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# 1 INTRODUCTION

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## 2.2 Classical and recent works in system identification

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## 2.4 End-to-end learning (black box models)

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