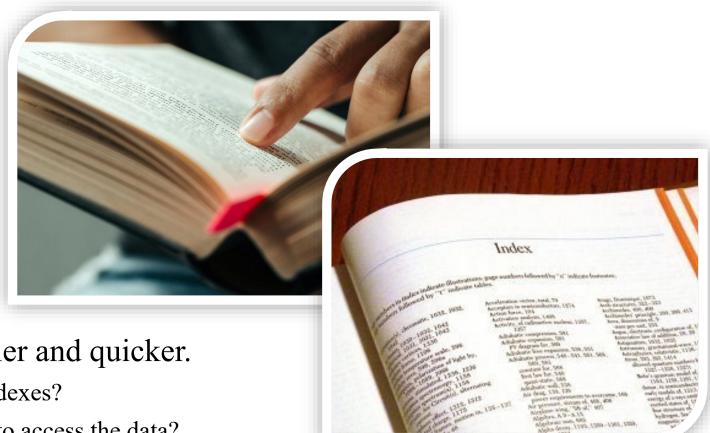
#### **Employees**

Eid	Name	Depart	
1	Jenkins	Manager	
2	Williams	Sales Rep	
3	Smith	Sales Rep	
4	Crosby	Manager	
5	Albright	Secretary	
6	Sawyer	Sales Rep	
7	Thomas	Secretary	
8	Albright	Worker	
9	Crawford	Manager	
<u>ک</u>			

100 records



An index is a structure that provides accelerated access to the rows of a table based on the values of one or more columns.



It makes our search simpler and quicker.

- ✓ How do we create the indexes?
- ✓ How these indexes help to access the data?



## Motivation-Searching for a Key Value

- Ex: Unsorted List
  - 1024x1024x1024 = 1,073,741,824 (I Billion elements –Approx.)
  - Takes 1 Billion comparisons in the worst case
- Ex|: Sorted List
  - 1024x1024x1024 = 1,073,741,824 (I Billion <u>sorted</u> elements –Approx.)
  - Takes 30 comparisons in the worst case
- 30 comparisons vs. 1 Billion comparisons
- Overhead involved in sorting is much lesser than that in searching?



Where do we store the index?

00.

How many blocks for storing index?

Index

Key	Pointer
1	•
2	<b>—</b>
3	+
4	
5	
400	

100 records

Dense Index **Employees** 

		• •	
	 Depart	Name	Eid
· ·	Manager	Jenkins	<b>→</b> 1
	Sales Rep	Williams	<b>→</b> 2
	Sales Rep	Smith	<del>)</del> 3
	Manager	Crosby	<b>&gt;</b> 4
4	Secretary	Albright	5
	Sales Rep	Sawyer	6
	Secretary	Thomas	7
В	Worker	Albright	8
b	Manager	Crawford	9

Block Size = 512 bytes

100 records



Tracks

Sectors

#### Index

Fields	Size
Eid	10
Pointer	6
Total size	16 bytes

Index
-------

Key	Pointer
1	<b>+</b>
2	<b>+</b>
3	+
4	
5	
100	•

100 entries

1 index entry requires : 16 bytes 100 entries require: 1600 bytes

100 entries can be stored in =  $1600/512 = 3.1 \approx 4$  blocks



Block Size = 512 bytes

Sectors

100 records

Secretary

Worker

Manager

**Employees** 

7

8

Thomas

Albright

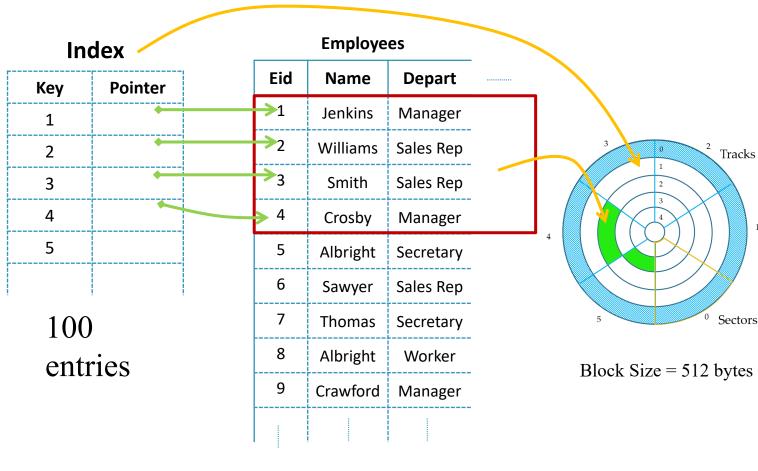
Crawford



**SELECT** Eid=7 **FROM** Employees

100 entries can be stored in = 1600/512 $\approx 4 \text{ blocks}$ 

Total number of blocks required = 4 +1
= 5 blocks



100 records



#### Index

Key	Pointer
1	
33	 

#### Index

Key	Pointer
1	+
2	+
3	+
4	
5	
100	) antrias

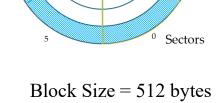
1000 entries

We require 40 blocks.

Can we have an index above an index?

#### **Employees**

Eid	Name	Depart
<b>&gt;</b> 1	Jenkins	Manager
<b>&gt;</b> 2	Williams	Sales Rep
3	Smith	Sales Rep
<b>&gt;</b> 4	Crosby	Manager
5	Albright	Secretary
6	Sawyer	Sales Rep
7	Thomas	Secretary
8	Albright	Worker
9	Crawford	Manager

