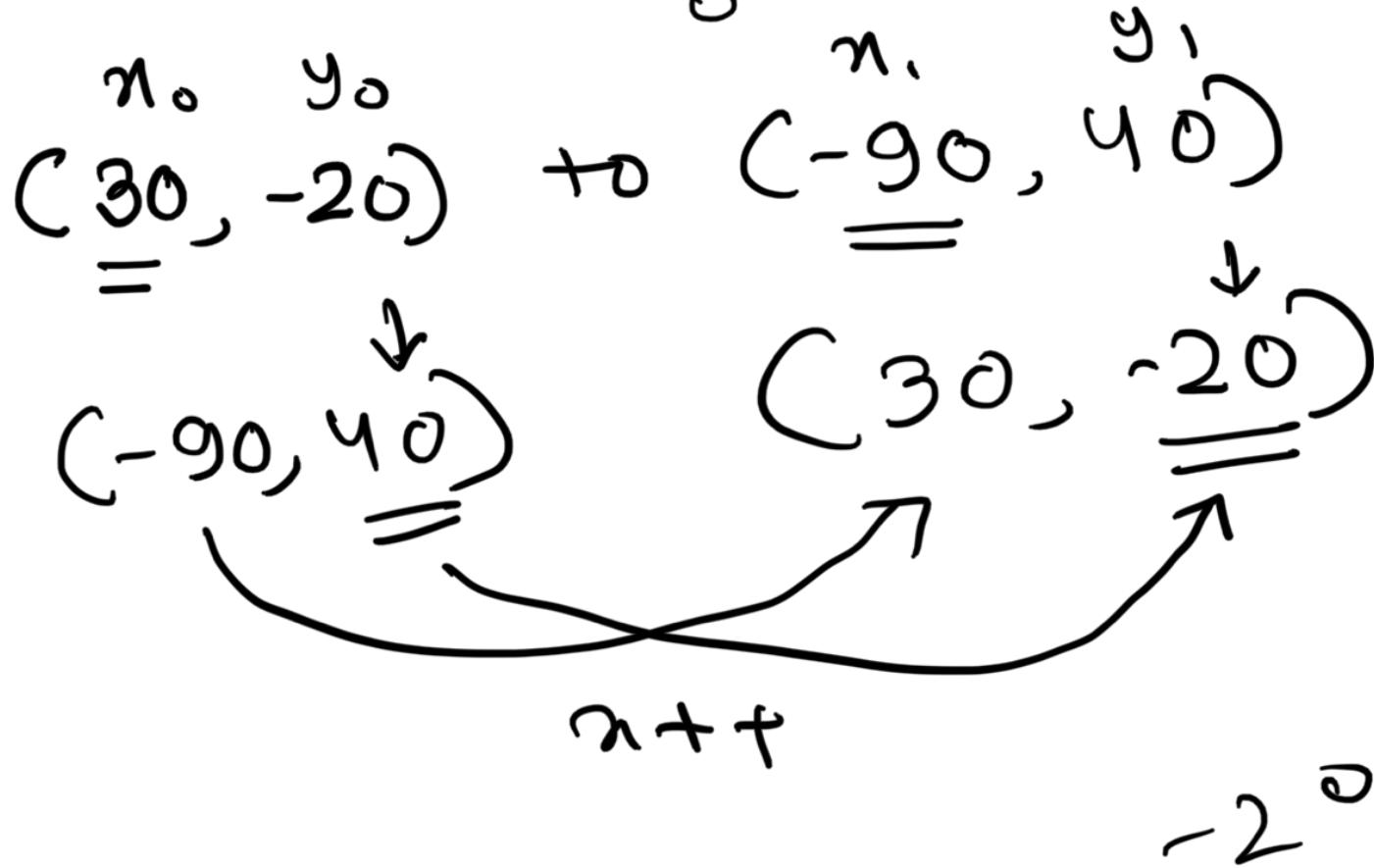
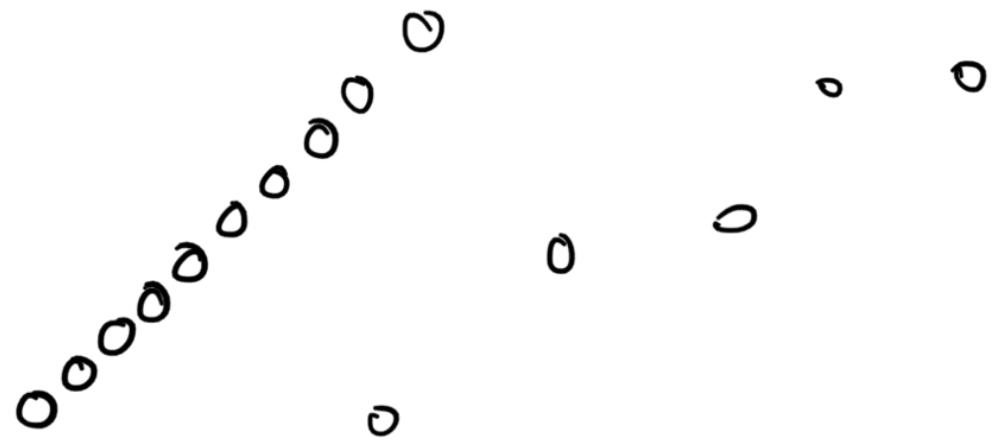


Week 2

midpoint
sym sym $y =$
 Problems!

