### Algorithms Introduction



**SoftUni Team Technical Trainers** 







**Software University** 

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#### Have a Question?



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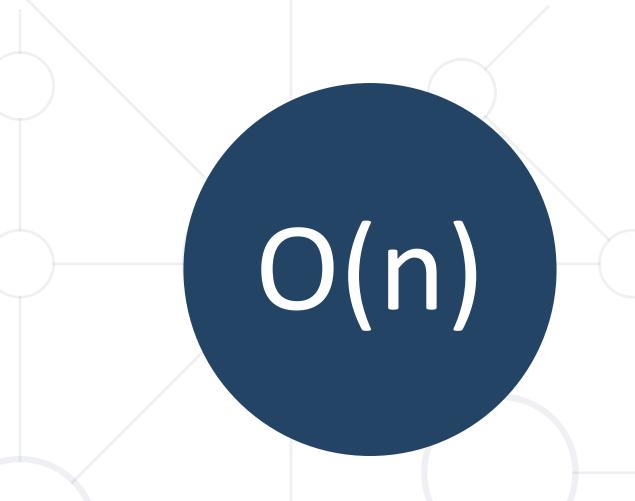
# #python-advanced

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  - Selection Sort
  - Bubble Sort
  - Insertion Sort





# **Algorithmic Complexity**

**Asymptotic Notation** 

#### **Algorithm Analysis**



- Why should we analyze algorithms?
  - Predict the resources the algorithm will need
    - Computational time (CPU consumption)
    - Memory space (RAM consumption)
    - Communication bandwidth consumption
    - Hard disk operations

#### **Get Number of Steps**



Calculate maximum steps to find the result

```
def get_operations_count(n):
    counter = 0
    for i in range(n):
        for j in range(n):
            counter += 1
    return counter
```

```
Solution:

T(n) = 3(n ^ 2) + 3n + 3
```

The input(n) of the function is the main source of steps growth

#### **Simplifying Step Count**



- Some parts of the equation grow much faster than others
  - $T(n) = 3(n^2) + 3n + 3$
  - We can ignore some part of this equation
  - Higher terms dominate lower terms -n > 2,  $n^2 > n$ ,  $n^3 > n^2$
  - Multiplicative constants can be omitted  $12n \rightarrow n$ ,  $2n^2 \rightarrow n^2$
- The previous solution becomes ≈ n²

#### **Time Complexity**

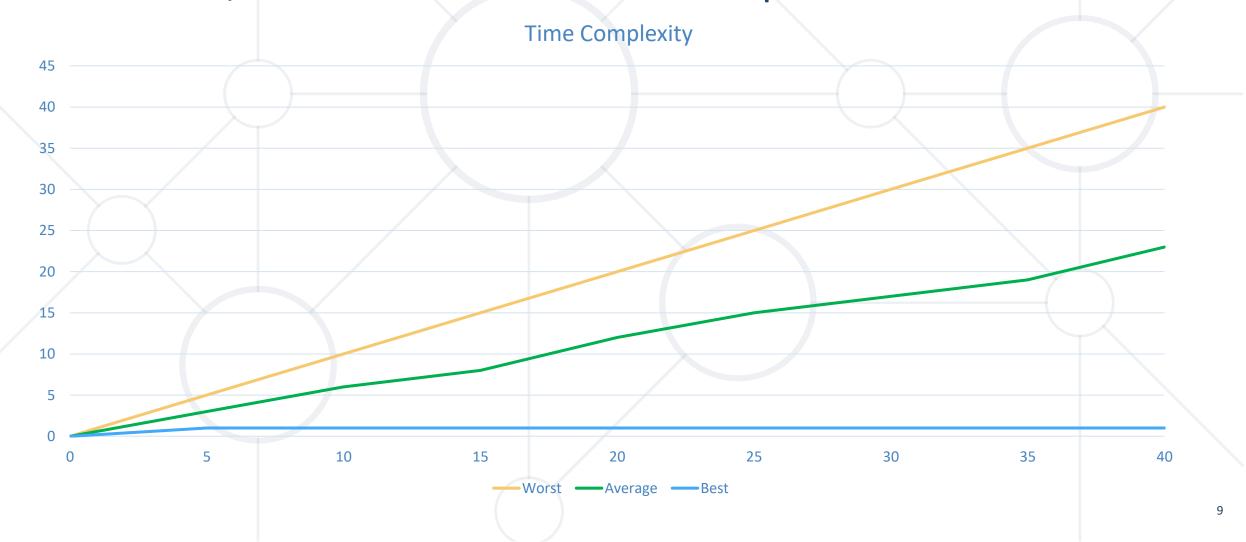


- Worst-case
  - An upper bound on the running time
- Average-case
  - Average running time
- Best-case
  - The lower bound on the running time (the optimal case)

#### **Time Complexity**



Therefore, we need to measure all the possibilities:



#### **Time Complexity**



- From the previous chart we can deduce:
  - For smaller size of the input (n) we don't care much for the runtime
  - So we measure the time as n approaches infinity
  - If an algorithm must scale, it should compute the result within a finite and practical time
  - We're concerned about the order of an algorithm's complexity,
     not the actual time in terms of milliseconds

#### **Asymptotic notations**







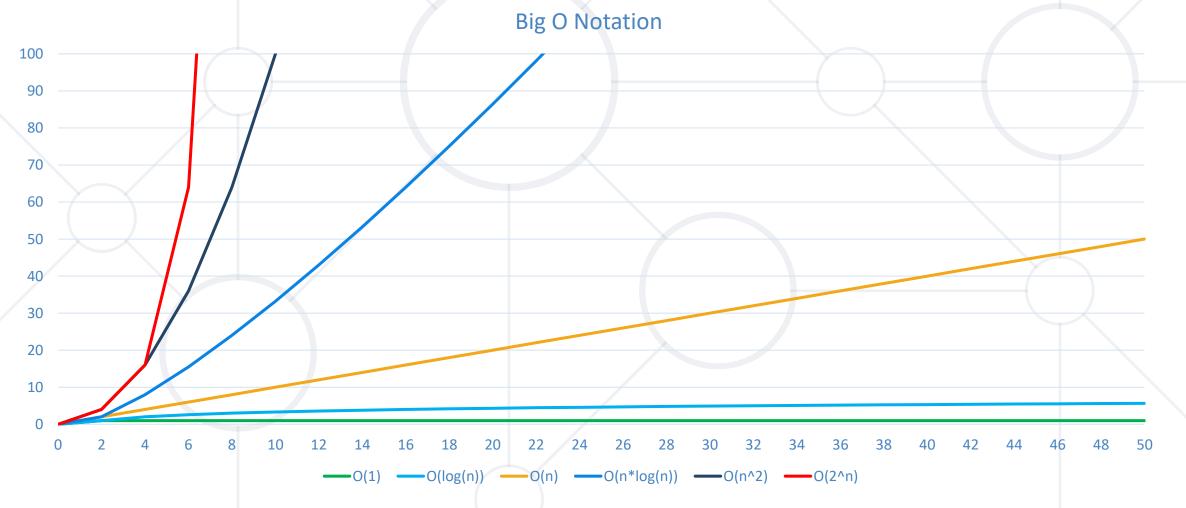
- Big O O(f(n))
- Big Theta Θ(f(n))
- Big Omega  $\Omega(f(n))$



#### **Asymptotic Functions**



Below are some examples of common algorithmic grow:



#### **Typical Complexities**

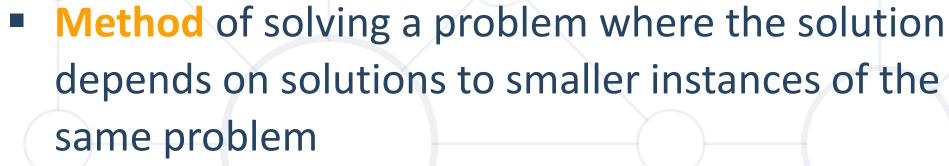


Complexity	Notation	Description
constant	O(1)	n = 1 000 $\rightarrow$ 1-2 operations
logarithmic	O(log n)	$n = 1000 \rightarrow 10$ operations
linear	O(n)	n = 1 000 → 1 000 operations
linearithmic	O(n*log n)	n = 1 000 $\rightarrow$ 10 000 operations
quadratic	O(n2)	n = 1 000 → 1 000 000 operations
cubic	O(n3)	n = 1 000 → 1 000 000 000 operations
exponential	O(n^n)	n = 10 → 10 000 000 000 operations



#### What is Recursion?





 A common computer programing tactic is to divide a problem into sub-problems of the same type as the original, solve those sub-problems, and combine the results



#### What is Recursion?



- A function or a method that calls itself one or more times until a specified condition is met
  - After the recursive call the rest code is processed from the last one called to the first



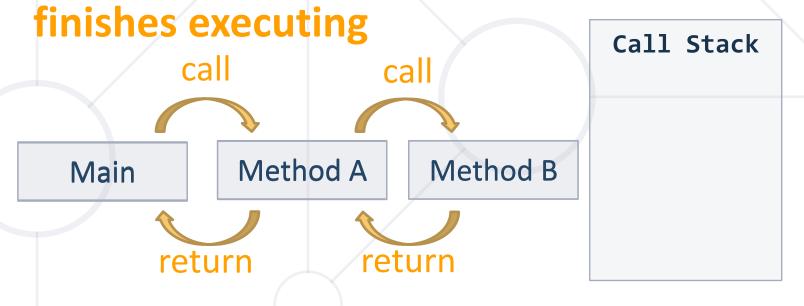


#### **Call Stack**





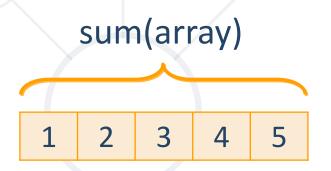
 Keeps track of the point to which each active subroutine should return control when it

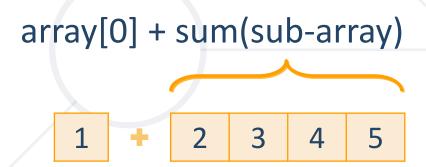


#### **Other Definition**



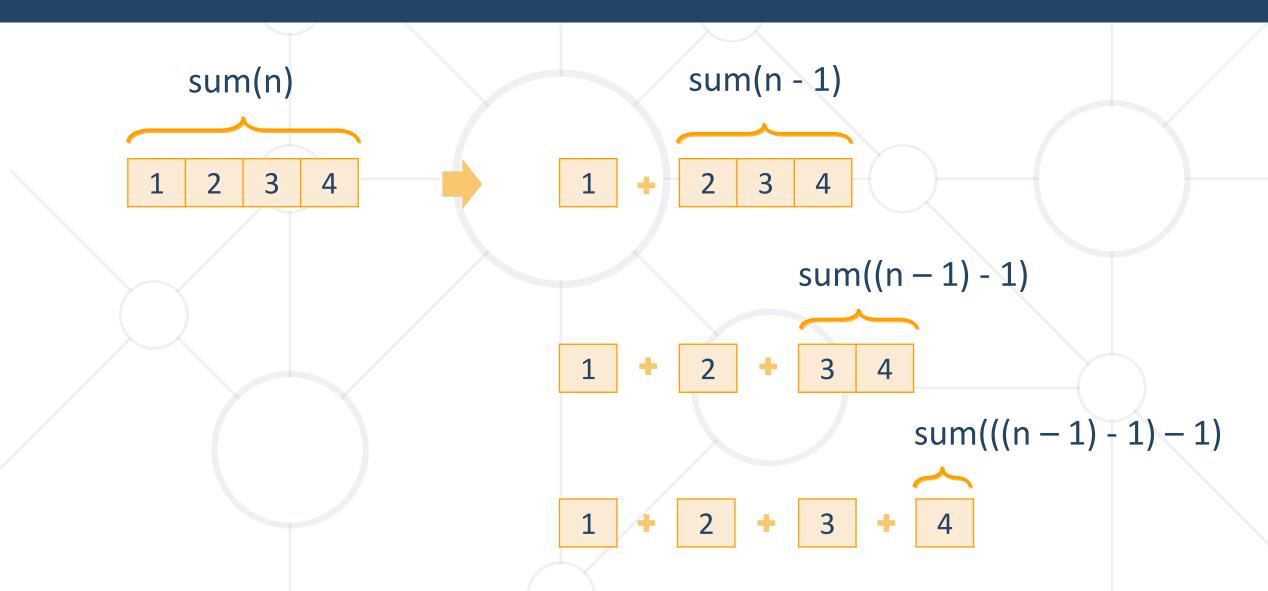
- Problem solving technique (In CS)
  - Involves a function calling itself
  - The function should have a base case
  - Each step of the recursion should move towards the base case