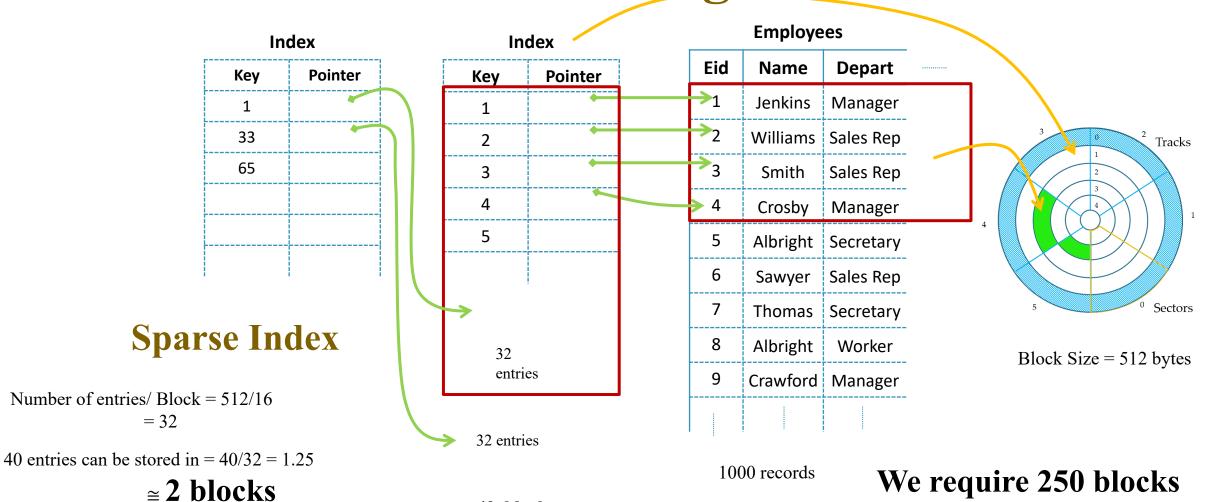


Tracks

1000 records

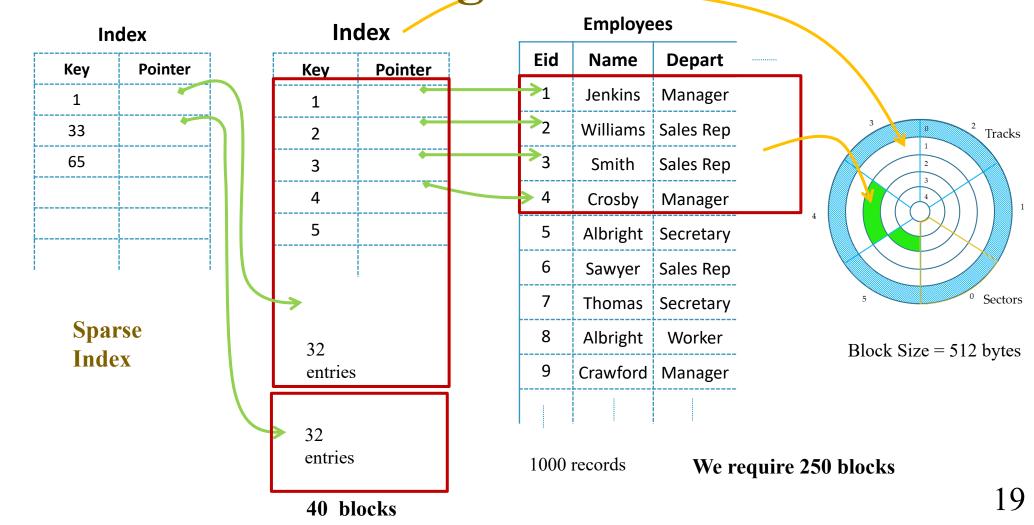
We require 250 blocks





40 blocks







**Pointer** 

#### Index

Key

# SELECT Eid=7 FROM Employees ?

Number of entries/ Block = 512/16 = 32

40 entries can be stored in = 40/32 = 1.25 $\approx 2 \text{ blocks}$ 

Total number of blocks required = 2 + 1 + 1 = 4 blocks

#### Index

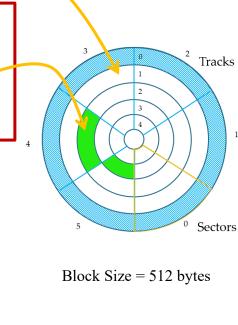
Key	Pointer
1	<b>+</b>
2	<del>\</del>
3	<b>+</b>
4	
5	
<b>\</b>	
32 entries	

32 entries

40 blocks

#### **Employees**

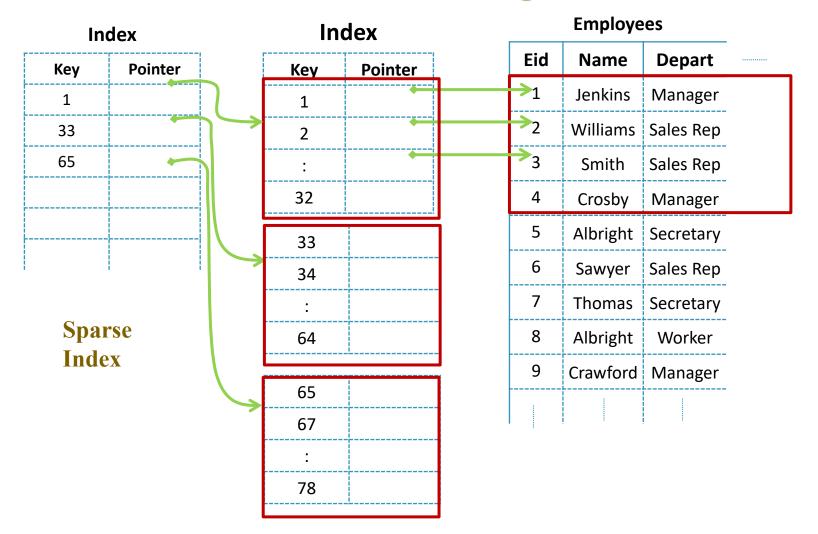
Eid	Name	Depart	
<b>→</b> 1	Jenkins	Manager	
<b>→</b> 2	Williams	Sales Rep	
→3	Smith	Sales Rep	
<b>&gt;</b> 4	Crosby	Manager	
5	Albright	Secretary	
6	Sawyer	Sales Rep	
7	Thomas	Secretary	
8	Albright	Worker	
9	Crawford	Manager	

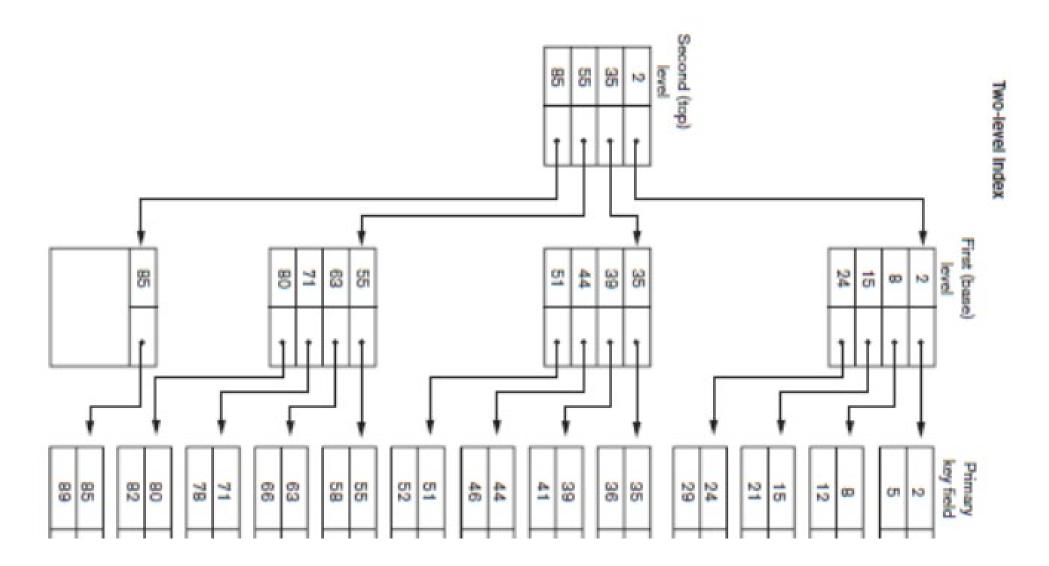


1000 records

We require 250 blocks







## Indexing cont.

- Database Indexes are special files which are stored along with the Data files of the Database
- Database indexes help the query processor to **expedite** search and retrieval of records from Blocks
- By default, the DBMS typically creates an index based on the PK of each table
  - However, depending on the type and frequency of queries, <u>users can create</u> their own indexes for better overall performance
- When queries corresponding to particular tables are executed, the corresponding index files (if any) are transferred to the main memory for the **query optimization** module to work on



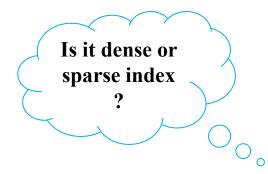
#### Single-Level Ordered Indexes

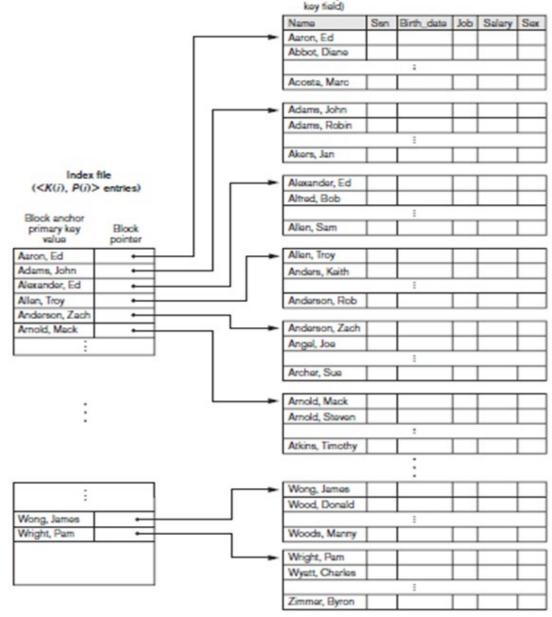
## Single-Level Ordered Index

- Primary Index
- Clustered Index
- Secondary Index

#### **Primary Indexes**

- Records are **sorted and stored** across blocks based on a key
- The first Record in each block is called the **Block anchor**
- Each block anchor has an entry in the index file that has a **pointer** to the block





