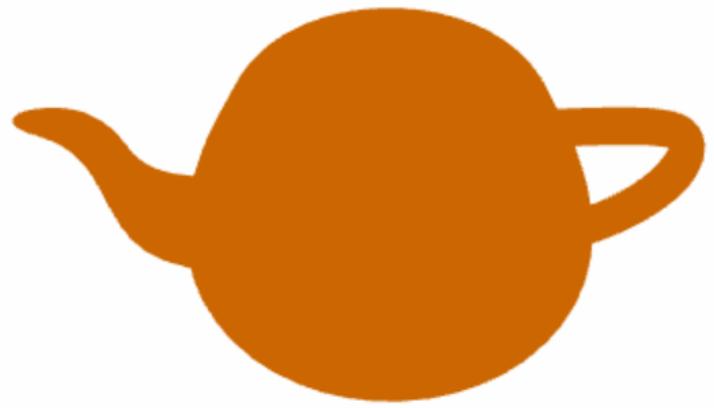


Lighting/Illumination/Reflection Model

Some of the contents used in this lecture belong to...

- Dr Jon Shiach, Manchester Metropoliton University, “Direct Lighting Model”,
<https://www.youtube.com/watch?v=7CdS8oOJtVA>
- Mr. Jacobson, University of Toronto, “WebGL Phong Shading”,
<http://www.cs.toronto.edu/~jacobson/phong-demo/>
- RapidCompact, “Simplifying a 3D Mesh”,
<https://rapidcompact.com/doc/cli/latest/Simplify/index.html>