#### Array Sum – Example

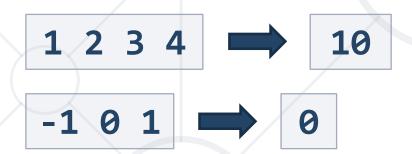




#### **Problem: Recursive Array Sum**



- Create a recursive method that
  - Finds the sum of all numbers stored in an array
  - Read numbers from the console



#### **Solution: Recursive Array Sum**



```
def calc_sum(numbers, idx):
    if idx == len(numbers) - 1:
        Base case
    return numbers[idx]

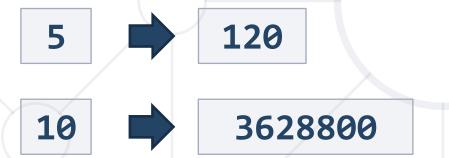
return numbers[idx] + calc_sum(numbers, idx + 1)
```

**Recursive call** 

#### **Problem: Recursive Factorial**



- Create a recursive method that calculates n!
  - Read n from the console



#### **Recursive Factorial – Example**



Recursive definition of n! (n factorial):

#### **Solution: Recursive Factorial**



```
def get_factorial(num):
    if num == 0:
        return 1

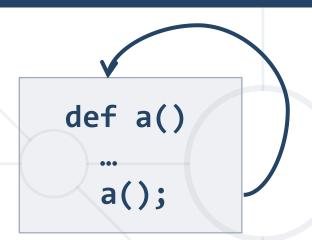
    return num * get_factorial(num - 1)

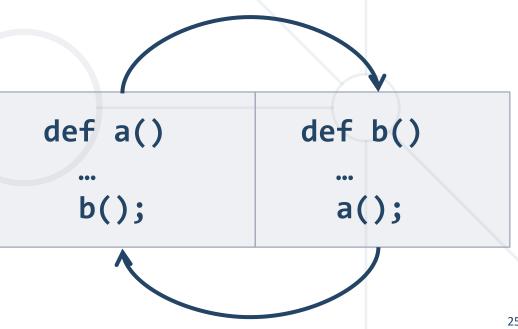
        Recursive call
```

#### **Direct and Indirect Recursion**



- Direct recursion
  - A method directly calls itself
- **Indirect recursion** 
  - Method A calls B, method B calls A
  - Or even  $A \rightarrow B \rightarrow C \rightarrow A$





#### **Recursion Pre-Actions and Post-Actions**



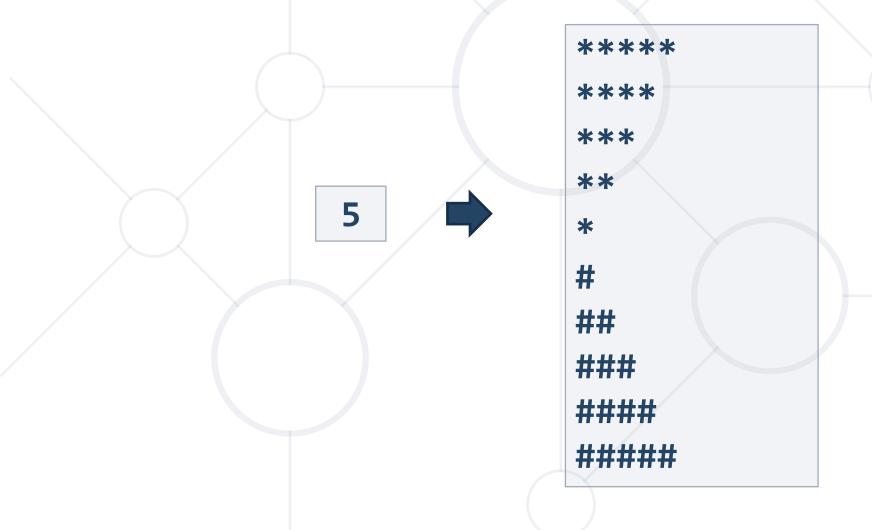
- Recursive methods have three parts:
  - Pre-actions (before calling the recursion)
  - Recursive calls (step-in)
  - Post-actions (after returning from recursion)

```
def recursion()
  # Pre-actions
  recursion()
  # Post-actions
```

#### **Problem: Recursive Drawing**



Create a recursive method that draws the following figure



#### **Pre-Actions and Post-Actions – Example**



```
def print_figure(n):
    if n <= 0:
        return
    # TODO: Pre-action: print n asterisks
    # Recursive call
    print_figure(n - 1)
    # TODO: Post-action: print n hashtags
```

#### Performance: Recursion vs. Iteration



- Recursive calls are slower
- Parameters and return values travel through the stack
- Good for branching problems

```
def fact(n):
    if n == 0:
        return 1
    return n * fact(n - 1)
```

- No function call cost
- Creates local variables
- Good for linear problems (no branching)

```
def fact(n):
    result = 1
    for i in range(1, n + 1):
        result *= i
    return result
```







- Trying all possible combinations
- Picking the best solution
- Usually slow and inefficient



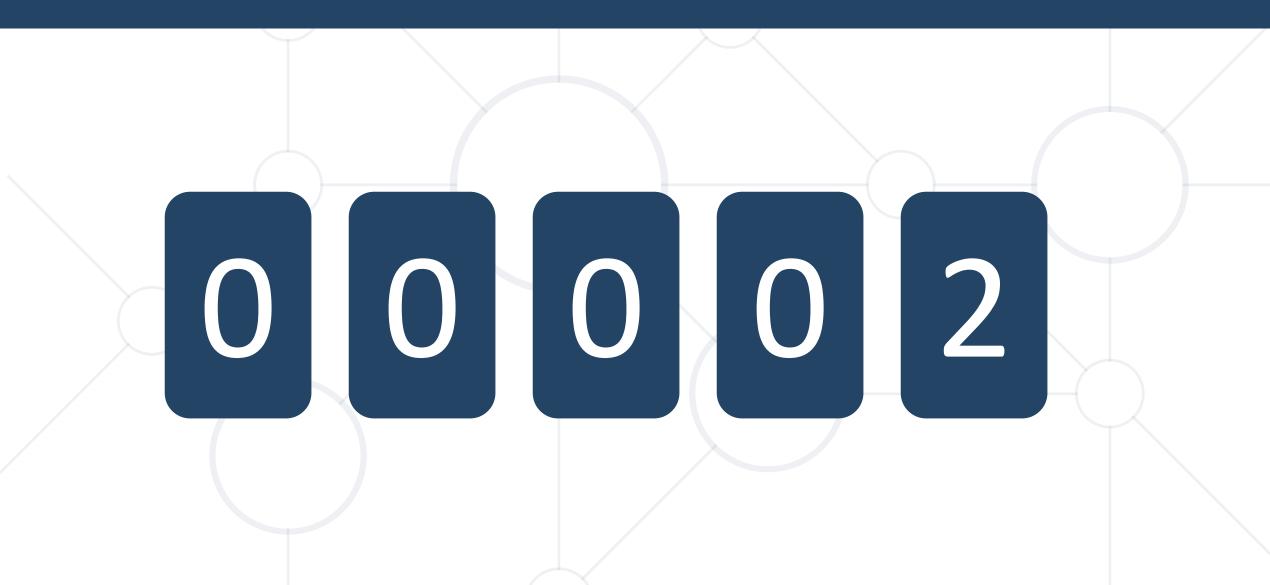














# 99999

 $10 \times 10 \times 10 \times 10 \times 10 = 100,000$  combinations



**Greedy Algorithms** 

## **Greedy Algorithms**





- Usually more efficient than the other algorithms
- Can produce a non-optimal (incorrect) result
- Pick the best local solution
  - The optimum for a current position and point of view
- Greedy algorithms assume that always choosing a local optimum leads to the global optimum



## **Optimization Problems**



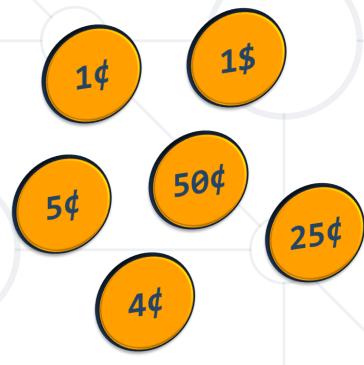
- Finding the best solution from all possible solutions
- Examples:
  - Find the shortest path from Sofia to Varna
  - Find the maximum increasing subsequence
  - Find the shortest route that visits each city and returns to the origin city



#### **Problem: Sum of Coins**



- Write a program, which gathers a sum of money, using the least possible number of coins
- Consider the US currency coins
  - **0.01**, 0.02, 0.05, 0.10
- Greedy algorithm for "Sum of Coins":
  - Take the largest coin while possible
  - Then take the second largest
  - etc.

























# **Greedy Failure Cases**

































#### **Solution: Sum of Coins**



```
def choose_coins(coins, target_sum):
    coins.sort(reverse=True)
    index = 0
    used_coins = {}
    while target_sum != 0 and index < len(coins):</pre>
   # Next slide
coin_input = input("Coins: ")
coins = list(map(int, coin_input.split(", ")))
target_sum = int(input("Sum: "))
print(choose coins(coins, target sum))
```

#### **Solution: Sum of Coins**



```
while target sum != 0 and index < len(coins):
       count_coins = target_sum // coins[index]
       target_sum %= coins[index]
       if count_coins > 0:
           used coins[coins[index]] = count coins
       index += 1
   if target_sum != 0:
       return "Error"
   else:
       # Sum found
```

#### **Problem: Set Cover**



- Write a program that finds the smallest subset of S, the union of which = U (if it exists)
- You will be given a set of integers U called "the Universe"
- And a set S of n integer sets whose union = U

```
Universe: 1, 2, 3, 4, 5
Number of sets: 4

1
2, 4
5
3
```

#### **Solution: Set Cover**



```
def set_cover(universe, sets):
    universe_set = set(universe)
    chosen_sets = []
    while universe_set:
   // Next slide
    return chosen_sets
universe_input = input("Universe: ")
num_sets = int(input("Number of sets: "))
```

#### **Solution: Set Cover**



```
while universe_set:
    best_set = max(sets, key=lambda s: len(universe_
set.intersection(s)))
    chosen_sets.append(best_set)
    universe_set -= set(best_set)

return chosen_sets
```

#### **Solution: Set Cover**



```
result = set cover(universe, sets)
for i in range(len(result)):
    result[i] = sorted(result[i])
print("\nSets to take ({}):".format(len(result)))
for s in result:
    print("{", ", ".join(map(str, s)), "}")
```



## **Searching Algorithms**

Linear and Binary Search

## **Search Algorithm**



- Search algorithm an algorithm for finding an item with specified properties among a collection of items
- Different types of searching algorithms:
  - For sub-structures of a given structure
    - A graph, a string, a finite group
  - Search for the min / max of a function, etc.

#### Linear Search



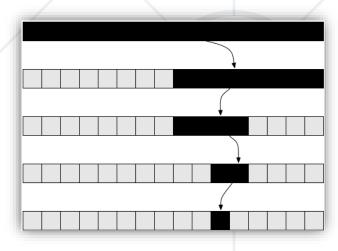
- Linear search finds a particular value in a list
  - Checking every one of the elements
  - One at a time, in sequence
  - Until the desired one is found
- Worst & average performance: O(n)

for each item in the list:
 if that item has the desired value,
 return the item's location
return nothing

## **Binary Search**



- Binary search finds an item within an ordered data structure
- At each step, compare the input with the middle element
  - The algorithm repeats its action to the left or right sub-structure
- Average performance: O(log(n))
- See the <u>visualization</u>



## **Binary Search (Iterative)**



```
def binary_search(numbers, target):
    left = 0
    right = len(numbers) - 1
    while left <= right:
        mid_idx = (left + right) // 2
        mid_el = numbers[mid_idx]
        if mid_el == target:
            return mid_idx
        if mid_el < target:</pre>
            left = mid_idx + 1
        else:
            right = mid_idx - 1
    return -1
```



## Simple Sorting Algorithms

Selection, Bubble and Insertion Sort

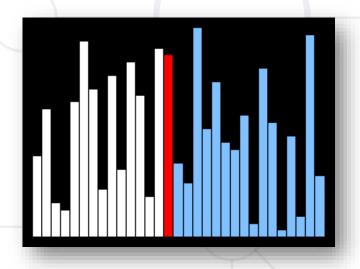
## What is a Sorting Algorithm?



