Remote Lensing

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Remote Lensing

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Abstract

The problem of the manipulation of remote data is typically solved used complex methods to guarantee consistency. This is an instance of the remote bidirectional transformation problem. From the inspiration that several versions of this problem has been addressed using lenses, we now extend this technique of lenses to the Remote Procedure Calls setting, and provide a few simple example implementations.

Taking the host side to be the strongly-typed language with lensing properties, and the client side to be a weakly-typed language with minimal lensing properties, this work contributes to the existing body of research that has brought lenses from the realm of math to the space of computer science. This shall give a formal look on remote editing of data in type safety with Remote Monads and their local variants.

Acknowledgements

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Chapter 1

Introduction

The origin of this work begins with looking for overall abstractions between remote object systems and investigating whether adding an ordered lens-like structure was possible between multiple systems. These remote systems could stimulate or in fact provide the simplicity of lenses to an end user, such that these abstractions were representative of systems already in existence. Due to the popularity of classical lenses, it was discovered that online applications attempt to bring this boilerplate into their own code with different levels of effectiveness across their own systems.

To begin with, Foster et al. (2007), this field has been strictly derived from the premise of database systems, with even this primary source having constrained itself to a strict representation in the fundamentals. The fact of this is not a surprise when considering that the original well-behaved lens laws were first formulated by Benjamin C. Pierce in the context of database manipulation, Pierce & Schmitt (2003); Foster et al. (2003). From this series of work, Lenses originated from studying bidirectional transformations, as providing convenience to the end user as well as layers of type safety. Most commonly in the functional programming community lenses are popular abstractions to provide an object-oriented accessor notation to an object's elements: the functions that wrap data into structures are able to be acted on by functions that unwrap or re-wrap data in a convenient way. There are extensional ideas that relate to this such as Traversable Structures, but that is not the primary focus of this research, although in the case of Remote Monad, the Traversable is very much implementable — albeit with some extra efforts.

There are several types of lenses that bridge the gap between remote and local interactions already in existence, with varying degrees of depth of implementation. From the broad categories of c-lenses to the category of d-lenses, Johnson & Rosebrugh (2013) use the concepts of opfibra-

Figure 1.1: Variety of Lenses

tions to encapsulate the nature of transition information between a system and a database. The previous work derives its motivation from database systems such as SQL and the manipulation of table or record information, i.e. the original derivation of the c-lens from the categorical notion of Grothendieck opfibration, Grothendieck (1971), for a solution to the view update problem for functorial update processes, Johnson et al. (2011). From the idea that a host can only see a certain amount of information from the client side's database system, but both must maintain a consistently updated view parameter, Ahman & Uustalu (2014).

In fact, the advancements in category theory are heavily rooted in earlier works that bridged the gaps between algebraic topology and algebraic geometry, Grothendieck (1960). Which nearly paralleled the formalization of Beck's work in the formalization of the monadicity theorem which established when a functor is monadic, Beck (1967). These and multiple many discoveries gave rise to the derivation of several important concepts, including bifibrations and the monad itself, the details of which are not in the scope of this manuscript. Which gives rise to the formality of lenses despite their very humble beginnings, Foster et al. (2003). The notions of what can be considered entirely a lens or a portion of the children a lens structure, is illustrated in Figure 1.1.

Much of the general theory has assumed a typical database relationship such as SQL or other

table based services, this is based from the hard coded implementations that preceded these constructed ideas, which are hand tailored in works such as Bohannon et al. (2006). Several of these works are representative of these direct methods and their specific heritage in database problems which would be too numerous to cite here, but an impactful reference on source-to-target and target-to-source transformations is Fuxman et al. (2006). Including a wide range of work finding uses for lenses outside of their typical domain, most notably Boomerang a bidirectional programming language for textual strings, Barbosa et al. (2010), with further development in Optician, Miltner et al. (2017).

Which is why there is still open space for pseudo-implementations of lenses that haven't received much coverage if any in literature, perhaps because they break from all of the much higher level concepts and exert effort in the more rudimentary space of custom constructed Domain Specific Languages (DSLs). A DSL that is built over existing systems, not from the ground up with an intention of being able to represent much deeper concepts. It is a focus on practical designing patterns that are concerned with construction in the execution space. Since one doesn't need more than an understanding of the well-behaved lens laws to be able to put them into application for remote and local systems.

Additionally, DSLs already have their own unique sub-field in the lensing community with respect to the bidirectional transformation problem Czarnecki et al. (2009). This topic focuses on the API advancements provided by the Remote Monad design pattern for remote calls to external systems for the purposes of Remote Procedure Calls that have their commands executed remotely before returned locally, Gill et al. (2015). The Remote Lensing is in the same vein as database lensing, but it distinguishes itself by being primarily focused on Remote Procedure Calls rather than the typical database view update problem — of the latter this is not an attempt to expand on. This manuscript is focused on bringing in the concepts of Remote Lenses which are neglected in documented literature, to an explicit focus on their usability and ease of implementation from the fundamental well-behaved rules, and the capacity to scaffold them onto existing API.

Chapter 2

The Haskell Lens

Lenses are a restudy of the old problem of bidirectional transformations (bx) that were historically solved using dictionary and record systems. It is still an active field of study, with many connections to different sub-fields of computer science. Explicitly described, "*bx* are a mechanism for maintaining the consistency of two (or more) related sources of information", Czarnecki et al. (2009). The nature of bidirectional transformations allows them to be applied to domain specific languages and the host language itself, as a means to translate between run-time values.

