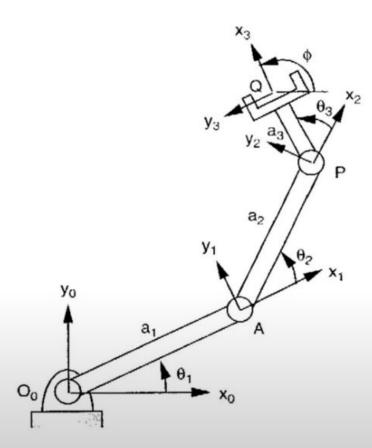
Introduction to Robotics CSE 461

Lecture 6: Forward Kinematics

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Angles of three joints are 30 degree, 45 degree and 10 degree. Length of arms are 20 cm, 32 cm and 10 cm.

Joint	α	а	d	θ
1	0	20	0	30°
2	0	32	0	45°
3	0	10	0	10°

$$T_{i} = \begin{bmatrix} c\theta_{i} & -c\alpha_{i}s\theta_{i} & s\alpha_{i}s\theta_{i} & a_{i}c\theta_{i} \\ s\theta_{i} & c\alpha_{i}c\theta_{i} & -s\alpha_{i}c\theta_{i} & a_{i}s\theta_{i} \\ 0 & s\alpha_{i} & c\alpha_{i} & d_{i} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_i = \begin{bmatrix} c\theta_i & -c\alpha_i s\theta_i & s\alpha_i s\theta_i & a_i c\theta_i \\ s\theta_i & c\alpha_i c\theta_i & -s\alpha_i c\theta_i & a_i s\theta_i \\ 0 & s\alpha_i & c\alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_{1} = \begin{bmatrix} cos30^{\circ} & -cos0^{\circ}sin30^{\circ} & sin0^{\circ}sin30^{\circ} & 20cos30^{\circ} \\ sin30^{\circ} & cos0^{\circ}cos30^{\circ} & -sin0^{\circ}cos30^{\circ} & 20sin30^{\circ} \\ 0 & sin0^{\circ} & cos0^{\circ} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_1 = \begin{bmatrix} 0.87 & -0.50 & 0 & 17.32 \\ 0.5 & 0.87 & 0 & 10 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_i = \begin{bmatrix} c\theta_i & -c\alpha_i s\theta_i & s\alpha_i s\theta_i & a_i c\theta_i \\ s\theta_i & c\alpha_i c\theta_i & -s\alpha_i c\theta_i & a_i s\theta_i \\ 0 & s\alpha_i & c\alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_2 = \begin{bmatrix} 0.71 & -0.71 & 0 & 22.72 \\ 0.71 & 0.71 & 0 & 22.72 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

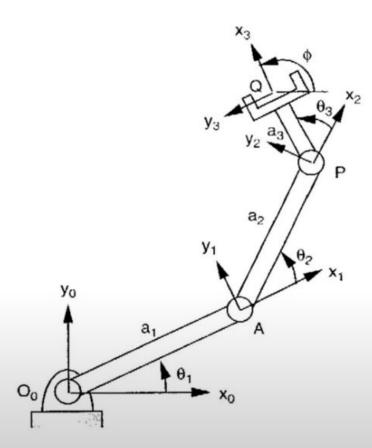
$$T_3 = \begin{bmatrix} 0.98 & -0.17 & 0 & 9.85 \\ 0.17 & 0.98 & 0 & 1.74 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_1 = \begin{bmatrix} 0.87 & -0.50 & 0 & 17.32 \\ 0.5 & 0.87 & 0 & 10 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad T_2 = \begin{bmatrix} 0.71 & -0.71 & 0 & 22.72 \\ 0.71 & 0.71 & 0 & 22.72 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad T_3 = \begin{bmatrix} 0.98 & -0.17 & 0 & 9.85 \\ 0.17 & 0.98 & 0 & 1.74 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Overall Transformation Matrix $T = T_1.T_2.T_3$

$$= \begin{bmatrix} 0.09 & -0.99 & 0 & 26.6 \\ 0.99 & 0.09 & 0 & 51.14 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

So from overall Transformation Matrix, x = 26.6, y = 51.14 and z = 0



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