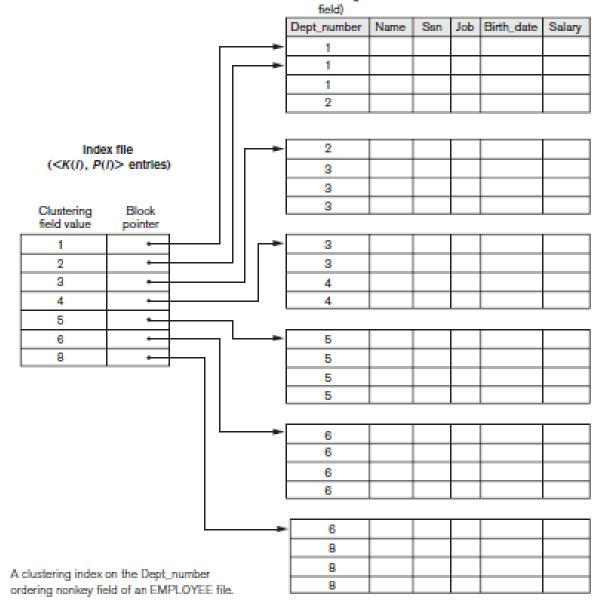


Data file

(Primary

### **Clustering Index**

- Records are sorted and stored across blocks based on a <u>Clustering Field</u> <u>value (non-key value)</u>
- Each Clustering Field value has an entry in the index file that has a **pointer** to the **first block** that contains the Clustering Field value

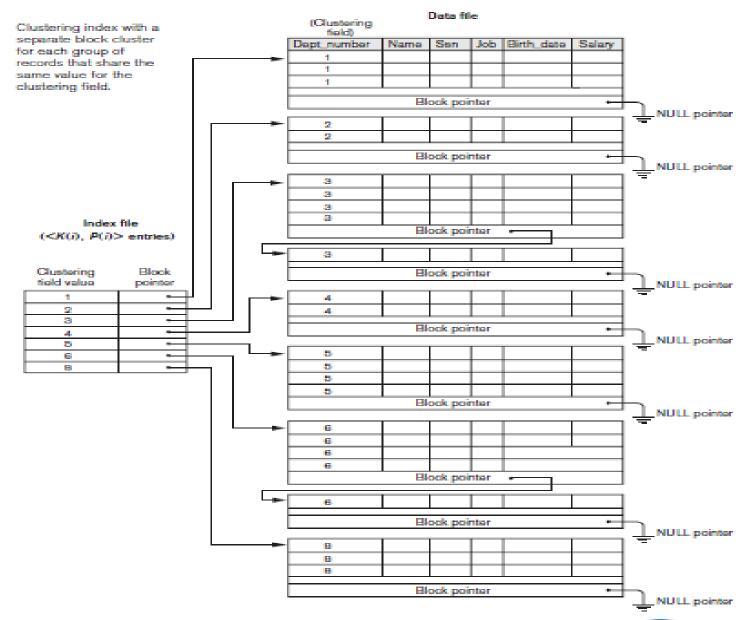


(Clustering)

Data file



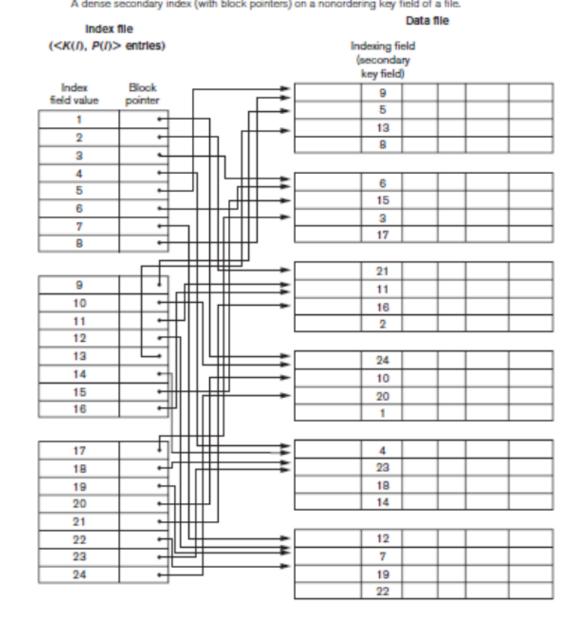
# Clustering Indexes with Separate Block Clusters





#### **Secondary Index**

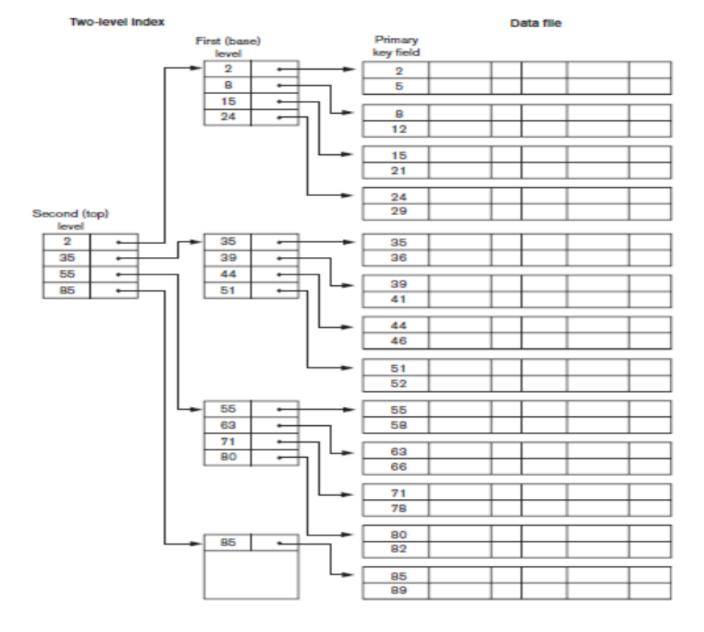
- Indexes based on **other key** values (which are not the PK)
- The records in this case are **not sorted** across the blocks based on
  the secondary key fields (Since
  they are sorted using the PK)
- Anchoring is not possible (Like in Primary Index)