From the implementation of lenses in the *bx* programming community there has been in recent years a new passion for their joint implementation in a larger variety of scenarios than they were initially imagined for. The study has broadened to the attempt to abstract and simplify over many sorts of structures, including their individual parts. The attempt at generality provides for opportunities in anything that might be presentable as a meaningful *bx*.

Lenses are characterized by the satisfaction of abstract laws and rules, established fully in Pierce & Schmitt (2003). Since there exist so called "not well-behaved" lenses that only follow some proper subset of the well-behaved lens rules and arbitrarily apply bidirectional transformations in ways that aren't consistent. Such "not well-behaved" lenses are beyond the scope of this manuscript, we will only deal with well-behaved lenses and their applications.

$$
\begin{aligned}
Set\big(obj,\, View(obj)\big) &= obj \\
View\big(Set(obj,\, item)\big) &= item \\
Set\big(Set(obj,\, item),\, item'\big) &= Set(obj,\, item')
\end{aligned}
\tag{2.1}
$$

It is an important note, that most definitions fix the direction of the lens operators *a priori*, i.e. where the *Set* or *View* will traverse along a given object to reach the designated destination.
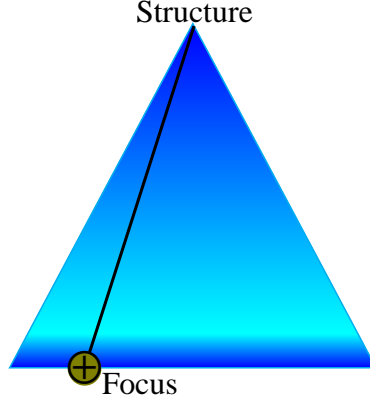
Figure 2.1: Lens Diagram

The only arguments to *View* are the structure itself, and with the only arguments to *Set* being the structure and item. The definitions assume that the overall pattern-matching system, which is the individually implemented lens for each focus in a structure, has been embedded before the configuration of *Set* and *View*, respectively, in its descriptive rules. In use, the lens is an active and changing argument that the programmer sets when they are establishing where they would like to mutate a structure. It is also possible to define the lens laws with an extra argument to determine the direction:

$$
\begin{aligned}
Set\big(acc,\ obj,\ View(acc,\ obj)\big) &= obj\,, \\
View\big(acc,\ Set(acc,\ obj,\ item)\big) &= item\,, \\
Set\big(acc,\ Set(acc,\ obj,\ item),\ item'\big) &= Set(acc,\ obj,\ item')\,.
\end{aligned}
\tag{2.2}
$$

This exposes some additional structure which the more instantiated definition in Equation (2.1) had previously obfuscated.

Figure 2.1 illustrates a simplistic lens, showing a means to pattern match internally and a navigation of that structure to the desired focus with the help of a lens. The diagram implies that it is possible to navigate into the focus, provided that the focus is a similarly formatted structure. This is true, provided that both the primary structure and all associated substructures have been constructed in a way that allows for pattern-matching. If this is the case, then pattern-matching over the entire structure is possible. This "stacking" of structures, enables lenses to be composed so that it becomes possible to find a focus even if it is nested two or more structures deep. The
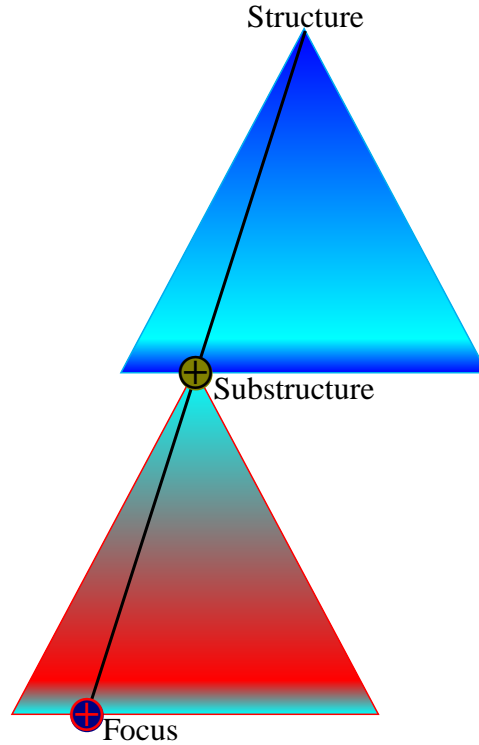
Figure 2.2: Diagram of Lens Composition

embedding of a lens equipped structure into a larger lens equipped and the resulting composition of lenses is illustrated in Figure 2.2.

There are some basic Haskell types as well as examples that show that the idea of lenses applies to many sorts of structures, including modifications or inspections of two-tuple structures as displayed in Figure 2.3. In simple cases, the general idea of pattern matching to obtain results is explicit and summarized inside the code itself. However, Haskell's compiler allows for implicit pattern matching to take place as well. The implicit calls to focus on specific elements of the two-tuple is handled in this manner, display in Figure 2.2. This holds true for both `view_a` and `set_a`, where the inspection of the two-tuple is enough to view or set the contents of the structures respectively.

