CSE460: VLSI Design

Lecture 8: Finite State Machines (Part 1)

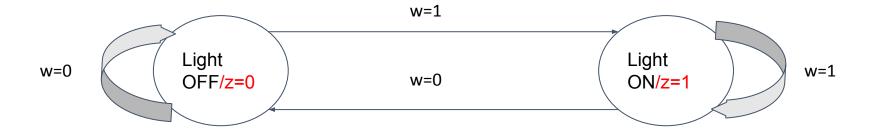
A very simple controller[a light switch!!]

```
Light OFF -> Light OFF [same state] [switch OFF, w=0]

Light OFF -> Light ON [change of state] [switch ON, w=1]

Light ON -> Light ON [same state] [Switch ON, w=1]

Light ON -> Light OFF [change of state] [switch OFF, w=0]
```

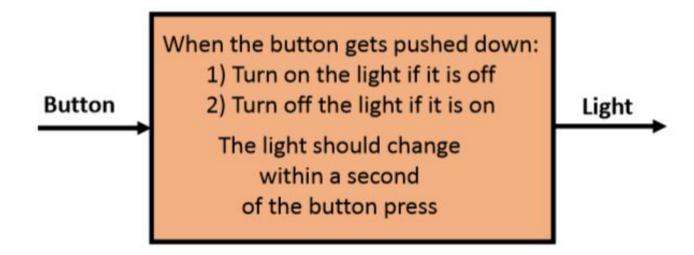


WHAT HAPPENS TO THE OUTPUT??

Light OFF -> z=0 Light ON -> z=1

Let's change the problem!!

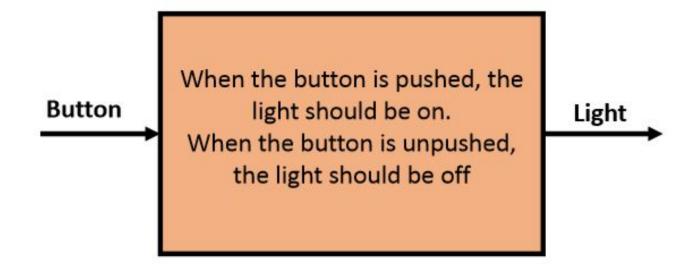
• What if you were given the following design specification:



What makes this circuit so different from those we've discussed before?

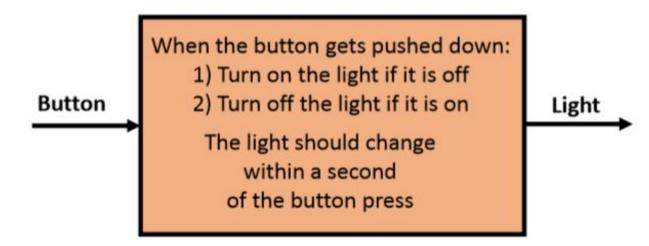
Something We Can Build (So Far)

• What if you were given the following design specification:



What makes this circuit so different from those we've discussed before?

Specifications:



- 1. "State" -i.e. the circuit has memory (become "state-ful").
- 2. The output was changed by an input "event" (pushing a button) rather than an input "value" (output may depend on previous inputs).

Illustration of the previous example

```
Light OFF -> Light OFF [same state] [Button unpushed, w=0]
Light ON -> Light ON [same state] [Button unpushed, w=0]

Light OFF -> Light ON [change of state] [Button pushed, w=1]
Light ON -> Light OFF [change of state] [[Button pushed, w=1]

w=1

Light
OFF/z=
0

w=1

Light
ON/z=1

w=0
```

WHAT HAPPENS TO THE OUTPUT??

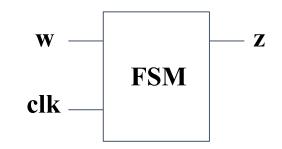
Light OFF -> z=0 Light ON -> z=1

Example 1

An automatically-controlled vehicle is designed to run at some predetermined speed. However, due to some operational conditions the speed may exceed the desirable limit, in which case the vehicle has to be slowed down. To determine when such action is needed, the speed is measured at regular intervals.

- Let a binary signal w indicate whether the speed exceeds the required limit, such that w = 0 means that the speed is within acceptable range and w = 1 indicates excessive speed.
- The desired control strategy is that if w = 1 during **two** or more consecutive measurements, **a** control signal z must be 1 to cause the vehicle to slow down. Thus, z = 0 allows the current speed to be maintained, while z = 1 reduces the speed. Let a signal Clock define the required timing intervals, such that the speed is measured once during each clock cycle.

