

Line Drawing Algorithm

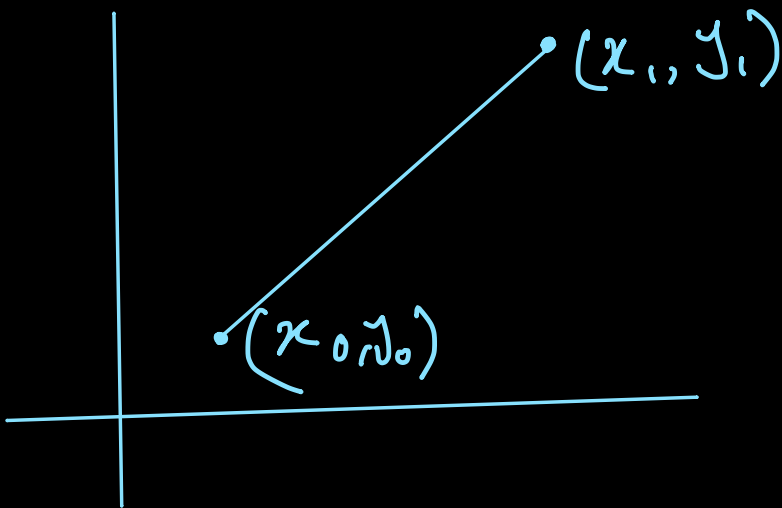
There are three ways to solve this

i) Simple Solution

ii) DDA

iii) Middle point Line Algorithm

Simple Solution



$$m = \frac{y_1 - y_0}{x_1 - x_0}$$

$$y = mx + c$$

$$\Rightarrow c = y - mx$$

$$(c = y_0 - mx_0 / c = y_1 - mx_1)$$

Using SS find out the intermediate pixel from (2,2) to (7,5)

$$m = \frac{5-2}{7-2} = \frac{3}{5} = 0.6$$

$$\begin{aligned} C &= y_0 - mx_0 \\ &= 2 - (0.6 \times 2) \\ &= 0.8 \end{aligned}$$

now, $y = 0.6x + 0.8$

	Pixel
$y(3) = 0.6 \times 3 + 0.8 = 2.6 \approx 3$	(3,3)
$y(4) = 0.6 \times 4 + 0.8 = 3.2 \approx 3$	(4,3)
$y(5) = 0.6 \times 5 + 0.8 = 3.8 \approx 4$	(5,4)
$y(6) = 0.6 \times 6 + 0.8 = 4.4 \approx 4$	(6,4)

Drawbacks

- 1) Multiplication is costly operation
- 2 Round off

DDA:

Digital Differential Analyzer

$(2, 2), (3, 0.6), (4, 2), (5, 3.8), (6, 4.4)$

$x \rightarrow 1 \quad y \rightarrow 0.6$

$$\left. \begin{aligned} x_{\text{new}} &= x_{\text{prev}} + 1 \\ y_{\text{new}} &= y_{\text{prev}} + m \end{aligned} \right\} \begin{array}{l} \text{when the slope, } m \text{ is} \\ \text{small value } m < 1 \end{array}$$

$$\left. \begin{aligned} x_{\text{new}} &= x_{\text{prev}} + \\ y_{\text{new}} &= y_{\text{prev}} + 1 \end{aligned} \right\} \begin{array}{l} \text{when the slope, } m \text{ is} \\ \text{big value } m > 1 \end{array}$$

Using DDA, find out the intermediate pixels from $(2, 2)$ to $(5, 7)$

$$m = \frac{7-2}{5-2} = \frac{5}{3} = 1.61 \dots$$

$x \left(+ \frac{1}{m} \right) \quad y (+1)$

2	2
2.6	3
3.2	4
3.8	5
4.4	6

Pixel

$(2, 2)$
$(3, 3)$
$(3, 4)$
$(4, 5)$
$(4, 6)$

Midpoint Line Algorithm

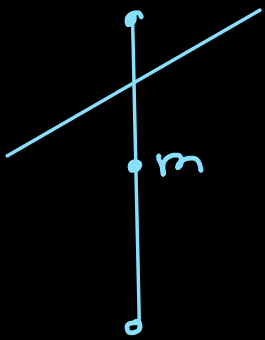
0

$$f(x, y) = ax + by + c$$

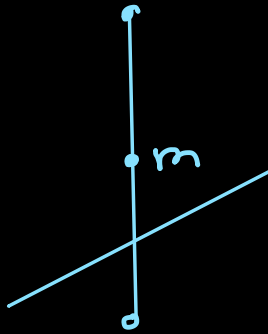
• $M(x_p, y_p)$ $\Rightarrow f(x_p, y_p) = ax_p + by_p + c = d$

0

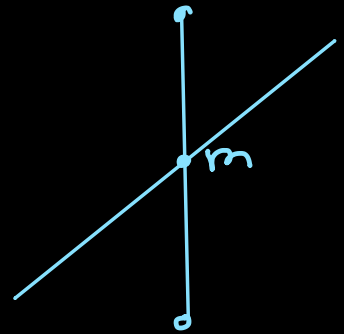
there can be three types of scenario here



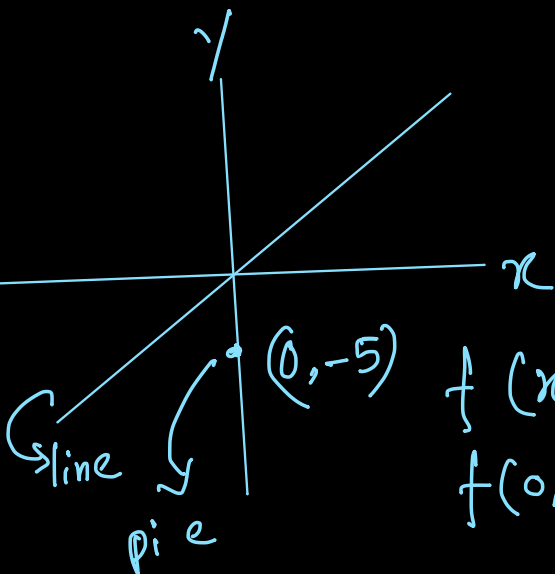
$d > 0$
(NE)



$d < 0$
(E)



$d = 0$
(E)



$$f(x, y) = x - y$$
$$f(0, -5) = 0 - (-5)$$
$$= 5$$