Lenses represent such a large sub-field of bx, and have been so generalized that a full view is well beyond the scope of this manuscript. The interested reader may refer to Czarnecki et al. (2009) for a good survey. These and many more topics will be restricted to monomorphic occurrences instead, whilst the rest will fall outside the scope of this thesis.

```
view :: w -> p
set :: w -> p -> w

view_a :: (a,b) -> a
view_a (x,y) = x

set_a :: (a,b) -> a -> (a,b)
set_a (x,y) x' = (x',y)
```

$$(x,y) \qquad set\_a\big((x,y),x'\big) = (x',y)$$
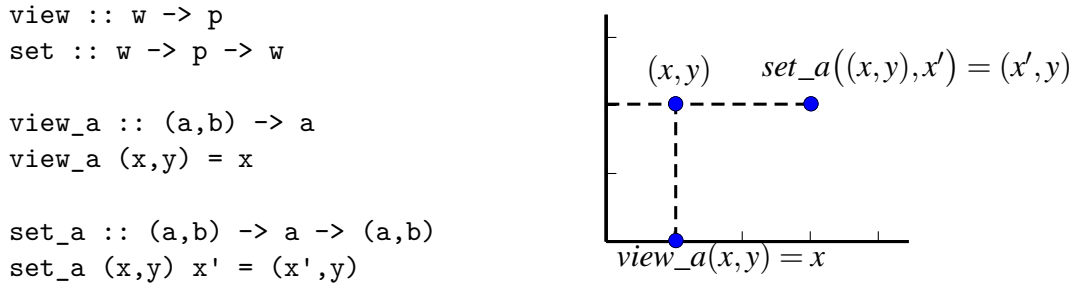
$$view\_a(x,y) = x$$

Figure 2.3: Elementary Haskell Lens

Expanding on how a lens may be implemented in Haskell, an important example to consider is how building lenses and operating on a structure work. Not an implicit lens like in Figure 2.3, but an explicit lens that allows access to a richer structure. One begins by initializing such a structure as follows below.

```
data MyStructure = MyStructure {
    MyName :: String
    , MyAge :: Int}
    deriving (Show, Eq)
```

The structure contains two important points of focus a String and an Int value, and one can make a lens with the ability to access either of the two elements. In similarity the two-tuple example, constructing an accessor to each element to view or set must be done individually. But in this case, there isn't a trick to get the Haskell compiler to do all the work, so a little bit of code is needed to break inside.

```
type MyLens s a = forall f. Functor f => (a -> f a) -> s -> f s

item_name :: MyLens MyStructure String
item_name some_function (MyStructure l r) =
                      (\l'->  MyStructure l' r) <$> (some_function l)
```

From this, there is a general structure that represents how a lens may be formed by the type abstraction of *MyLens*. Specifically instantiated the expansion for *item_name* would appear something along the lines of `String -> f String) -> MyStructure -> f MyStructure`. Which allows a set or view implementation to provide some functor that renders the inspection or modification of the structure in compliance with the well-behaved features of lenses. Another way to

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see this, is that upon inspecting the instantiation of *item_name*, it is possible to spot out the initial pattern matching of the structure. The leftmost argument having *some_function* applied to it, before being injected back into the structure.

```
set :: forall s a. MyLens s a -> (a -> s -> s)
view :: MyLens s a -> (s -> a)

getName :: MyStructure -> String
getName = view item_name

setName :: MyStructure -> String -> MyStructure
setName = set item_name
```

The specifics of how *Set* and *View* are implementing their individual accesses to the structure aren't terribly important, they are only giving instantiation to the much more familiar usage and format of the well-behaved lens laws in Equation (2.1). This is made more clear in the *Name* functions and type definitions, where after applying the lens to the set or view, then only the classic arguments are needed, since the lens has already focused on a specific area of the structure.

Chapter 3

Extending Lenses

As described, the two primary components of lenses are the *Set* and *View* functions which produce as a result of applying them both at the same time a command referenced as *Over*. When one applies *View* to the structure in Figure 3.1, an element of that structure is retrieved. We may then modify that retrieved element with some function before applying *Set* to that very same structure. This results in a new structure which accomplishes the same as having applied *Over* from the very beginning.

The application of *View* and *Set* in this sequence is equivalent to *Over*. For the a command sequence to be equal to *Over*, it must directly perform a given function onto the focus whilst in in the same singular injective process. This process of modeling the *Over* function can be best described as the following composition, $Set\left(obj, F\left(View(obj)\right)\right) =: Over(obj, F)$. For all valid objects, applying the desired function to the viewed object and then setting that modified object is equivalent to overing the object with that same function. That is to say, for any *obj* with the corresponding application of *Set*, *View*, and *F* there will be an resulting *obj'*. A modeling of the same result if for the same *obj* had been exposed to the application of *Over* and *F*, which would result in the same *obj'*.