Effects of Lighting

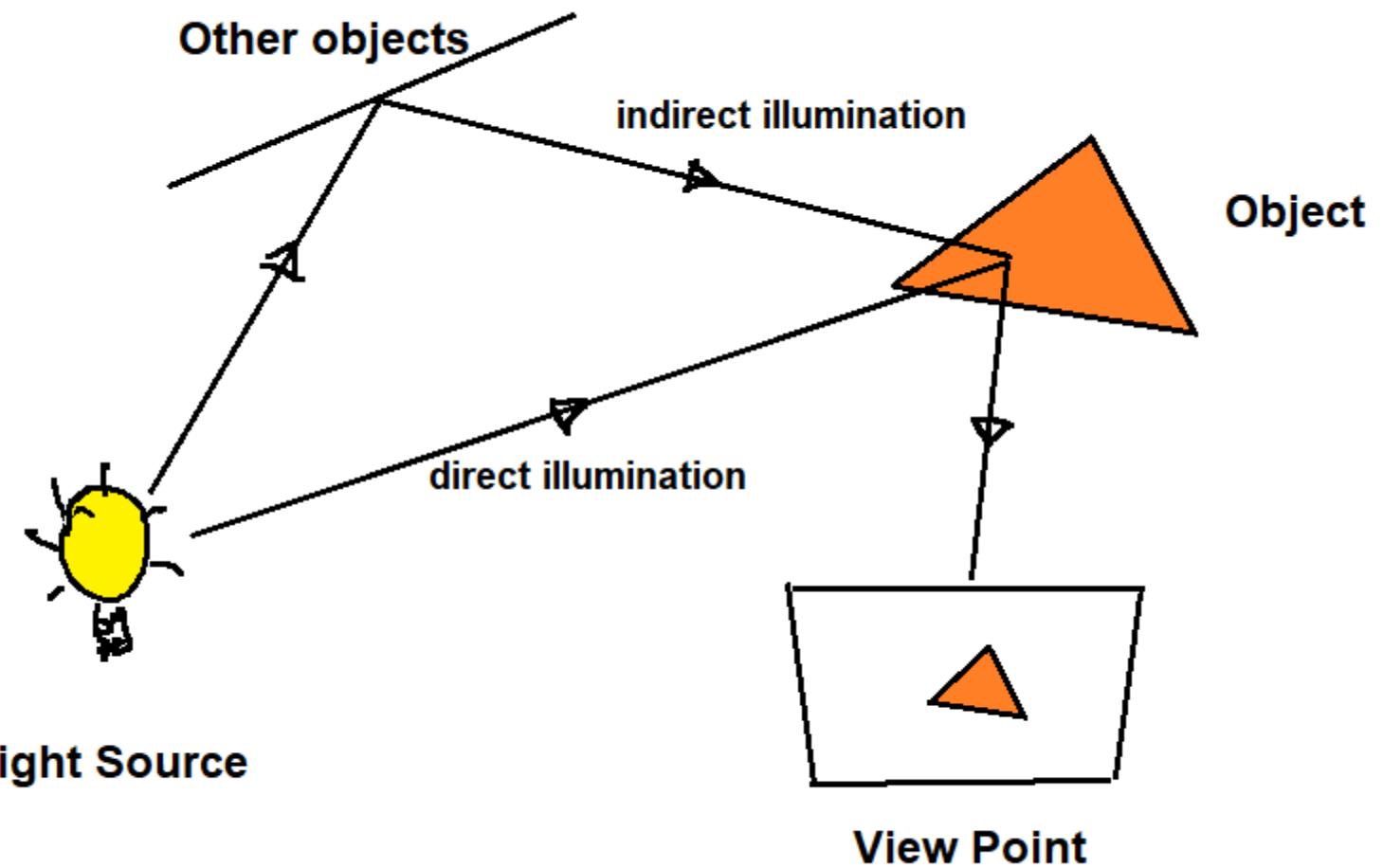


Pixel colours only

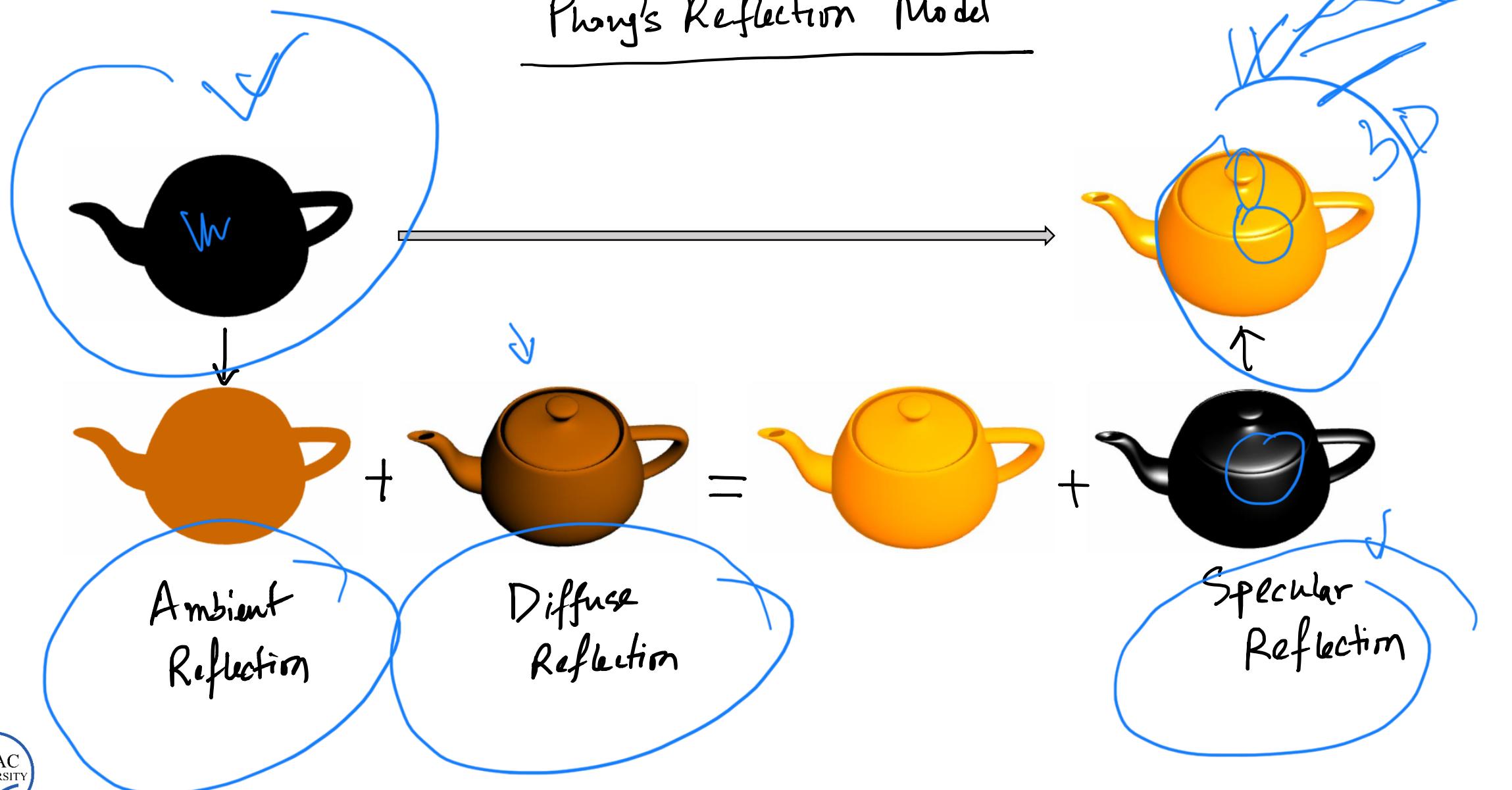


Pixel colours and lighting

Illumination



Phong's Reflection Model



Ambient Reflection

- **Ambient reflection** is the reflection of light that does not come directly from a light source
- Even in a darkened room, we can make out the edges of objects – this is because of light bouncing off of objects
- Since Phong is a **direct** lighting model, we assume that ambient light falls equally on all objects, i.e.,

$$A = \underline{I_a k_a} //$$

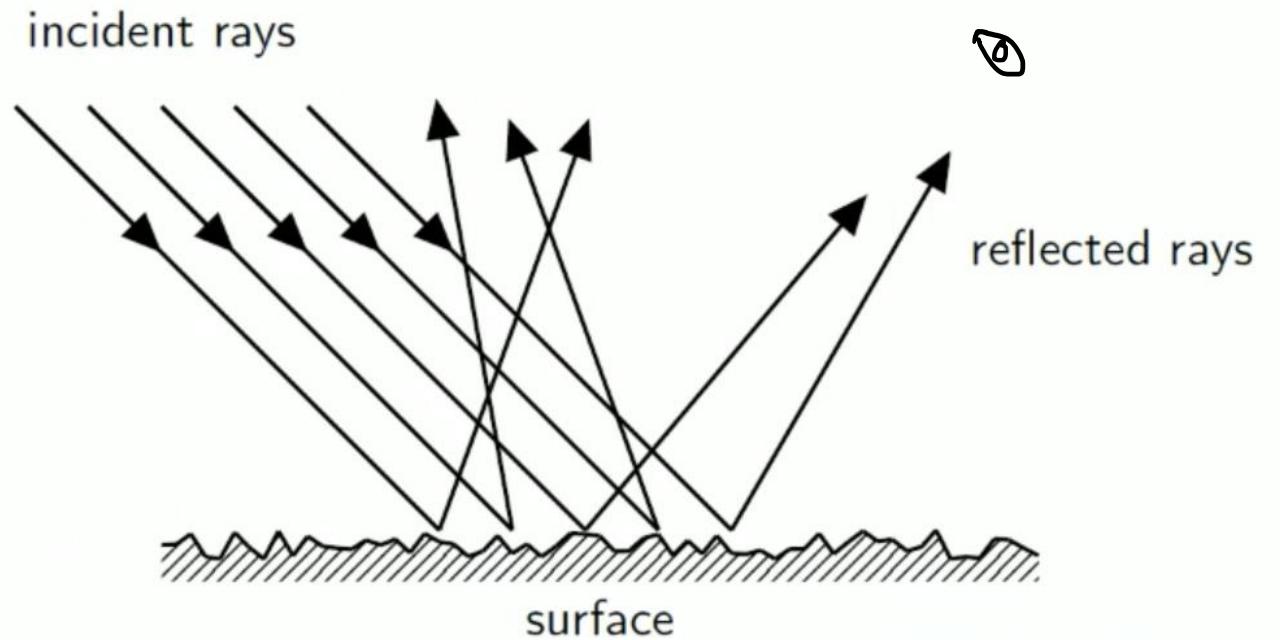
where I_a is the intensity of the ambient light and $k_a \in [0, 1]$ is the **ambient coefficient**

