Calculation of Methane Production from Volumetric Measurements*

Sasha D. Hafner, Nanna Løjborg, Sergi Astals, Christof Holliger, Konrad Koch, and Sören Weinrich

sasha.hafner@eng.au.dk

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1 Introduction

This document describes calculations for processing volumetric measurements of biogas production, typically from laboratory experiments aimed at measuring biochemical methane potential (BMP). Volumetric measurement systems are not described here, but details can be found elsewhere [Owen et al., 1979, Rozzi and Remigi, 2004, VDI, 2016].

In volumetric methods, biogas is typically allowed to accumulate over measurement intervals, which are the periods between measurements. Biogas volume and composition are measured at the end of each measurement interval. Measurements might be interval, where the measurement system is reset after each measurement. For example, when bottles sealed with septa are used, the biogas that accumulates in each bottle's headspace during a measurement interval is typically removed (vented) at the end of the interval, and its volume is measured. In the process the headspace pressure is reset to ambient. Or measurements may be cumulative, where the biogas quantity measured at a

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particular time is the cumulative total produced in all preceding measurement intervals. For example, biogas might accumulate in a separate vessel also used to measure volume (e.g., a eudiometer) that is emptied of biogas only at the end of the experiment, although cumulative volume is recorded at the end of each measurement interval. Measurement of biogas composition must reflect the approach used for volume, i.e., it does not make sense to work with interval volume data if composition measurements are made on a cumulative mixture of biogas produced. Once measurements are converted to standardized biogas and $\mathrm{CH_4}$ volume, cumulative data can be calculated from interval or vice versa.

As with manometric methods, two methods are commonly used to address the problem of biogas dilution with flushing gas, and both are described here: one based on normalized $\mathrm{CH_4}$ concentrations (method 1) and one that explicitly includes estimation of $\mathrm{CH_4}$ in the bottle headspace (method 2). Expected results from the two methods are effectively identical; differences in cumulative $\mathrm{CH_4}$ production are due only to error in measurement of biogas composition or headspace volume, in addition to small effects of changes in biogas composition between measurement intervals.

2 Standardization of measured gas volume

The approach used for standardization of biogas volume is identical for all biogas methods [Hafner et al., 2020a,b,c,d]. Standard gas volume is calculated from measured volume (V_{meas}) by correcting for water vapor, temperature, and pressure:

$$V_{std} = V_{meas} \cdot \frac{(p_{meas} - p_{\text{H}_2\text{O}})}{101.325 \,\text{kPa}} \cdot \frac{273.15 \,\text{K}}{(T_{meas} + 273.15)} \tag{1}$$

where p_{meas} is the gas pressure (kPa), T_{meas} is the gas temperature at the time of volume measurement in °C, $p_{\rm H_2O}$ the water vapor partial pressure (kPa), 273.15 K (0°C) is the standard temperature, 101.325 kPa is the standard pressure (kPa), and V_{std} is the standardized gas volume. Eq. (1) combines Boyle's, Charles's, and Dalton's laws [Negi and Anand, 1985], which are appropriate for the pressure and temperature ranges encountered in BMP experiments. Other units can, of course, be used, but standard temperature and pressure must be equivalent (e.g., 1.01325 bar, 1.0 atm, 32°F) and Eq. (1) is based on absolute temperature (note the conversion of °C within the equation by + 273.15)¹.

Typically, the value of $p_{\rm H_2O}$ for biogas should be assumed to be the saturation vapor pressure, because biogas is expected to be near equilibrium with an aqueous phase. This is reasonable as long as volume is measured at or below the temperature of the bottle, and has not undergone substantial expansion due to a drop in pressure after removal from the bottle. Or, if expansion has occurred, the approach is still suitable if the gas has also been cooled enough

¹ Other standard conditions for temperature and pressure exist, but these are the values used in the biogas field. In particular, that this standard pressure used in the biogas field is different from the value recommended by IUPAC (1.0 bar).

so the temperature is at or below the dew point². Saturation vapor pressure can be calculated using, e.g., the Magnus-form equation given below (Eq. 21 in Alduchov and Eskridge [1996])³.

$$p_{\text{H}_2\text{O}} = 0.61094e^{(17.625 \cdot T_{meas}/(243.04 + T_{meas}))}$$
 (2)

3 Calculation of methane production

3.1Method 1

In the first method, biogas is assumed to consist of only CH_4 and CO_2 at the time of production (i.e., as produced by the microbial community) and CH₄ production is calculated from vented (removed) biogas only. With this method, each measurement interval is independent of the others; CH₄ production for each interval is determined from the biogas volume and composition for that interval. This method is described in Richards et al. [1991, Section 3] and VDI [2016, Eq. (7)]. Relying on the assumptions that all gas production is biogas and all CH₄ and CO₂ are from biogas⁴, this provides the simplest approach for calculating CH₄ production.

Concentrations of CH_4 and CO_2 are normalized so they sum to 1.0:

$$x_{\text{CH}_4, n} = x_{\text{CH}_4} / (x_{\text{CH}_4} + x_{\text{CO}_2})$$
 (3)

where $x_{\rm CH_4}$ and $x_{\rm CO_2}$ are the measured ${\rm CH_4}$ and ${\rm CO_2}$ concentrations as volume (mole) fraction (possibly including a correction for water vapor—this has no effect here) and $x_{CH_4,n}$ is the normalized CH_4 volume fraction.