There exist many degrees of abstracting over elementary lenses like those provided in Figure 2.3. The documentation is not focused on the fuller expanses of the system of abstractions for lensing mechanisms inside of mathematics and programming, but instead finds relevance in the most simple formation of lenses which is now provided.

```
data BasicLens a b = BasicLens {
    viewer :: (a,b) -> a
    , setter :: (a,b) -> a -> (a,b)}
```
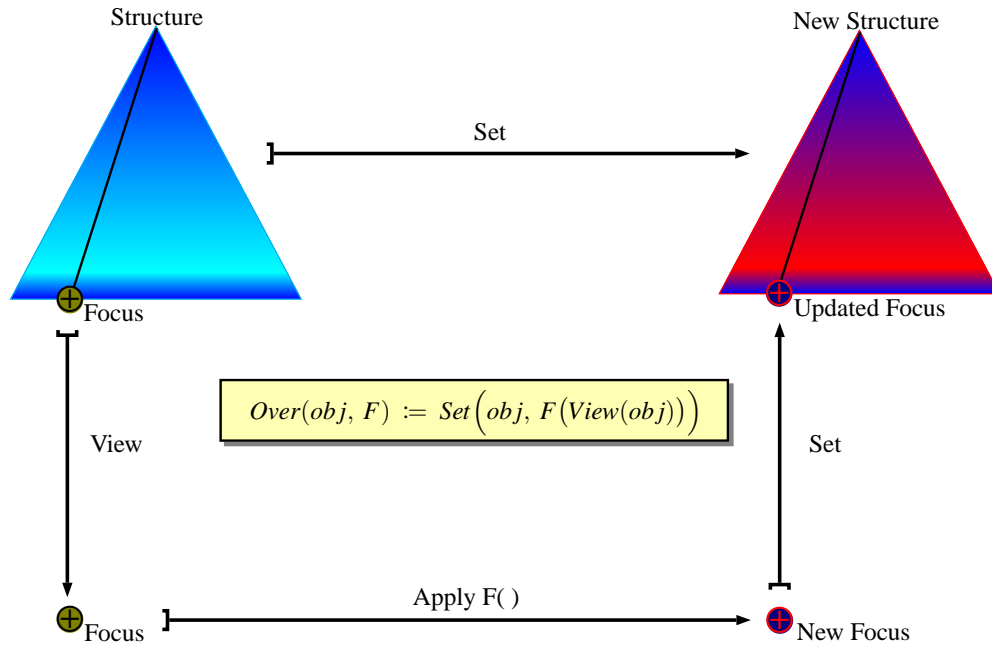
Figure 3.1: Over Construction

This shows the capacity to build the lens datatype from a structure that contains the view and set explicitly for a given focus. Additionally, the ability to retrieve both the viewer and the setter as independent but composable functions is maintained.

```
applyview ::  BasicLens a b -> (a, b) -> a
applyview (BasicLens viewer setter) s = viewer s

applyset ::  BasicLens a b -> (a,b) -> a -> (a,b)
applyset (BasicLens viewer setter) s = setter s
```

As shown above, `applyview` and `applyset` both use pattern matching to expose the internals of the elementary Haskell lens. The exposure of these components can also be accomplished without the use of this helper functions, but for the purposes of completeness with the standard lens methodology this has been provided.

```
a_Lens :: BasicLens a b a_Lens = BasicLens {
    viewer = view_a
    , setter = set_a}
```

The initialized version of this simplistic lens structure, preforms it's role for the *Set* and *View* defined in Figure 2.3. This is the *A-Lens*, a parameterized structure over the `view_a` and the `set_a` from last chapter. Such as it is defined, a lens that successfully encapsulates the full structure of

both the ability to view the *a-element* and to set the *a-element* with a new value. Whilst the *A-Lens* maintaining the ability to recover the View and Set that were grouped into it's larger structure. Allowing one to preform both the operations over the a-element without needing to refer to anything but this structure.

It is realized that a much stronger case for this can be made, if it is possible to make the inherent pattern matching explicit and this case is generalized to the abstractions typically provided in the earlier chapter's `MyLens`. This effort does result in the not so surprising result that this is indeed possible, without any loss of type information.

```
a_ln :: MyLens (a,b) a
a_ln my_functor (a,b) = (\a'->  (a',b)) <$> (my_functor a)

a_view :: (a,b) -> a
a_view = view' a_ln

a_set :: a -> (a,b) -> (a,b)
a_set = set' a_ln
```

In the provided case, an abstraction results in an explicit reference to the *a-element* and allows for specialization in it's behavior depending on what functor is applied. This code results in leaving for both `view_a` and `set_a` to be recreated from earlier in `a_view` and `a_set`, with no great alterations besides the rearrangement of second function's arguments.

This leads to the assertion that although defined in heavy detail and with great investment in the proofing of algebraic geometry, category theory, and homotopy type theory — the hard coded versions of lenses do not need to subject themselves to these abstractions. In fact, the levels of proofing and rigor abstract away what lenses can be defined to do, such as when shoving a lens into a monadic container. Which is why only the well-behaved lens laws in Equation (2.2), are considered for the details of the manuscripts later chapters. If one has a curiosity if the pseudo-implementations of lenses discussed may be represented as standard lenses, then the continued reading is deeply recommended for those interested.

Chapter 4

Remote Lenses and The Remote Monad

In this chapter, we detail a novel extension of lenses to remote structures making use of the Remote Monad. The definitions provided in the previous chapters allow for one to describe a variation of lenses that copies the syntactical sugar and programmatic intent of these operators over a remote connection between a client and a host device, the host running Haskell and the client running some other language. We refer to this variation from standard local lenses and other classical variants as the *Remote Lens*.