#### Multilevel Indexes

#### **Two-Level Primary Index**



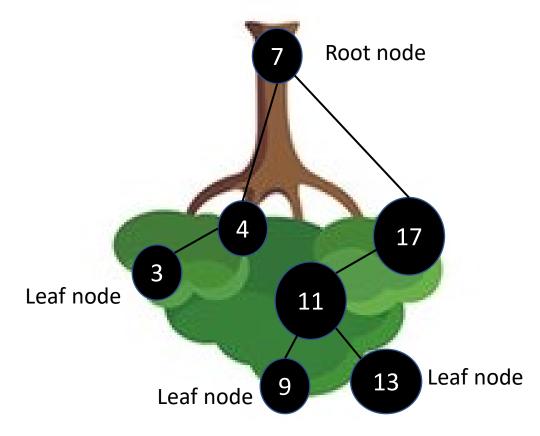


# Dynamic Multilevel Indexes using B Trees and B+ Trees

#### TREE

Tree: An organizational structure for the storage and retrieval of data

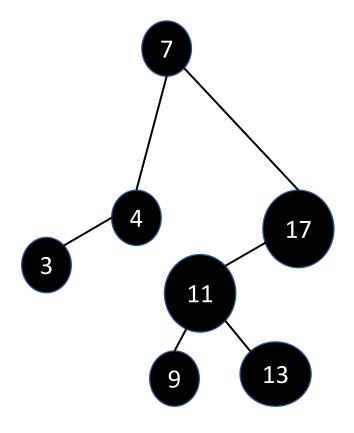




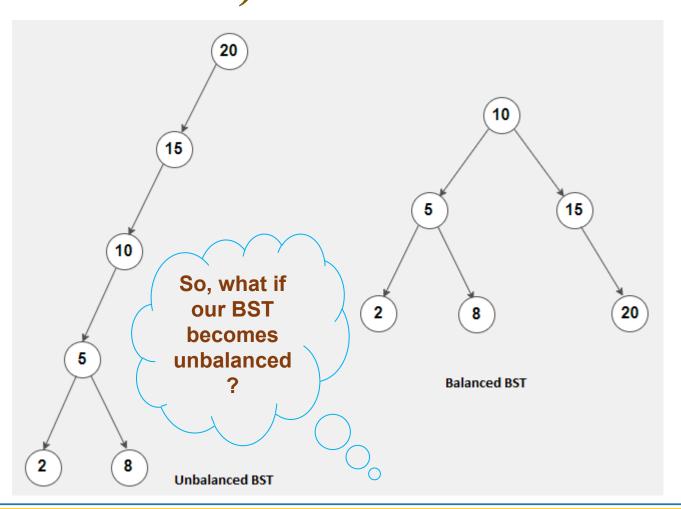


## **Binary Search Tree**

- Binary search trees allow binary search for fast lookup, addition, and removal of data items.
- A node can have utmost two children.



## Binary Search Tree BST (Balanced vs. Unbalanced)



- Balanced BST: The difference between the height of the left subtree and the right sub-tree of every node is not more than 1
- The time complexity of operations on the binary search tree is directly proportional to the height of the tree.

Balanced BST: O(log(n))
Unbalanced BST: O((n))

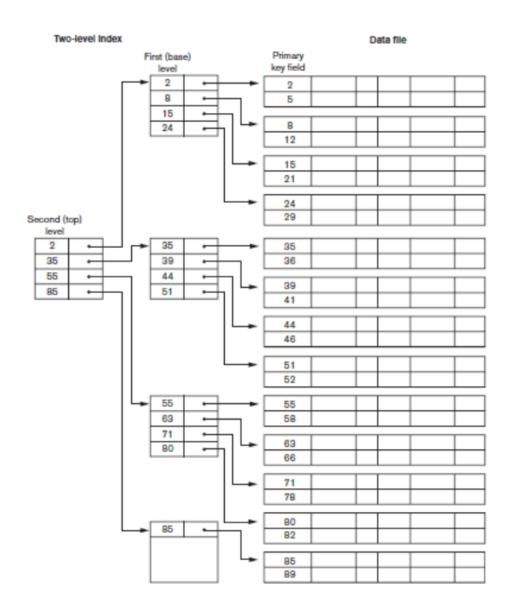
- It can also be expressed in terms of its height (h) as O(h)
- A balanced BST minimizes the search time by minimizing the value of *h*

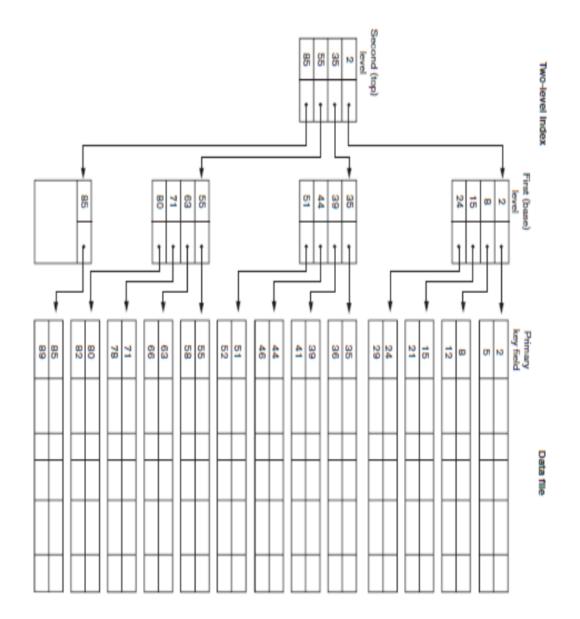


#### **B-Tree**

- A B-tree is a <u>self-balancing</u> tree data structure that maintains sorted data and allows searches, sequential access, insertions, and deletions in logarithmic time.
- Invented by Rudolf Bayer and Ed McCreight in 1972
- The B-tree generalizes the binary search tree
  - Allows nodes with more than two children (Whereas a node in a BST cannot have more than two children)
- Useful for implementing multi-level indexing



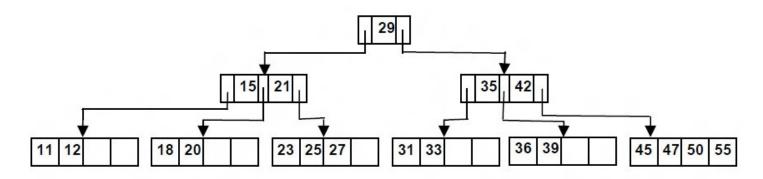




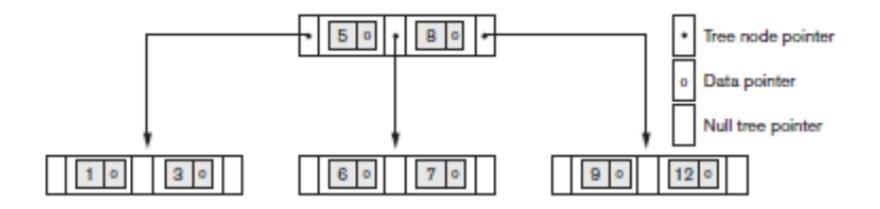


# **B** Tree Rules

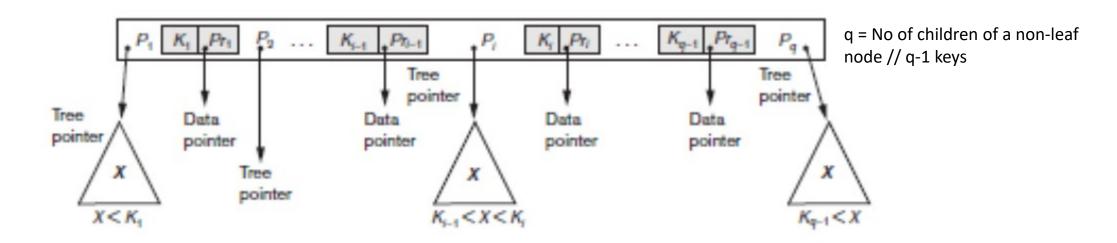
- A B-tree of order m is a tree which satisfies the following properties:
  - Every node has at most m children.
  - Every non-leaf node (except root) has at least [m/2] child nodes.
  - The root has at least two children if it is not a leaf node.
  - A non-leaf node with k children contains k 1 keys.



