# Lecture 7: Training Neural Networks, Part I

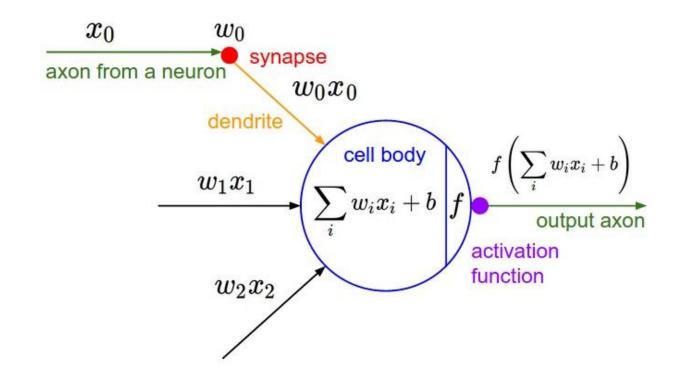
# Overview

# 1. One time setup activation functions, preprocessing, weight initialization, regularization, gradient checking

- 2. Training dynamics transfer learning, babysitting the learning process, parameter updates, hyperparameter optimization
- 3. Evaluation model ensembles, test-time augmentation

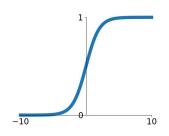
# Part 1

- Activation Functions
- Data Preprocessing
- Weight Initialization
- Batch Normalization
- Transfer learning

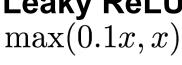


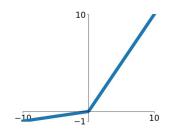
#### **Sigmoid**

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



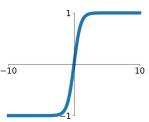
### Leaky ReLU





#### tanh

tanh(x)

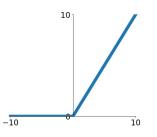


#### **Maxout**

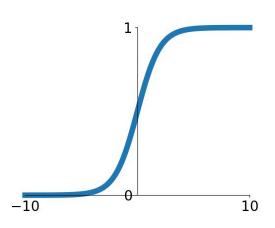
 $\max(w_1^T x + b_1, w_2^T x + b_2)$ 

#### ReLU

 $\max(0,x)$ 

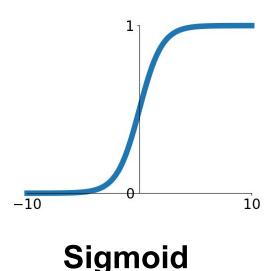


$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

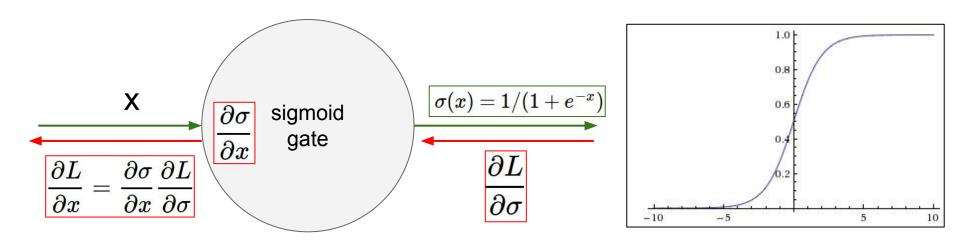


$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

#### 3 problems:

Saturated neurons "kill" the gradients

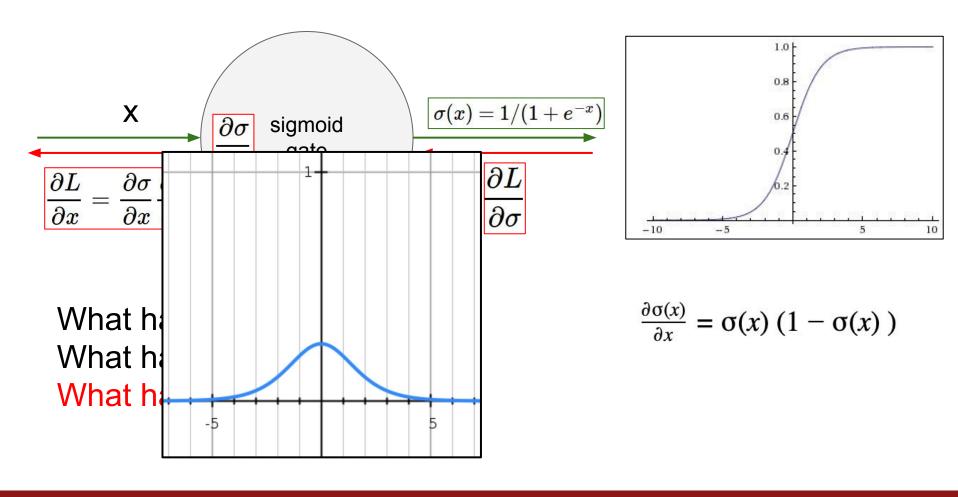


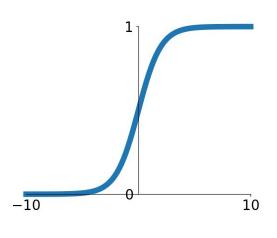
What happens when x = -10? What happens when x = 0?

What happens when x = 10?