- k_a is set to provide the right amount of ambient light for a scene, e.g., $k \rightarrow 1$ for bright scenes and $k \rightarrow 0$ for dark or nighttime scenes.

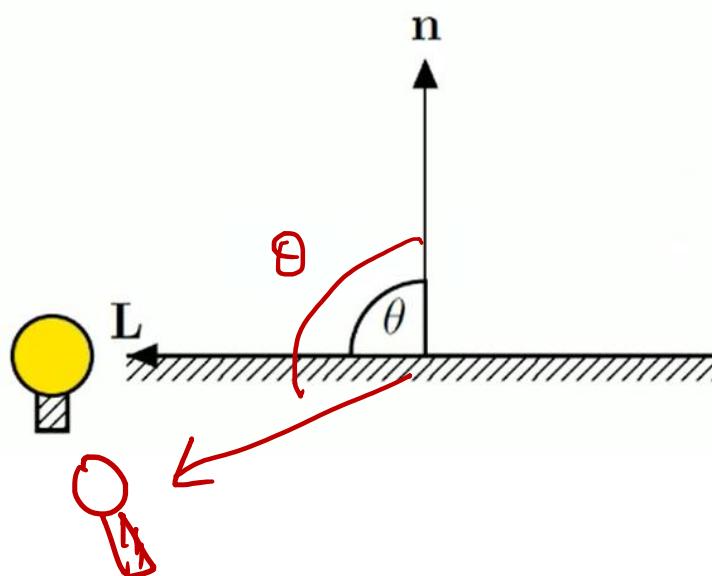
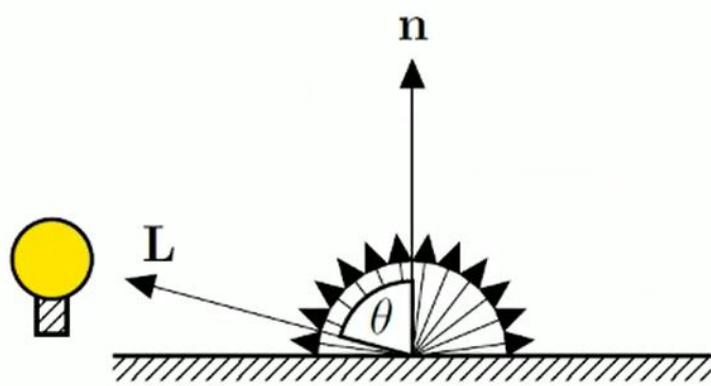
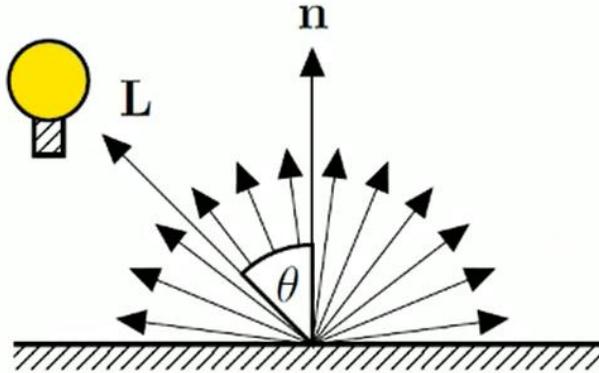
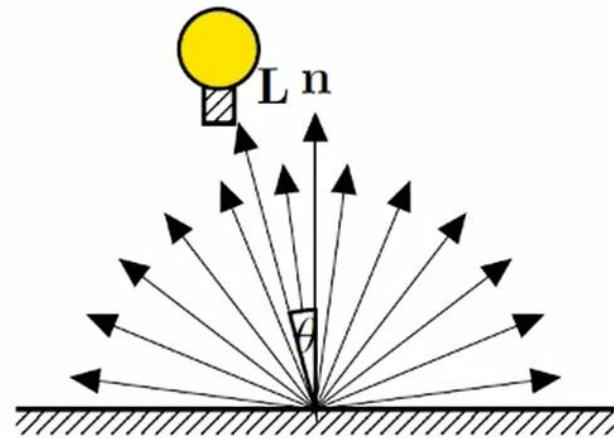


Diffuse Reflection

- ▣ Parallel rays from light source
- ▣ Reflected rays are scattered
- ▣ Direction of reflection
- ▣ Some are visible, some are not