B-Tree of order 5



**B-Tree of order 3 (With Tree-Node Pointer and Data Pointer** 

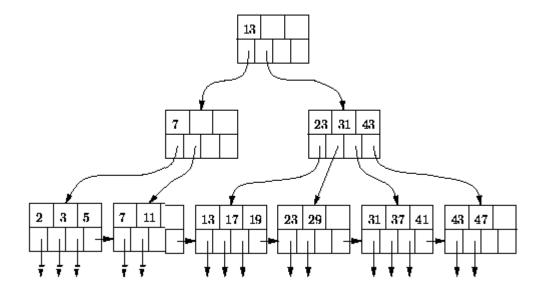


A node in a B-Tree with q-1 search values



# **B+ Trees**

• Data pointers only at the leaf node to facilitate faster search





# B TREE DEMO



# **INDEX CREATION**

### The general form

```
CREATE [ UNIQUE ] INDEX <index name>
ON  ( <column name> [ <order> ] { , <column name> [ <order> ] } )
[ CLUSTER ] ;
```

CREATE INDEX DnoIndex

**ON** EMPLOYEE (Dno)

CLUSTER; //Clustered Index

• **CREATE INDEX** EmpAgeIndex

ON EMPLOYEE(Age DESC)

CLUSTER; //Clustered Index

• CREATE INDEX EmpEmailIndex

ON EMPLOYEE (Email) // Creates a secondary index

• CREATE INDEX EmpAgeService

ON EMPLOYEE(Age, Years Of Service); //Dense Index



# **Choose indexes – Guidelines for choosing 'wish-list'**

- 1. Do not index small relations.
- 2. Add secondary index to a FK if it is frequently accessed.
- 3. Add secondary index to any attribute heavily used as a secondary key.
- 4. Add secondary index on attributes involved in: selection or join criteria; ORDER BY; GROUP BY; and other operations involving sorting (such as UNION or DISTINCT).
- 5. Add secondary index on attributes involved in built-in functions.
- 6. Avoid indexing an attribute or relation that is frequently updated.
- 7. Avoid indexing an attribute if the query will retrieve a significant proportion of the relation.
- 8. Avoid indexing attributes that consist of long character strings.



# Choose indexes

Suppose, we have a table named buyers where the SELECT query uses indexes like below:

```
SELECT buyer_id /* no need to index */
FROM buyers

WHERE first_name='Carolyn' /* consider to use index */
AND last_name='Begg' /* consider to use index */
```

Since "buyer\_id" is referenced in the SELECT portion, MySQL will not use it to limit the chosen rows. Hence, there is no great need to index it

The below is another example little different from the above one:

```
SELECT buyers.buyer_id, country.name /* no need to index */
FROM buyers LEFT JOIN country ON buyers.country_id=country.country_id /* consider to use index */
WHERE first_name='Carolyn' /* consider to use index */
AND last name='Begg' /* consider to use index */
```

According to the above queries first\_name, last\_name columns can be indexed as they are located in the WHERE clause. Also an additional field, country\_id from country table, can be considered for indexing because it is in a JOIN clause. So indexing can be considered on every field in the WHERE clause or a JOIN clause.



# **Downsides of Indexes**

- Extra space
- Index creation
- Index maintenance

# **Summary and Conclusion**

- File Organization
- Introduction to Indexing
- Single-Level Ordered Indexes
  - Primary Indexes //SPARSE
  - Clustering Indexes // SPARSE (Optionally with Block Pointer)
  - Secondary Indexes //DENSE
- Multilevel Indexes
  - Two-Level Primary Indexing //SPARSE
- Dynamic Multilevel Indexes
  - B Trees //Generalized version of Balances Search Tree- Allows more than 2 children per node
  - B+ Trees // SELF BALANCING Data Pointers only at the leaf level
- CREATE INDEX Command in SQL
- Choosing an INDEX

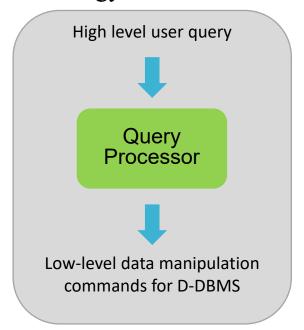


# Extra Material

# **Query Processing**

### • **Aim**:

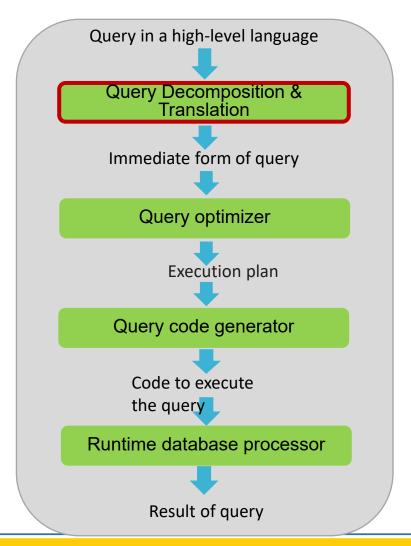
Transform a query written in a high-level language, typically SQL, into a correct and efficient execution strategy expressed in a low-level language (implementing the relational algebra), and to execute the strategy to retrieve the required data.



An important aspect of query processing is query optimization.



# **Query Processing**



Transform a high-level query into a relational algebra query and to check whether the query is syntactically and semantically correct.

### The typical stages:

- ✓ Analysis,
- ✓ Normalization,
- ✓ Semantic analysis,
- ✓ Simplification, and
- ✓ Query restructuring.



# Query Decomposition -

### Analysis:

Select staffNumber From Staff Where position > 10;

### Staff

StaffNo	fName	IName	Position	Sex	DOB	Salary	BranchNo
SL21	John	White	Manager	M	1-Oct-45	30000	B005
SG37	Ann	Beech	Assistant	F	10-Nov-60	12000	B003
SG14	David	Ford	Supervisor	M	24-Mar-58	18000	B003
SA9	Mary	Howe	Assistant	F	19-Feb-70	9000	B007
SG5	Susan	Brand	Manager	F	3-Jun-40	24000	B003
SL41	Julie	Lee	Assistant	F	13-Jun-65	9000	B005

This query would be rejected on two grounds:

- (1) In the select list, the attribute staffNumber is not defined for the Staff relation (should be staffNo).
- (2) In the WHERE clause, the comparison ">10" is incompatible with the data type position, which is a variable character string.



# **Query Decomposition**

### **Normalization:**

- ✓ The normalization stage of query processing converts the query into a normalized form that can be more easily manipulated.
- ✓ Predicate can be converted into one of two forms:
  - Conjunctive normal form: (position= 'Manager' v salary >20000) ^ branchNo = 'B003'
  - Disjunctive normal form: (position = 'Manager' Ù branchNo = 'B003') Ú (salary >20000 Ù branchNo = 'B003')

### **Semantic analysis:**

- ✓ The objective of semantic analysis is to reject normalized queries that are incorrectly formulated or contradictory.
- ✓ For example:

the predicate (position = 'Manager' Ù position = 'Assistant') on the Staff relation > contradictory



# **Query Decomposition**

### **Simplification:**

- ✓ detect redundant qualifications,
- ✓ eliminate common subexpressions, and
- ✓ transform the query to a semantically equivalent but more easily and efficiently computed form.
- ✓ Access restrictions, view definitions, and integrity constraints are considered at this stage.
  - o introduce redundancy.
- ✓ Assuming user has appropriate access privileges, first apply well-known idempotency rules of Boolean algebra.

```
\begin{array}{ll} p\ \dot{U}\ (p) \equiv p & p\ \dot{U}\ (p) \equiv p \\ p\ \dot{U}\ false \equiv false & p\ \dot{U}\ false \equiv p \\ p\ \dot{U}\ true \equiv p & p\ \dot{U}\ true \equiv true \\ p\ \dot{U}\ (\sim\!p) \equiv false & p\ \dot{U}\ (\sim\!p) \equiv true \\ p\ \dot{U}\ (p\ \dot{U}\ q) \equiv p & p\ \dot{U}\ (p\ \dot{U}\ q) \equiv p \end{array}
```



# **Query Decomposition**

For example, consider the following integrity constraint,:

```
CREATE ASSERTION OnlyManagerSalaryHigh
CHECK ((position <> 'Manager' AND salary< 20000)
OR (position= 'Manager' AND salary> 20000));
```

and consider the effect on the query:

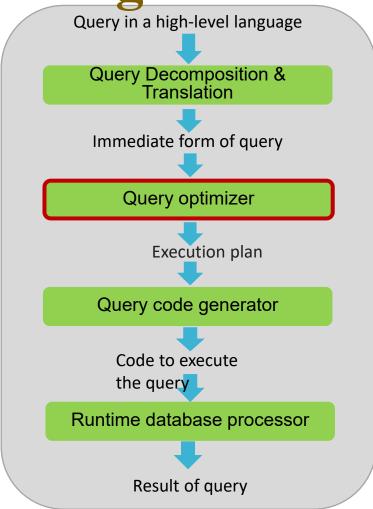
```
SELECT *
FROM Staff
WHERE (position = 'Manager' AND salary = 15000);
```

A contradiction of the integrity constraint so there can be no tuples that satisfy this predicate.