Example 1



From previous example 1, we wish to design the circuit that meets the following specification:

- 1. The circuit has one input w, and one output z.
- 2. All changes in the circuit occur on the **positive edge** of a clock signal.
- 3. The output z is equal to 1 if during two immediately preceding clock cycle the input w was equal to 1. Otherwise the value of z is equal to 0.

Clockcycle:	t_0	t_1	t_2	t_3	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
w:	0	1	0	1	1	0	1	1	1	0	1
<i>z</i> :	0	0	0	0	0	1	0	0	1	1	0

Figure 3: Sequences of input and output signals.

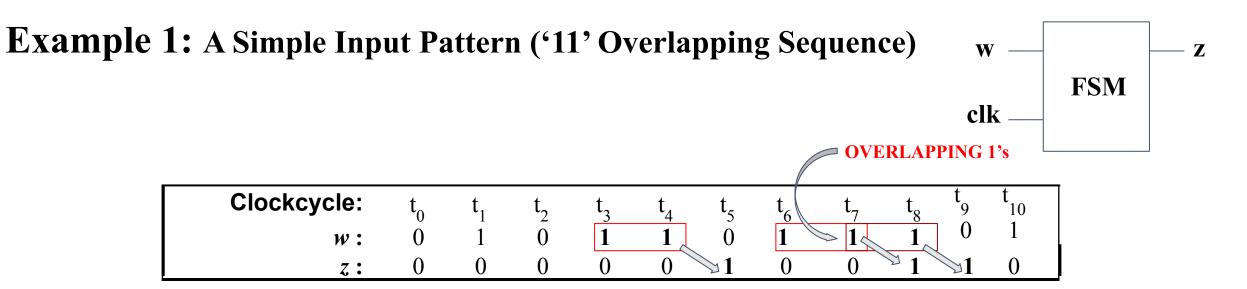
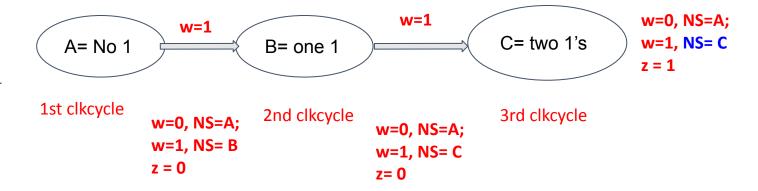


Figure 4: Sequences of input and output signals.

The circuit detects two consecutive '1'. So, it must keep in memory how many '1' it received in its input. So, a state diagram is introduced.

- A state- no '1' in input,
- **B** state- one '1' in input and
- C state- two '1' in input.



Example 1: A Simple Input Pattern ('11' Overlapping Sequence) Detection Circuit - Moore Type

State Diagram

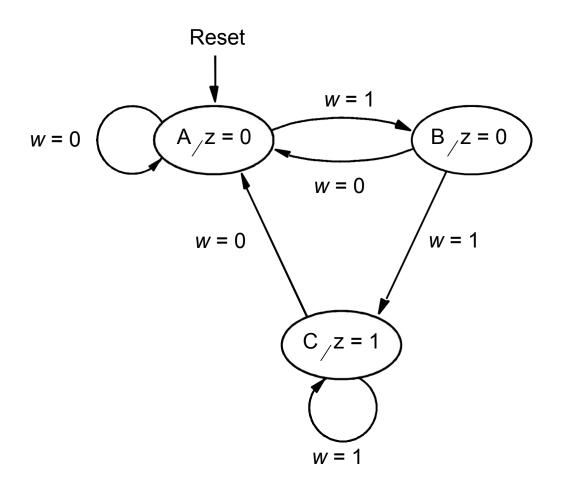


Figure 5: State diagram of a simple sequential circuit.

Example 1: A Simple Input Pattern ('11' Overlapping Sequence) Detection Circuit [State Table]

State Table					
Present	Nex	Output			
state	w = 0	w = 1	Z		
А	Α	В	0		
В	Α	С	0		
C	Α	С	1		

Note: n bits can represent 2ⁿ states.

Figure 6: State table for the sequential circuit in Figure 5.

Example 1: A Simple Input Pattern ('11' Overlapping Sequence) **Detection Circuit** [State Assigned Table]

	Present	Next s		
	state	w=0 $w=1$		Output
	^y 2 ^y 1	<i>Y</i> ₂ <i>Y</i> ₁	<i>Y</i> ₂ <i>Y</i> ₁	Z
A	00	00	01	0
В	01	00	10	0
C	10	00	10	1
	11	dd	dd	d

We need to find expressions (K-map) for

- next state (Y_2, Y_1)
- output (z).