- Sorting algorithm
  - An algorithm that rearranges elements in a list
    - In non-decreasing order
  - Elements must be comparable
- More formally
  - The input is a sequence / list of elements



In non-decreasing order



## **Sorting – Example**



- Efficient sorting algorithms are important for:
  - Producing human-readable output
  - Canonicalizing data making data uniquely arranged
  - In conjunction with other algorithms, like binary searching
- Example of sorting:



## **Sorting Algorithms: Classification**

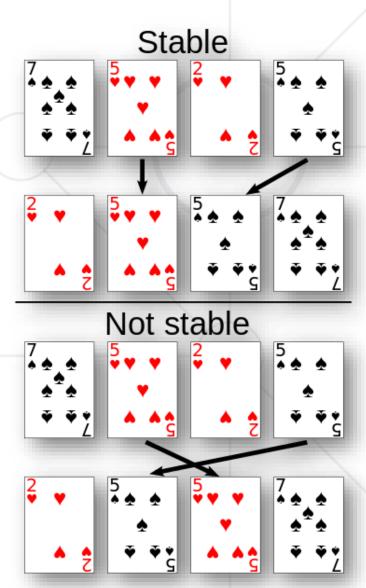


- Sorting algorithms are often classified by:
  - Computational complexity and memory usage
    - Worst, average and best-case behavior
  - Recursive / non-recursive
  - Stability stable / unstable
  - Comparison-based sort / non-comparison based

## Stability of Sorting



- Stable sorting algorithms
  - Maintain the order of equal elements
  - If two items compare as equal, their relative order is preserved
- Unstable sorting algorithms
  - Rearrange the equal elements in unpredictable order
- Often different elements have the same key used for equality comparing



#### **Selection Sort**



- Selection sort simple, but inefficient algorithm
  - Swap the first with the min element on the right, then the second, etc.
  - Memory: 0(1)
  - Time: O(n²)
  - Stable: No
  - Method: Selection