Query restructuring: the query is restructured to provide a more efficient implementation



**Query Processing** 



### Aim:

As there are many equivalent transformations of the same high-level query, choose the one that minimizes resource usage.

There are two main techniques for query optimization.

- **✓** Heuristic rules
- ✓ Systematically estimating



# **Query optimization**

### **Heuristic rules:**

✓ Uses **transformation rules** to convert one relational algebra expression into an equivalent form that is known to be more efficient.

1. Conjunctive Selection operations can cascade into individual Selection operations (and vice versa).

$$\sigma_{p \wedge q \wedge r}(R) = \sigma_p(\sigma_q(\sigma_r(R)))$$

Sometimes referred to as cascade of Selection.

$$\sigma_{\text{branchNo='B003'} \land \text{salary>15000}}(\text{Staff}) = \sigma_{\text{branchNo='B003'}}(\sigma_{\text{salary>15000}}(\text{Staff}))$$



2. Commutativity of Selection operations.

$$\sigma_{p}(\sigma_{q}(R)) = \sigma_{q}(\sigma_{p}(R))$$

For example:

$$\sigma_{\text{branchNo='B003'}}(\sigma_{\text{salary>15000}}(\text{Staff})) = \sigma_{\text{salary>15000}}(\sigma_{\text{branchNo='B003'}}(\text{Staff}))$$



3. In a sequence of Projection operations, only the last in the sequence is required.

$$\Pi_{\mathsf{L}}\Pi_{\mathsf{M}} \dots \Pi_{\mathsf{N}}(\mathsf{R}) = \Pi_{\mathsf{L}}(\mathsf{R})$$

For example:

$$\Pi_{\text{IName}}\Pi_{\text{branchNo, IName}}(\text{Staff}) = \Pi_{\text{IName}} (\text{Staff})$$



### 4. Commutativity of Selection and Projection.

If predicate p involves only attributes in projection list, Selection and Projection operations commute:

$$\Pi_{Ai_1,...,Am}(\sigma_p(R)) = \sigma_p(\Pi_{Ai_1,...,Am}(R)) \qquad \text{where } p \in \{A_1, A_2, ..., A_m\}$$

For example:

$$\Pi_{\text{fName, IName}}(\sigma_{\text{IName='Beech'}}(\text{Staff})) = \sigma_{\text{IName='Beech'}}(\Pi_{\text{fName,IName}}(\text{Staff}))$$



5. Commutativity of Theta join (and Cartesian product).

$$R \bowtie_p S = S \bowtie_p R$$
  
 $R X S = S X R$ 

Rule also applies to Equijoin and Natural join

For example:

Staff ⋈ <sub>staff.branchNo=branch.branchNo</sub> Branch = Branch ⋈ <sub>staff.branchNo=branch.branchNo</sub> Staff



### 6. Commutativity of Selection and Theta join (or Cartesian product).

If the selection predicate involves only attributes of one of the relations being joined, then the Selection and Join (or Cartesian product) operations commute:

$$\sigma_p(R \bowtie_r S) = (\sigma_p(R)) \bowtie_r S$$
  
 $\sigma_p(R \bowtie S) = (\sigma_p(R)) \bowtie S$  where  $p \in \{A_1, A_2, ..., A_n\}$ 

If selection predicate is conjunctive predicate having form (p  $\wedge$  q), where p<sub>Branch</sub> involves attributes of R, and q only attributes of S, Selection and Theta join operations commute as:

$$\sigma_{p \wedge q}(R \bowtie_r S) = (\sigma_p(R)) \bowtie_r (\sigma_q(S))$$
  
 $\sigma_{p \wedge q}(R \bowtie S) = (\sigma_p(R)) \bowtie_r (\sigma_q(S))$ 

For example:

 $σ_{position='Manager' \land city='London'}(Staff <math>\bowtie_{Staff.branchNo=Branch.branchNo} Branch) = St een 3SU$   $(σ_{position='Manager'}(Staff)) \bowtie_{Staff.branchNo=Branch.branchNo} (σ_{city='London'}(Branch)) = St een 3SU$ 

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### 7. Commutativity of Projection and Theta join (or Cartesian product).

If projection list is of form  $L = L_1 \cup L_2$ , where  $L_1$  only has attributes of R, and  $L_2$  only has attributes of S, provided join condition only contains attributes of L, Projection and Theta join commute:

$$\Pi_{\mathsf{L1} \cup \mathsf{L2}}(\mathsf{R} \bowtie_{\mathsf{r}} \mathsf{S}) = (\Pi_{\mathsf{L1}}(\mathsf{R})) \bowtie_{\mathsf{r}} (\Pi_{\mathsf{L2}}(\mathsf{S}))$$

If join condition contains additional attributes not in L (M =  $M_1 \cup M_2$  where  $M_1$  only has attributes of S), a final projection operation is required:

$$\Pi_{\mathsf{L1} \cup \mathsf{L2}}(\mathsf{R} \bowtie_{\mathsf{r}} \mathsf{S}) = \Pi_{\mathsf{L1} \cup \mathsf{L2}}((\Pi_{\mathsf{L1} \cup \mathsf{M1}}(\mathsf{R})) \bowtie_{\mathsf{r}} (\Pi_{\mathsf{L2} \cup \mathsf{M2}}(\mathsf{S})))$$

For example:

$$\Pi_{\text{position,city,branchNo}}(\text{Staff} \bowtie_{\text{Staff.branchNo=Branch.branchNo}} \text{Branch}) = (\Pi_{\text{position, branchNo}}(\text{Staff})) \bowtie_{\text{Staff.branchNo=Branch.branchNo}} (\Pi_{\text{city,}})$$

and using the latter rule:

$$\Pi_{\text{position, city}}(\text{Staff} \bowtie \text{Staff.branchNo=Branch.branchNo}) = \Pi_{\text{position, city}}((\Pi_{\text{position, branchNo}}(\text{Staff}))$$

Staff.branchNo=Branch.branchNo

(  $\Pi_{\text{city, branchNo}}$  (Branch)))



8. Commutativity of Union and Intersection (but not set difference).

$$R \cup S = S \cup R$$

$$R \cap S = S \cap R$$

9. Commutativity of Selection and set operations (Union, Intersection, and Set difference).

$$\sigma_{p}(\mathsf{R} \cup \mathsf{S}) = \sigma_{p}(\mathsf{S}) \cup \sigma_{p}(\mathsf{R})$$

$$\sigma_{p}(R \cap S) = \sigma_{p}(S) \cap \sigma_{p}(R)$$

$$\sigma_p(R - S) = \sigma_p(S) - \sigma_p(R)$$

10. Commutativity of Projection and Union.

$$\Pi_{L}(R \cup S) = \Pi_{L}(S) \cup \Pi_{L}(R)$$



### 11. Associativity of Theta join (and Cartesian product).

Cartesian product and Natural join are always associative:

$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

$$(R X S) X T = R X (S X T)$$

If join condition q involves attributes only from S and T, then Theta join is associative:

$$(R \bowtie_{p} S) \bowtie_{q \land r} T = R \bowtie_{p \land r} (S \bowtie_{q} T)$$

For example:

(Staff ⋈ Staff.staffNo=PropertyForRent.staffNo PropertyForRent) ⋈ ownerNo=Owner.ownerNo ∧ staff.lName=Owner.lName

Owner = Staff ⋈ staff.staffNo = PropertyForRent.staffNo ∧ staff.lName=lName (PropertyForRent ⋈ ownerNo Owner)



12. Associativity of Union and Intersection (but not Set difference).

$$(R \cup S) \cup T = S \cup (R \cup T)$$

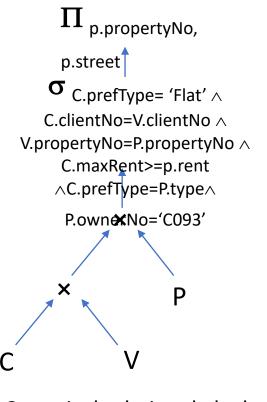
$$(R \cap S) \cap T = S \cap (R \cap T)$$

# **Example: Use of Transformation Rules**

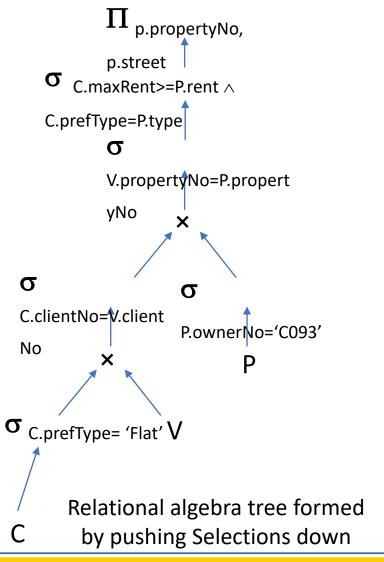
For prospective renters of flats, find properties that match requirements and owned by CO93.

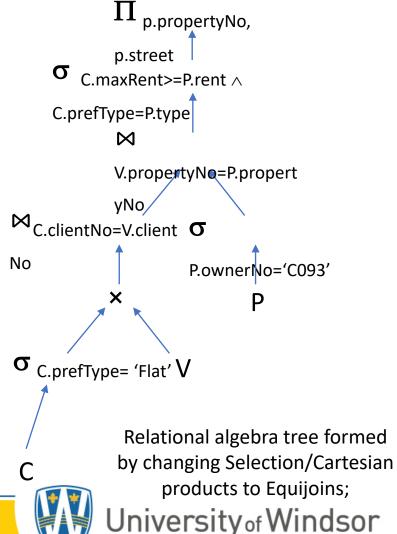
```
\Pi_{\text{p.propertyNo, p.street}} (\sigma_{\text{c.prefType= 'Flat'} \land \text{c.clientNo=v.clientNo} \land} \\ \text{v.propertyNo=p.propertyNo} \land \text{c.maxRent>=p.rent} \land \\ \text{c.prefType=p.type} \land \text{p.ownerNo='C093'} ((c \times v) \times p))
```

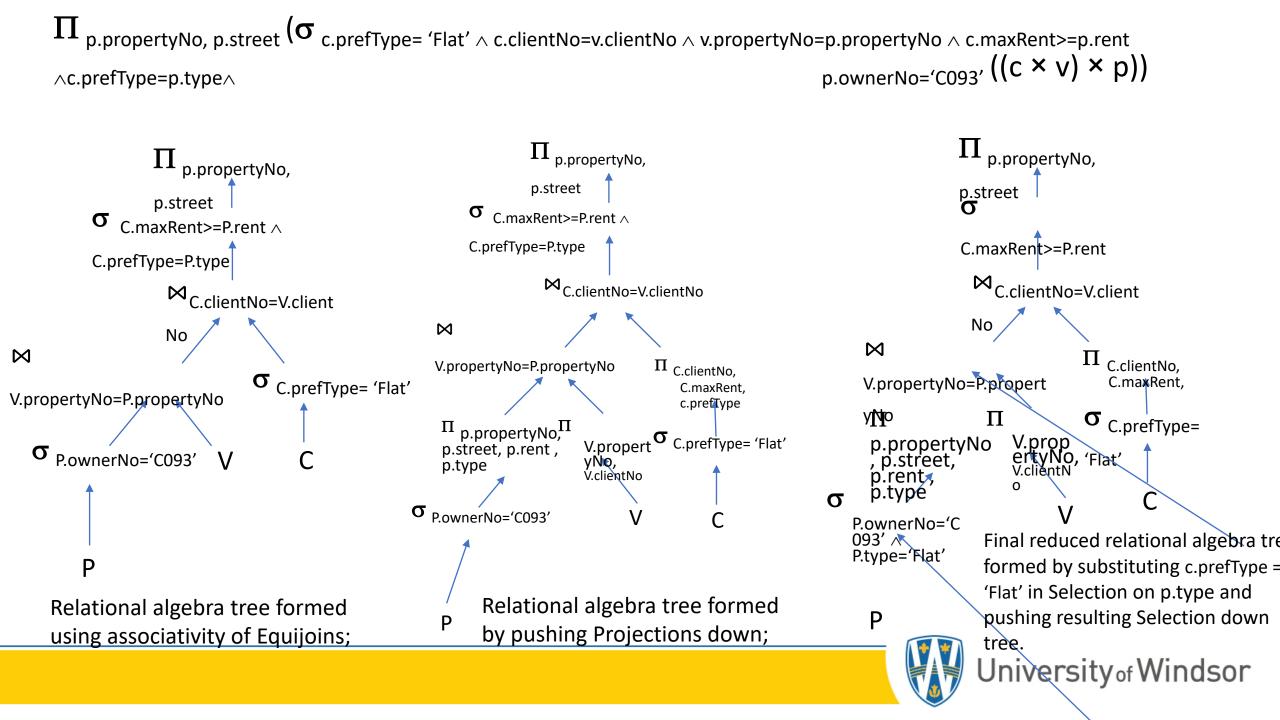




Canonical relational algebra tree







# Heuristical Processing Strategies

- 1. Perform Selection operations as early as possible.
  - ✓ Keep predicates on same relation together.
- 2. Combine Cartesian product with subsequent Selection whose predicate represents join condition into a Join operation.

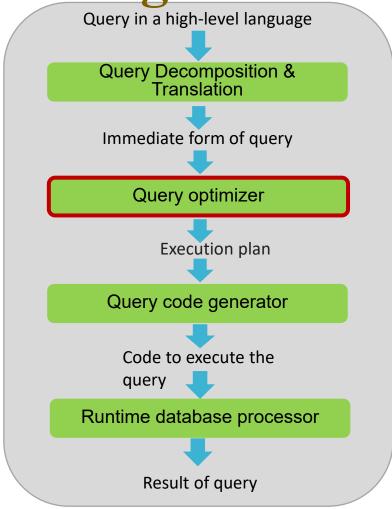
$$\sigma_{R.a \theta S.b}(RXS) = R \bowtie_{R.a \theta S.b} (S)$$

$$(R \bowtie_{R.a \theta S.b} S) \bowtie_{S.c \theta T.d} T$$

- 3. Use associativity of binary operations to rearrange leaf nodes so leaf nodes with most restrictive Selection operations executed first.
- 4. Perform Projection as early as possible.
  - ✓ Keep projection attributes on same relation together.
- 5. Compute common expressions once.
  - ✓ If common expression appears more than once, and result not too large, store result and reuse it when required.
  - ✓ Useful when querying views, as same expression is used to construct view each time.



**Query Processing** 



### Aim:

As there are many equivalent transformations of the same high-level query, choose the one that minimizes resource usage.