Diffuse Reflection - Phong's model

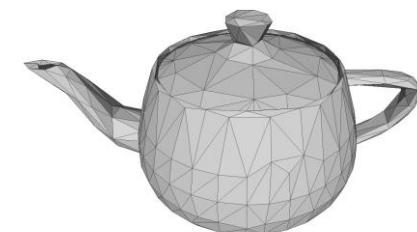


❑ Point light source

❑ Light reflected equally
in all direction

❑ "Magnitude" of reflection
depends on θ

❑ Direction of L reversed?
 $\rightarrow [-L]$



Diffuse Reflection - Phong's model



- Phong's diffuse reflection model depends upon the position of the light source relative to the surface

$$D = I_p k_d \max[\cos(\theta), 0]$$

where

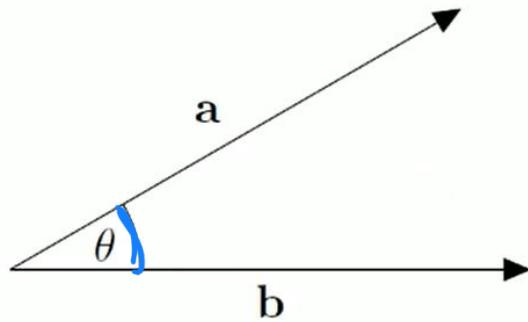
- I_p is the intensity of the point light source
- $k_d \in [0, 1]$ is the **diffuse coefficient**
- θ is the angle between the lighting vector and the surface normal
- The $\max[\cos(\theta), 0]$ is used so that no light is reflected if the light source is behind the surface

Diffuse Reflection - Phong's model

Dot product $\leftrightarrow \cos(\theta)$



$$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos \theta$$



- The definition of the dot product is

$$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos(\theta)$$

$$\underline{\underline{\mathbf{a} \cdot \mathbf{b}}} = \underline{\underline{\cos(\theta)}}$$

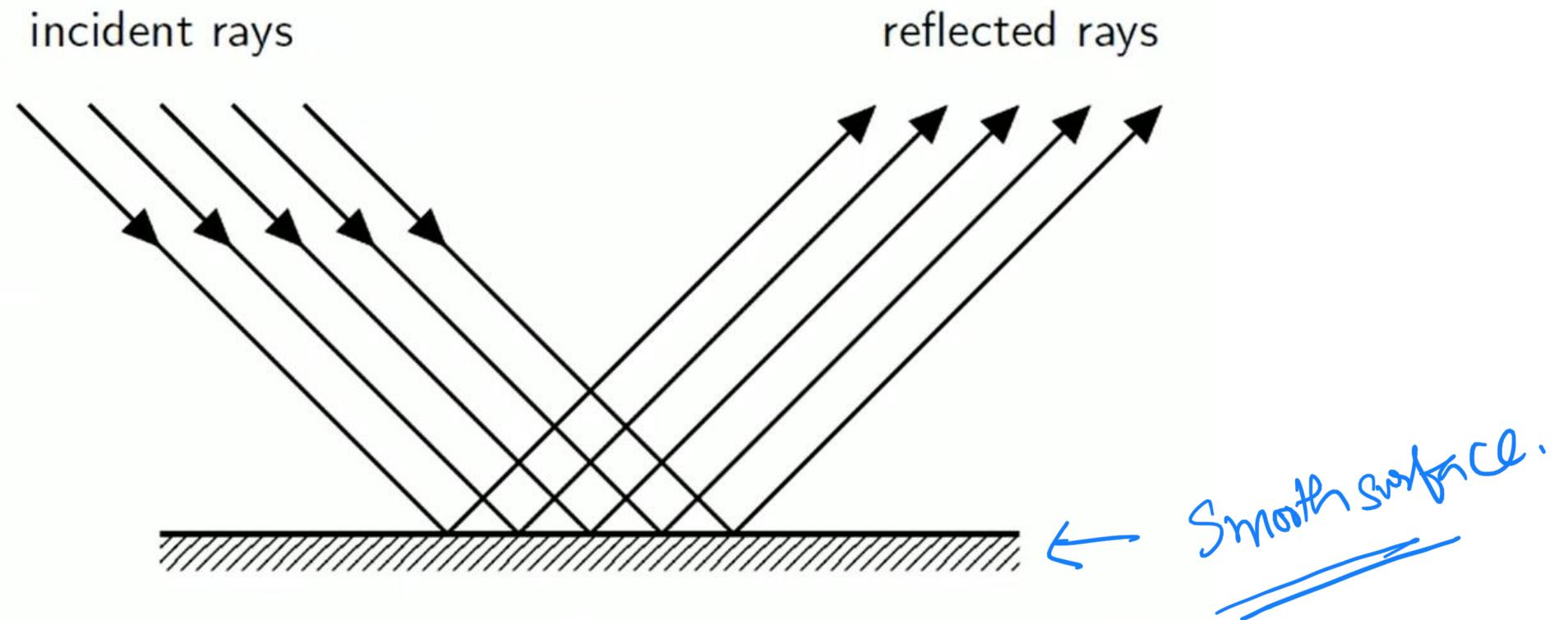
- If \mathbf{L} and \mathbf{n} are unit vectors then