$$m > 1$$

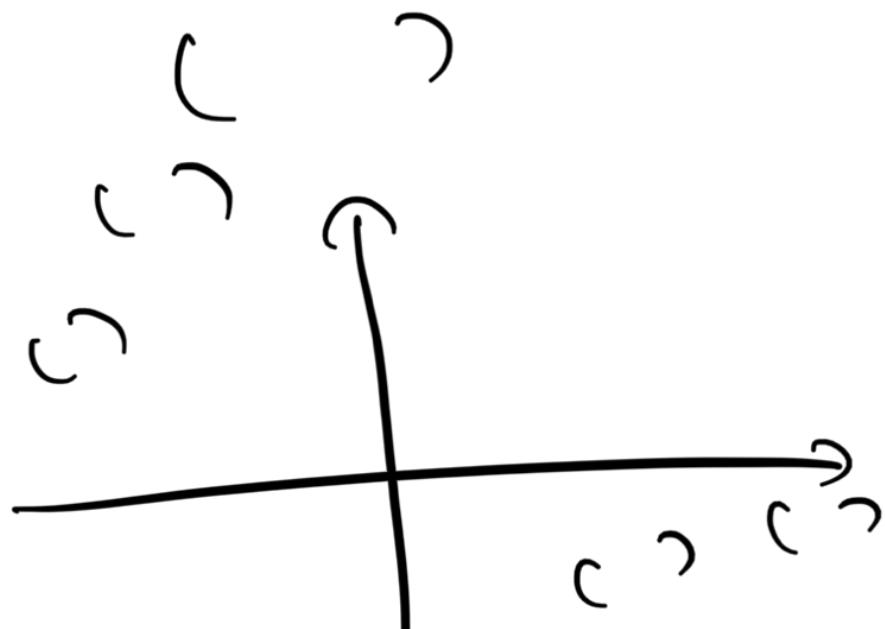


$u_0 + +$

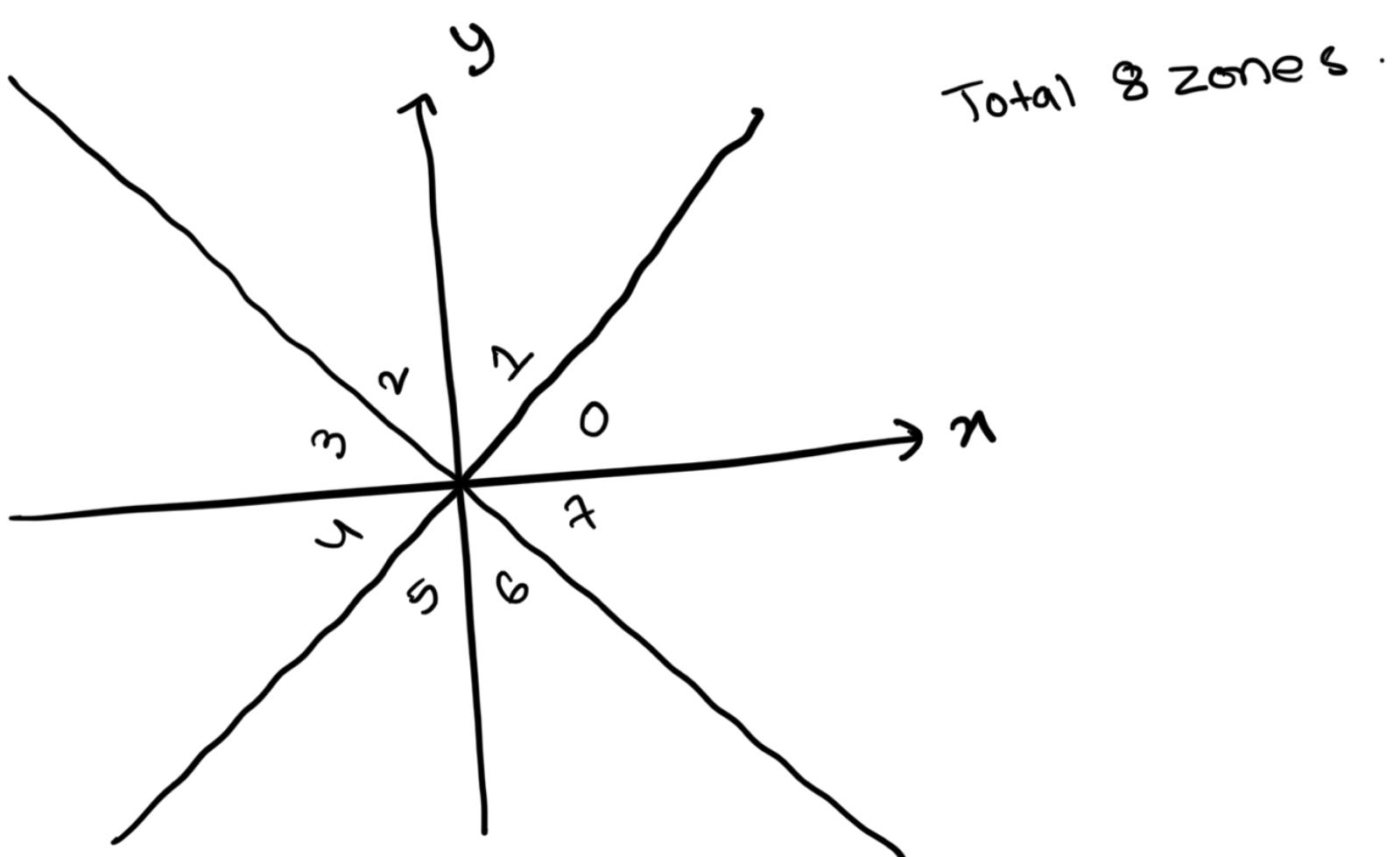
$y - -$

$\pi + +$

$\pi + +$
 $y + +$



Eight-way Symmetry

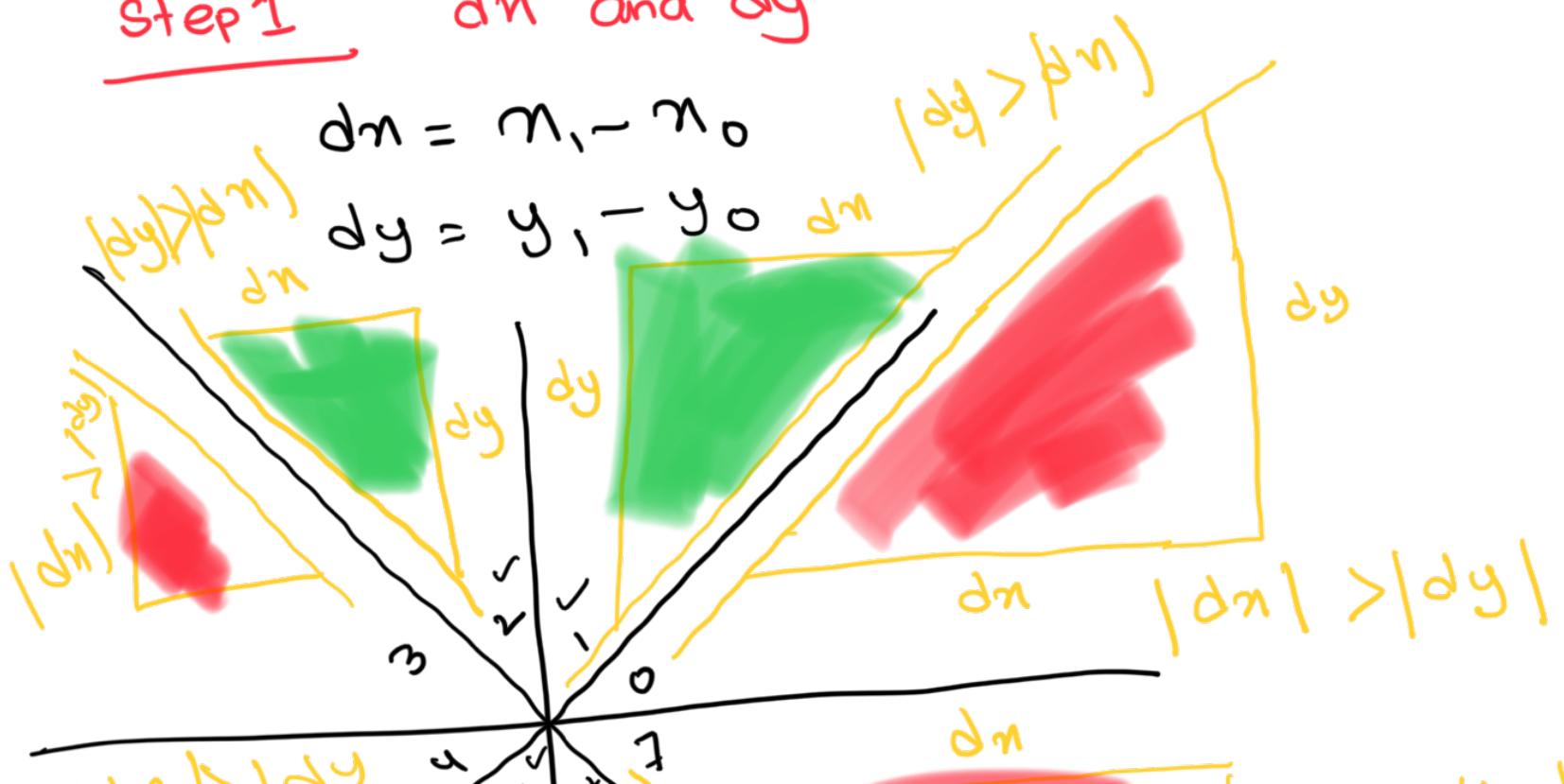


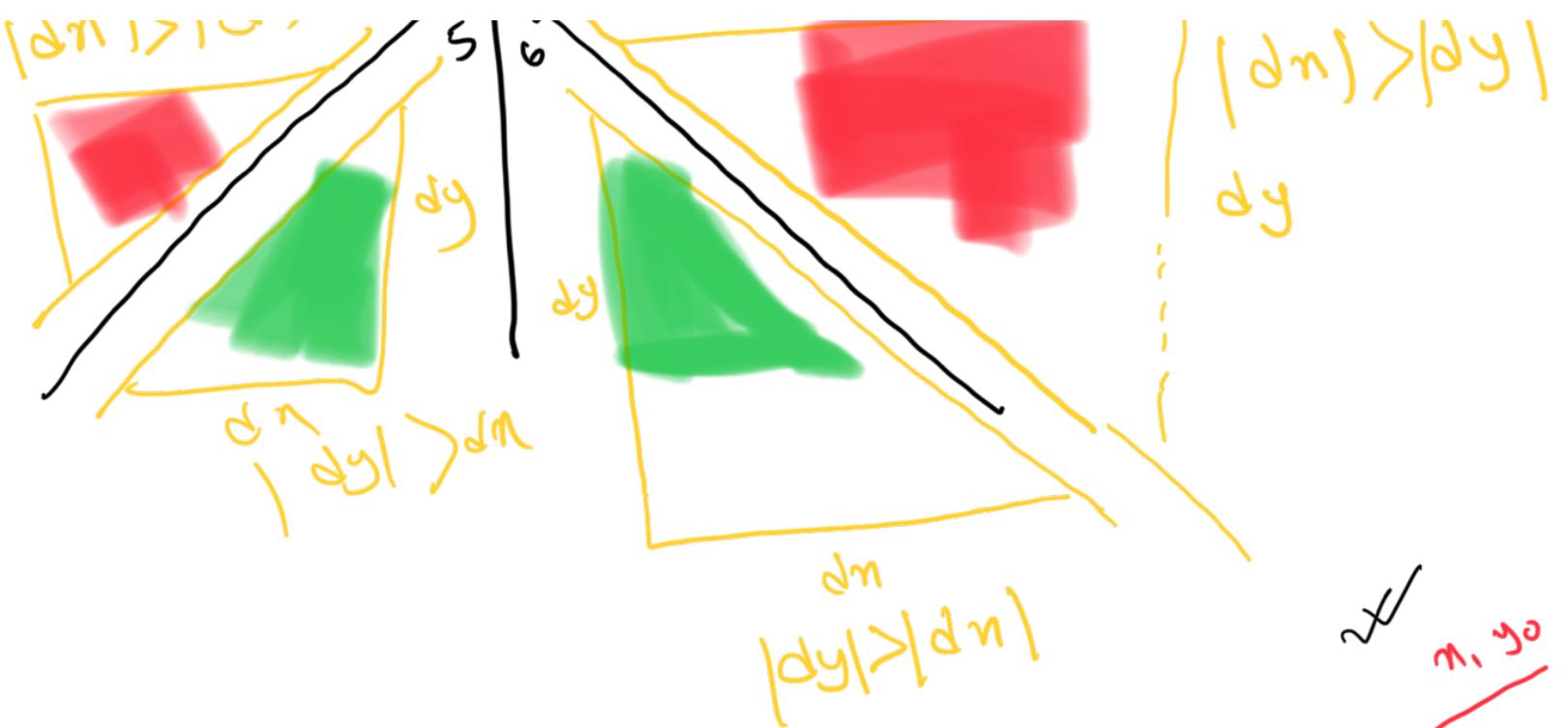
Initially, To draw a line,

Step 1 find dn and dy

$$\Delta n = n_1 - n_0$$

$$dy = y_1 - y_0 \quad \text{d}y$$





Step2 Findzone

Two types of zone

zone 1, 2, 6, 5

zone 0, 7, 3, 4

$|dy| > |dn|$

$|dn| > |dy|$

findzone (int n_0 , int y_0 , int n_1 , int y_1)

$$\text{int } dn = n_1 - n_0$$

$$\text{int } dy = y_1 - y_0$$

if ($|dn| > |dy|$) \rightarrow { //zone 0, 3, 4, 7

 if ($dn \geq 0$ $\&$ $dy \geq 0$)

 zone 0

 elif ($dn \leq 0$ and $dy \geq 0$)