Note that,

$$Y_1 = f(w,y_1,y_2)$$

$$Y_2 = f(w,y_1,y_2)$$

$$z = f(y_1,y_2)$$

$$>$$
 z = f(y₁,y₂)

Figure 7: State-assigned table for the sequential circuit in Figure 7.

Example 1: A Simple Input Pattern ('11' Overlapping Sequence) Detection Circuit [K-Map]

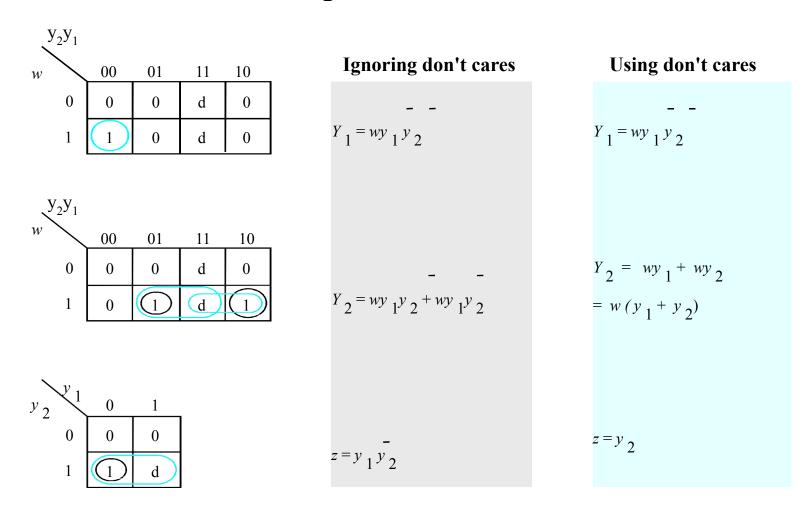


Figure 8: Derivation of logic expressions for the sequential circuit in Figure 7.

Example 1: A Simple Input Pattern ('11' Overlapping Sequence) Detection Circuit [Circuit]

Note that,

- > # flipflops = # bits to represent current state (#y)
- \triangleright Outputs of flipflops correspond to current state bits (y_1, y_2)
- > Inputs of flipflops correspond to next state bits (Y₁, Y₂)

In this problem, we need **two flipflops** as we have used **two bits** (y_1, y_2) to assign all the present states (A, B, C).

Example 1: A Simple Input Pattern ('11' Overlapping Sequence) Detection Circuit [Circuit]

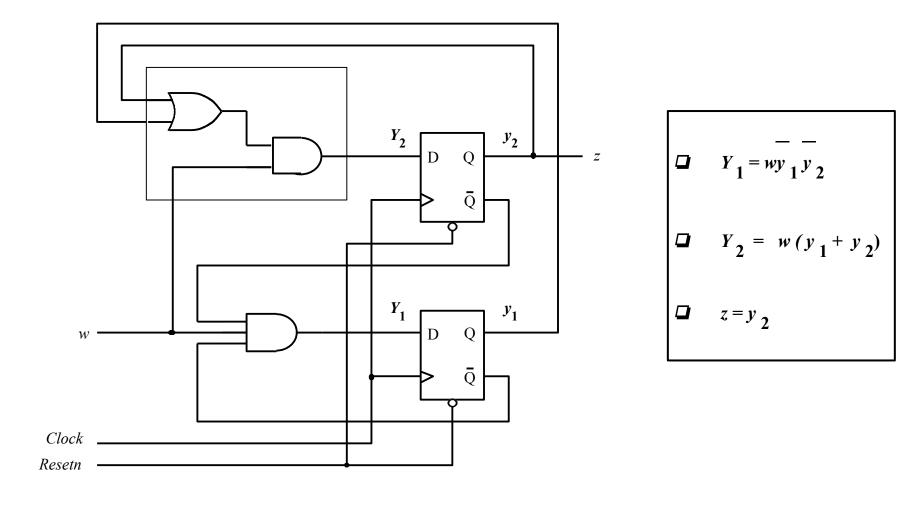


Figure 9. Final implementation of the sequential circuit derived in Figure 8.