April 28, 2020

 $\frac{\partial \sigma(x)}{\partial x} = \sigma(x) (1 - \sigma(x))$ 





Sigmoid

$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

#### 3 problems:

- Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on  $\overline{\mathbf{w}}$ ?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

So!! Sign of gradient for all w<sub>i</sub> is the same as the sign of upstream scalar gradient!

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream\_gradient$$

Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

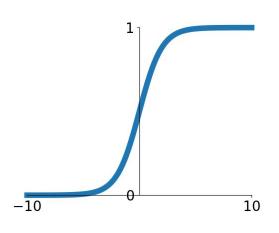
What can we say about the gradients on **w**?

Always all positive or all negative : ( inefficient 4 updating

(For a single element! Minibatches help)

sign of the upstream gradient gradient coming down update directions zig zag path allowed gradient update directions hypothetical optimal w vector

allowed

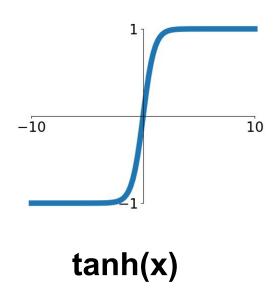


$$\sigma(x) = 1/(1+e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

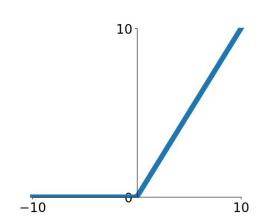
#### 3 problems:

- Saturated neurons "kill" the gradients
- Sigmoid outputs are not zero-centered
- exp() is a bit compute expensive



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

[LeCun et al., 1991]

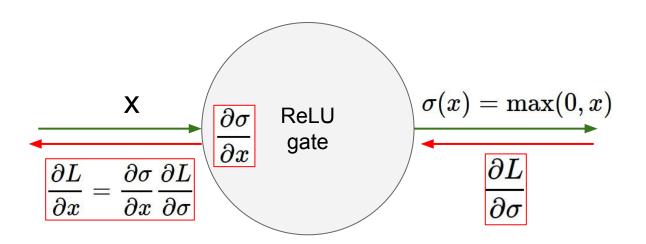


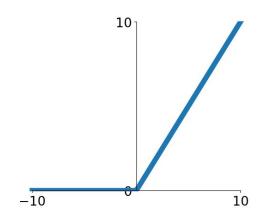
**ReLU** (Rectified Linear Unit)

- Computes f(x) = max(0,x)
- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

- Not zero-centered output
- An annoyance:

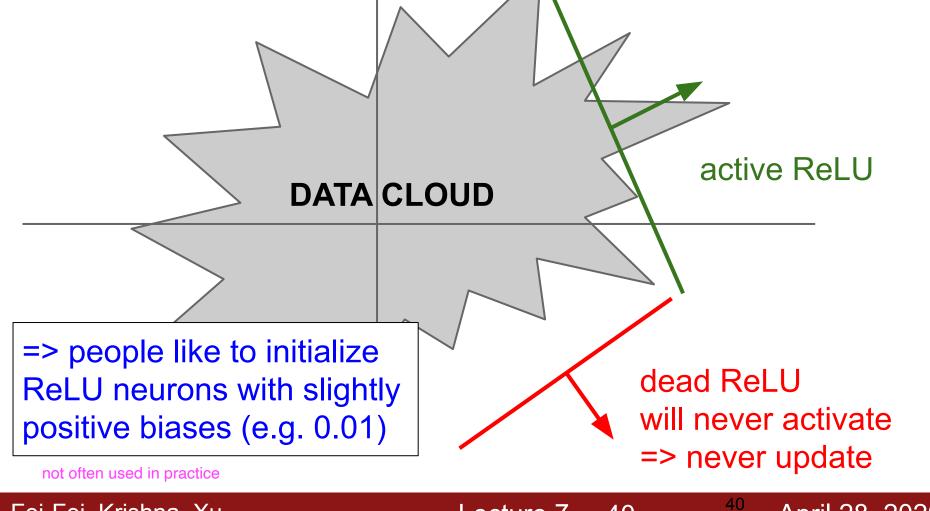
hint: what is the gradient when x < 0?





What happens when x = -10? What happens when x = 0?

What happens when x = 10?

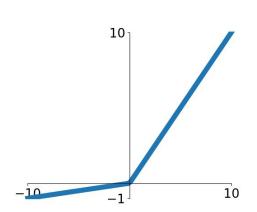


Fei-Fei, Krishna, Xu

Lecture 7 - 40

April 28, 2020





- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

#### Leaky ReLU

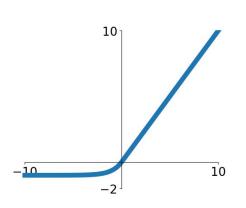
$$f(x) = \max(0.01x, x)$$

#### Parametric Rectifier (PReLU)

$$f(x) = \max(\alpha x, x)$$

backprop into \alpha (parameter)

#### **Exponential Linear Units (ELU)**

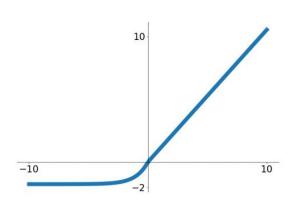


$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha & (\exp(x) - 1) & \text{if } x \le 0 \end{cases}$$
(Alpha default = 1)

- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

- Computation requires exp()

#### Scaled Exponential Linear Units (SELU)



$$f(x) = egin{cases} \lambda x & ext{if } x > 0 \ \lambda lpha(e^x - 1) & ext{otherwise} \end{cases}$$

- Scaled version of ELU that works better for deep networks
- "Self-normalizing" property;
- Can train deep SELU networks without BatchNorm
  - (will discuss more later)

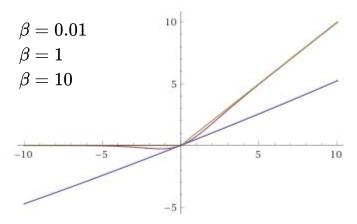
#### Maxout "Neuron"

- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

Problem: doubles the number of parameters/neuron:(

#### **Swish**

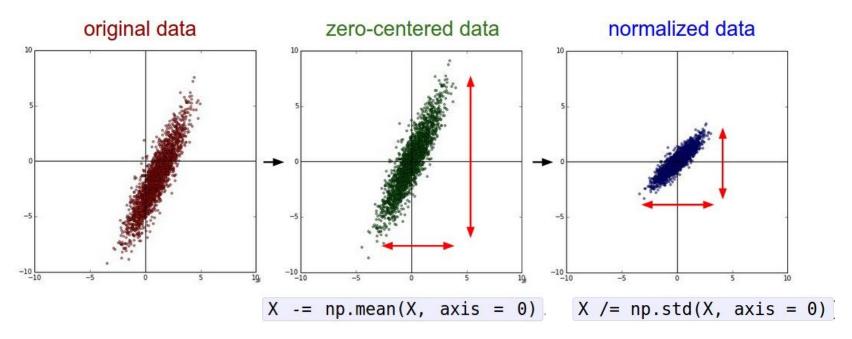


$$f(x) = x\sigma(\beta x)$$

- They trained a neural network to generate and test out different non-linearities.
- Swish outperformed all other options for CIFAR-10 accuracy

#### **TLDR:** In practice:

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU / SELU
  - To squeeze out some marginal gains
- Don't use sigmoid or tanh



(Assume X [NxD] is data matrix, each example in a row)

Remember: Consider what happens when the input to a neuron is always positive...

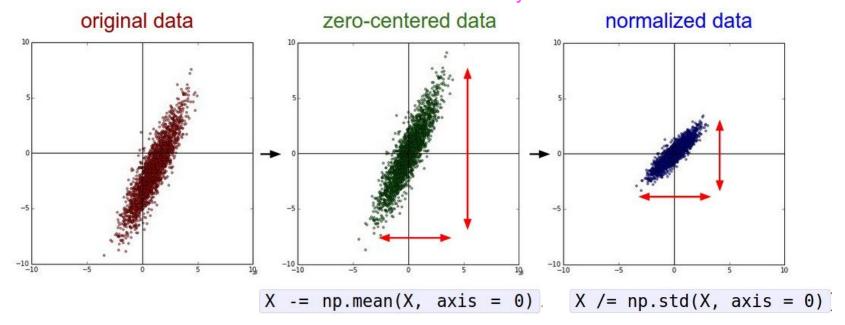
$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

What can we say about the gradients on **w**? Always all positive or all negative :( (this is also why you want zero-mean data!)

allowed gradient update directions zig zag path allowed gradient update directions hypothetical optimal w

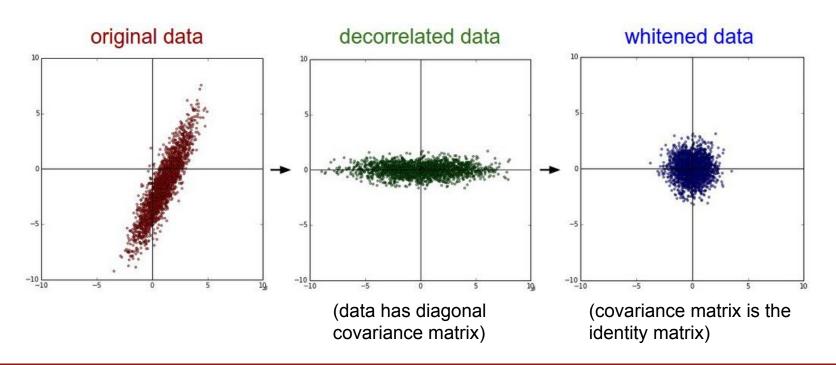
vector

0 mean can solve the problem of sigmoid for only the first layer of neuron network. we still get this problem in the hidden layers.