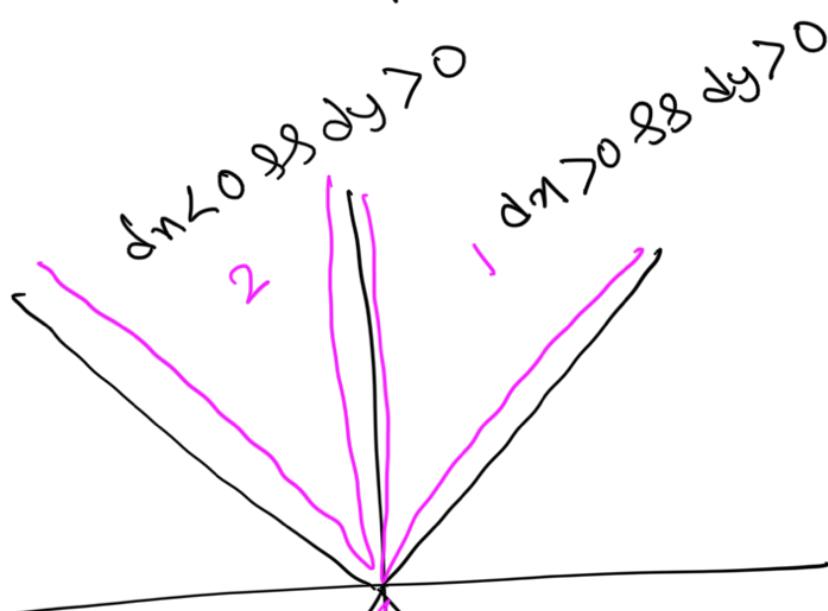
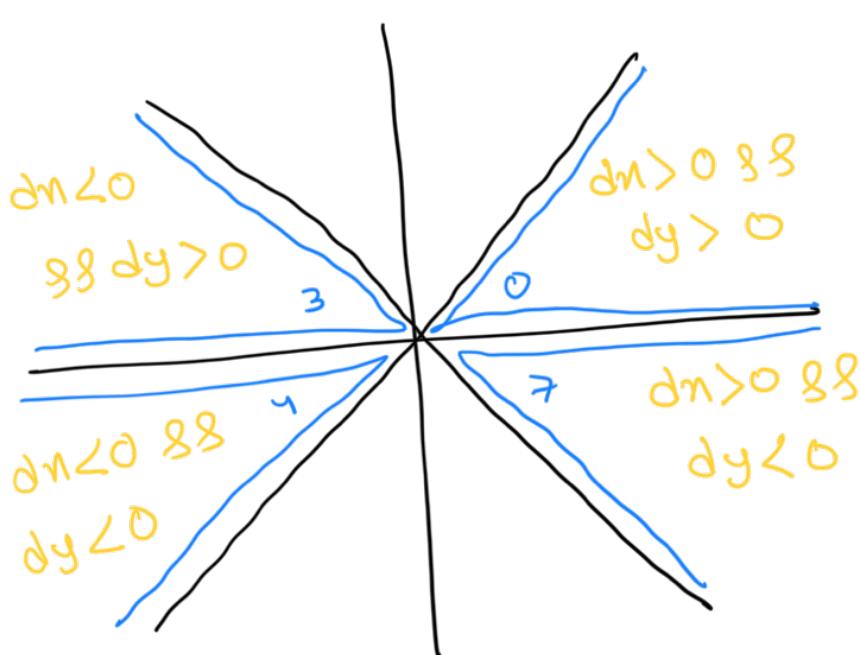
 zone = 3

 elif ($dn \geq 0$ and $dy \leq 0$)

 zone = 7

 elif ($dn \leq 0$ $\&$ $dy \leq 0$)

 zone = 4

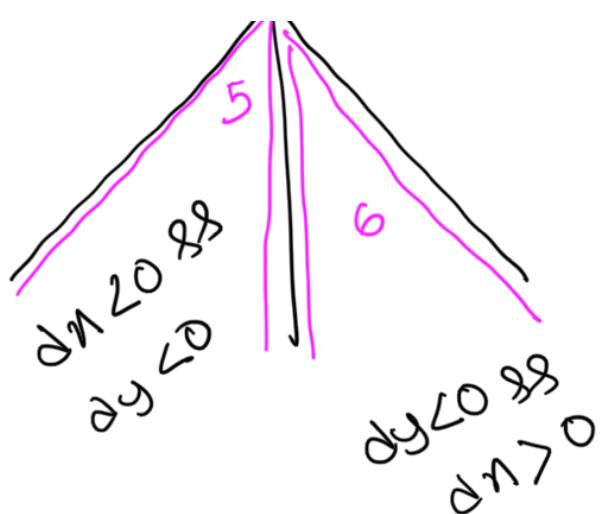


else:

 if ($dn \geq 0$ $\&$ $dy \geq 0$)

 zone = 1

 elif ($dn \leq 0$ and $dy \geq 0$)



zone=2
elif ($dn \geq 0$ $\&$ $dy \leq 0$)
zone=6
elif ($dn \leq 0$ $\&$ $dy \geq 0$)
zone=5.

For example: $(-30, -10)$ to $(-10, 30)$

$$dn = -10 - (-30) = 20 \quad dn > 0$$

$$dy = 30 - (-10) = 40 \quad dy > 0$$

$$dy > dn$$

zone=1 ←

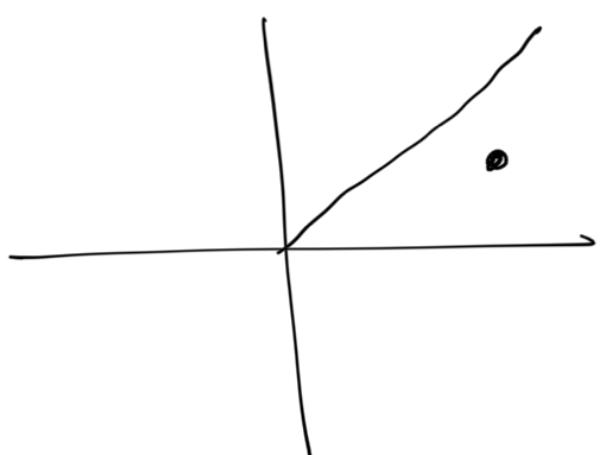
↓ ending

Step 3 Convert to zone 0 (int n, y, zone)

$$\begin{aligned} X &= 0 \\ Y &= 0 \end{aligned}$$

if (zone == 0)

$$X = n, Y = y$$



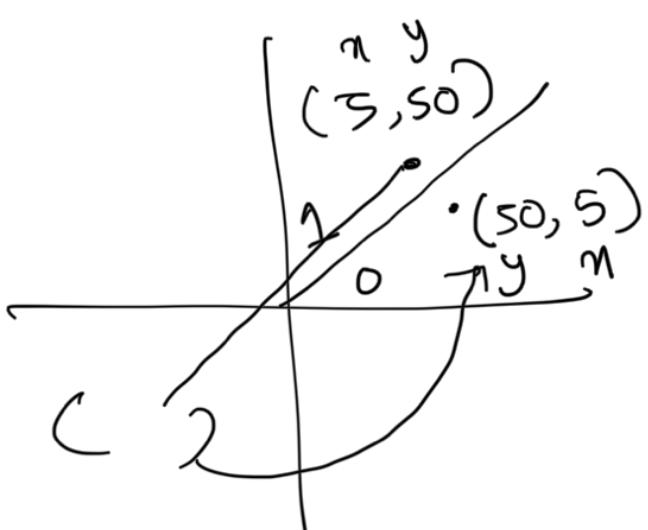
if (zone == 1)

$$X = y, Y = n$$

if (zone == 2)

$$X = y$$

$$Y = -n$$



if (zone == 3)

$$X = -n$$

$y = y$
if (zone == 4)

$x = -n$

$y = -y$

if (zone == 5)

$x = -y$

$y = -n$

if (zone == 6)

$x = -y$

$y = n$

if (zone == 7)

$x = n$

$y = -y$

New Coordinate,

(x_0, y_0)

(x_1, y_1)

x_1, y_1

x_0, y_0

Step 4 Apply Midpoint Line Algorithm

midpoint (x_0, y_0, x_1, y_1)