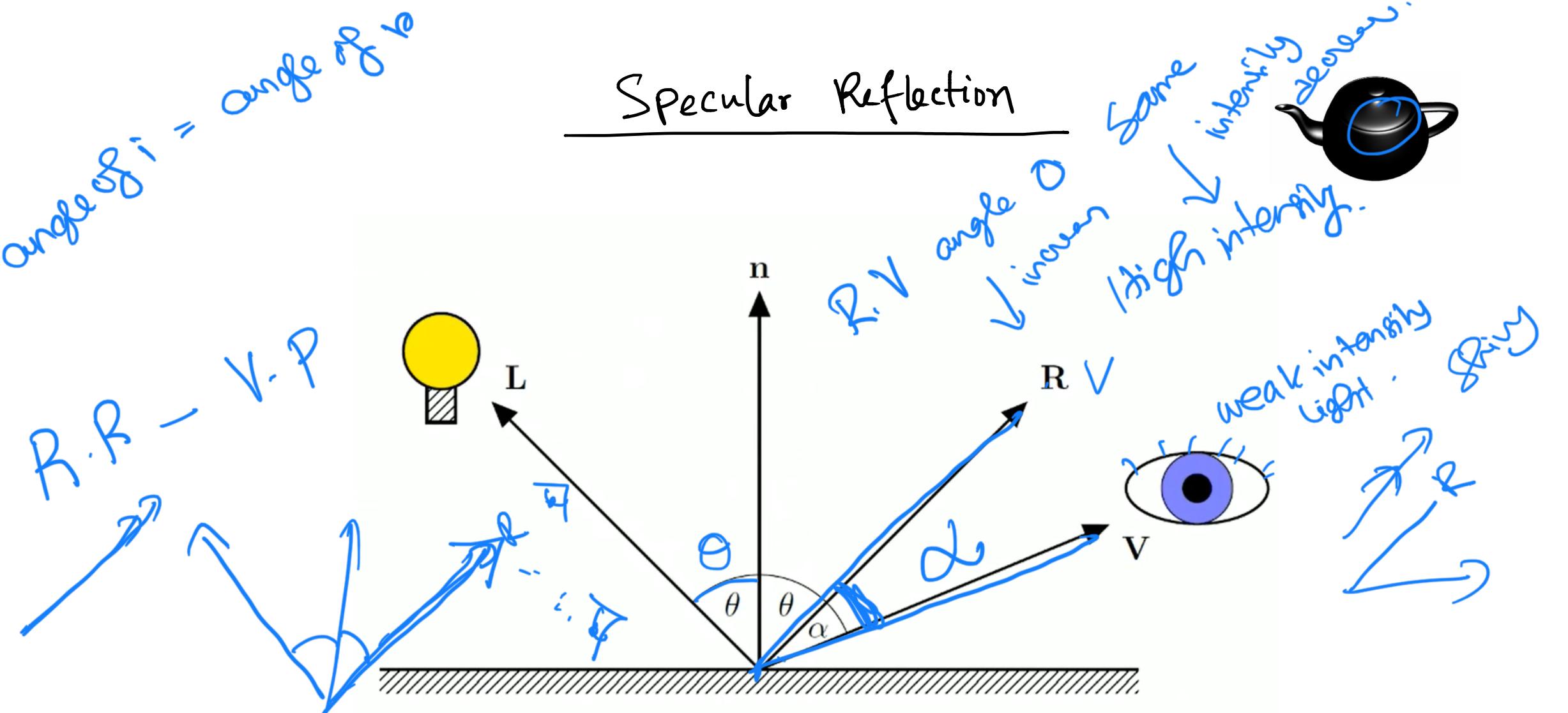
$$\mathbf{L} \cdot \mathbf{n} = \cos(\theta)$$