We now extend the abstract identities in Equation (2.2) to the Remote Lens setting, obtaining the *Remote Lens Identities*,

$$
\begin{aligned}
RemoteSet\big(acc,\ RemoteView(acc,\ obj),\ obj\big) &\equiv obj\,,\\
RemoteView\big(acc,\ RemoteSet(acc,\ item,\ obj)\big) &\equiv item\,,\\
RemoteSet(acc,\ item,\ obj)\ ;\ RemoteSet(acc,\ item2,\ obj) &\equiv RemoteSet(acc,\ item2,\ obj)\,.
\end{aligned}
\tag{4.1}
$$

Whereas a lens interacts with a structure, a Remote Lens interacts with a Remote Structure. The ";" in the equations above denotes the sequence of operations and "≡" denotes equivalence but not equality. The fundamental distinction for why classical equality is not used is that operations on either side of the "≡" are not identical in all respects. Equivalence is narrowly interpreted to abstract away the individual operations that take place between the host and client when executing remote commands. The process of wrapping and sending commands then receiving and unpacking them is equivalent to the process being carried out by the remote system without interaction from the local system. A correct analogy would be taking the maintained connection to be a pointer to an object, then dereferencing the pointer and preforming some operations to the object which ultimately results in no change to the object. This procedure it is the same as having never started

the pointer dereference in the first place. Precisely, the left and right sides of Equations (4.1) are *Observably Equivalent*, Milner (1984), so they do not produce a different result from one another given the same input, though they are not formally identical.

The essentials of what is required to construct the Remote Lens Identities inside of Haskell is similar to the Haskell lenses given in the elementary Prelude constructions of Chapters 2 and 3. The first argument typically taken by any lens operator, *acc* as shown above, is a function that will access a deep-rooted parameter inside of a structure. In the same vein, the Remote Lens accomplishes this with an abstraction of the Remote Structure's nested fields that are to be queried once the command is sent from host to client. The primary difference is in how this is handled by Haskell. Rather than simply pattern matching into the already existing structure, a completely different approach is needed instead due to to the structure being remote. To define the individual components of Remote Lenses for an arbitrary type system we begin by providing the relevant abstract type definitions below.

```
RemoteView :: (String -> String) -> (Wrapped a) -> (ReturnType b)
RemoteSet :: (String -> String) -> String -> (Wrapped a) ->
↪  ReturnType (Wrapped a)
RemoteOver :: (String -> String) -> (t -> a) -> (Wrapped a) ->
↪  ReturnType (Wrapped a)
```

This approach is best summarized as a melding between the fundamental methods used in typical lens methods that rely strongly on internal pattern matching for the composability of lens, and the existence of a remote connection that prevents that internal pattern matching to take place. This is relevant to any scenario where accessing a structure isn't possible inside of the host system, and it is necessary to query a client system. This is illustrated in Figure 4.1, which should be distinguished and contrasted with the much similar local implementation in Figure 2.2.

Remote Lenses will involve internally forming a conjointment of the parameters such that each of the parameters that normally would be accessed with a composition of pattern matching functions, must instead be accessed with a composition of the Remote Object's internal parameters. This is equivalent to representing the target object as a remote record with the means to access the contents completely dependent on how that record is implemented inside of the client's language.
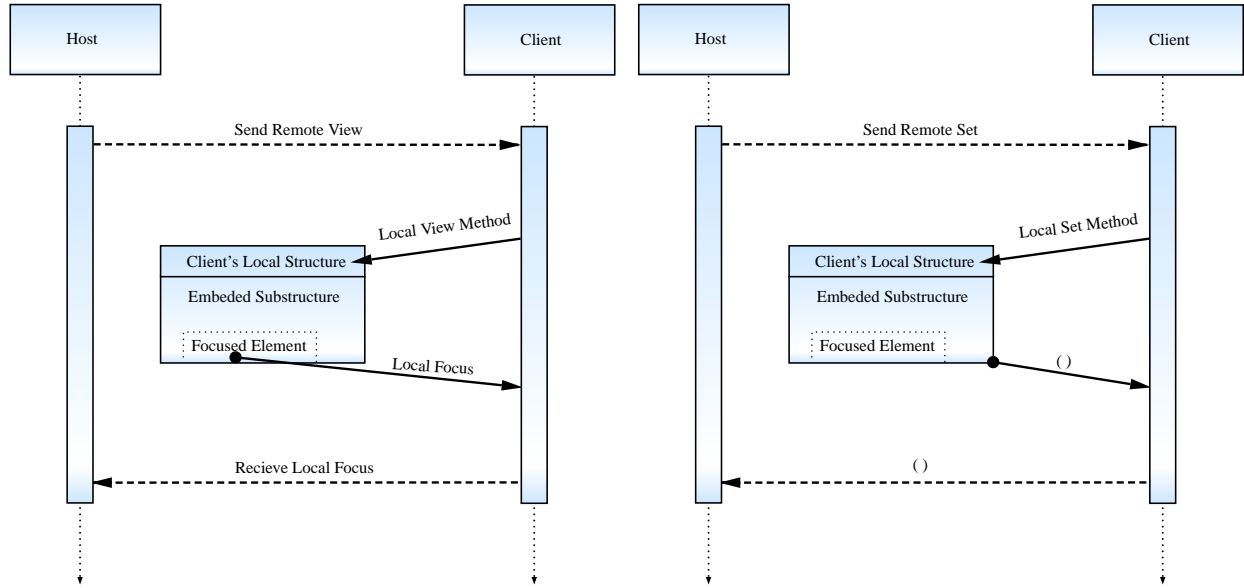
Figure 4.1: Remote Diagrams. The left diagram illustrates Remote View, while the right illustrates the Remote Set. Solid lines are local executions, dashed lines are remote transactions, dotted lines are the continuing connection.