There are two main techniques for query optimization.

- ✓ Heuristic rules
- ✓ Systematically estimating



# Cost Estimation for the Relational Algebra Operations

- Many different ways of implementing Relational Algebra (RA) operations.
- Aim of Query Optimization(QO) is to choose most efficient one.
   Use formulae that estimate costs for a number of options and select one with lowest cost.
- Consider only cost of disk access, which is usually dominant cost in QP.
- Many estimates are based on cardinality of the relation, so need to be able to estimate this.



# **Database Statistics**

The success of estimating the size and cost of intermediate relational algebra operations depends on the amount and currency of the statistical information that the DBMS holds.

### For each base relation R:

- ✓ nTuples(R)- the number of tuples (records) in relation R (that is, its cardinality).
- ✓ bFactor(R)- the blocking factor of R (that is, the number of tuples of R that fit into one block).
- ✓ nBlocks(R)- the number of blocks required to store R.

### For each attribute A of base relation R:

- $\checkmark$  nDistinct<sub>A</sub>(R)- the number of distinct values that appear for attribute A in relation R.
- $\checkmark$  min<sub>A</sub>(R), max<sub>A</sub>(R)- the minimum and maximum possible values for the attribute A in relation R.
- $\checkmark$  SC<sub>A</sub>(R)—the selection cardinality of attribute A in relation R.

### For each multilevel index I on attribute set A:

- $\checkmark$  nLevels<sub>A</sub>(I)—the number of levels in I.
- ✓ nLfBlocks<sub>A</sub>(I)—the number of leaf blocks in I.



# Selection Operation (S = $\sigma_p(R)$ )

Predicate may be simple or composite.

Number of different implementations, depending on file structure, and whether attribute(s) involved are indexed/hashed.

### Main strategies are:

- 1. Linear Search (Unordered file, no index): [nBlocks(R)/2], for equality condition on key attribute nBlocks(R), otherwise
- Binary Search (Ordered file, no index): [log<sub>2</sub> (nBlocks(R))], for equality condition on ordered attribute [log<sub>2</sub> (nBlocks(R))] + [SC<sub>A</sub> (R)/bFactor(R)] 1, otherwise
- 3. Equality on hash key: 1, assuming no overflow
- Equality condition on primary key: nLevels<sub>A</sub> (I) + 1
- 5. Inequality condition on primary key: nLevels<sub>A</sub> (I) + [nBlocks(R)/2]
- 6. Equality condition on clustering (secondary) index:  $nLevels_A(I) + [SC_A(R)/bFactor(R)]$
- 7. Equality condition on a non-clustering (secondary) index: nLevels<sub>A</sub>(I) + [SC<sub>A</sub>(R)]
- 8. Inequality condition on a secondary B+-tree index:  $nLevels_A(I) + [nLfBlocks_A(I)/2 + nTuples(R)/2] nLevels_A(I) + 1$



# Selection Operation (S = $\sigma_p(R)$ )

Cost estimation for Selection operation:

We make the following assumptions about the Staff relation:

There is a hash index with no overflow on the primary key attribute staffNo.

There is a clustering index on the foreign key attribute branchNo.

There is a B+-tree index on the salary attribute.

The Staff relation has the following statistics stored in the system catalog:

```
\begin{array}{ll} \text{nTuples(Staff)} = 3000 \\ \text{bFactor(Staff)} = 30 \\ \text{nDistinct}_{\text{branchNo}}(\text{Staff}) = 500 \\ \text{nDistinct}_{\text{position}}(\text{Staff}) = 10 \\ \text{nDistinct}_{\text{salary}}(\text{Staff}) = 500 \\ \text{min}_{\text{salary}}(\text{Staff}) = 10,000 \\ \text{nLevels}_{\text{branchNo}}(\text{I}) = 2 \\ \text{nLevels}_{\text{salary}}(\text{I}) = 2 \\ \end{array} \begin{array}{ll} \Rightarrow \text{nBlocks(Staff)} = 100 \\ \Rightarrow \text{SC}_{\text{branchNo}}(\text{Staff}) = 6 \\ \Rightarrow \text{SC}_{\text{position}}(\text{Staff}) = 300 \\ \Rightarrow \text{SC}_{\text{salary}}(\text{Staff}) = 6 \\ \text{max}_{\text{salary}}(\text{Staff}) = 50,000 \\ \text{nLfBlocks}_{\text{salary}}(\text{I}) = 50 \\ \end{array}
```

The estimated cost of a linear search on the key attribute staffNo is 50 blocks,

The cost of a linear search on a non-key attribute is 100 blocks.

Consider the following Selection operations:

S1:  $\sigma_{\text{staffNo='SG5'}}(\text{Staff})$ 

Equality condition on the primary key. the attribute staffNo is hashed, estimate the cost as 1 block. The estimated cardinality of the result relation is  $SC_{staffNo}(Staff) = 1$ .

S2:  $\sigma_{position='manager'}$ (Staff)

The attribute in the predicate is a non-key, non-indexed attribute, so we cannot improve on the linear search method, giving an estimated cost of 100 blocks. The estimated cardinality of the result relation is  $SC_{position}(Staff) = 300$ 



# Join Operation $(T = (R \bowtie_{F}S))$

The most time-consuming operation to process. The main strategies for implementing the Join operation.

✓ Block Nested Loop Join:

```
nBlocks(R) 1 (nBlocks(R) * nBlocks(S)), if buffer has only one block for R and S nBlocks(R) 1 [nBlocks(S)*(nBlocks(R)/(nBuffer 2 2))], if (nBuffer 2 2) blocks for R nBlocks(R) 1 nBlocks(S), if all blocks of R can be read into database buffer
```

✓ Indexed Nested Loop Join:

```
Depends on indexing method; for example:

nBlocks(R) 1 nTuples(R)*(nLevelsA (I) 1 1), if join attribute A in S is the primary key

Blocks(R) 1 nTuples(R)*(nLevelsA (I) 1 [SCA (R)/bFactor(R)]), for clustering index I on
attribute A
```

✓ Sort-Merge Join:

```
nBlocks(R)*[log2 (nBlocks(R)] 1 nBlocks(S)*[log2 (nBlocks(S)], for sorts nBlocks(R) 1 nBlocks(S), for merge
```

✓ Hash Join:

```
3(nBlocks(R) 1 nBlocks(S)), if hash index is held in memory 2(nBlocks(R) 1 nBlocks(S))*[lognBuffer–1 (nBlocks(S)) 2 1] 1 nBlocks(R) 1 nBlocks(S), otherwise
```



# Projection Operation(S = $\Pi_{A1,A2,...,Am}(R)$ )

To implement projection, need to:

- ✓ Remove attributes that are not required;
- ✓ Eliminate any duplicate tuples produced from previous step.

Estimating the cardinality of the Projection operation:

When the Projection contains a key attribute: the cardinality of the Projection is: nTuples(S) = nTuples(R)

If the Projection consists of a single non-key attribute ( $S = \Pi_A(R)$ ), we can estimate the cardinality of the Projection as:  $nTuples(S) = SC_A(R)$ 

Two main approaches to eliminating duplicates:

- ✓ Sorting;
- ✓ Hashing.



# The Relational Algebra Set Operations(T = R $\cup$ S, T = R $\cap$ S, T = R - S)

Implemented by

- ✓ sorting both relations on same attributes, and
- ✓ then scanning through each of sorted relations once to obtain desired result.

For all these operations, we could develop an algorithm using the sort–merge join algorithm as a basis.

The estimated cost in all cases is simply: nBlocks(R) + nBlocks(S) + nBlocks(R)\*[log<sub>2</sub> (nBlocks(R))]

+ nBlocks(S)\*[log<sub>2</sub> (nBlocks(S))]



# **Any Questions**

