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#### 1 INTRODUCTION

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- 1.3 Research Questions and Contribution
- 1.4 Overview of content

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- 2.1.1 Classical and recent works in system identification
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