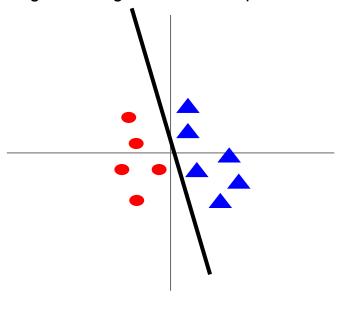
(Assume X [NxD] is data matrix, each example in a row)

In practice, you may also see PCA and Whitening of the data



Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize

**After normalization**: less sensitive to small changes in weights; easier to optimize



#### TLDR: In practice for Images: center only

0 mean only, no normalization

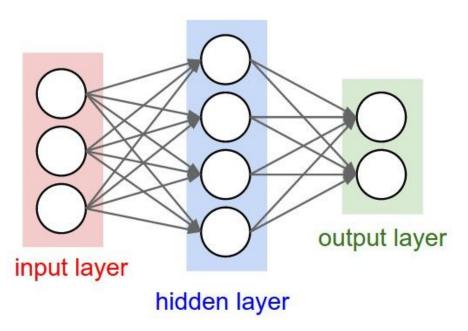
e.g. consider CIFAR-10 example with [32,32,3] images

- Subtract the mean image (e.g. AlexNet) (mean image = [32,32,3] array)
- apply both on training set and test set.
- Subtract per-channel mean (e.g. VGGNet) (mean along each channel = 3 numbers)
- Subtract per-channel mean and Divide by per-channel std (e.g. ResNet) (mean along each channel = 3 numbers)

Not common to do PCA or whitening

# Weight Initialization

#### - Q: what happens when W=constant init is used?



all neurons are going to do the same thing, and get the same gradient, update in the same way, so that learn the same thing.

But we want neurons to learn different things.

- First idea: **Small random numbers** (gaussian with zero mean and 1e-2 standard deviation)

Works ~okay for small networks, but problems with deeper networks.

#### Weight Initialization: Activation statistics

```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

#### What will happen to the activations for the last layer?

as we multiply by this W, these small numbers at each layer, this quickly shrinks and collapses all of these values. By the end, we get all of these zeroes.

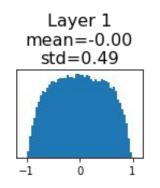
#### Weight Initialization: Activation statistics

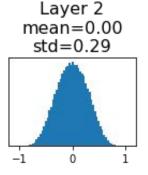
```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

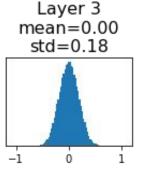
All activations tend to zero for deeper network layers

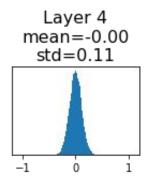
**Q**: What do the gradients dL/dW look like?

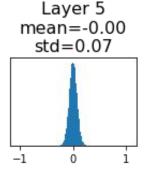
A: All zero, no learning =(

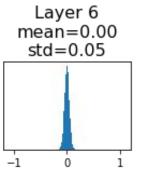












## Weight Initialization: Activation statistics

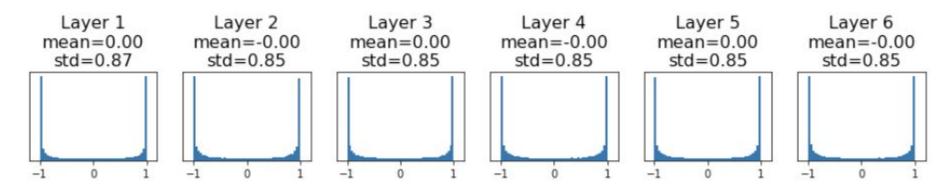
What will happen to the activations for the last layer?

### Weight Initialization: Activation statistics

All activations saturate

**Q**: What do the gradients look like?

A: Local gradients all zero, no learning =(



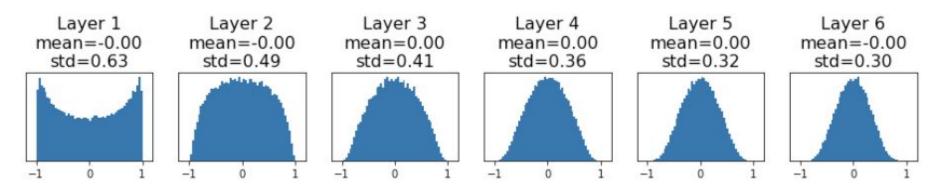
we specify that we want the variance of the input to be the same as the variance of the output.

Intuitively with this kind of means is that if you have a small number of inputs, then we're going to divide by the smaller number and get larger weights. We need larger weights because with small inputs you need a larger weights to get the same larger variance at output.

Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

April 28, 2020

"Just right": Activations are nicely scaled for all layers!

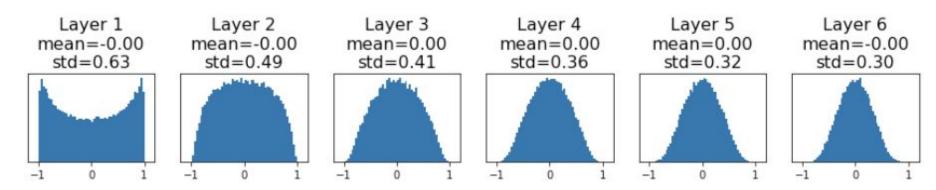


Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

66

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter\_size<sup>2</sup> \* input\_channels



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is kernel\_size<sup>2</sup> \* input\_channels

#### **Derivation:**

[Assume x, w are iid]
[Assume x, w independant]
[Assume x, w are zero-mean]

Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

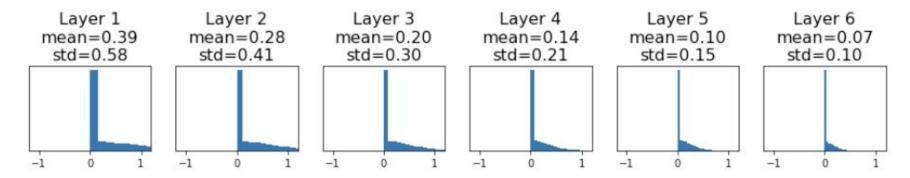
## Weight Initialization: What about ReLU?

because ReLU is kill half of your units, it's actually halving the variance that you get out of this. You won't actually get the right variance coming out, it's going to be too small.