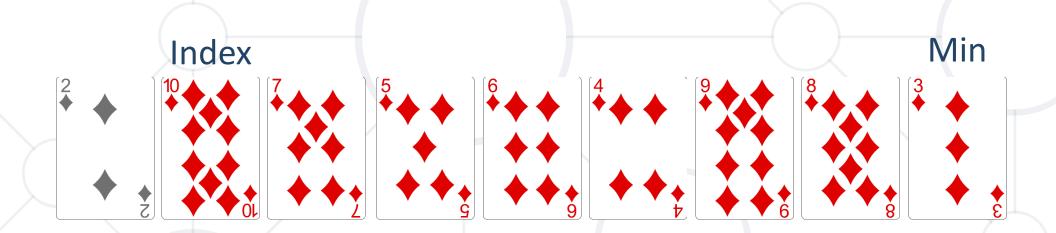
#### **Selection Sort Visualization**





## **Selection Sort Visualization**

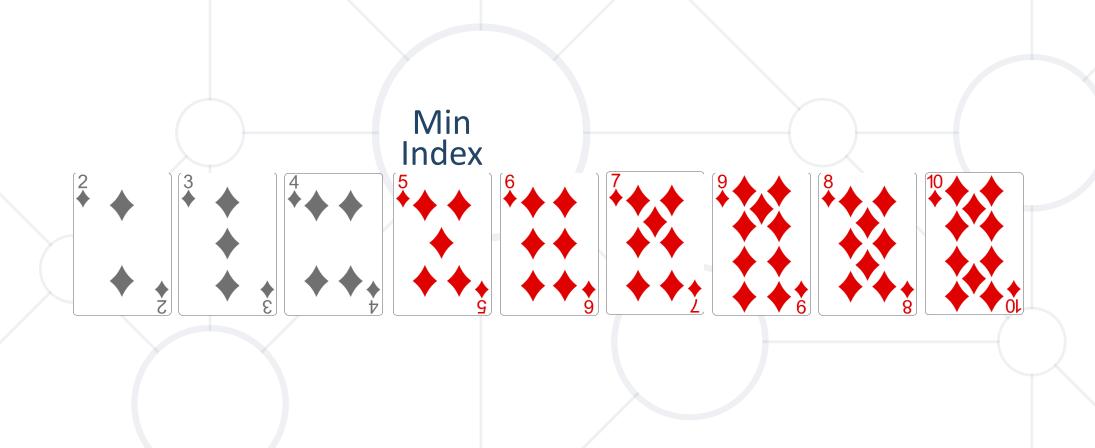








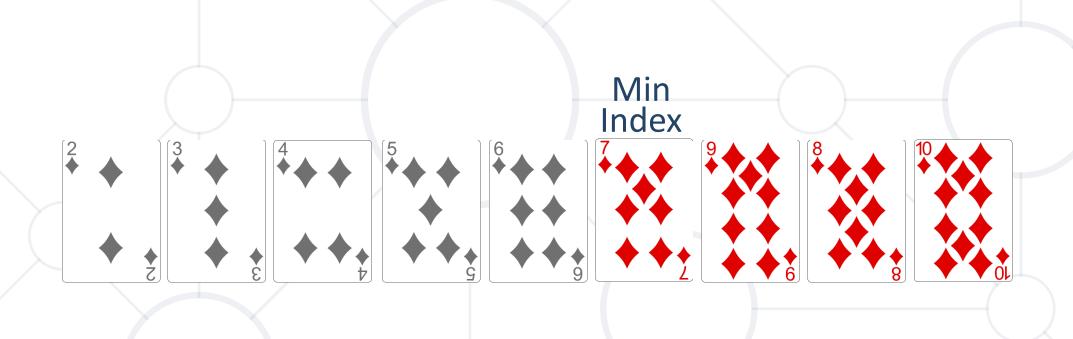




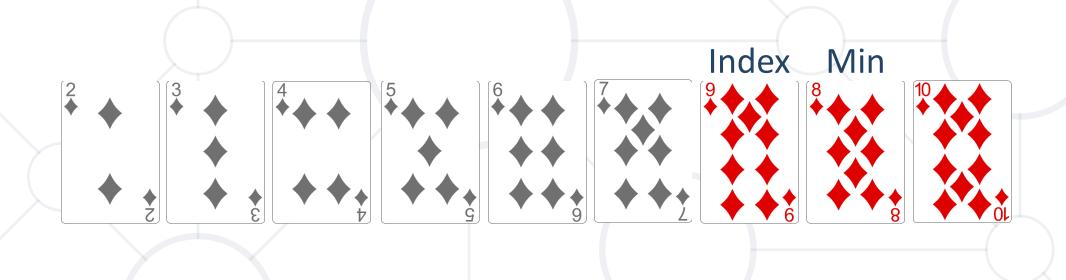




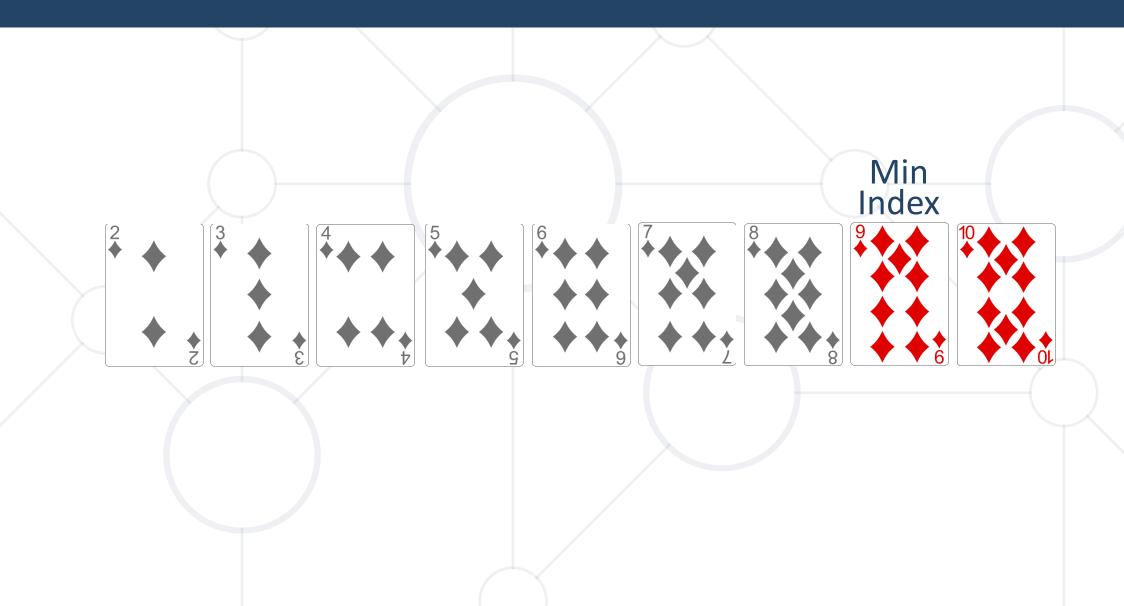




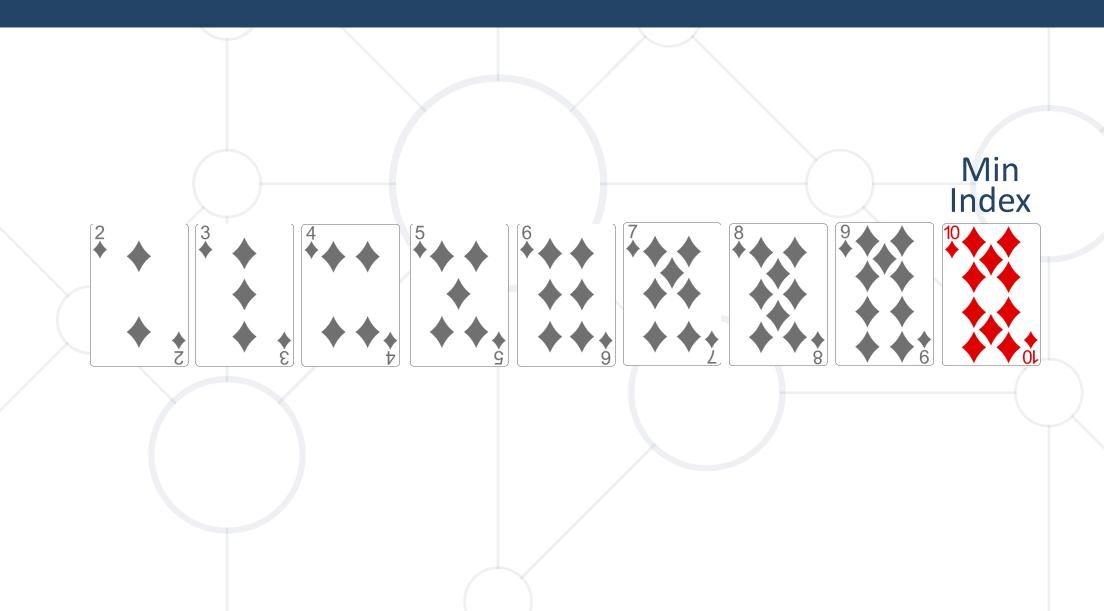




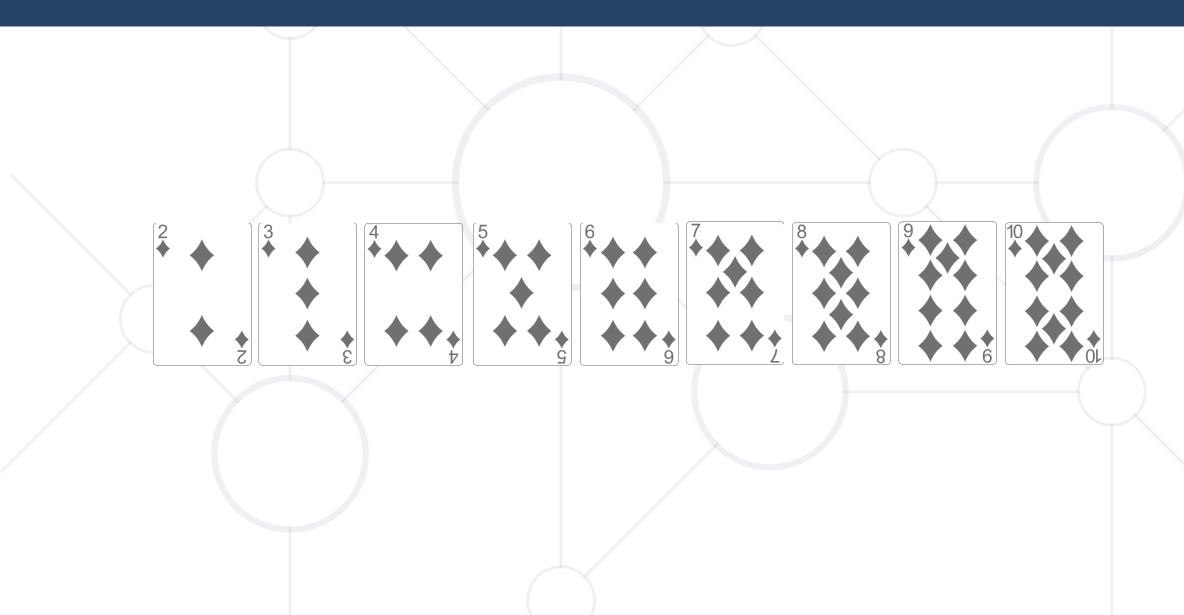




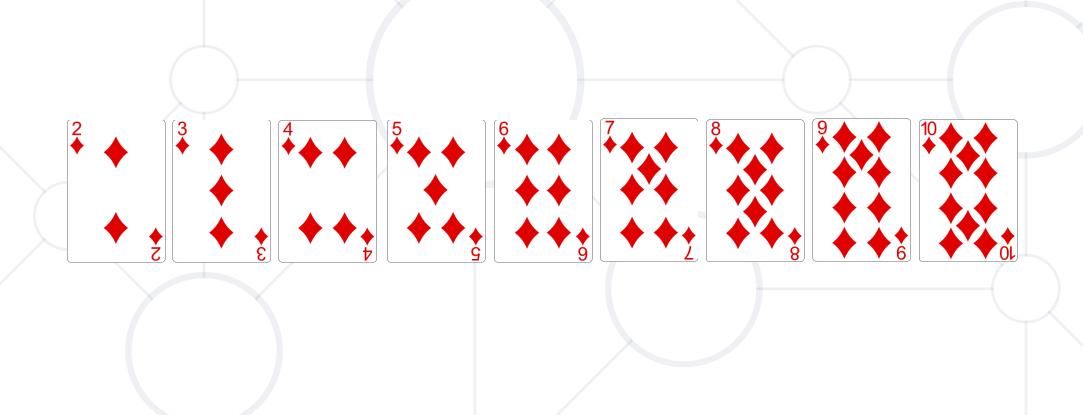












#### **Selection Sort**



```
def selection_sort(nums):
    for idx in range(len(nums)):
        min idx = idx
        for curr_idx in range(idx + 1, len(nums)):
            if nums[curr_idx] < nums[min_idx]:</pre>
                min_idx = curr_idx
        nums[idx], nums[min_idx] = nums[min_idx], nums[idx]
```

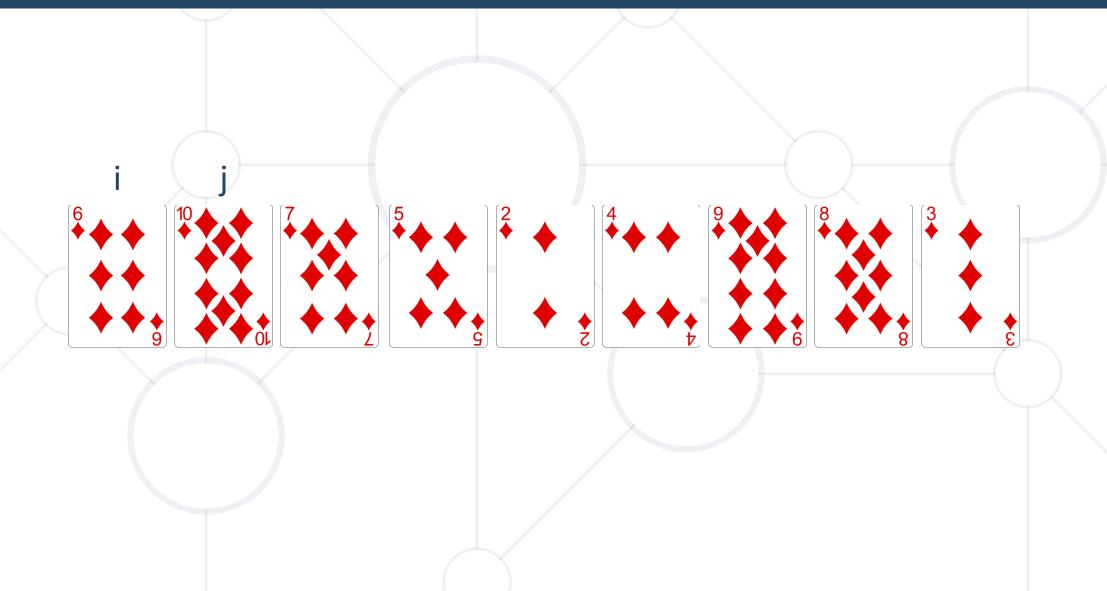
#### **Bubble Sort**



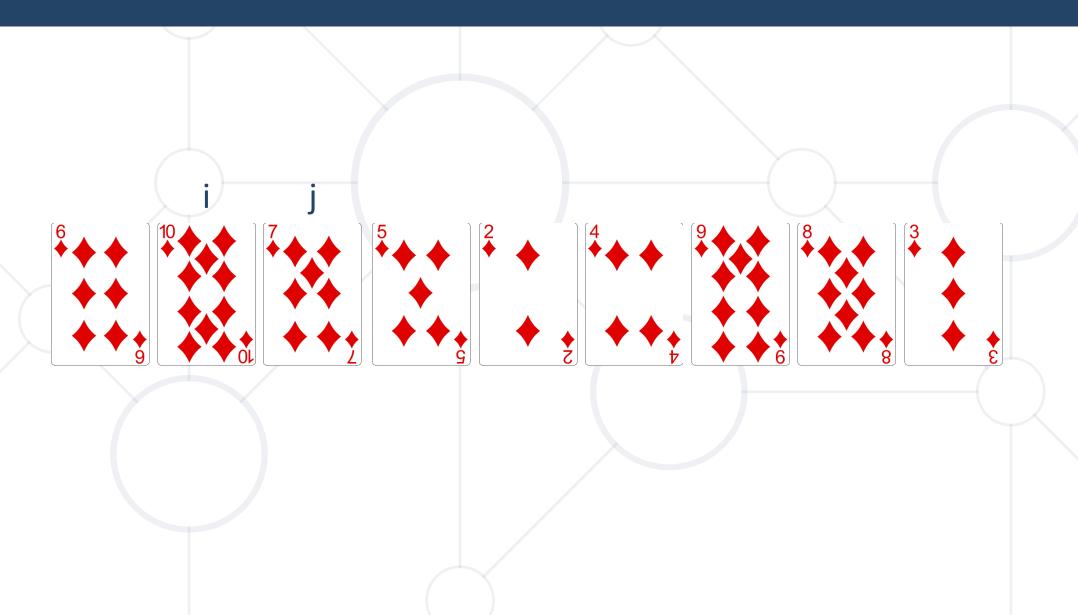
- Bubble sort simple, but inefficient algorithm
- Swaps to neighbor elements when not in order until sorted
  - Memory: 0(1)
  - Time: O(n²)
  - Stable: Yes
  - Method: Exchanging