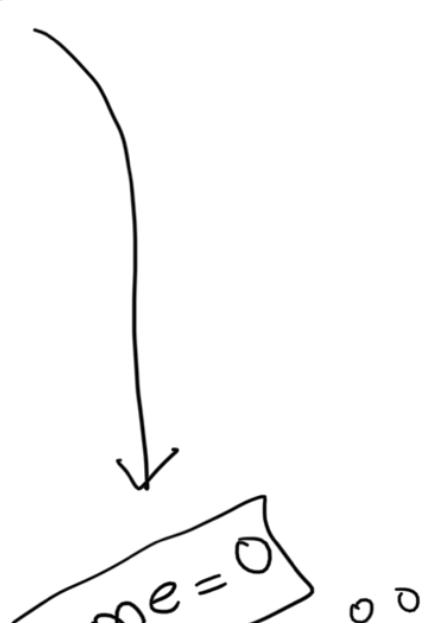
$d_n = x_1 - x_0$

$d_y = y_1 - y_0$

$D = 2 * d_y - d_n$

$DNE = 2 * (d_y - d_n)$

$D_n = 2 * d_n$



$x = -1 \quad 0 \quad 1$
 $y = 0 \quad 1 \quad 0$
 $\text{while } (n \leq x \leq 1) \{$
 Draw(n, y); ←
 $n++;$
 if ($D < 0$) {
 $D = D + DE;$ }
 else {
 $D = 0 + DNE;$ }
 $y++;$
 }
 y end

Step 5 zeroToOriginalZone(zone, x, y)

$n = 0$
 $y = 0$
 if ($zone == 0$)
 $n = x \quad y = 1$
 if ($zone == 1$)
 $n = y$ ←
 $y = n$
 if ($zone == 2$)
 $n = -y$
 $y = x$ C
 if ($zone == 3$)
 $x = -n$ C
 $y = y$
 if ($zone == 4$)
 $x = -n$
 " " "

Step 3
 OriginalZoneToZero
 $n = y, y = n$
 -
 $n = -n$
 $n = -n$
 $y = y$
 $n = -n$
 $y = -y$

$$y = -x$$

$$\text{if } (\text{zone} == 5)$$

$$x = -y$$

$$y = -n$$

$$\text{if } (\text{zone} == 6)$$

$$x = y$$

$$y = -n$$

$$\text{if } (\text{zone} == 7)$$

$$x = n$$

$$y = -y$$

Overall Step:

Two coordinates given :

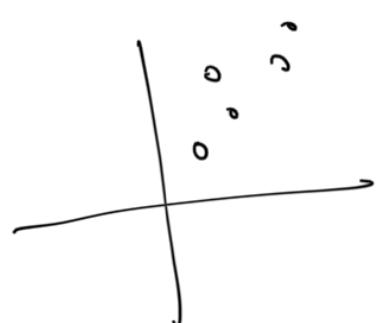
- ① Find Δx , Δy
- ② Find zone with conditions.
- ③ Convert (x, y) to zone 0
- ④ Midpoint rule Algorithm.
- ⑤ Convert to Original zone.

Example

\downarrow

$(-10, -20) \rightarrow (-20, 70)$

$x_0 \quad y_0$ $x_1 \quad y_1$



Step 1

$$dn = -20 - (-10) = -10 \quad dn < 0$$

$$dy = 70 - (-20) = 90 \quad dy > 0$$

$$dy > dn \quad |(dy) > dn|$$

$$dn \leq 0 \quad \text{as } dy > 0$$

Step 2

Zone = 2

$$(-10, -20) \quad (-20, 70)$$

Step 3

$$\begin{array}{c|cc} & n=y, y=-n & \\ \begin{matrix} (-10, -20) \\ (-20, 70) \end{matrix} & \begin{matrix} (-20, 10) \\ (70, 20) \end{matrix} & \\ \begin{matrix} n_0 \\ y_0 \end{matrix} & \begin{matrix} n_1 \\ y_1 \end{matrix} & \end{array}$$