Summary

Steps->

- > State diagram
- > State table
- > State assigned table
- K-map (next states & outputs)
- > Circuit

Example 1(cont.): A Simple Input Pattern ('11' Non-Overlapping Sequence) (Detection Circuit - Moore Type)

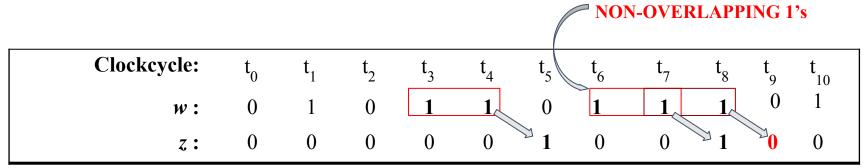
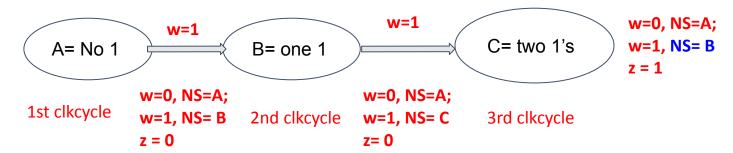
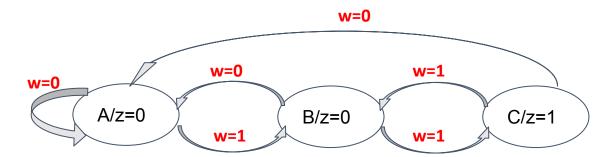
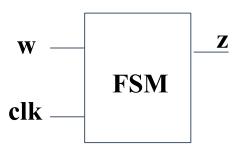


Figure 4: Sequences of input and output signals.



STATE DIAGRAM





General form of a sequential circuit

- W represents input/s
- Z represents output/s
- Flip-flops are used to save the "present" state of the circuit, Q
- Also called Finite State Machine (FSM) or simply, machine
- 2 types: depending on the connection drawn in pink on the circuit

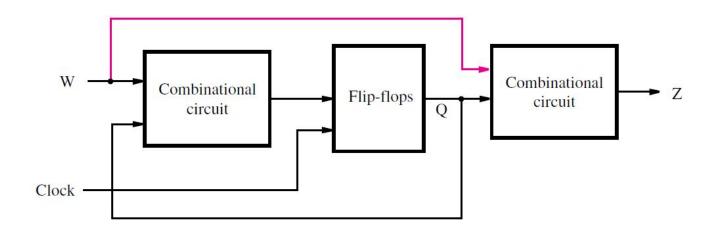
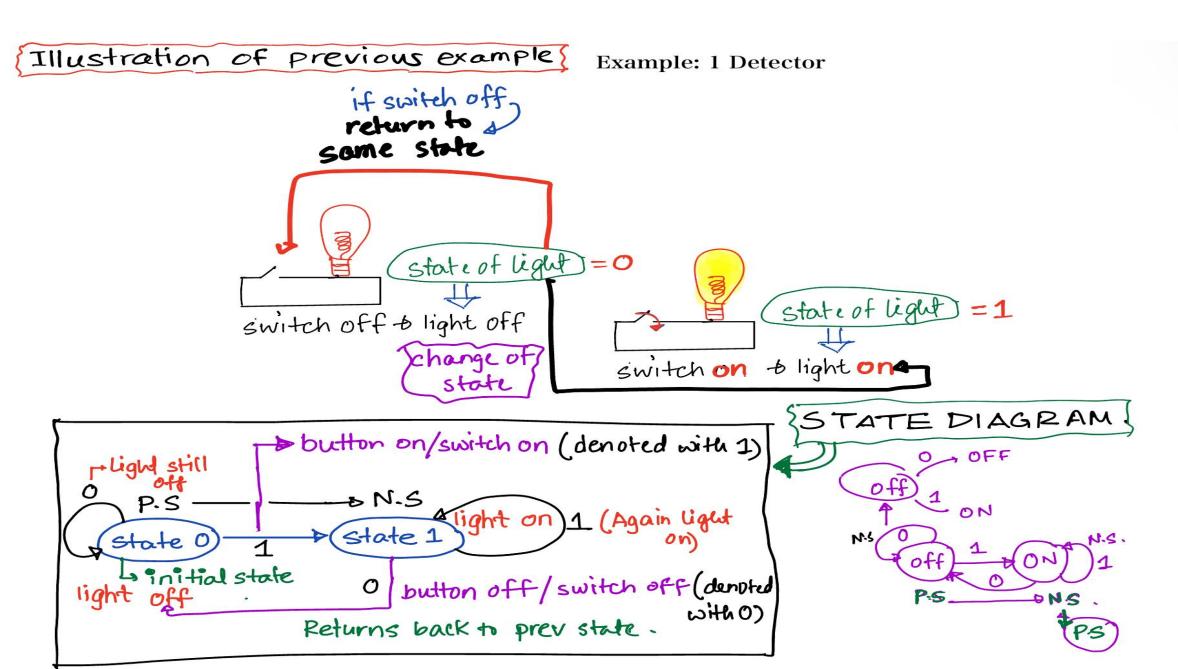
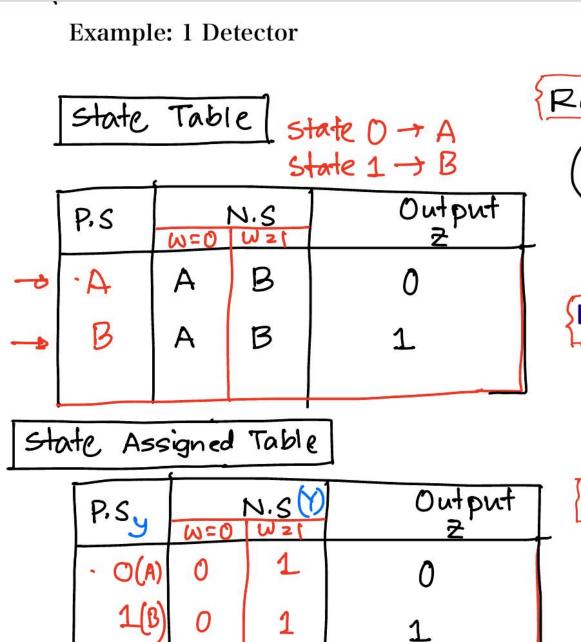
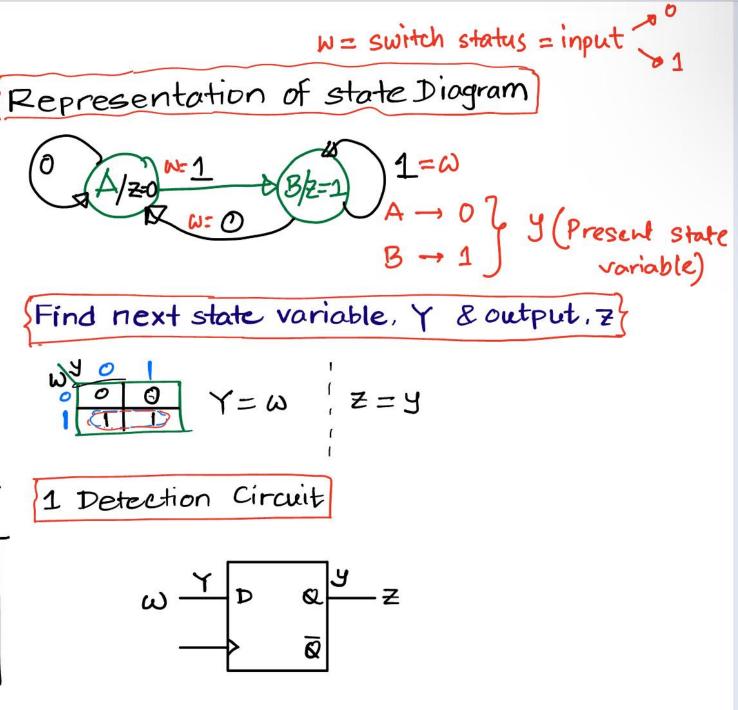