so we can replace the expensive cosine calculation by an easy dot product, i.e,

$$D = I_p k_d \max(\mathbf{L} \cdot \mathbf{n}, 0)$$

Specular Reflection





Specular Reflection



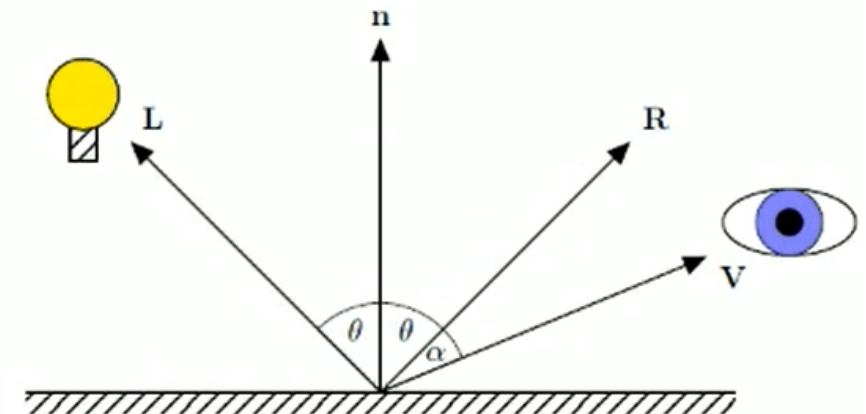
- Phong's specular model is

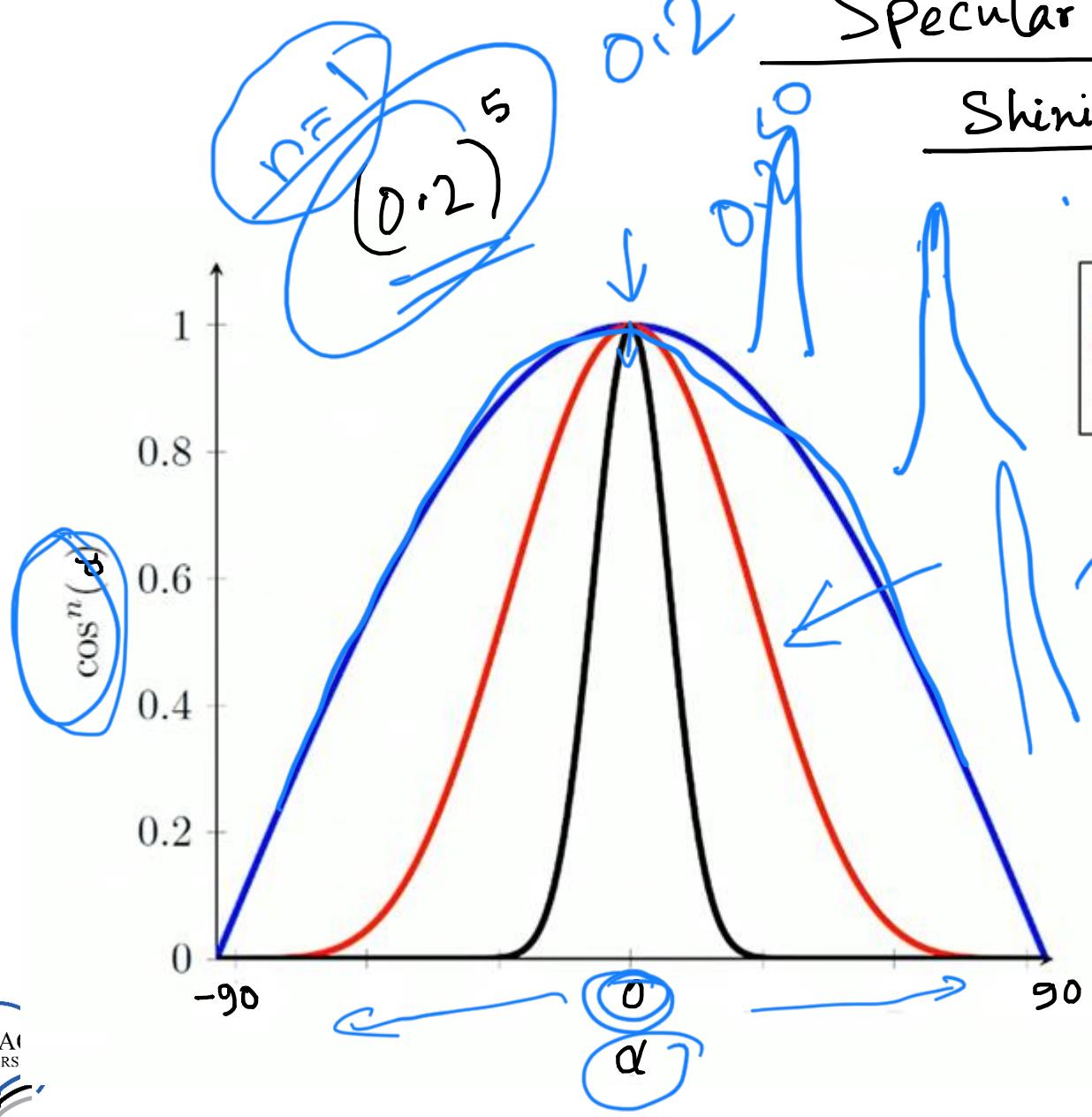
$$S = I_p k_s \cos^n(\alpha)$$

$\equiv \uparrow \uparrow - \quad I_p \times 1 = I_R$

where

- $k_s \in [0, 1]$ is the **specular coefficient**
- n is the **specular exponent** (*shininess*)
- α is the angle between \mathbf{R} and \mathbf{V}
- The $\cos^n(\alpha)$ term determines the amount of light that is reflected