## Weight Initialization: What about ReLU?

Xavier assumes zero centered activation function

Activations collapse to zero again, no learning =(



# Weight Initialization: Kaiming / MSRA Initialization

```
dims = [4096] * 7
hs = []

x = np.random.randn(16, dims[0])

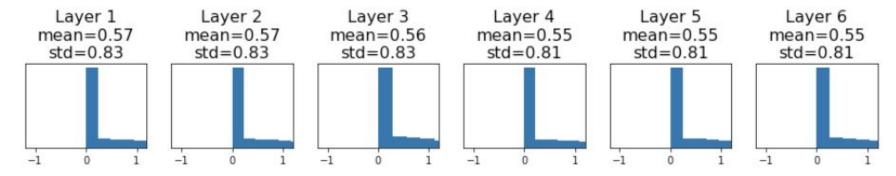
for Din. Dout in zip(dims[:-1], dims[1:]):

W = np.random.randn(Din, Dout) * np.sqrt(2/Din)

x = np.maximum(0, x.dot(W))
hs.append(x)
```

"Just right": Activations are nicely scaled for all layers!

note: here we change division to multiplication, it is same as '/ np.sqrt( Din/2 )'



He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

### Proper initialization is an active area of research...

Understanding the difficulty of training deep feedforward neural networks by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

**Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification** by He et al., 2015

Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

All you need is a good init, Mishkin and Matas, 2015

Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019

# **Batch Normalization**

a related idea of weight initialization, idea of wanting to keep activations in a gaussian range.

### **Batch Normalization**

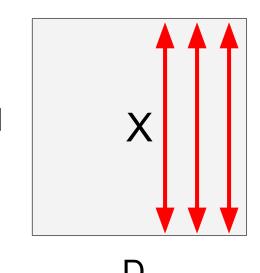
"you want zero-mean unit-variance activations? just make them so."

consider a batch of activations at some layer. To make each dimension zero-mean unit-variance, apply:

$$\widehat{x}^{(k)} = \frac{x^{(k)} - E[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

this is a vanilla differentiable function...

Input:  $x: N \times D$ 



$$\mu_j = \frac{1}{N} \sum_{i=1}^N x_{i,j} \quad \text{Per-channel mean,} \\ \text{shape is D}$$

$$\sigma_j^2 = \frac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2 \quad \mbox{Per-channel var,} \\ \mbox{shape is D}$$

$$\hat{x}_{i,j} = rac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + arepsilon}}$$
 Normalized x, Shape is N x D

Problem: What if zero-mean, unit variance is too hard of a constraint?

## **Batch Normalization: Test-Time**

Estimates depend on minibatch; can't do this at test-time!

Input:  $x: N \times D$ 

# Learnable scale and shift parameters:

$$\gamma, \beta: D$$

Learning  $\gamma = \sigma$ ,  $\beta = \mu$  will recover the identity function!

$$\mu_j = rac{1}{N} \sum_{i=1}^N x_{i,j}$$
 Per-channel mean, shape is D

$$\sigma_j^2 = rac{1}{N} \sum_{i=1}^N (x_{i,j} - \mu_j)^2$$
 Per-channel var, shape is D

$$\hat{x}_{i,j} = rac{x_{i,j} - \mu_j}{\sqrt{\sigma_i^2 + \varepsilon}}$$
 Normalized x, Shape is N x D

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$
 Output, Shape is N x D

### **Batch Normalization: Test-Time**

why do we want to learn this  $\gamma,\beta$  to be able to learn the identity function back? because we want to give it the flexibility. Even though in general BN is a good idea, it's not always exactly the best thing to do, so maybe we want

Input:  $x:N\times D$ 

$$\mu_j = {}^{ ext{(Running)}} ext{ average of values seen during training}$$

Per-channel mean, shape is D

Per-channel var,

shape is D

### Learnable scale and shift parameters:

$$\gamma, \beta: D$$

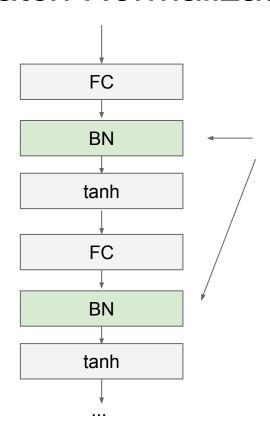
During testing batchnorm becomes a linear operator! Can be fused with the previous fully-connected or conv layer

$$\sigma_j^2 = {}^{ ext{(Running)}} \, {}^{ ext{average of values seen during training}}$$

$$\hat{x}_{i,j} = \frac{x_{i,j} - \mu_j}{\sqrt{\sigma_j^2 + \varepsilon}}$$

$$y_{i,j} = \gamma_j \hat{x}_{i,j} + \beta_j$$

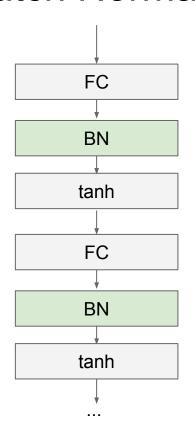
#### **Batch Normalization**



Usually inserted after Fully Connected or Convolutional layers, and before nonlinearity.