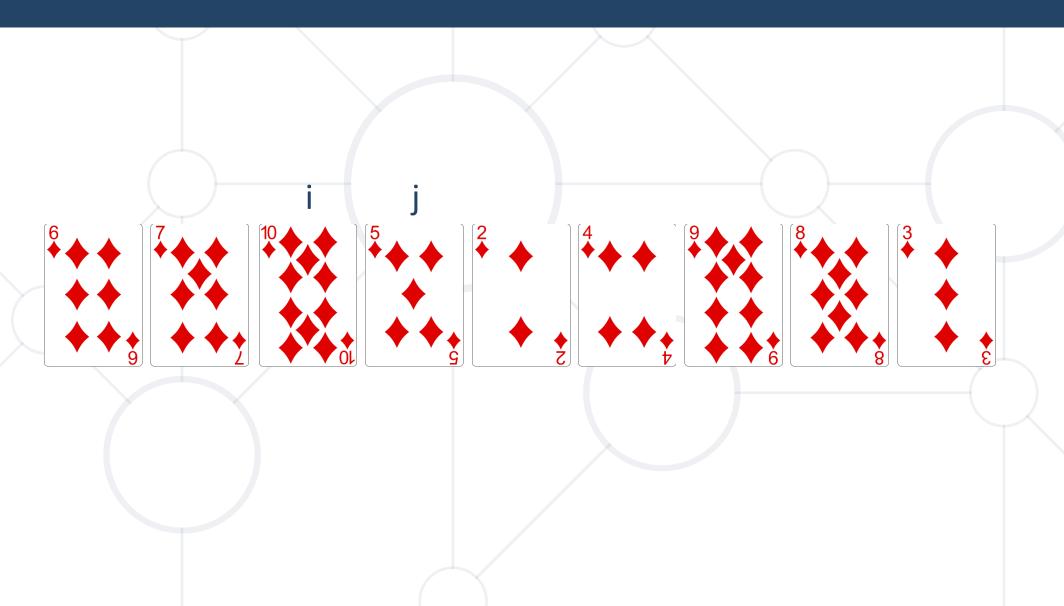




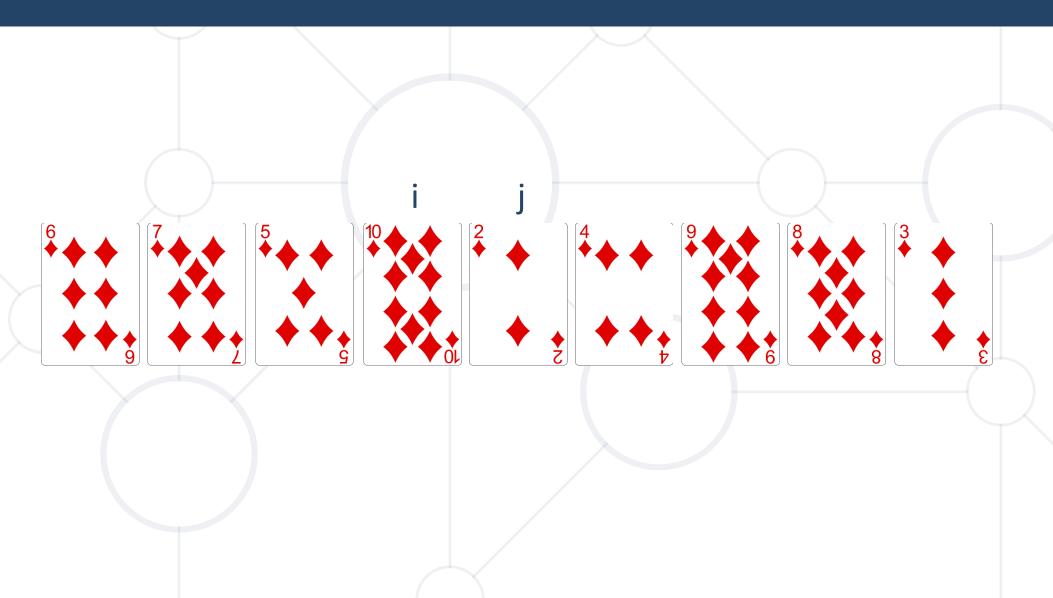




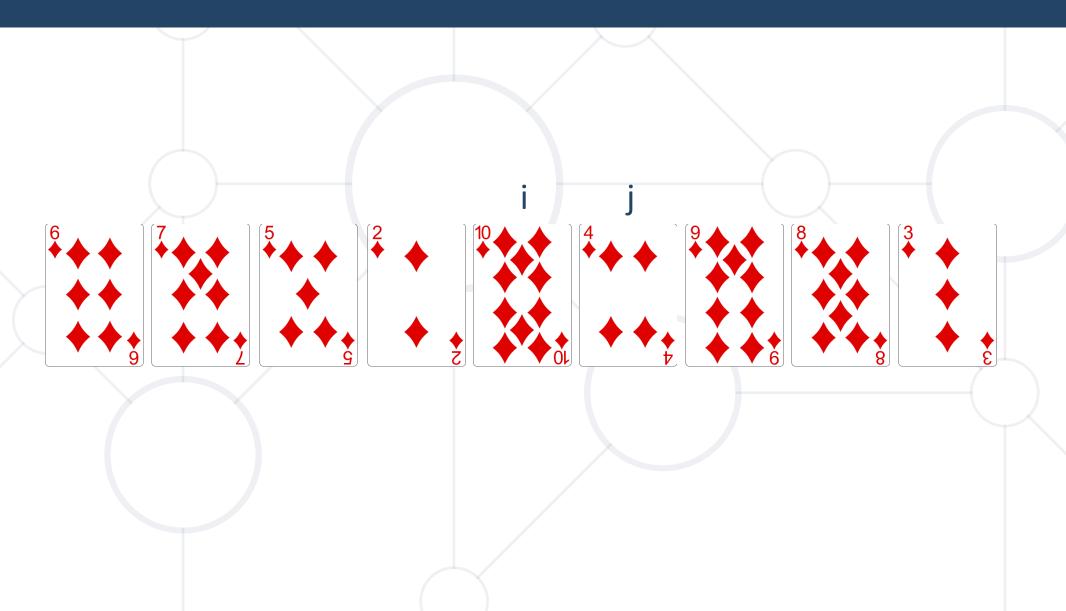




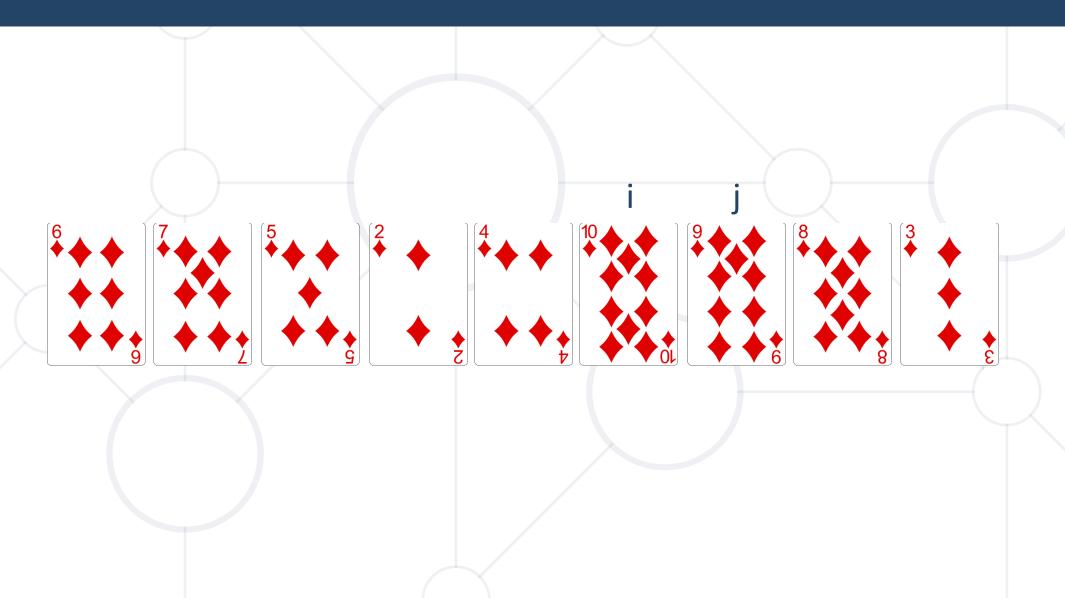




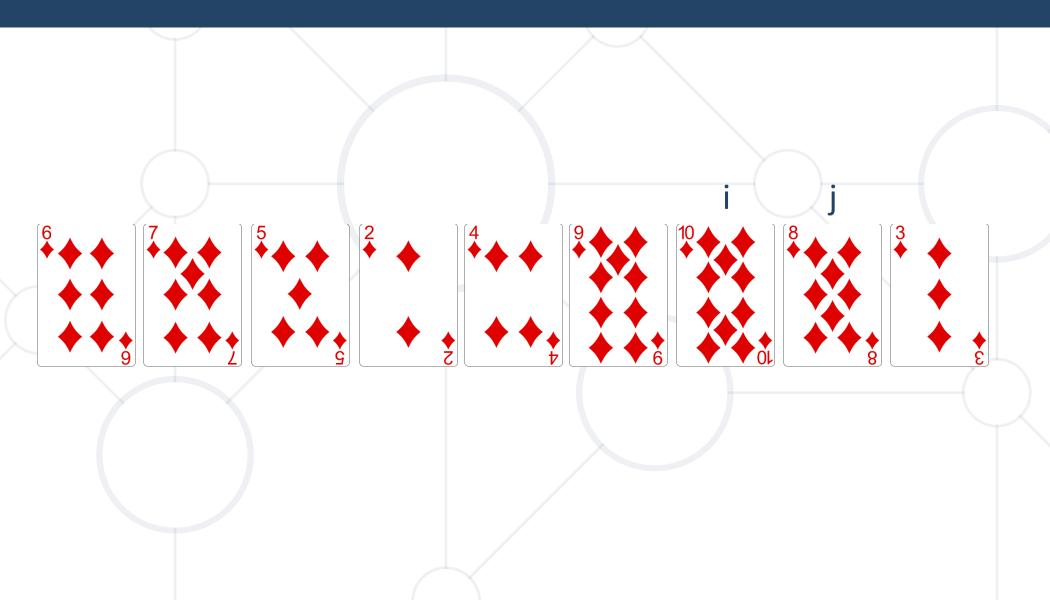




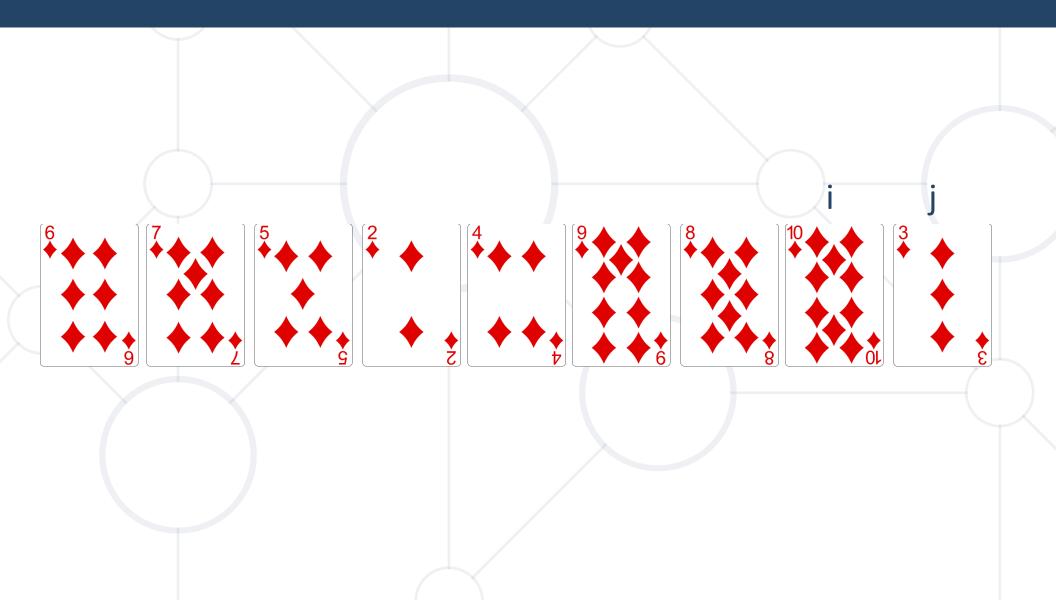




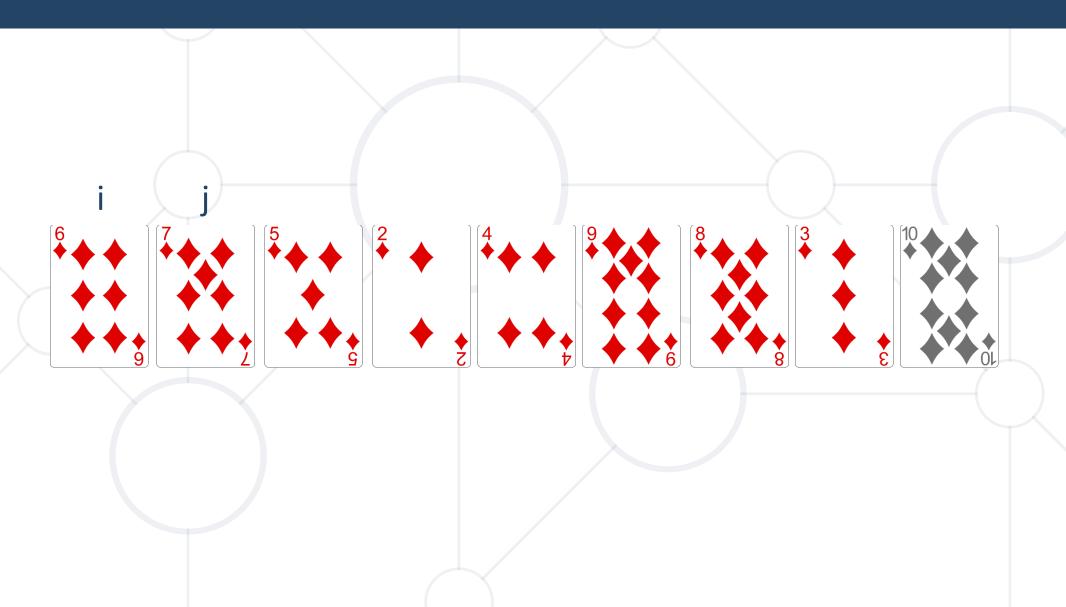




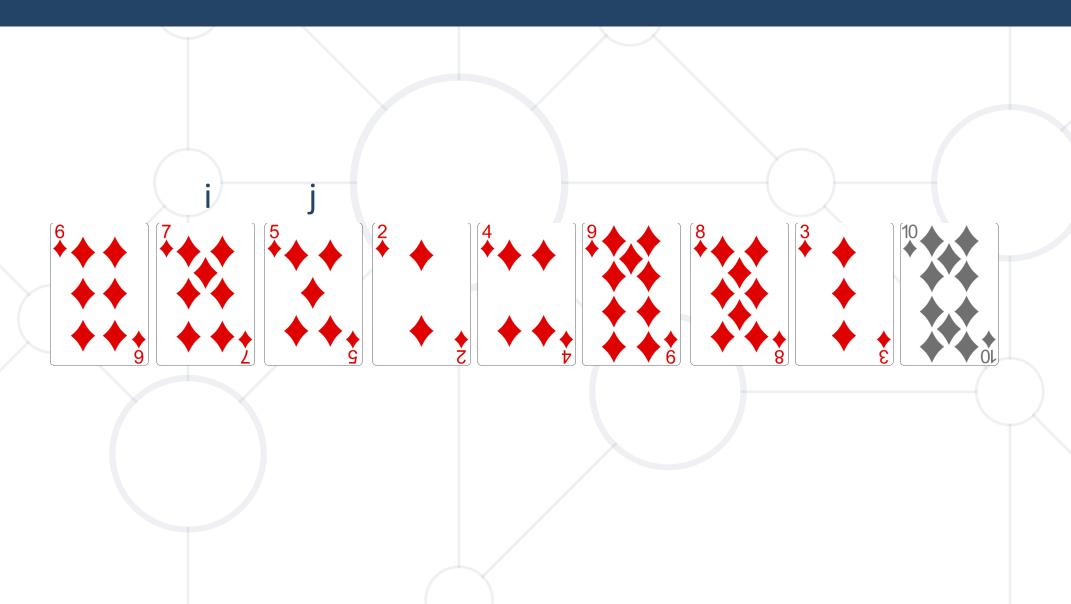




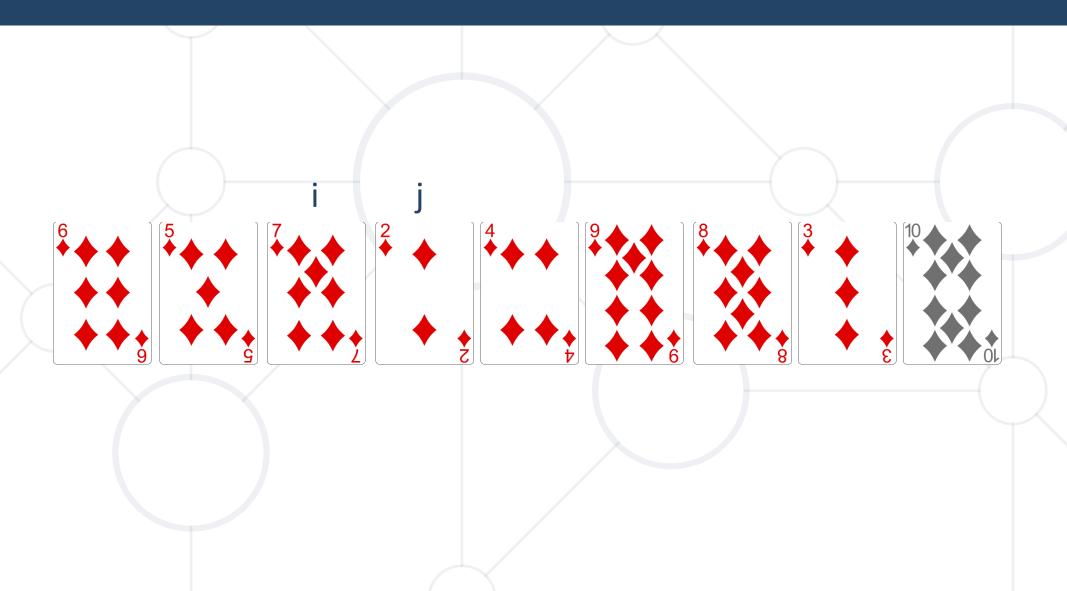




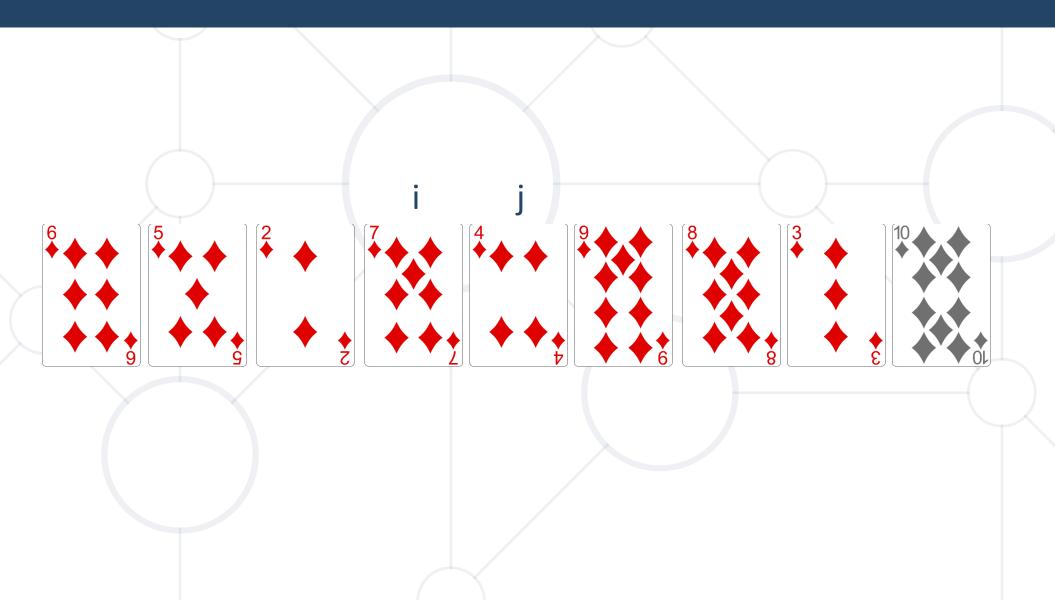




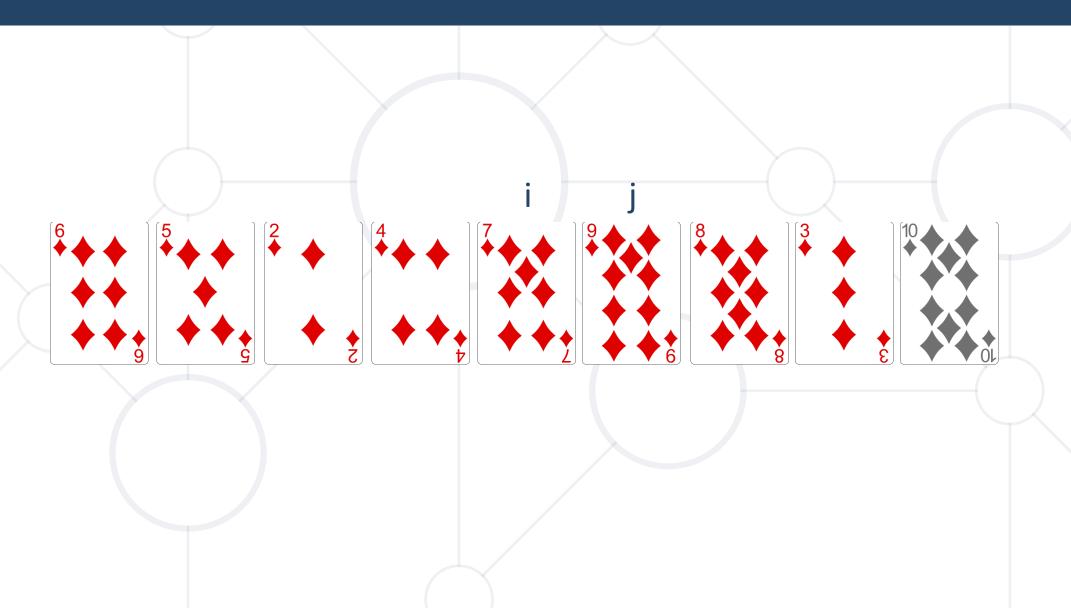




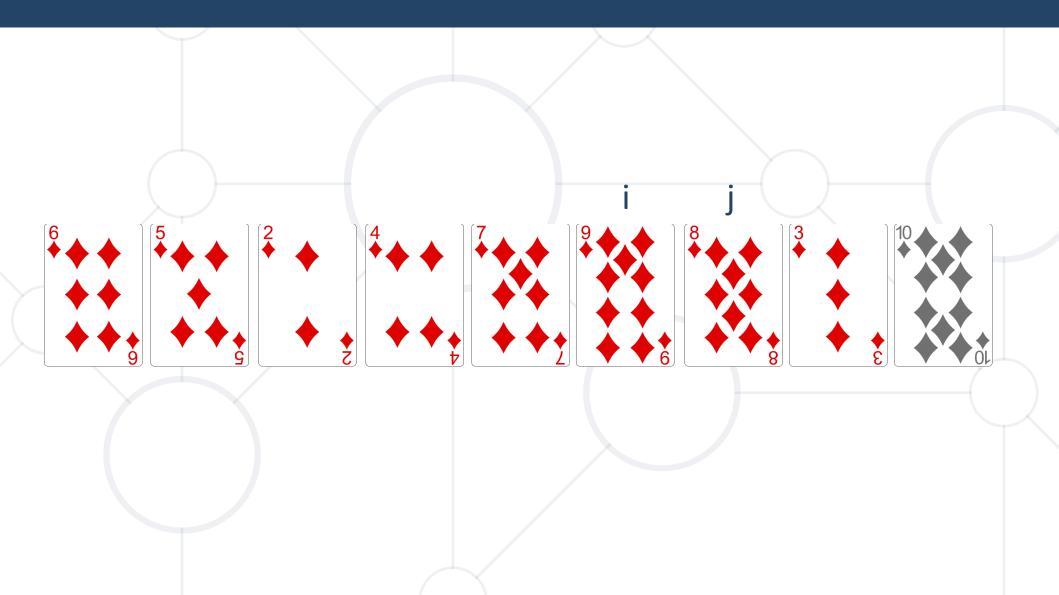




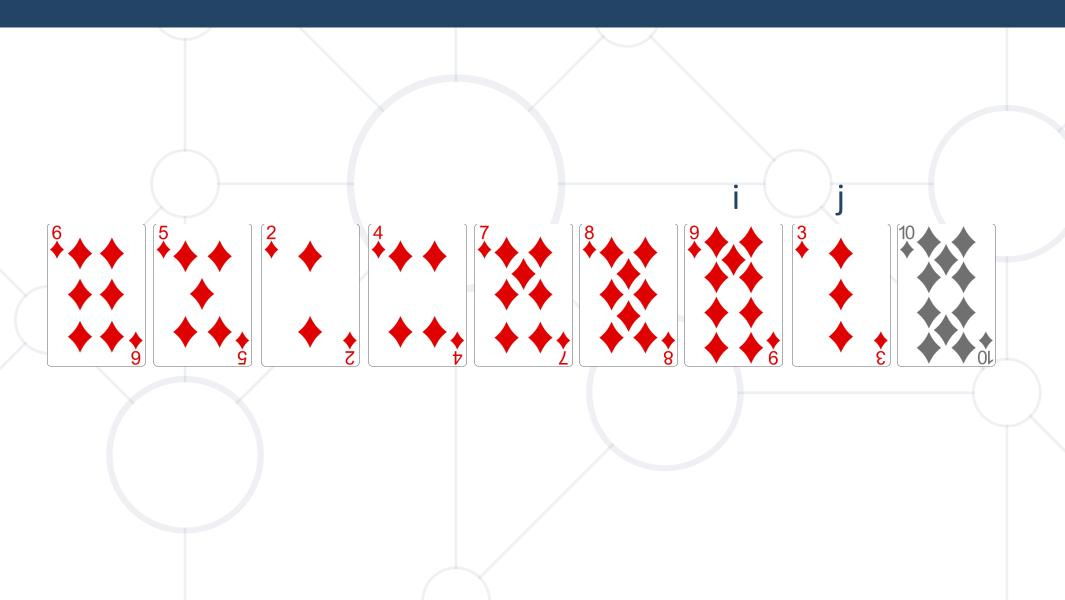