Step 4

$$dn = 70 + 20 = 90$$

$$dy = 20 - 10 = 10$$

$$\rightarrow D = 2 \times 10 - 90 = -70$$

$$DNE = 2 \times (10 - 90) = -100$$

$$DE = 2 \times 10 = \underline{20}$$

$$n = -20, y = 10$$

$$n^0 < n^1 \xleftarrow{\text{Pixel } (-20, 10)} \xleftarrow[n=-10]{1/-70 < 0}$$

$$D < 0$$

$$d = -70 + 20 = -50$$

$$\textcircled{2} \text{ pixel } (-10, 10)$$

$$-50 < 0 \quad \begin{matrix} n = -18 \\ // E \end{matrix}$$

Zone 0

$$(-20, 10)$$

$$(-10, 10)$$

$$(-18, 10)$$

$$d = -50 + 20$$

$$\text{Zone 2} \quad (-y, n) = -30$$

$$(-10, -20) \quad \textcircled{3} \text{ pixel } (-18, 10)$$

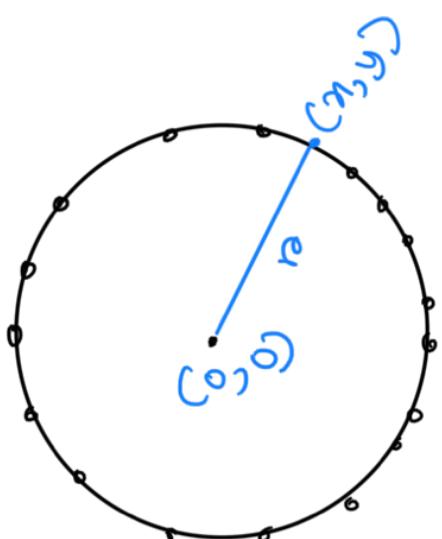
$$(-10, -10)$$

$$(-10, -18)$$

Ans

KS

Midpoint Circle



$$r = \sqrt{(x-0)^2 + (y-0)^2}$$

$$r^2 = x^2 + y^2$$

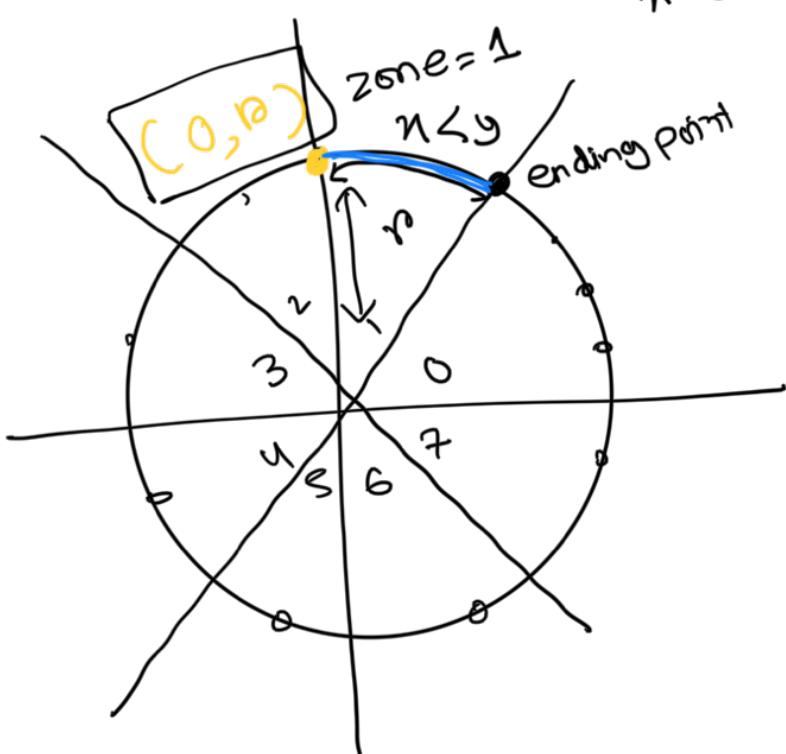
$$x^2 + y^2 - r^2 = 0$$

$$f(x, y) = x^2 + y^2 - r^2$$

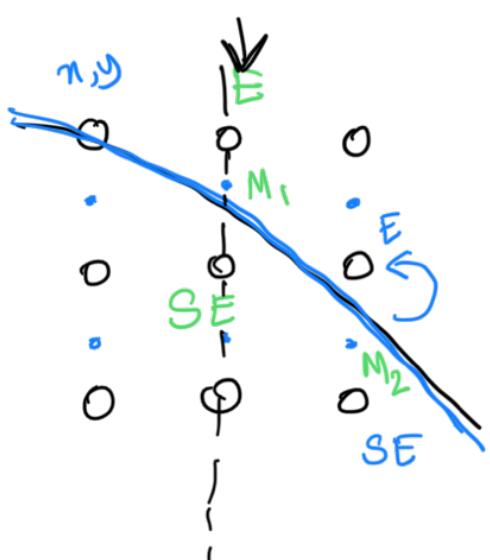
If points are on the boundary of circle

$$f(x, y) = 0$$

- arc length same
- equally divided into sectors



Zone 1



If midpoint outside the circle

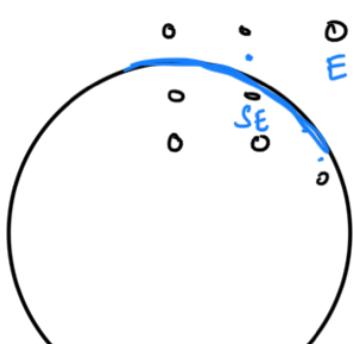
$$f(x, y) > 0$$

Choose Lower Pixel / SE

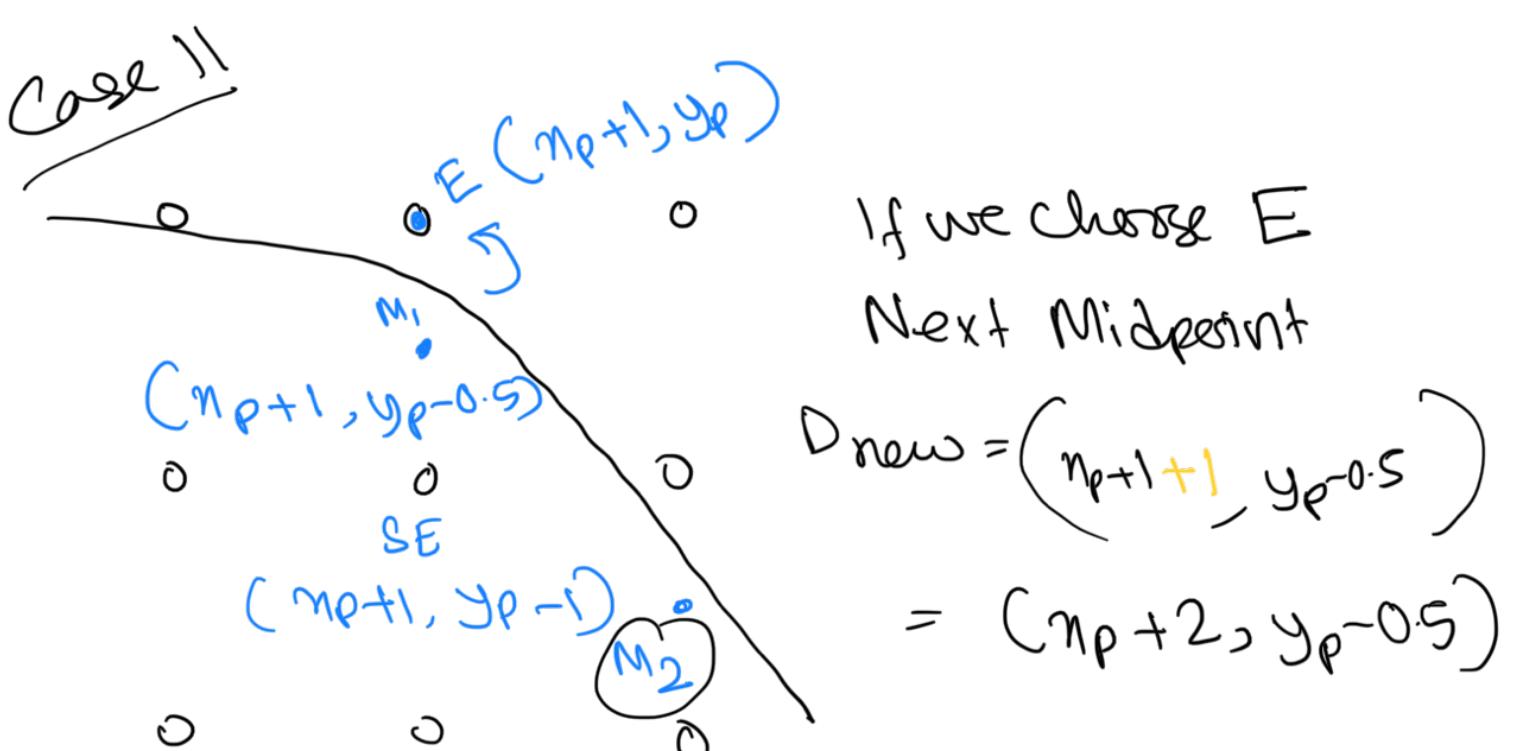
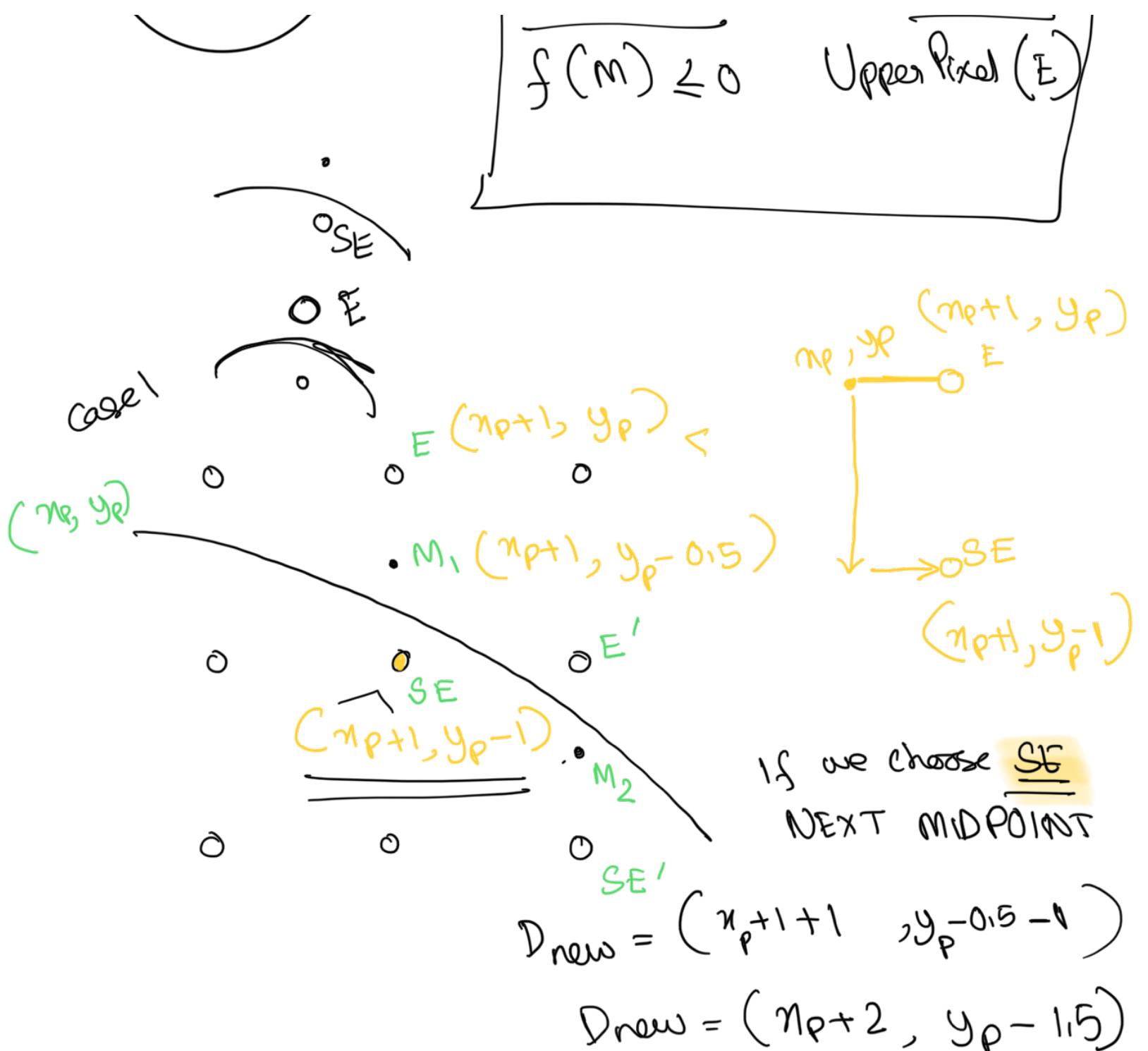
If midpoint is inside the circle