$$\widehat{x}^{(k)} = \frac{x^{(k)} - E[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

### **Batch Normalization**



- Makes deep networks much easier to train!
- Improves gradient flow
- Allows higher learning rates, faster convergence
- Networks become more robust to initialization
- Acts as regularization during training some reg
- Zero overhead at test-time: can be fused with conv!
- Behaves differently during training and testing: this
  is a very common source of bugs!

## Batch Normalization for ConvNets

Batch Normalization for fully-connected networks

$$\mathbf{x}: \mathbf{N} \times \mathbf{D}$$
Normalize
$$\mu, \sigma: \mathbf{1} \times \mathbf{D}$$

$$\gamma, \beta: \mathbf{1} \times \mathbf{D}$$

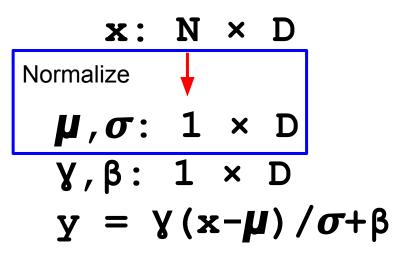
$$y = \gamma(\mathbf{x} - \mu) / \sigma + \beta$$

Batch Normalization for convolutional networks (Spatial Batchnorm, BatchNorm2D)

Normalize 
$$\mathbf{x}: \mathbf{N} \times \mathbf{C} \times \mathbf{H} \times \mathbf{W}$$
 $\mu, \sigma: \mathbf{1} \times \mathbf{C} \times \mathbf{1} \times \mathbf{1}$ 
 $\gamma, \beta: \mathbf{1} \times \mathbf{C} \times \mathbf{1} \times \mathbf{1}$ 
 $\gamma = \gamma(\mathbf{x} - \mu) / \sigma + \beta$ 

# **Layer Normalization**

**Batch Normalization** for fully-connected networks



Layer Normalization for fully-connected networks
Same behavior at train and test!
Can be used in recurrent networks

Normalize
$$\mu, \sigma: N \times D$$

$$\mu, \sigma: N \times 1$$

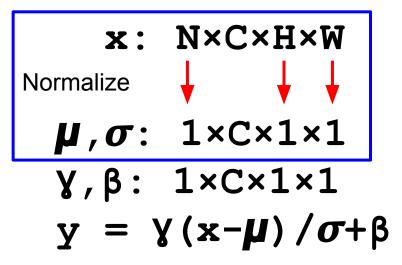
$$y, \beta: 1 \times D$$

$$y = \frac{y(x-\mu)}{\sigma+\beta}$$

Ba, Kiros, and Hinton, "Layer Normalization", arXiv 2016

## Instance Normalization

**Batch Normalization** for convolutional networks



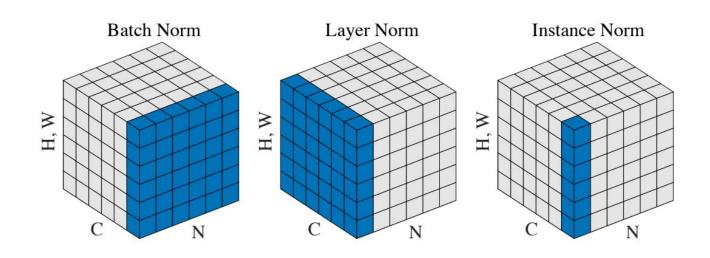
**Instance Normalization** for convolutional networks Same behavior at train / test!

Normalize  

$$\mu, \sigma: N \times C \times 1 \times 1$$
  
 $\mu, \sigma: N \times C \times 1 \times 1$   
 $\gamma, \beta: 1 \times C \times 1 \times 1$   
 $\gamma = \gamma(x - \mu) / \sigma + \beta$ 

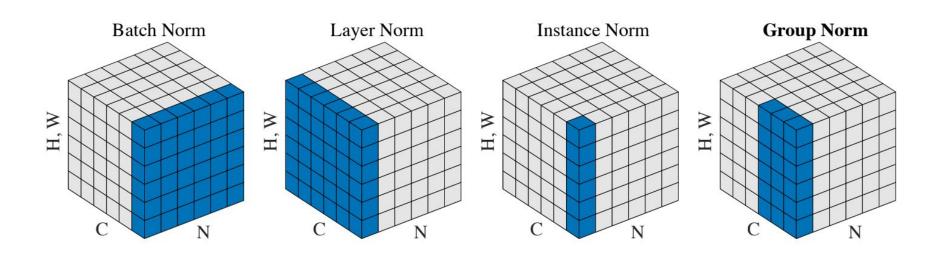
Ulyanov et al, Improved Texture Networks: Maximizing Quality and Diversity in Feed-forward Stylization and Texture Synthesis, CVPR 2017