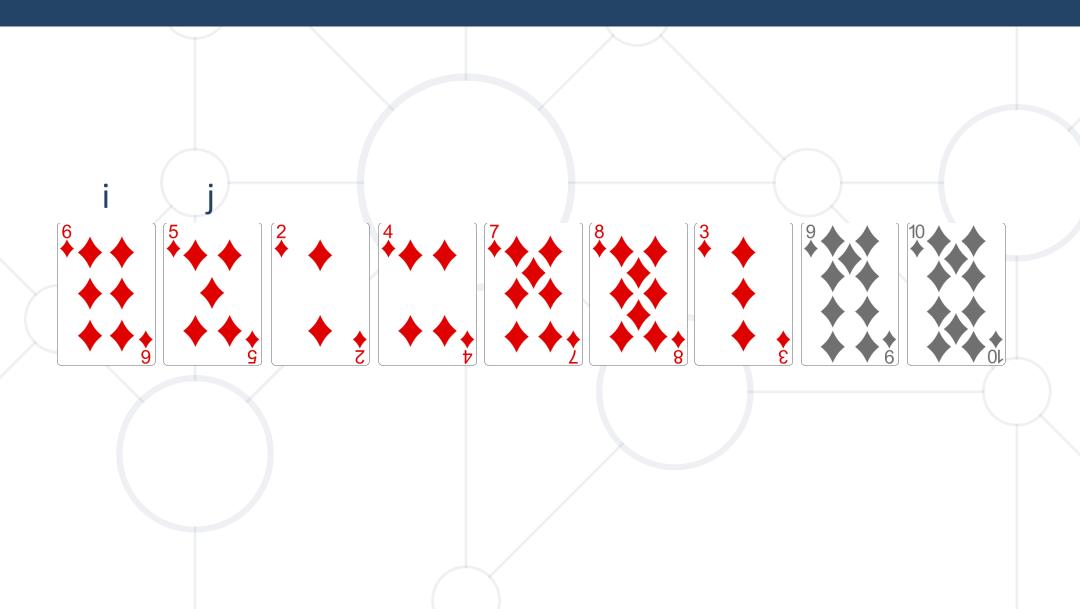












#### **Bubble Sort**



```
def bubble_sort(nums):
   is sorted = False
   i = 0
   while not is_sorted:
        is_sorted = True
        for j in range(1, len(nums) - i):
            if nums[j - 1] > nums[j]:
                nums[j], nums[j - 1] = nums[j - 1], nums[j]
                is_sorted = False
```

# **Comparison of Sorting Algorithms**



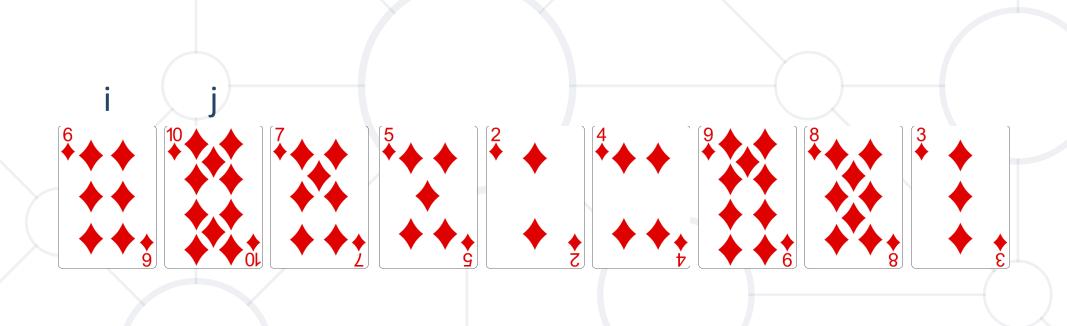
Name	Best	Average	Worst	Memory	Stable	Method
Selection	n <sup>2</sup>	n <sup>2</sup>	n <sup>2</sup>	1	No	Selection
Bubble	n	n²	n <sup>2</sup>	1	Yes	Exchanging