Choose Upper Pixel / E

$$f(x, y) < 0$$



$f(M)$	Pixel
$f(M) > 0$	Lower Pixel (SE)



$$\begin{aligned}
 D &= f(x_{p+1}, y_p - 0.5) & x^r + y^r - r^2 \\
 &= (x_{p+1})^r + (y_p - 0.5)^r - r^2 \\
 &= \boxed{x_p^r + 2x_p + 1 + y_p^r - y_p + 0.25 - r^2}
 \end{aligned}$$

If Pixel SE, $|d| > 0$

$$\begin{aligned}
 D_{\text{new}} &= f(n_p + 2, y_p - 1.5) \\
 &= (n_p + 2)^2 + (y_p - 1.5)^2 - r^2 \\
 &= n_p^2 + 4n_p + 4 + y_p^2 - 3y_p + 2.25 - r^2
 \end{aligned}$$

$$D_{\text{new}} - D = 2n_p + 3 - 2y_p + 2$$

$$D_{\text{new}} = D + 2n_p - 2y_p + 5 \quad \begin{matrix} d > 0 \\ // SE \end{matrix}$$

If E // $d < 0$

$$D_{\text{new}} = f(n_p + 2, y_p - 0.5)$$

$$D_{\text{new}} = (n_p + 2)^2 + (y_p - 0.5)^2 - r^2$$

$$= n_p^2 + 4n_p + 4 + y_p^2 - y_p + 0.25 - r^2$$

$$\begin{aligned}
 D_{\text{new}} - D &= n_p^2 + 4n_p + 4 + y_p^2 - y_p + 0.25 - r^2 \\
 &\quad - n_p^2 - 2n_p - 1 - y_p^2 - y_p - 0.25 + r^2
 \end{aligned}$$

$$D_{\text{new}} = D + 2n_p + 3 \quad \leftarrow$$

Stashing

$$\begin{aligned}
 D_{in} &= f(n_p + 1, y_p - 1/2) \quad \begin{cases} n_p = 0 \\ y_p = r \end{cases} \\
 &= f(1, r - 0.5) \\
 &= 1^2 + (r - 0.5)^2 - r^2 \\
 &= 1 + y_p^2 - r^2 + 0.25 - r^2
 \end{aligned}$$

$$D = 1.25 - r$$

Round off

$$D = 1 - r$$

func Midpoint Circle (int r, int value)

int n, y, d;

$$d = 1 - r^2$$

$$n = 0$$

$$y = r$$

Circle points (n, y, value)