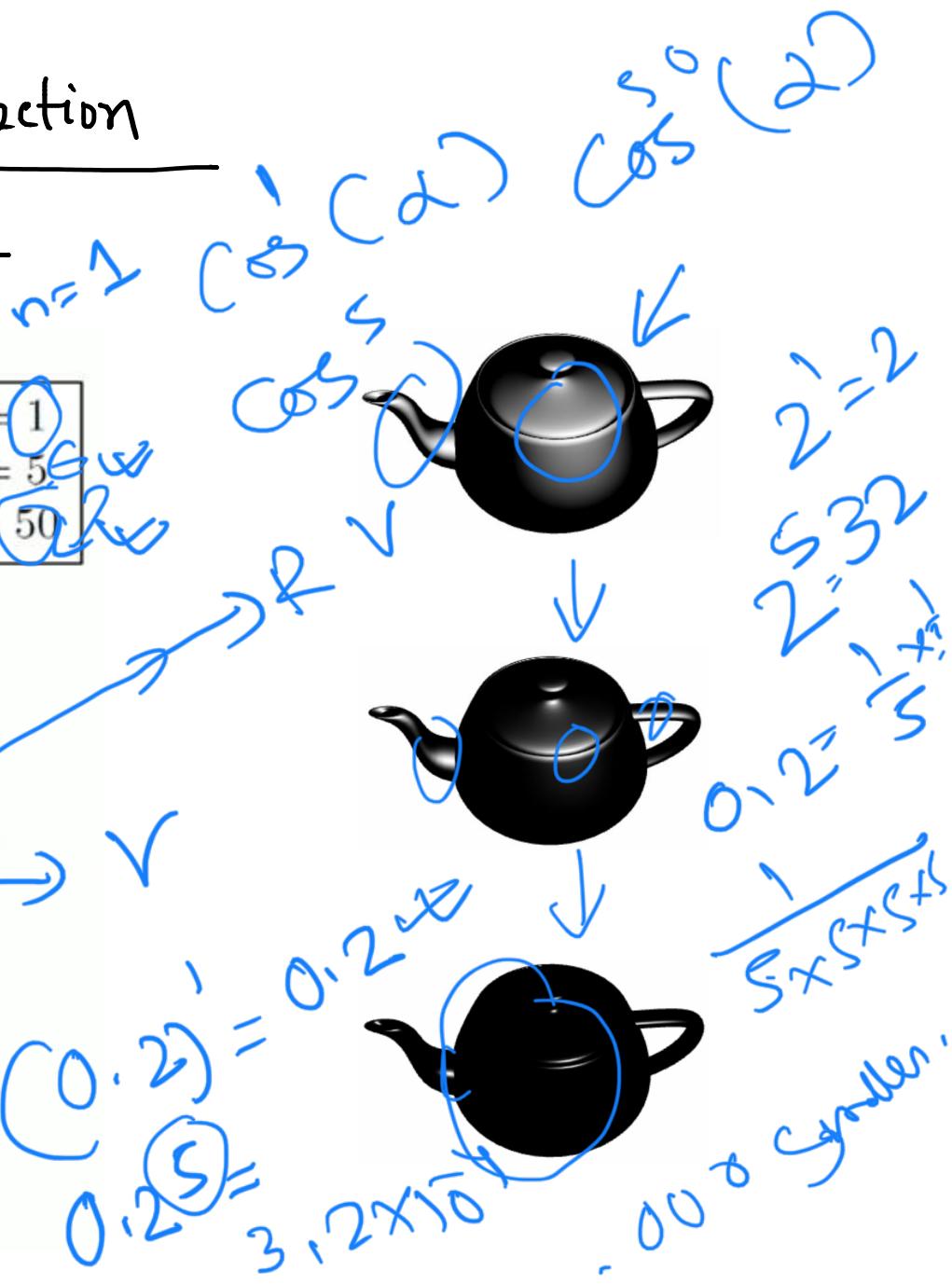




Specular Reflection

Shininess

- $n = 1$
- $n = 5$
- $n = 50$



Specular Reflection



$$S = I_p k_s \cos^n(\alpha)$$

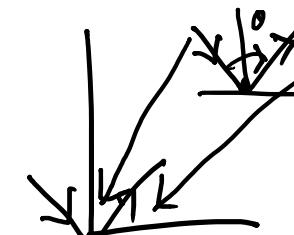
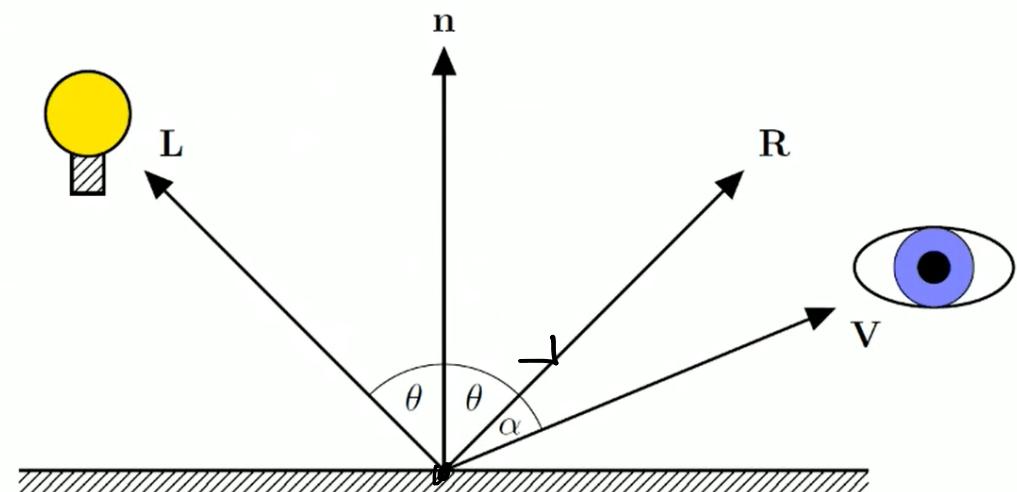
Calculate $\alpha, \cos(\alpha)$

Ⓐ $\cos(\alpha) = \underline{V \cdot R}$ [unit vectors]