#### **Insertion Sort**

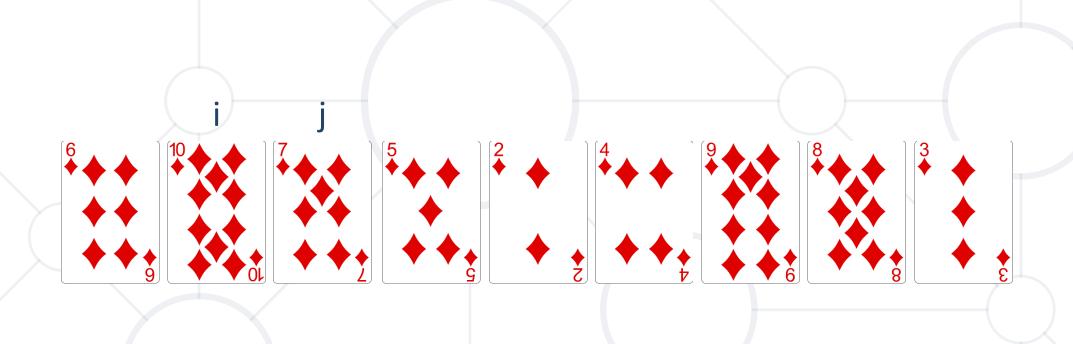


- Insertion Sort simple, but inefficient algorithm
  - Move the first unsorted element left to its place
  - Memory: O(1)
  - Time: O(n<sup>2</sup>)
  - Stable: Yes
  - Method: Insertion