The *obj* argument in Equation (4.1) represents a reference to the location of what is to be accessed upon sending the constructed command. Since one is manipulating only a reference to the actual object on the client's side, this implies that directly accessing the information is not possible. That is, the conjointment method described in the former paragraph is needed to focus in on the remote structure. Bundling the reference to the Remote Object along with the preformed command to operate on the Remote Object is necessary, otherwise none of the methods to view or alter the contents of that structure can be accomplished. As anytime that one wishes to operate on a Remote Object, the host side needs to know where in the client side it is accessing and what it is going to do once it arrives there.

The final common parameter of Equations (2.2) and (4.1) is the returned item from the result of applying a lens operator to the structure that is being inspected. Where *RemoteView* returns the queried item wrapped in the remote operator that allowed for the operation to take place and for *RemoteSet/RemoteOver* the returned item will be the reference to the altered structure wrapped up in the same remote operator. The only major consideration when manipulating the returned

structure, is that one must assign the type of the expected viewed parameter or trust that there is sufficient information that Haskell can self-interpret the type for itself.

Now it is possible to introduce the primary example that this manuscript will cover, specifically the *Remote Lens* as it relates to the *Remote Monad*. This has been selected because the Javascript *RPCs* are representative of a weakly typed client language and Haskell is able to represent a strongly typed host language, Gill et al. (2015). Additionally, the Remote Monad provides all of the functionality necessary to implement the desired lens functions. Now given below is the construction of the Remote Lens' key functions.

```
RemoteView :: (FromJSON b) => (String -> String) -> (RemoteValue a) ->
↪   (RemoteMonad b)
RemoteSet :: (String -> String) -> String -> (RemoteValue a) ->
↪   RemoteMonad (RemoteValue a)
RemoteOver :: (FromJSON t, Show a) => (String -> String) -> (t -> a) ->
↪   (RemoteValue a) -> RemoteMonad (RemoteValue a)
```

These are the types for the set of functions that seek to emulate the methods of *View*, *Set*, and *Over* that have been defined specifically for a Remote Lens based on using the Remote Monad. Though they emulate *View*, *Set*, and *Over* — they do not share the same internal structure. These definitions are specific to the Remote Monad but they demonstrate a universal design pattern. This example shows that for any client-host system in which there is a an interaction between a host language, a client language, and a remote structure, that a fully formed method of communicating between the two is presentable as a Remote Lens in this way, implemented in Haskell below.

```
RemoteView accessor object = do{
        g <- constructor $ JavaScript $ pack $ accessor (var_text object)
        procedure $ var g
}

RemoteSet accessor new_item object = constructor $ JavaScript $ pack $
↪   (accessor (var_text objectName)) ++ " = " ++ new_item

RemoteOver accessor my_function object = do{
        item <- RemoteView accessor object
        let new_item = show $ my_function item
        RemoteSet accessor new_item object
}
```

It is worth noting that due to the fact that we are dealing with a remote connection, the connection must be passed as a parameter in addition to the structure that one wants to manipulate, the accessor to the individual segment of the structure, and a value if using the `RemoteSet` function. While in Haskell one normally manipulates and creates new objects every time one runs a function or assigns a value, in Javascript new objects are never created within the Remote Monad implementation. Thus, any code one would want to write with these methods on the Haskell side would need to keep in mind that one is never dealing with a fresh object. The connection will always make sure one is pointing to the one and only original Javascript object one is trying to manipulate.

(Left Off Here Last Time)A key distinction on the improvements is that this removes any sort of backend coding, where the user is directly manipulating the delicate remote monad commands. And instead has a predefined way of accessing, editing, and setting values with minimal contact to the ideas and command structure beneath. One gets an abstraction and type safety on every component of the command, and modularity that clearly expresses your intent to the reader of your code. In the following examples, similarities and contrasts between Remote Lenses and Local Lenses will be made clear to the reader.

With basic syntactical sugar, with *RemoteView* as `^.` and composition of remote lens fields as `>>>` one gets a clear expression that shows to anyone else on ones coding team what one was doing. The traditional point-style notations is mostly maintained along with a slight alteration to the composability of "." to the ">>>". The case usage below showing for the remote-object of person, one is accessing two layers into it's fields to retrieve a double value from extra2.

```
f :: Double <- person ^. nest >>> nest2 >> extra2
```

The normal syntax for this would be represented as the following nested structure.

```
RemoteView (extra3(nest2(nest))) person
```

This expands out fully instantiated and unwrapped in the weeds as a slightly harder to read structure, requiring more knowledge of the underlying construction. This way of writing code is particularly undesirable, particularly when abstractions exist for the purpose of making the legibility easier to the trained and untrained reader.

```
g <- constructor $ JavaScript $ pack $ (extra3(nest2(nest))) (var_text
 ↪  person)
procedure $ var g
```