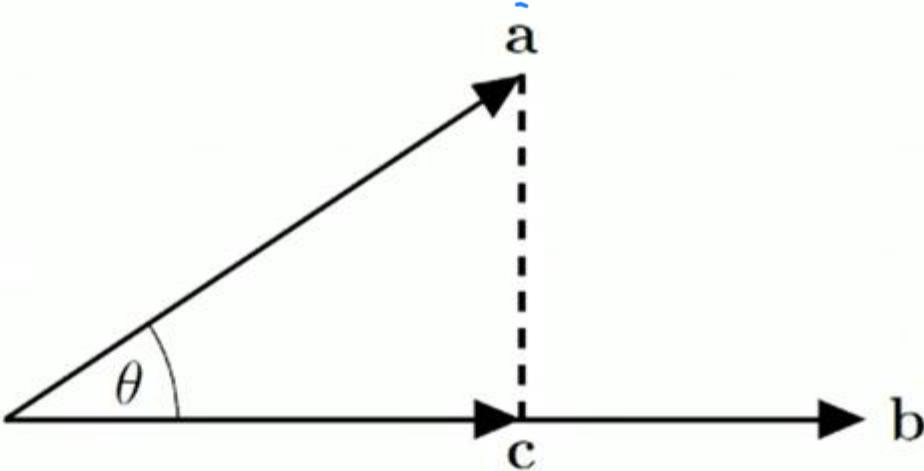
Ⓑ R

↳ Using Rotation

↳ projection of vector



Vector Projection



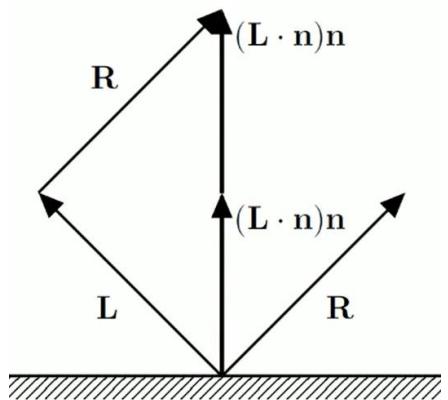
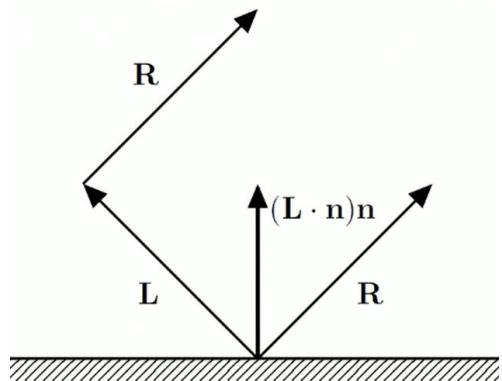
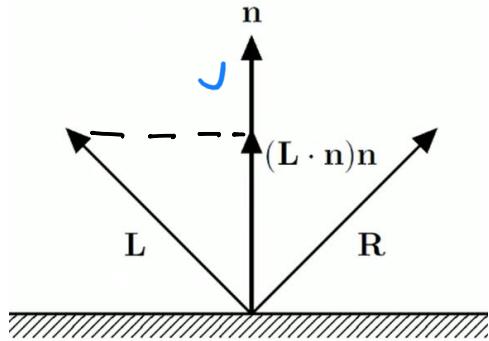
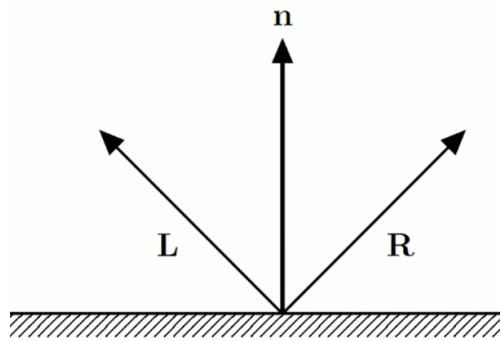
- Using the definition of a dot product

$$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos(\theta) = |\mathbf{a}| |\mathbf{b}| \frac{|\mathbf{c}|}{|\mathbf{a}|} = |\mathbf{b}| |\mathbf{c}|$$

$$\therefore |\mathbf{c}| = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{b}|}$$

- If \mathbf{b} is a unit vector then $|\mathbf{c}| = \mathbf{a} \cdot \mathbf{b}$ and

$$\mathbf{c} = \underline{(\mathbf{a} \cdot \mathbf{b})} \mathbf{b} \equiv$$



$$\begin{aligned} L + R &= 2(L \cdot n)n \\ \therefore R &= 2(L \cdot n)n - L \end{aligned}$$

Phong's Reflection Model

$$I = \frac{I_a K_d}{c} + \frac{I_p K_d \max(L_n, 0)}{\cdot} + \frac{I_p K_s (\max(V \cdot R, 0))^n}{\cdot}$$

Attenuation

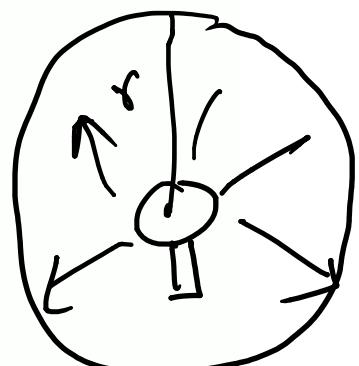
- **Attenuation** is the loss of light energy over space
- In Phong's model attenuation is account for by the variable f_{att} and applied to diffuse and specular components
- Theoretically is should follow the inverse square law, i.e.,

$$f_{att} = \frac{1}{d^2}$$

- In practice this removes too much light, Phong's model uses

$$f_{att} = \max\left[-\left(\frac{d}{r}\right)^2, 0 \right]$$

where r is the radius of the light source's sphere of influence



- Combining ambient, diffuse, specular and attenuation models results in Phong's model of reflection

$$I = \underbrace{I_a K_a}_{\text{amb}} + \cancel{I_p f_{att}} \left(\underbrace{K_d \max(L \cdot n, 0)}_{\text{diff}} + K_s (\max(V \cdot R, 0))^n \right) \underbrace{\text{Spec}}$$

- For multiple light sources, the diffuse and specular components are calculated for each light source and added together, i.e.,

$$I = \underbrace{I_a K_a}_{\text{amb}} + \sum_{i=1}^m I_{P_i} f_{att} \left(K_d \max(L_i \cdot n, 0) + K_s (\max(V \cdot R_i, 0))^n \right)$$

Shading

whether an object, or some part of an object is obstructed by another object.

- Z buffer / Depth buffer

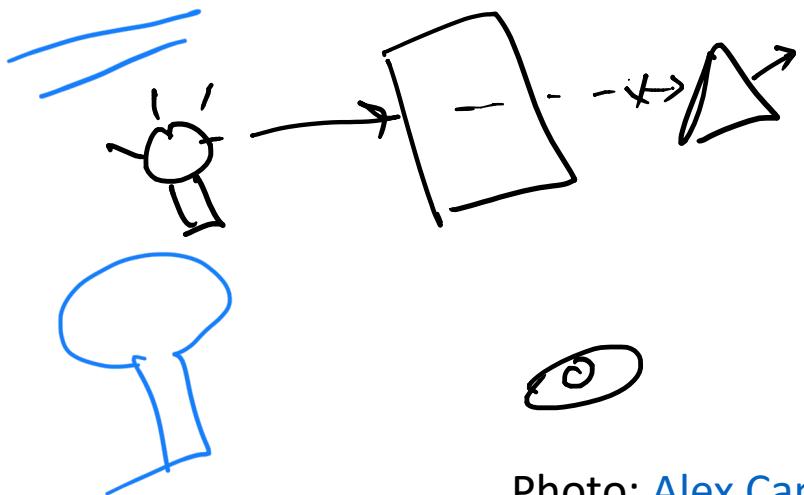


Photo: [Alex Canclini](#)