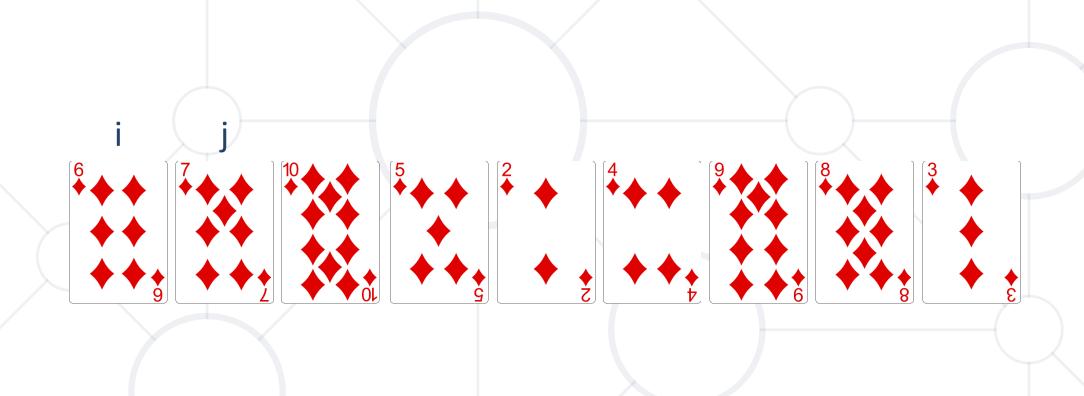




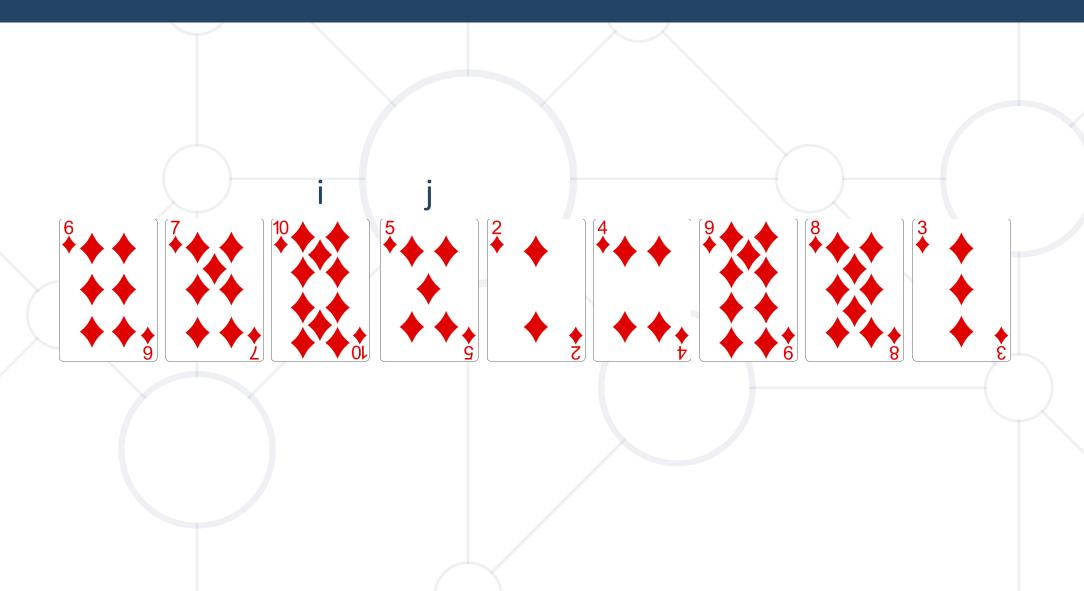




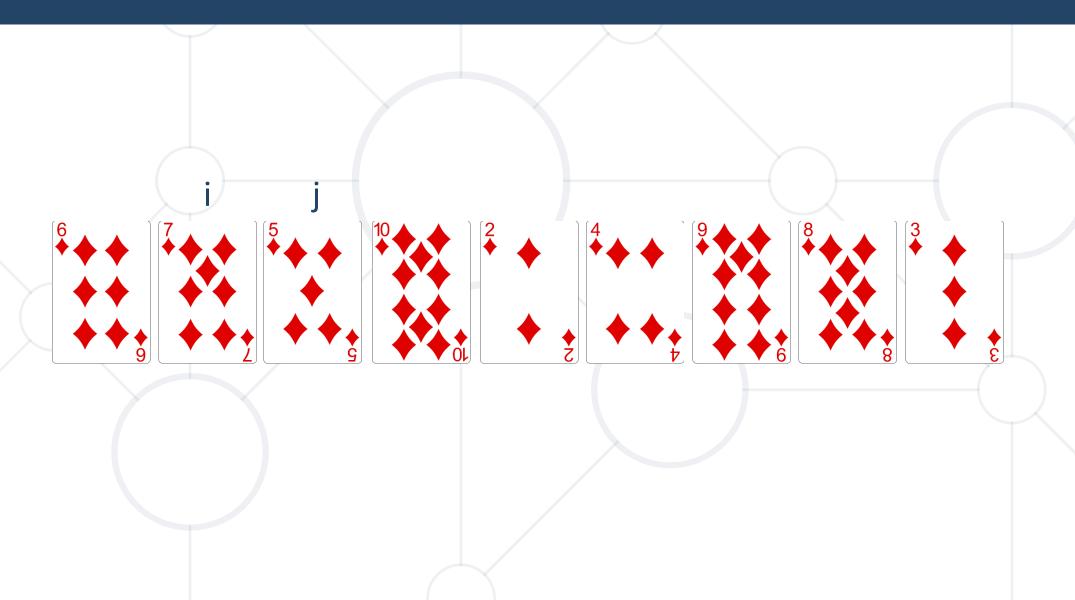




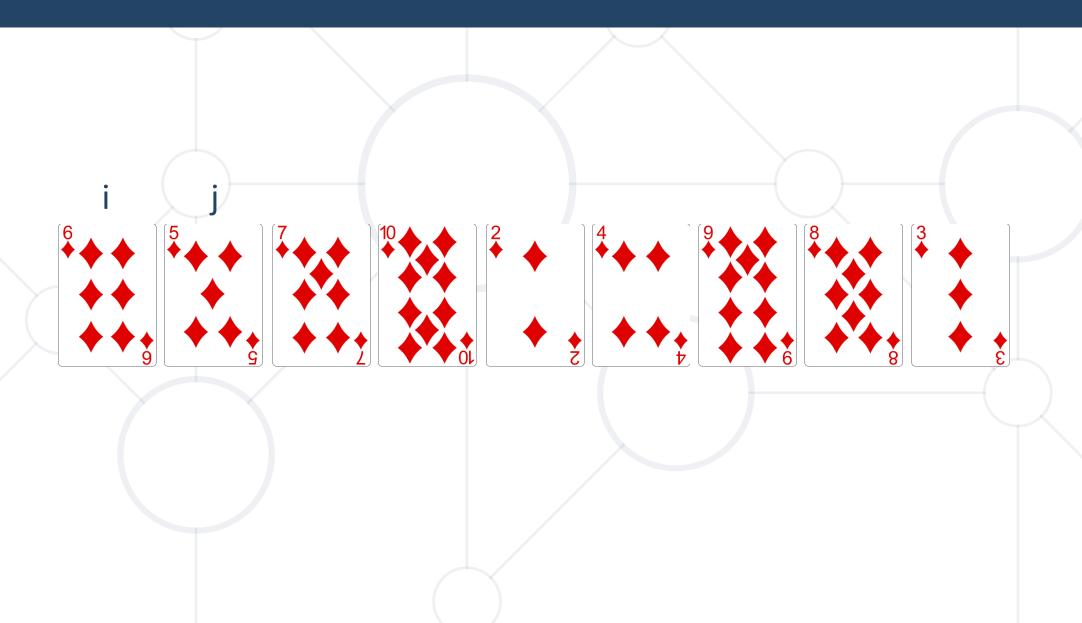




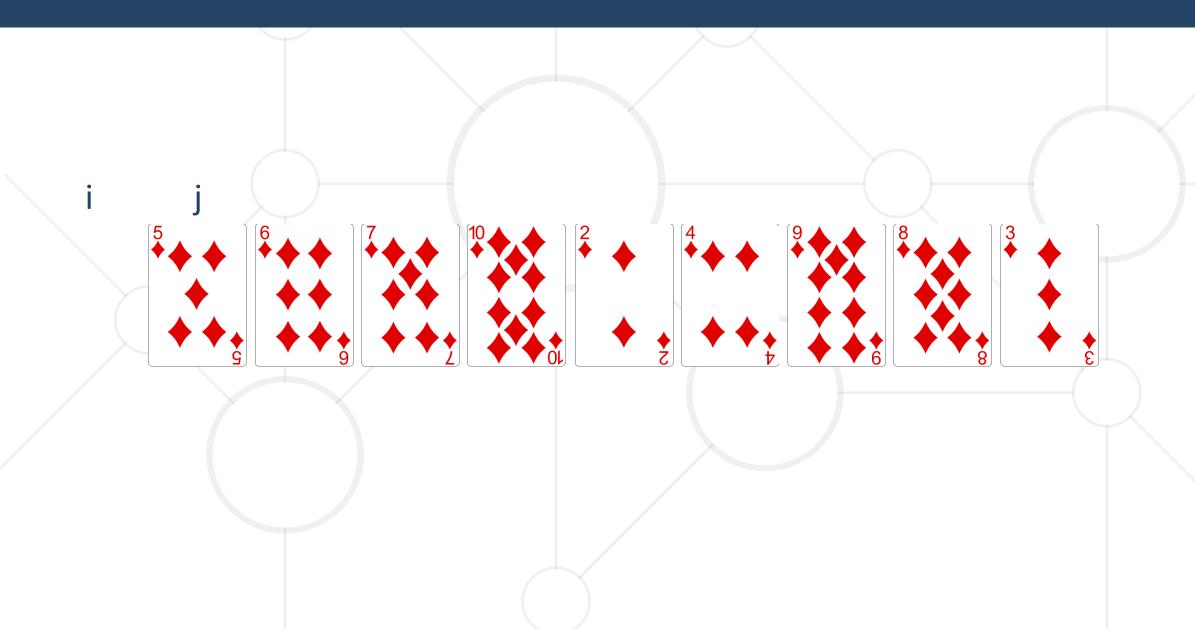




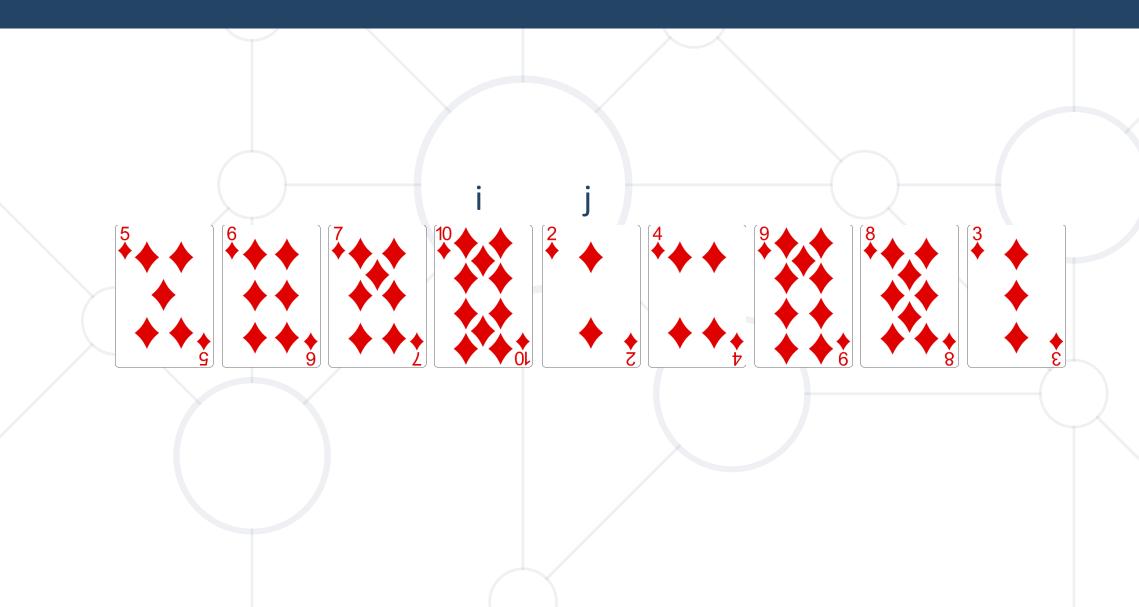




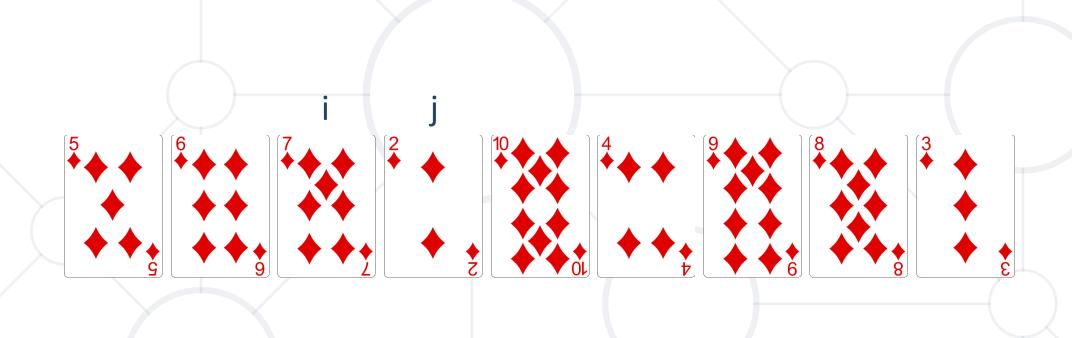




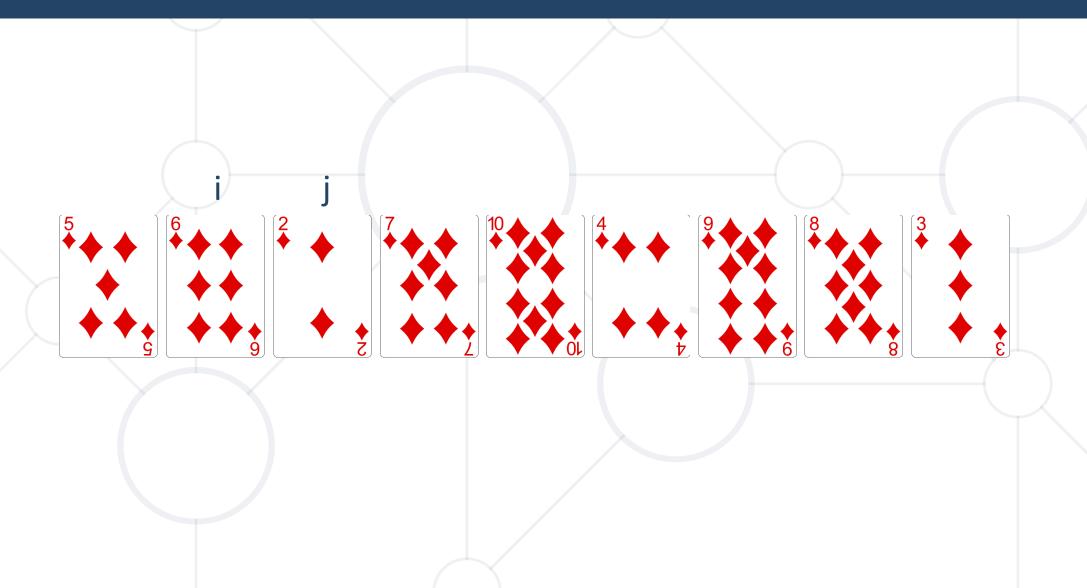




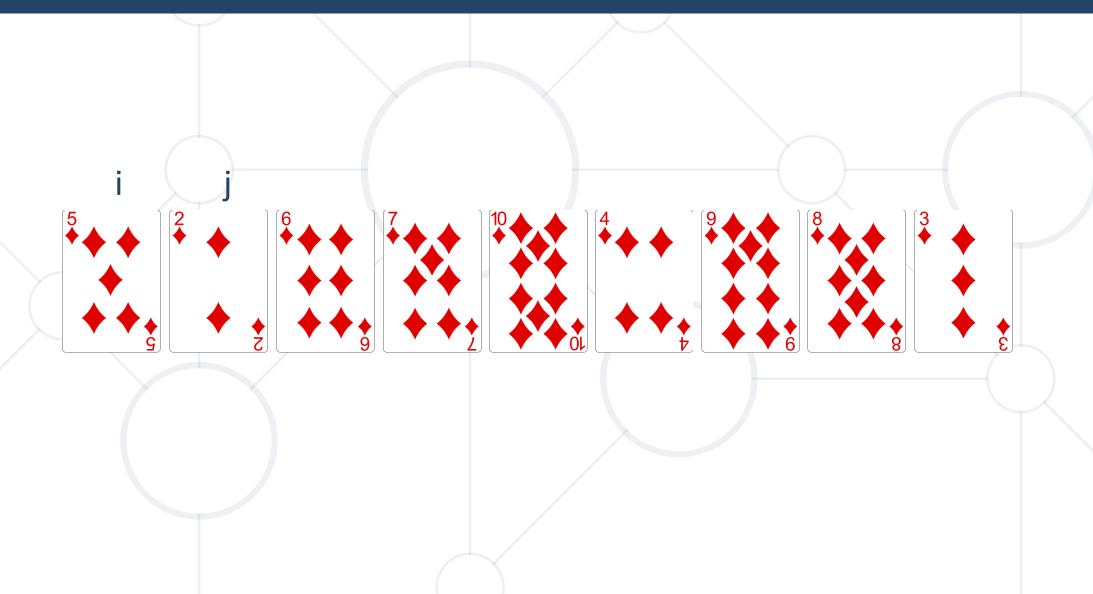




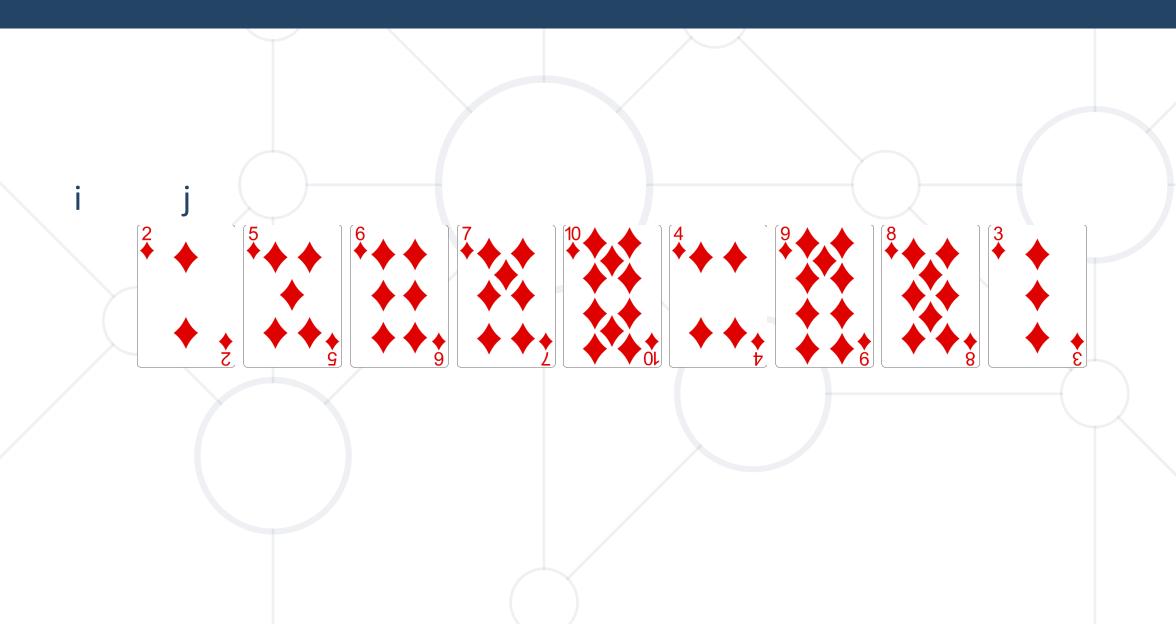












#### **Insertion Sort**



```
def insertion_sort(nums):
    for i in range(1, len(nums)):
        for j in range(i, 0, -1):
            if nums[j] < nums[j - 1]:</pre>
                 nums[j], nums[j - 1] = nums[j - 1], nums[j]
    return nums
```

# **Comparison of Sorting Algorithms**



Name	Best	Average	Worst	Memory	Stable	Method
Selection	n²	n <sup>2</sup>	n²	1	No	Selection
Bubble	n	n <sup>2</sup>	n <sup>2</sup>	1	Yes	Exchanging
Insertion	n	n <sup>2</sup>	n²	1	Yes	Insertion

# Summary

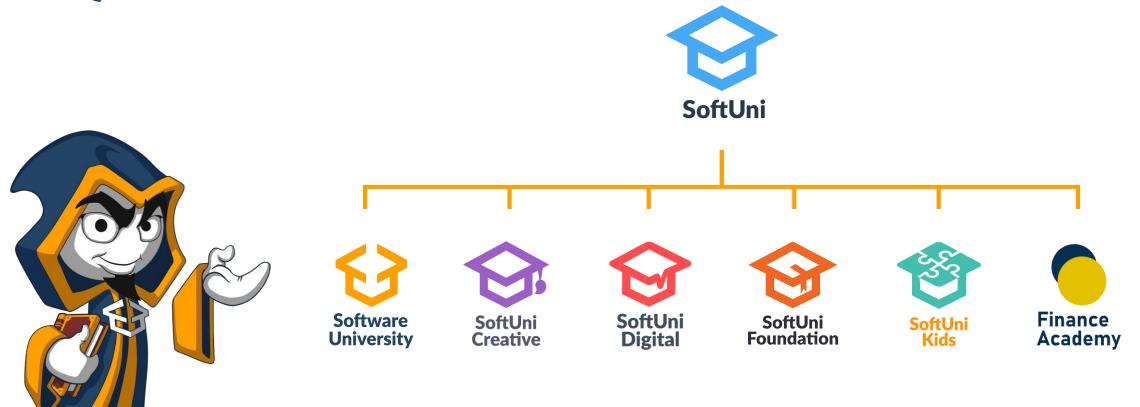


- Algorithmic Complexity
- Recursion a function calls itself
- Brute-Force trying all the possible solutions
- Greedy picking a locally optimal solution
- Searching algorithms:
  - Binary Search, Linear Search
- Sorting algorithms:
  - Selection sort, Bubble sort, Insertion sort





# Questions?



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Решения за твоето утре















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