Methane production in an individual measurement interval is then calculated from the standardized biogas volume measured in that interval $(V_{b,std})$ with:

$$V_{\text{CH}_4} = x_{\text{CH}_4,n} \cdot V_{b,std} \tag{4}$$

If measurements are interval, cumulative CH₄ production is taken as the cumulative sum of interval values.

3.2 Method 2

Method 2 relies on fewer assumptions, but requires the true concentration of CH₄ (volume fraction) within the bottle headspace, with correction only for

² For example, biogas within a bottle headspace with an absolute pressure of 250 kPa at 35°C has a saturation vapor pressure for water of 5.6 kPa based on Eq (1). If volume is then measured at ambient pressure and room temperature (ca. 101 kPa and 20 $^{\circ}$ C) $p_{\rm H_2O}$ would be 2.4 kPa due to volume expansion. In comparison, saturation vapor pressure at 20 °C is slightly lower, at 2.3 kPa, so the assumption of saturation with water vapor is reasonable. For a much higher headspace pressure, or higher gas temperature at the time of measurement, this assumption is not valid and $p_{\mathrm{H}_2\mathrm{O}}$ may be adjusted based on volume expansion if the error is more than ca. 0.5%.

³ Other options exist [Richards et al., 1991, VDI, 2016], and will provide nearly identical values. 4 Therefore, this approach is not suitable when CO_2 is included in the flushing gas.

water vapor. This method was briefly described in Owen et al. [1979, p 488]. Here, CH_4 production in an interval has two components: a vented part that is naturally interval (but could be measured in a cumulative manner via accumulation in an external vessel), and a residual headspace part, that is naturally cumulative. Because determination of CH_4 production in an individual interval depends on multiple intervals, a subscript i for measurement interval is introduced here.

Vented CH_4 for interval i ($V_{CH_4, v, i}$) is calculated simply as the product of standardized vented (removed) biogas volume and CH_4 mole fraction for that interval:

$$V_{\text{CH}_4, v, i} = x_{\text{CH}_4, i} \cdot V_{b, std, i} \tag{5}$$

Cumulative CH_4 production at the end of interval i can be calculated by adding headspace CH_4 to the cumulative sum of vented CH_4 :

$$V_{\text{CH}_4, cum, i} = \sum_{i=1}^{i} V_{\text{CH}_4, v, i} + x_{\text{CH}_4, i} \cdot V_{h, std, i}$$
 (6)

where $V_{h,std,i}$ is the post-venting total standardized volume of gas in the bottle headspace (calculated using Eq. (1)). If vented measurements are cumulative instead of interval, the summation operation is omitted and a single value from interval i is added instead.

References

- O. A. Alduchov and R. E. Eskridge. Improved Magnus form approximation of saturation vapor pressure. *Journal of Applied Meteorology*, 35(4):601–609, 1996. doi: 10.1175/1520-0450(1996)035\(0601:IMFAOS\)\(0.2003.0.CO; 2.
- S. D. Hafner, S. Astals, P. Buffiere, N. Løjborg, C. Holliger, K. Koch, and S. Weinrich. Calculation of Methane Production from Manometric Measurements. Standard BMP Methods document 202, version 2.5., 2020a. URL https://www.dbfz.de/en/BMP.
- S. D. Hafner, C. Justesen, R. Thorsen, S. Astals, C. Holliger, K. Koch, and S. Weinrich. Calculation of Methane Production from Gas Density-Based Measurements. Standard BMP Methods document 203, version 1.5., 2020b. URL https://www.dbfz.de/en/BMP.
- S. D. Hafner, N. Lø jborg, S. Astals, C. Holliger, K. Koch, and S. Weinrich. Calculation of Methane Production from Volumetric Measurements. Standard BMP Methods document 201, version 1.7., 2020c. URL https://www.dbfz.de/en/BMP.
- S. D. Hafner, B. K. Richards, S. Astals, C. Holliger, K. Koch, and S. Weinrich. Calculation of Methane Production from Gravimetric Measurements. Standard BMP Methods document 203, version 1.0., 2020d. URL https://www.dbfz.de/en/BMP.

- A. S. Negi and S. C. Anand. *A Textbook of Physical Chemistry*. New Age International, 1985. ISBN 978-0-85226-020-3.
- W. F. Owen, D. C. Stuckey, J. B. Healy Jr, L. Y. Young, and P. L. McCarty. Bioassay for monitoring biochemical methane potential and anaerobic toxicity. *Water Research*, 13(6):485–492, 1979. doi: 10.1016/0043-1354(79) 90043-5.
- B. Richards, R. Cummings, T. White, and W. Jewell. Methods for kinetic-analysis of methane fermentation in high solids biomass digesters. *Biomass and Bioenergy*, 1(2):65–73, 1991. doi: 10.1016/0961-9534(91)90028-B.
- A. Rozzi and E. Remigi. Methods of assessing microbial activity and inhibition under anaerobic conditions: A literature review. *Re/Views in Environmental Science and Bio/Technology*, 3(2):93–115, June 2004. ISSN 1569-1705, 1572-9826. doi: 10.1007/s11157-004-5762-z.
- VDI. Fermentation of organic materials: Characterisation of the substrate, sampling, collection of material data, fermentation tests. Technical Report VDI 4630, Verein Deutsch er Ingenieure e.V., Düsseldorf, Germany, 2016.