while $n < y$ {

if ($d < 0$) { // E

$$d = d + 2n + 3$$

$$n = n + 1 \quad \}$$

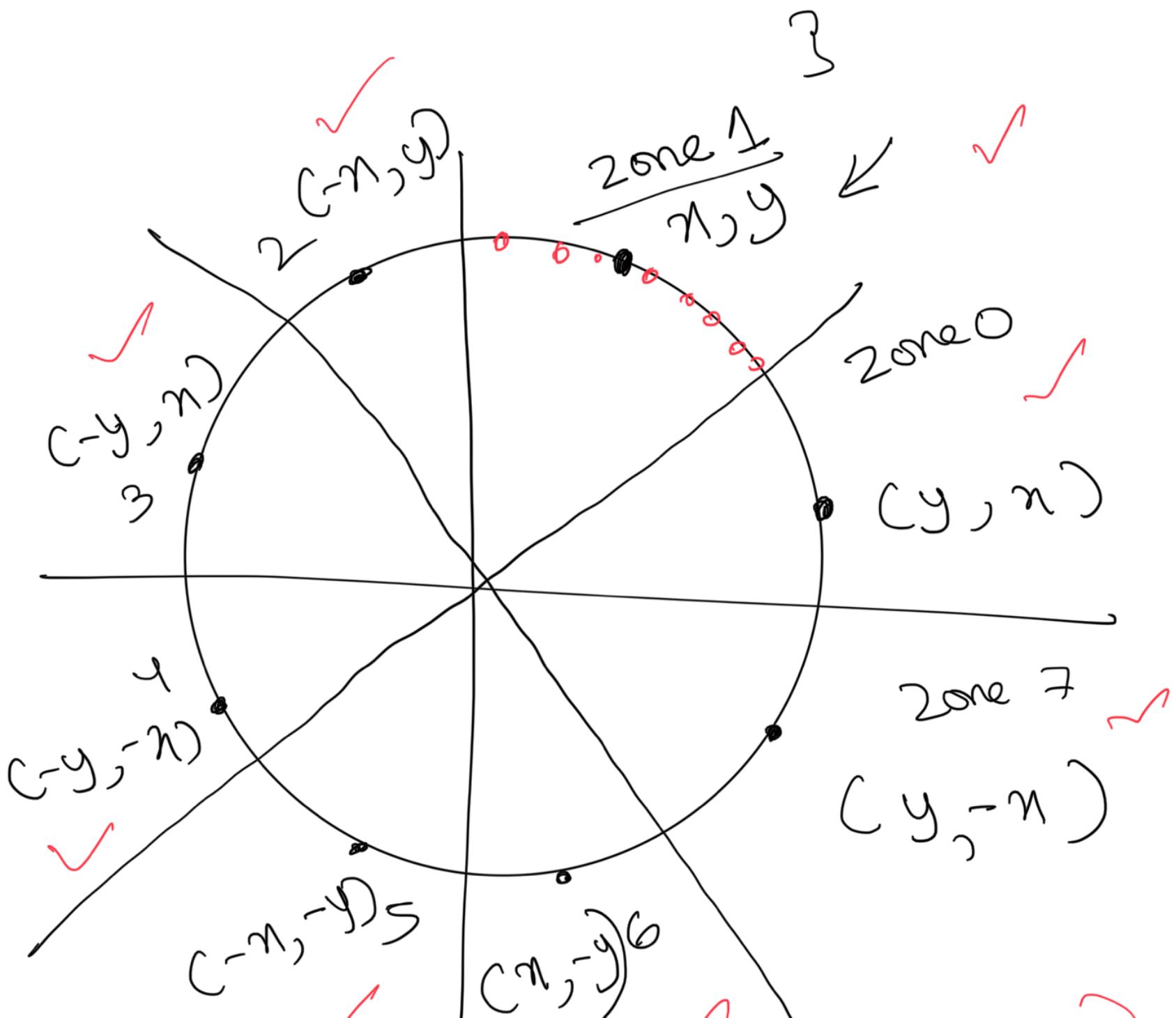
else { // SE

$$d = d + 2n - 2y + 5$$

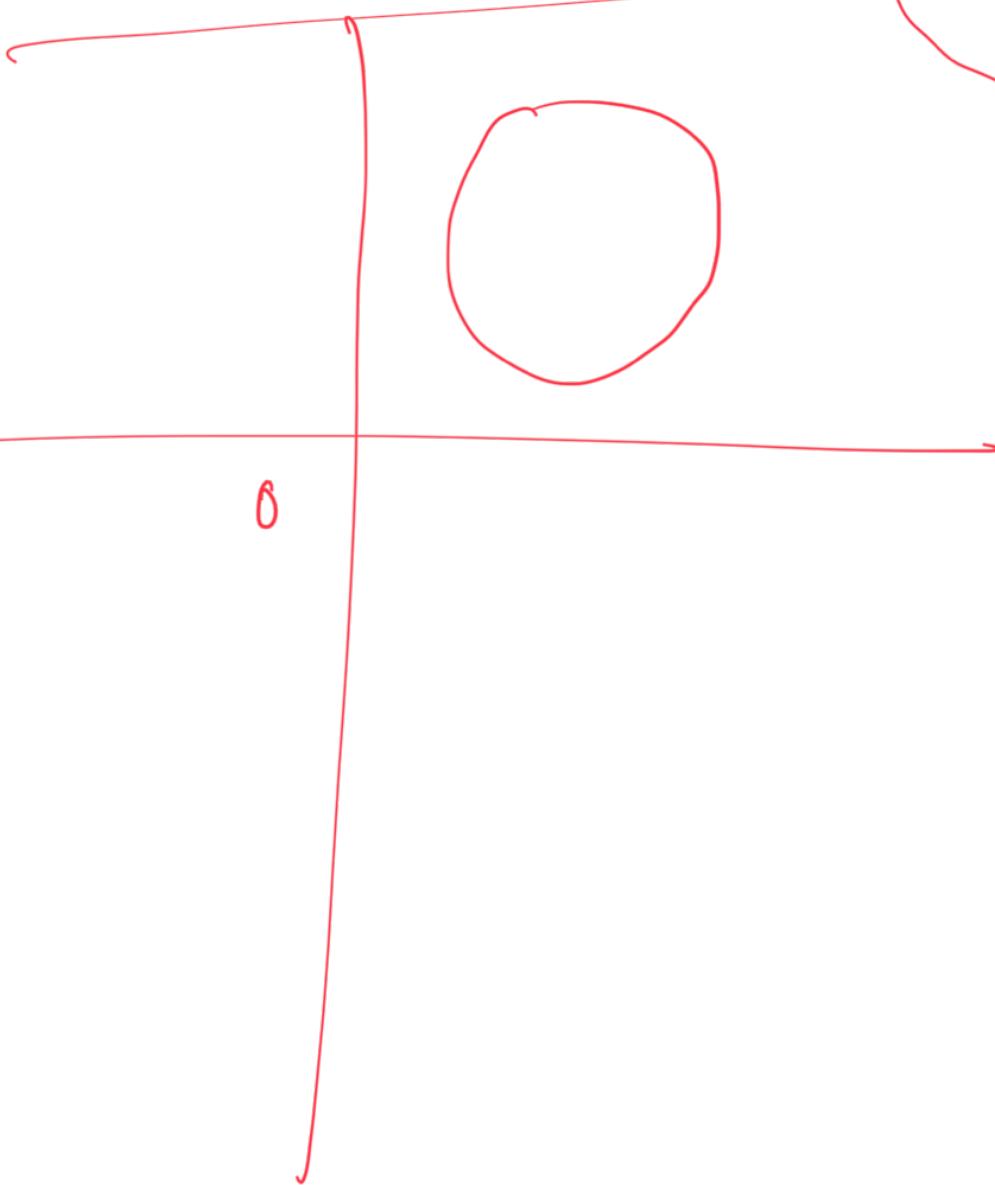
$$n = n + 1$$

$$y = y - 1 \quad \}$$

Circle $(n, y, \text{value}) \}$



$(5, 6)$



$(\cancel{O_2}, \cancel{S})$
 (O, \cancel{O})
Curve

m, y $m+5, y+6$

Two sets of parallel horizontal arrows pointing right, indicating translation vectors.

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