# Comparison of Normalization Layers



Wu and He, "Group Normalization", ECCV 2018

# **Group Normalization**



Wu and He, "Group Normalization", ECCV 2018

Lecture 7 - 89

Transfer learning

Lecture 7 - 90

April 24, 2018

Fei-Fei Li & Justin Johnson & Serena Yeung

"You need a lot of a data if you want to train/use CNNs"

"You need a lot of a antal you want to train/use CNNs"

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image** 

Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64

**Image** 

2. Small Dataset (C classes)

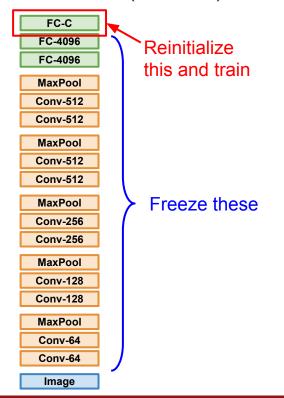


Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

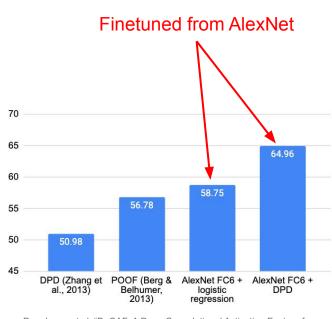
1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64 **Image** 

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014

1. Train on Imagenet

FC-1000 FC-4096 FC-4096 MaxPool Conv-512 Conv-512 MaxPool Conv-512 Conv-512 MaxPool Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64 Conv-64

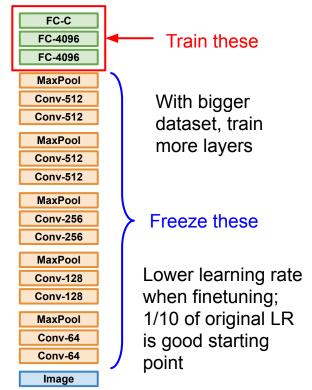
**Image** 

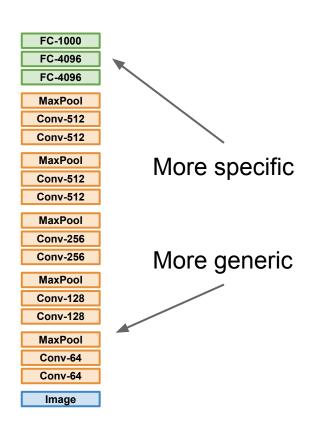
2. Small Dataset (C classes)



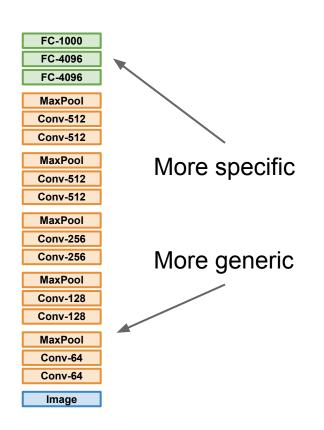
Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

3. Bigger dataset

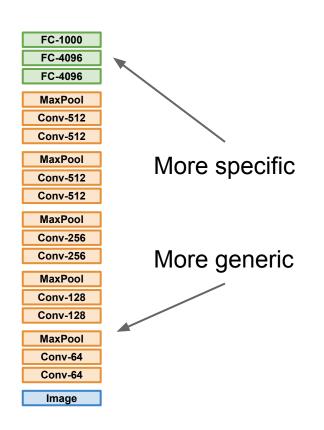




	very similar dataset	very different dataset
very little data	?	?
quite a lot of data	?	?



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	?
quite a lot of data	Finetune a few layers	?



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	You're in trouble Try linear classifier from different stages
quite a lot of data	Finetune a few layers	Finetune a larger number of layers

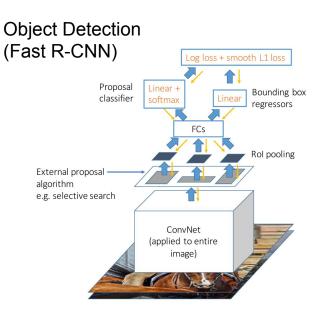
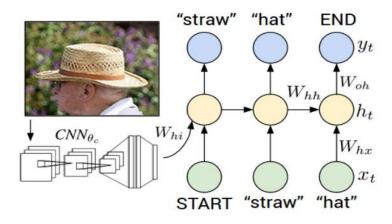
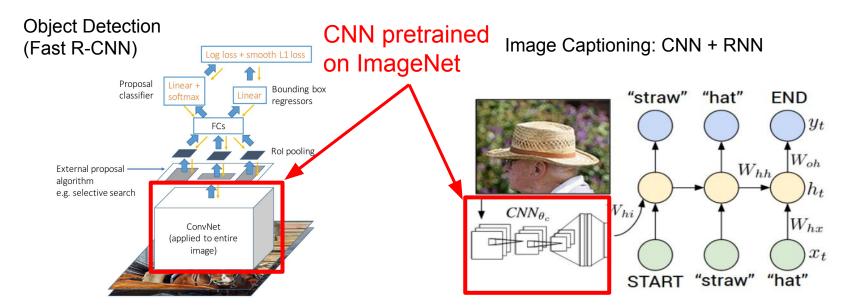