The code shows the virtualization of machinery from each layer to the next in this system, and that whilst the syntactical sugar for *RemoteSet* and *RemoteOver* has not been shown, these share the same levels of abstractions. For completeness, examples of their basic calling is provided now so that one isn't left curious to the reasonable invocations to their Haskell counterparts.

```
RemoteSet (extra3(nest2(nest))) "4" person
```

```
RemoteOver (extra3(nest2(nest))) (\ x -> (x + 1::Double)) person
```

There is a particularly complete example from the first exercise of Haskell lensing from FP Complete, that was subsequently adapted to *RemoteMonad* and *Remote Lens* so that it could be clearly illustrated in long form what some of the major similarities and differences might be between remote and local implementations. Starting off the simple construction of the "lens" arguments is provided, in the case of the Javascript back-end this can be viewed as using the point-styled object-oriented accessor methods, common in non-functional programming languages.

```
address objectName = objectName ++ ".address"
street objectName = objectName ++ ".street"
city objectName = objectName ++ ".city"
name objectName = objectName ++ ".name"
age objectName = objectName ++ ".age"
```

There is now provided a series of example constructions for normal lens-like syntax, particularly constructed calls to view the age of a person as well as the street they live on. Additionally, a function to modify the street name via a set and a function to over the age with an age incrementing argument — are both provided.

```
wilshire :: String
wilshire = "\"Wilshire Blvd\""

aliceWilshire :: RemoteValue a -> RemoteMonad (RemoteValue a)
aliceWilshire newperson = RemoteSet (address >>> street) wilshire newperson

getStreet :: RemoteValue a -> (RemoteMonad String)
getStreet newperson = RemoteView (address >>> street) newperson
```

```
birthday :: RemoteValue Int -> RemoteMonad (RemoteValue Int)
birthday newperson = RemoteOver age (\ x -> (x + 1::Int)) newperson

getAge :: RemoteValue a -> (RemoteMonad Int)
getAge newperson = RemoteView age newperson
```

The last piece is provided now to show the effective usage of the lens-like functions and how they provide a clear flow, with each action they take on the client side once the host has sent them over as packets.

```
exercise1 :: Engine -> IO ()
exercise1 eng = do
        send eng $ do
                command $ call "console.log" [string "starting..."]
                render $ "Exercise1"
                newperson <- initializeObjectAbstraction2 "alice" alice
                aliceWilshire newperson
                mystreet_person <- getStreet newperson
                birthday newperson
                herNewAge <- getAge newperson
                render $ "mystreet_person: " ++ mystreet_person
                render $ "herNewAge: " ++ show herNewAge
```

From the large set of examples, the necessity of making abstractions is made clear and the larger case for why Remote Lenses are useful tools, whilst it isn't possible to provide every single amenity that the classical lenses are able to give programmers.

Chapter 5

Extending Remote Lenses

This chapter explicitly will deal with a compare and contrast to the Extended Lenses chapter, along with any additional information that was out of place in the Remote Monad Chapter. The end goal is a reasonable intuition if *Remote Lenses* are indeed *Lenses*. One having paid careful mind in the detailing of implementation and theory discussed about the *Remote Lenses*, should have come to a question about the exact degree of resemblance that these structures have to their locally designed counterparts. In fact, keeping the methods of creating a total lens structure, a way to show the closeness between *Local Lenses* and *Remote Lenses* would be to attempt expressing their remote nature in the style of the local abstractions. Now we will start with attempting to shape the structure of *RemoteView* and *RemoteSet* into a data structure.

```
data RemoteLens a b = RemoteLens {
    remote_view ::  (FromJSON b) => (String -> String) -> (RemoteValue a) ->
    ↪  (RemoteMonad b)
    , remote_set :: (String -> String) -> String -> (RemoteValue a) ->
    ↪  RemoteMonad (RemoteValue a)}

applyview :: FromJSON b => RemoteLens2 a b -> (String -> String) ->
↪  RemoteValue a -> RemoteMonad b
applyview (RemoteLens2 remote_view remote_set) = remote_view

applyset :: RemoteLens2 a b -> (String -> String) -> String -> RemoteValue a
↪  -> RemoteMonad (RemoteValue a)
applyset (RemoteLens2 remote_view remote_set) = remote_set

a_Lens :: RemoteLens a b
a_Lens = RemoteLens {
    remote_view = RemoteView
    , remote_set = RemoteSet}
```

Whilst the nature of being able to neatly wrap the generalized *Remote Lens* commands together

is easily implemented, this immediately approach doesn't come close to the meaning held in the local variation in Chapter 3. The meaning of wrapping the *View* and *Set* together in a *Local Lens*, is to wrap together the means of accessing a specific focus. In this case, we have wrapped together a general *RemoteView* and *RemoteSet*, that can be specialized to access anywhere in the larger *Remote Structure*. Essentially this form of abstraction only complicates the use of the original commands, while pointlessly obfuscating the underlying ease of use that the composability of the pseudo-accessor functions were supposed to provide.

