

BRAC UNIVERSITY
Merul Badda, Dhaka, Bangladesh
CSE331 : Automata and Computability
Assignment 1
Summer 2024

1. Construct DFA for the following regular languages:

$L_1(M) \rightarrow \{w \in \Sigma^* \mid w \text{ doesn't contain } 00\}, \text{ where } \Sigma = \{0, 1\}.$

$L_2(M) \rightarrow \{w \in \Sigma^* \mid w \text{ doesn't contain } 11\}, \text{ where } \Sigma = \{0, 1\}.$

- A. $L(M) \rightarrow (L_1 \cap L_2)'$
- B. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{the sum of the symbols of } w \text{ is a multiple of } 3\}, \text{ where } \Sigma = \{0, 1, 2\}.$
- C. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{the decimal equivalent of } w \text{ is a multiple of } 5\}, \text{ where } \Sigma = \{0, 1\}.$
- D. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ is any string not in } 0^*1^*\}, \text{ where } \Sigma = \{0, 1\}.$

2. Write the RE for the following regular languages:

$L_1(M) \rightarrow \{w \in \Sigma^* \mid \text{every third position in } w \text{ is } 1\}, \text{ where } \Sigma = \{0, 1\}.$

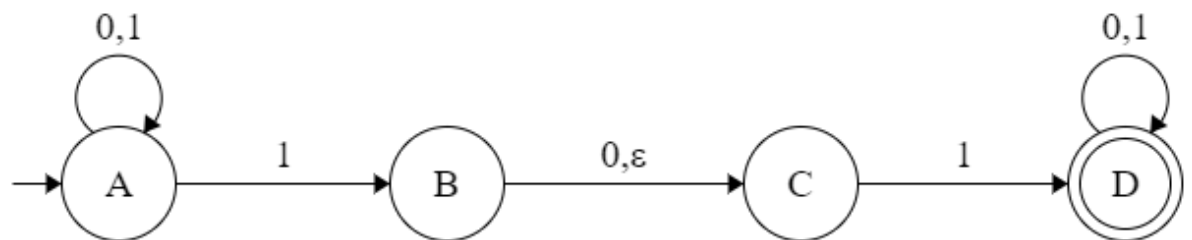
$L_2(M) \rightarrow \{w \in \Sigma^* \mid \text{every } 1 \text{ in } w \text{ is followed by at least two } 0\}, \text{ where } \Sigma = \{0, 1\}.$

- A. $L(M) \rightarrow L_1 \cap L_2$
- B. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ starts and ends with the same symbol}\}, \text{ where } \Sigma = \{0, 1\}.$
- C. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains equal numbers of } 01 \text{ and } 10\}, \text{ where } \Sigma = \{0, 1\}.$
- D. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ does not contain } 101\}, \text{ where } \Sigma = \{0, 1\}.$

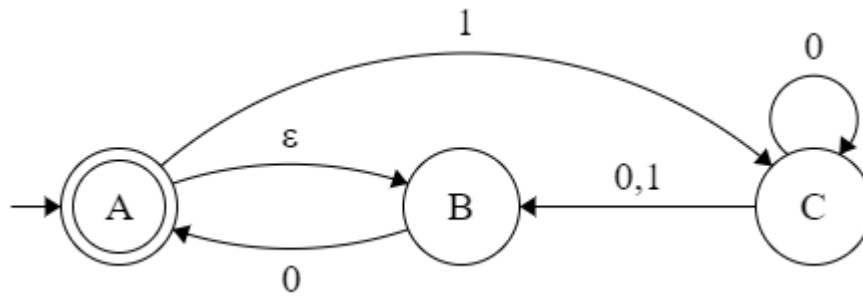
3. Construct NFA for the following regular languages:

- A. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains } 1001 \text{ or } 11\}, \text{ where } \Sigma = \{0, 1\}. \text{ (use 5 states.)}$
- B. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains a } 1 \text{ in the third position from the end}\}, \text{ where } \Sigma = \{0, 1\}.$
- C. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{length of } w \text{ is a multiple of } 2 \text{ or } 3\}, \text{ where } \Sigma = \{0, 1\}.$

4. Convert the following NFA into DFA:



A.



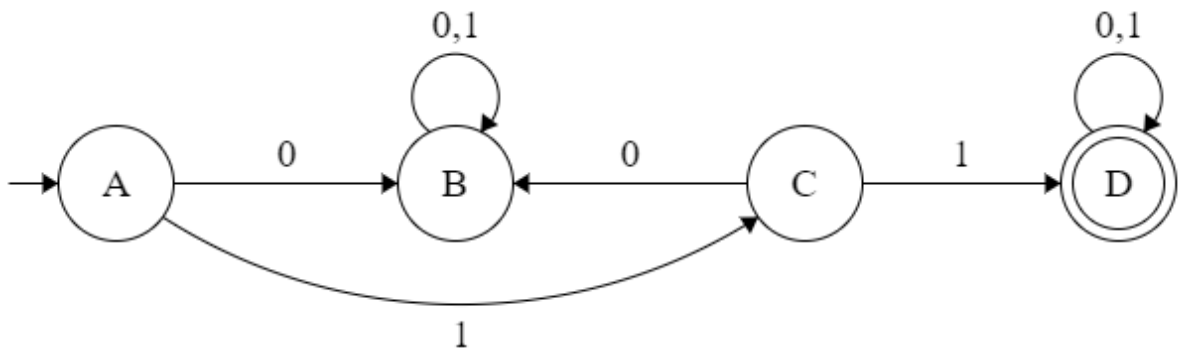
B.

5. Convert the following RE into NFA:

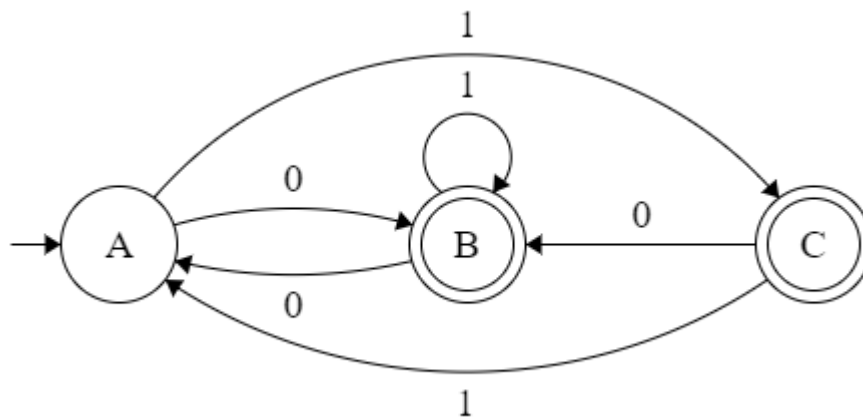
A. $(01 \mid 0)^*$

B. $(0 \mid 1)^*010$

6. Convert the following DFA into RE:



A.



B.