Image Captioning: CNN + RNN

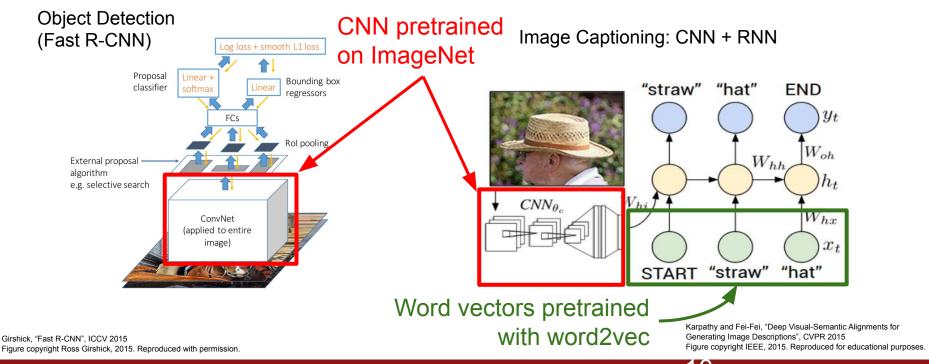


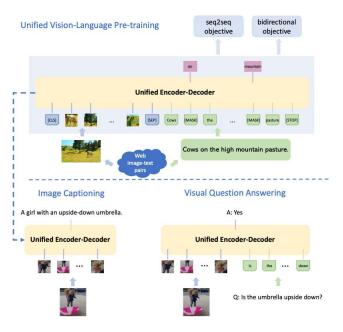
Girshick, "Fast R-CNN", ICCV 2015
Figure copyright Ross Girshick, 2015. Reproduced with permission

Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015 Figure copyright IEEE, 2015. Reproduced for educational purposes.



Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015 Figure copyright IEEE, 2015. Reproduced for educational purposes.





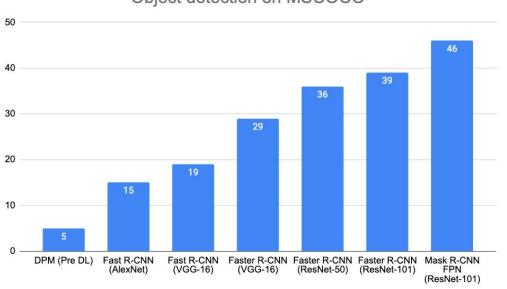
- Train CNN on ImageNet
- Fine-Tune (1) for object detection on Visual Genome
- Train BERT language model on lots of text
- Combine(2) and (3), train for joint image / language modeling
- 5. Fine-tune (4) for image captioning, visual question answering, etc.

Zhou et al, "Unified Vision-Language Pre-Training for Image Captioning and VQA" CVPR 2020 Figure copyright Luowei Zhou, 2020. Reproduced with permission.

Krishna et al, "Visual genome: Connecting language and vision using crowdsourced dense image annotations" IJCV 2017 Devlin et al. "BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding" ArXiv 2018

# Transfer learning with CNNs - Architecture matters

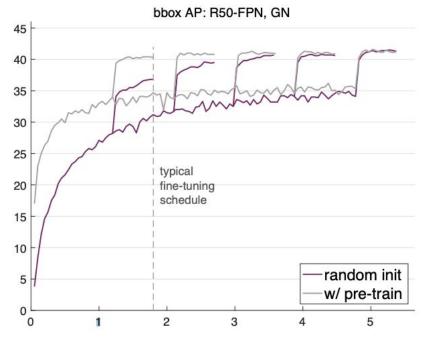




We will discuss different architectures in detail in two lectures

Girshick, "The Generalized R-CNN Framework for Object Detection", ICCV 2017 Tutorial on Instance-Level Visual Recognition

# Transfer learning with CNNs is pervasive... But recent results show it might not always be necessary!



Training from scratch can work just as well as training from a pretrained ImageNet model for object detection

But it takes 2-3x as long to train.

They also find that collecting more data is better than finetuning on a related task

He et al, "Rethinking ImageNet Pre-training", ICCV 2019 Figure copyright Kaiming He, 2019. Reproduced with permission.

## Takeaway for your projects and beyond:

Transfer learning be like



Source: Al & Deep Learning Memes For Back-propagated Poets

## Takeaway for your projects and beyond:

Have some dataset of interest but it has < ~1M images?

- 1. Find a very large dataset that has similar data, train a big ConvNet there
- 2. Transfer learn to your dataset

Deep learning frameworks provide a "Model Zoo" of pretrained models so you don't need to train your own

TensorFlow: <a href="https://github.com/tensorflow/models">https://github.com/tensorflow/models</a>

PyTorch: <a href="https://github.com/pytorch/vision">https://github.com/pytorch/vision</a>

# Summary

**TLDRs** 

We looked in detail at:

- Activation Functions (use ReLU)
- Data Preprocessing (images: subtract mean)
- Weight Initialization (use Xavier/He init)
- Batch Normalization (use this!)
- Transfer learning (use this if you can!)

# Next time: Training Neural Networks, Part 2

- Parameter update schemes
- Learning rate schedules
- Gradient checking
- Regularization (Dropout etc.)
- Babysitting learning
- Evaluation (Ensembles etc.)
- Hyperparameter Optimization
- Transfer learning / fine-tuning