   Not to easily give up hope just yet that an equivalent method exists, the next significant attempt is to instantiate a far less general *Remote Lens* data type and the way to do this is to start talking about the primary example from Chapter 4. The abstraction will be directly over the accessor methods, much in the similar way that the abstractions are attempted on a per element basis in normal automatic generation of *Local Lens* constructions.

```
data RL_ObjectA  = RL_ObjectA {
    rl_address :: String -> String
    , rl_street :: String -> String
    , rl_city :: String -> String
    , rl_name :: String -> String
    , rl_age :: String -> String}
    deriving (Show)

a_Object :: RL_ObjectA a_Object = RL_ObjectA {
    rl_address = address
    , rl_street = street
    , rl_city = city
    , rl_name = name
    , rl_age = age}
```

This doesn't provide anything but a formalization of the ways that *Remote Lenses* were already being handled. Which surprisingly, only adds unnecessary bulk to the already clear methods of invoking the remote calls. The following code shows this specialization does maintain the ability to write generalized accessors, that would act on any *Remote Lens Object* that was properly instantiated.

```
remote_view :: FromJSON b => RL_ObjectA -> RemoteValue a -> RemoteMonad b
remote_view object newperson = RemoteView (rl_name object) newperson
```

```
remote_set :: RL_ObjectA -> String -> RemoteValue a -> RemoteMonad b
remote_set object item newperson = RemoteView (rl_name object) item
↪   newperson
```

If keeping this line of attempts to specialize, then another perspective would be to take the valid

alternative construction approach from Chapter 3 to it's full conclusion with this specific case in

Remote Lenses. Rather than one specializing the accessors, providing them bundled together just

like *A-lens* will allow for a more safe and clear means of using these commands. In the provided

implementation below, the first introduced method is now having it's *RemoteView* and *RemoteSet*

instantiated with the focus of name.

```
data RemoteLens a b = RemoteLens {
    remote_view :: FromJSON b => (RemoteValue a) -> (RemoteMonad b)
    , remote_set :: String -> (RemoteValue a) -> RemoteMonad (RemoteValue
    ↪   a)}

applyview :: FromJSON b => RemoteLens a b -> RemoteValue a -> RemoteMonad b
applyview (RemoteLens2 remote_view remote_set) = remote_view

applyset :: RemoteLens a b -> String -> RemoteValue a -> RemoteMonad
↪   (RemoteValue a)
applyset (RemoteLens2 remote_view remote_set) = remote_set

a_Lens :: RemoteLens a b
a_Lens = RemoteLens {
    remote_view = RemoteView name
    , remote_set = RemoteSet name}
```

The full exposure provided in this method resembles the closest to the nature of the two-tuple

example provided in the previous chapters, but it lacks certain properties that one would define in

a classically constructed lens.

It is finally time to deal with the largest question posed in this manuscript, are *Remote Lenses*

truly *Lenses*? An assessment that will be argued over in multiple parts, starting with the meaning

of the generalized lens type signature and its relationship to the *Remote Lens* and ending with an

exploration of the mechanical work being accomplished irregardless of the type signature.

Starting off with the first part, it is now time to look at broad difference between the type

signature of anything that is remotely similar to a lens and the type signature of the *Remote Lens*

itself. Abstracting away the finer details, if this were to be valid code shown below, one might imagine the following generalizations.

```
LocalLensView :: MyObject -> MyItem
LocalLensSet :: MyItem -> MyObject -> MyObject

RemoteLensView :: PointertoObject -> ReturningData
RemoteLensSet :: ValueToBeSent -> PointertoObject -> ReturningData
```

To a careful reader, there is a stern contrast that likely might have sat in the background of the mind for a long while: wondering what is so off about the usage of the syntactical sugar, despite how closely it appeared to mimic the familiar counterpart. That is, in a *Local Lens* the input object and the output object from the definition of *Set* is always the same. If given a two-tuple, then a two-tuple is what will be returned. Fundamentally what is a mechanical difference between *Local Lenses* and *Remote Lenses*, results from the fact that in *Remote Lenses* the returning information from a *Set* operation is simply an indication of a job done, not the pointer to the changed object. If one was inclined, asserting that they are not lenses would be a fair judgment on the nature of these two creatures. in fact, it wouldn't make sense, the abstraction to begin with is based on the capacity to abstract cleverly with a functor. Here we are dealing with a situation where it isn't abstractable in a sensible way to a functor.

The one thing left that might save this from being merely a design pattern, would be if on the client side an act of lensing was taking place to have it's result retrieved and decoded on the host side. This is in fact the case, as the accessing of the client's objects fields via point-styled references is a synonymous situation with using lens methodology. As one might remember, the major motivation for lenses is to provide an abstraction in the *bx* field. The oldest and least type safe method of handling this in the context of objects, is directly calling on their parameterized accessors. If the client and host are interacting in a method such as in the *Remote Monad*, then it is possible to make the *Remote Lens* use the *Local Lens* on the client's side.

Ultimately, while the *Remote Lens* does not type check as a *Local Lens*, the *Remote Lens* can promise to the user that it is acting as if it were a *Local Lens*. Which fits squarely in what a DSL provides, abstraction of commands for the sake of usability and convenience. But if forced to pick

a binary choice, the *Remote Lens* is not a *Lens* — rather it is a means to an end of being able to use

a *Lens*.

Chapter 6

Conclusion

Given the material proceeding this, how to structure a conclusion? A brief aside to the Python

and SQL? A series of remarks that bring together the contents together again in some way?

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