Figure: General form of a sequential circuit

Illustration of light switch problem







FSM types

Moore type FSM
 Output (Z) depends only
 on the "present" state
 (Q) of the circuit

Mealy type FSM

Output (Z) depends on both the primary inputs (W) and the "present" state (Q) of the circuit

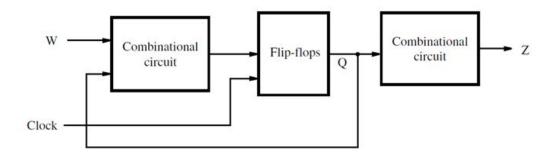


Figure: Moore type FSM

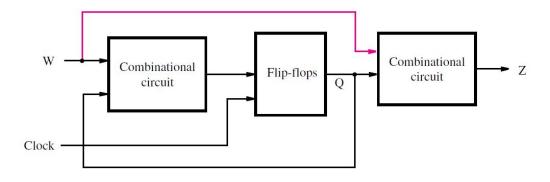


Figure: Mealy type FSM

Moore vs. Mealy type machines

Moore Machine	Mealy Machine			
 Output depends only on the present state. 	 Output depends both on the present state and the present input. 			
 Generally, it has more states than Mealy Machine. 	 Generally, it has fewer states than Moore Machine. 			
 The output is a function of the current state and changes at clock edges 	 The output is a function of the transitions and can change any instant 			
 In Moore machines, more logic is required to decode the outputs resulting in more circuit delays. They generally react one clock cycle later. 	 Mealy machines react faster to inputs. They generally react in the same clock cycle. 			