## **FSM**

Q1. Kelvin is tasked with building an FSM which would detect **10 or 011 overlapping** sequences coming out of a communication channel. A sample is given below:

(w indicates input sequence values and z indicates output)

Clock cycle	t0	t1	t2	t3	t4	t5	t6	t7	t8	t9	t10	t11	t12	t13
W	1	0	1	1	0	0	1	1	0	1	0	1	0	0
Z	0	0	1	0	1	1	0	0	1	1	0	1	0	1

Note: Use the table below for **Gray coding** if needed.

Decimal Equivalent		Binary Cod	le	Gray Code					
	B2	B1	<b>B</b> 0	G2	G1	G0			
0	0	0	0	0	0	0			
1	0	0	1	0	0	1			
2	0	1	0	0	1	1			
3	0	1	1	0	1	0			
4	1	0	0	1	1	0			
5	1	0	1	1	1	1			
6	1	1	0	1	0	1			
7	1	1	1	1	0	0			

(a)	<b>Determine</b> the type of <b>FSM</b> (Mealy/Moore) to be implemented						
(b)	<b>Draw</b> the state diagram. Use no more than <b>6 states</b> . Using more states will result in deduction of marks.	[4]					
(c)	Draw the state assignment table using Binary encoding.	[3]					
(d)	<b>Determine</b> the expression of only the output, <b>z</b> . No need to draw circuit.	[2]					

Q2. **Design** a finite state machine (FSM) for a car alarm system. The system has two binary inputs: x, indicating the lock status of the car door ( $\mathbf{x} = \mathbf{1}$  if unlocked,  $\mathbf{x} = \mathbf{0}$  if locked) and y, indicating the door status ( $\mathbf{y} = \mathbf{1}$  if the door is open,  $\mathbf{y} = \mathbf{0}$  if closed). The output z is used to control the alarm:  $\mathbf{z} = \mathbf{1}$  when the alarm is active, and  $\mathbf{z} = \mathbf{0}$  otherwise. The alarm should be

triggered (z = 1) if the door is opened (y = 1) while it is still locked (x = 0) for two consecutive clock cycles. An example is shown below:

X	1	0	1	0	0	0	1	1	0	0	0	0	1	0
y	0	0	1	1	1	0	1	0	1	1	1	0	0	1
z	0	0	0	0	1	0	0	0	0	1	1	0	0	0

(a)	<b>Determine</b> the type of <b>FSM</b> that would be needed for the given problem and design the state diagram for the corresponding FSM.	[2]
(b)	<b>Derive</b> the state-assigned table using the <b>Gray encoding</b> from your state diagram in (a).	[2]
(c)	Find the expression for the next state and the output for the FSM using KMAP.	[3]
(d)	<b>Calculate</b> the number of flip-flops required for the circuit implementation and <b>draw</b> the circuit for this FSM.	[3]