



In the discrete case

$$\epsilon_B = \sum_{x \in \mathcal{X}} p(y_{\min} | x) \cdot p(x)$$

$$\epsilon_{1NN} = \sum_{x \in \mathcal{X}} (p(y_1 | x) p(y_2 | x') + p(y_2 | x) p(y_1 | x')) \cdot p(x) \leq 2\epsilon^*$$

$$\epsilon_B = \frac{1}{3} \times \frac{3}{20} + \frac{2}{5} \times \frac{5}{20} = \frac{3}{20}$$

$p(y_2 | x) \quad p(x)$

$$\epsilon_{1NN} = \left(\frac{2}{3} \times \frac{1}{3} + \frac{1}{3} \times \frac{2}{3} \right) \times \frac{3}{20} + \left(\frac{2}{5} \times \frac{3}{5} + \frac{3}{5} \times \frac{2}{5} \right) \times \frac{5}{20}$$

$p(y_1 | x) \quad p(y_2 | x') \quad p(y_1 | x) \quad p(y_2 | x') \quad p(x)$

$$= \frac{4}{3 \times 20} + \frac{12}{5 \times 20} = 0.186$$

$$0.186 \leq 2 \times 0.15$$

$$\epsilon_{1NN} \leq 2 \epsilon_B$$